

A GUIDE BOOK  
TO THE  
LOCAL MARINE BOARD  
EXAMINATION.

ORDINARY EXAMINATION

BY T. L. AINSLEY.

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*June 1876.*

TO THE

# LOCAL MARINE BOARD

EXAMINATION.

THE ORDINARY EXAMINATION.

BY THOMAS L. AINSLEY,

TEACHER OF NAVIGATION.

*Thirty-second Edition.*

SOUTH SHIELDS:

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## PREFACE TO THE FIRST EDITION.

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THIS WORK is intended as a Guide to the Officers of all grades of the Merchant Service, in the examinations they are required to undergo before the Local Marine Board. It will be issued in Two parts:—Part I containing what is termed the Ordinary Examination, and Part II containing the Extra Examination.

The present volume, which relates to the Ordinary Examination, contains model solutions of examples in the various problems required of Candidates when under Examination, with numerous Exercises to each Problem, together with a variety of Examination Papers. It also contains all requisite information respecting the Deviation of the Compass; Lights of the English, St. George's, and Bristol Channels, &c.; Scowage of Cargoes; Invoice; Charter Party; Bottomry Bonds, &c.

In the preparation of the articles on Seamanship, the following works have been consulted:—"The Kedge Anchor," by W. Brady, U.S.N.; "The Seaman's Friend," by R. H. Dana, jun; "The Sheet Anchor," by Darcy Lever, Esq.; while my obligations to other works have been duly acknowledged. The works of ABBOTT, LEES, STEELE, and M'CULLOCH, &c., are the authorities that have been consulted on the subjects of Charter Party, Bills of Lading, &c.

T. L. A.

*South Shields, July 10th, 1856.*



**ADVERTISEMENT**  
TO  
**THE THIRTY-SECOND EDITION.**

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IN this Edition of the "GUIDE BOOK," such alterations and additions have been made in the work as were necessary to adapt it to the present requirements of the Examinations—considerable alterations in the Examination Papers having come into operation on March 1st, 1872.

T. L. A.

*South Shields,  
September 13th, 1875.*

## ERRATA ET CORRIGENDA.

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- Page 18, line 20 from the top (Ex. 1), for 490 read 6497, and for 25 read 835.
- „ 29, Ex. 2, the first divisor should be 9, not 8; and the second divisor should be 8, not 9.
- „ 58, No. 20, for 5'000027 read 5'000000.
- „ 23, for 4'722522 read 4'722552.
- „ 27, for 6'602062 read 6'602060.
- „ 65, Ex. 7, the log. of .4828 should be 9'683767, not 9'683687; and the log. of quotient .04056 is 8'608046.
- „ 69, paragraph 96, for nat. sine  $136^{\circ} 42' =$  sine  $43^{\circ} 18'$  read nat. sine  $156^{\circ} 42' =$  sine  $23^{\circ} 18'$ ; and for nat. sine  $104^{\circ} 16'$  read  $140^{\circ} 16'$ .
- „ 81, paragraph 110, line 2, for *learned* read *learner*.
- „ 98, line 17 from bottom, for *towards the spectator* read *towards what the spectator, &c.*
- „ 140, No. 2, the ship's head by compass should be S.S.E.
- „ 149, line 20 from top, for *the central shows* read *the central line shows*.
- „ 312, Day's Work, for ship's head S.S.E.  $\frac{1}{2}$  E., read S.E.  $\frac{1}{2}$  E.
- „ 319, Ex. 8, line 2 from bottom, the variation should be  $30^{\circ} 28' W.$ , not  $30^{\circ} 28' E.$
- „ 328, Reduction to meridian, after *slow* on app. time at ship, insert  $4^h 8^m 12^s$ .
- „ 392, Paper XVII, Day's Work, second dist. should be 53', instead of 30'.

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# EXAMINATION OF MASTERS AND MATES

FOR

## CERTIFICATES OF COMPETENCY

*Under "The Merchant Shipping Act, 1854,"*

AND

## VOLUNTARY EXAMINATION IN STEAM.

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1. UNDER the provisions of the "Merchant Shipping Act, 1854," no "Foreign-going ship"\* or "Home Trade Passenger Ship"\* can obtain a clearance or transire, or legally proceed to sea, from any port in the United Kingdom unless the Master thereof, and in the case of a Foreign-going Ship the First and Second Mates, or Only Mate (as the case may be), and in the case of a "Home Trade Passenger Ship" the First or Only Mate (as the case may be), have obtained and possess valid Certificates, either of Competency or Service, appropriate to their several stations in such ship, or of a higher grade; and no such ship, if of one hundred tons burden or upwards, can legally proceed to sea unless at least one officer besides the Master has obtained and possesses a valid Certificate, appropriate to the grade of Only Mate therein, or to a higher grade; and every person who having been engaged to serve as Master, or as First or Second Mate or Only Mate of any "Foreign-going Ship," or as Master or First or Only Mate of a "Home Trade Passenger Ship," goes to sea as such Master or Mate without being at the time entitled to and possessed of such a Certificate as the Act requires, or who employs any person as Master, or First, Second, or Only Mate of any "Foreign-going Ship," or as Master or First or Only Mate of any "Home Trade Passenger Ship," without ascertaining that he is at the time entitled to and possessed of such Certificate, for each offence incurs a penalty not exceeding Fifty Pounds.

2. Every Certificate of Competency for a "Foreign-going Ship" is to be deemed to be of a higher grade than the corresponding Certificate for a "Home Trade Passenger Ship," and entitles the lawful holder to go to sea in the corresponding grade in such last-mentioned Ship; but no Certificate for a "Home Trade Passenger Ship" entitles the holder to go to sea as Master or Mate of a "Foreign-going Ship."

3. Certificates of Competency will be granted to those persons who pass the requisite examinations, and otherwise comply with the requisite conditions. For this purpose examiners have been appointed, and arrangements have been made for holding examinations at the ports and upon the days mentioned in the Table marked A, page 13. The days for examination are so arranged for general convenience, that a candidate wishing to proceed to sea, and missing the day at his own port, may proceed to another port where an examination is coming forward.

4. Candidates for examination must give in their names to the Local Marine Board if the place where they intend to be examined is a port where there is a Local Marine Board, on or before the day of examination (except in the case of London† and Liverpool), and must

\* By a "Foreign-going Ship" is meant one which is bound to some place out of the United Kingdom beyond the limits included between the River Elbe and Brest; and by a "Home Trade Passenger Ship" is meant any Home Trade Ship employed in carrying Passengers; and it is to be observed that *Foreign Steam Ships when employed in carrying Passengers between places in the United Kingdom* are subject to all the provisions of the Act, as regards Certificates of Masters, Mates, and Engineers, to which British Steam Ships are subject: s. 291 of the Merchant Shipping Act, 1854, and s. 5 of the Merchant Shipping Act, &c., Amendment Act, 1862.

† At London applications for examination must be made on Fridays from 10 till 4, and on Saturdays from 10 till 3.

At Liverpool applications for examination must be made on Tuesdays, Wednesdays, Thursdays, and Saturdays, during office hours.

conform to any regulations in this respect which may be laid down by the Local Marine Board; and if this be not done, delay may be occasioned.

5. Testimonials of character, and of sobriety, experience, ability, and good conduct on board of ship will be required of all applicants, and without producing them no person will be examined. As such testimonials may have to be forwarded to the office of the Registrar-General of Seamen in London for verification before any certificates can be granted, it is desirable that candidates should lodge them as early as possible. The testimonials of servitude of Foreigners and of British Seamen serving in foreign vessels, which cannot be verified by the Registrar-General of Seamen, must be confirmed either by the consul of the country to which the ship in which the candidate served belonged, or by some other recognized official authority of that country, or by the testimony of some other credible person on the spot having personal knowledge of the facts required to be established. Upon application to the Superintendent of the Mercantile Marine Office candidates will be supplied with a form (Exn. 2), which they will be required to fill up and lodge with their testimonials in the hands of the examiners.

6. Services which cannot be verified by the proper Entries in the Articles of the Ships in which the Candidates have served cannot be counted. Thus,—for instance, a Man will state his Service to have been as Second or Only Mate, and to support this assertion will produce a Certificate of Discharge or Employment by the Master stating that he served as Mate, when on reference to the Articles it appears that he has actually been rated as boatswain; the service in such a case will not be regarded as having been in the capacity of Mate.

Whenever a Man has, from any cause, been regularly promoted on a vacancy in the course of the Voyage from the rank for which he first shipped, and such promotion, with the ground on which it has been made, is properly entered in the Articles and in the Official Log Book, he will of course receive credit for his service in the higher grade for the period subsequent to his promotion.

7. The examinations will commence early in the forenoon on the days mentioned in page 13, and will be continued from day to day until all the candidates whose names appear upon the Superintendent's list on the day of examination are examined.

8. Where the Local Marine Board are in every respect satisfied with the testimonials of a candidate, service in the coasting trade may be allowed to count as service, in order to qualify him for examination for a Certificate of Competency for Foreign-going Ships as a Mate, and two years' service as Mate in the coasting trade may be allowed to count as service for a Master's Certificate, provided the candidate's name has been entered as Mate on the Coasting Articles, and provided he has already passed an examination.

### QUALIFICATIONS FOR CERTIFICATES OF COMPETENCY FOR A "FOREIGN-GOING SHIP."

The qualifications required for the several ranks undermentioned are as follow:—

9. **A SECOND MATE** must be seventeen years of age, and must have been four years at sea.

**In Navigation.**—He must write a legible hand, and understand the first five rules of arithmetic, and the use of logarithms. He must be able to work a day's work complete, including the bearings and distance of the port he is bound to, by Mercator's method; to correct the sun's declination for longitude, and find his latitude by meridian altitude of the sun; and to work such other easy problems of a like nature as may be put to him. He must understand the use of the sextant, and be able to observe with it, and read off the arc. (See List A, page 9.)

**In Seamanship.**—He must give satisfactory answers as to the rigging and unrigging of ships, stowing of holds, &c.; must understand the measurement of the log-line, glass, and lead-line; be conversant with the rule of the road, as regards both steamers and sailing vessels, and the lights and fog signals carried by them, and will also be examined as to his acquaintance with "the Commercial Code of Signals for the use of all Nations."

10. **AN ONLY MATE** must be nineteen years of age, and have been five years at sea.

**In Navigation.**—In addition to the qualification required for a Second Mate, an Only Mate must be able to observe and calculate the amplitude of the sun, and deduce the

variation of the compass therefrom, and be able to find the longitude by chronometer by the usual methods. He must know how to lay off the place of the ship on the chart, both by bearings of known objects, and by latitude and longitude. He must be able to determine the error of a sextant, and to adjust it, also to find the time of high water from the known time at full and change. (See List A, page 9.)

In Seamanship.—In addition to what is required for a Second Mate, he must know how to moor and unmoor, and to keep a clear anchor; to carry out an anchor; to stow a hold; and to make the requisite entries in the ship's log. He will also be questioned as to his knowledge of the use and management of the mortar and rocket lines in the case of the stranding of a vessel, as explained in the official log-book.

11. A FIRST MATE must be nineteen years of age, and have served five years at sea, of which one year must have been as either Second or Only Mate, or as both.\*

In Navigation.—In addition to the qualification required for an Only Mate, he must be able to observe azimuths and compute the variation; to compare chronometers and keep their rates, and find the longitude by them from an observation of the sun; to work the latitude by single altitude of the sun off the meridian; and be able to use and adjust the sextant by the sun.

In Seamanship.—In addition to the qualification required for an Only Mate, a more extensive knowledge of seamanship will be required, as to shifting large spars and sails, managing a ship in stormy weather, taking in and making sail, shifting yards and masts, &c., and getting heavy weights, anchors, &c., in and out; casting a ship on a lee-shore; and securing the mast in the event of accident to the bowsprit.

12. A MASTER must be twenty-one years of age, and have been six years at sea, of which at least one year must have been as First or Only Mate, and one year as Second Mate.

In addition to the qualification for a First Mate, he must be able to find the latitude by a star, &c. He will be asked questions as to the nature of the attraction of the ship's iron upon the compass, and as to the method of determining it. He will be examined in so much of the laws of the tides as is necessary to enable him to shape a course, and to compare his soundings with the depths marked on the charts. He will be examined as to his competency to construct jury rudders and rafts; and as to his resources for the preservation of the ship's crew in the event of wreck. He must possess a sufficient knowledge of what he is required to do by law, as to entry and discharge, and the management of his crew, and as to penalties and entries to be made in the official log; and a knowledge of the measures for preventing and checking the outbreak of scurvy on board ship. He will be questioned as to his knowledge of invoices, charter-party, Lloyd's agent, and as to the nature of bottomry, and he must be acquainted with the leading lights of the channel he has been accustomed to navigate, or which he is going to use. (See List B, page 9.)

In cases where an applicant for a certificate as Master Ordinary has only served in a fore-and-aft-rigged vessel, and is ignorant of the management of a square-rigged vessel, he may obtain a certificate on which the words "*fore-and-aft-rigged vessel*" will be written. This certificate does not entitle him to command a square-rigged ship. This is not, however, to apply to Mates, who, being younger men, are expected for the future to learn their business completely.

13. An EXTRA MASTER'S EXAMINATION is voluntary, and intended for such persons as wish to prove their superior qualifications, and are desirous of having certificates for the highest grade granted by the Board of Trade.

In Navigation.—As the vessels which such Masters will command frequently make long voyages, to the East Indies, the Pacific, &c., the candidate will be required to work a lunar observation by both sun and star, to determine the latitude by the moon, by Polar star off the meridian, and also by double altitude of the sun, and to verify the result by Sumner's method. He must be able to calculate the altitudes of the sun or star when they cannot be observed for the purposes of lunars,—to find the error of a watch by the method of equal altitudes,—and to correct the altitudes observed with an artificial horizon.

He must understand how to observe and apply the deviation of the compass; and to

\* Service in a superior capacity is in all cases to be equivalent to service in an inferior capacity.

deduce the set and rate of the current from the D. R. and observation. He will be required to explain the nature of great circle sailing, and know how to apply practically that knowledge, but he will not be required to go into the calculations. He must be acquainted with the law of storms, so far as to know how he may probably best escape those tempests common to the East and West Indies, and known as hurricanes.

In Seamanship.—The extra examination will consist of an inquiry into the competency of the applicant to heave a ship down, in case of accident befalling her abroad; to get lower masts in and out; and to perform such other operations of a like nature as the Examiner may consider it proper to examine him upon.

### QUALIFICATIONS FOR CERTIFICATES OF COMPETENCY FOR A "HOME TRADE PASSENGER SHIP."

14. A MATE must write a legible hand, and understand the first four rules of arithmetic. He must know and understand the rule of the road, and describe and show that he understands the Admiralty regulation as to lights. He must be able to take a bearing by compass, and prick off the ship's course on a chart. He must know the marks in the lead-line, and be able to work and heave the log.

15. A MASTER must have served one year as a Mate in the Foreign or Home Trade. In addition to the qualifications required for a Mate, he must show that he is capable of navigating a ship along any coast, for which purpose he will be required to draw upon a chart produced by the Examiner, the courses and distances he would run along shore from headland to headland, and to give in writing the courses and distances corrected for variation, and the bearings of the headlands and lights, and to show when the courses should be altered either to clear any danger, or to adapt it to the coast. He must understand how to make his soundings according to the state of the tide. He will also be questioned as to his knowledge of the use and management of the mortar and rocket lines in the case of the stranding of a vessel, as explained in the Official Log Book.

A first-class Pilot may be examined for a Master's Certificate of Competency for Home Trade Passenger Ships, notwithstanding that he may not have served in the capacity of Mate.

### GENERAL RULES AS TO EXAMINATIONS AND FEES.

16. The candidates will be allowed to work out the various problems according to the method and the tables they have been accustomed to use, and will be allowed five hours to perform the work; at the expiration of which time, if they have not finished, they will be declared to have failed, unless the Local Marine Board see fit to extend the time.

17. The fee for examination must be paid to the Superintendent of the Mercantile Marine Office (Shipping Master). If a candidate fail in his examination, half the fee he has paid will be returned to him by the Superintendent of Mercantile Marine Office, on his producing the Form Exn. 17, late HH, which will be given him by the Examiner. The fees are as follow:—

#### "FOR FOREIGN-GOING SHIPS."

|  | £ | s. | d. |
|--|---|----|----|
| Second Mate . . . . .  | 1 | 0  | 0  |
| First and Only Mate, if previously possessing an<br>inferior certificate . . . . .                 | 0 | 10 | 0  |
| If not . . . . .   | 1 | 0  | 0  |
| Master, whether Extra or Ordinary . . . . .  | 2 | 0  | 0  |
| Master, if previously in possession of a certificate<br>for "fore-and-aft-rigged vessels . . . . . | 1 | 0  | 0  |

*N.B.*—Any person having a Master's Certificate of Competency for Foreign-going Ships may go up for an Extra examination without payment of any fee, but if he fails in his first examination, half a Master's fee will be charged for each subsequent examination.

#### FOR "HOME-TRADE PASSENGER SHIPS."

|                  | £ | s. | d. |
|------------------|---|----|----|
| Mate . . . . .   | 0 | 10 | 0  |
| Master . . . . . | 1 | 0  | 0  |

18. If the applicant passes he will receive the Form Exn. 16, late GG, from the Examiner, which will entitle him to receive his Certificate of Competency from the Superintendent of the Mercantile Marine Office, at the port to which he has directed it to be forwarded. If his testimonials have been sent to the Registrar to be verified, they will be returned with his Certificate.

19. If an applicant is examined for a higher grade and fails, but passes an examination of a lower grade, he may receive a certificate accordingly, but no part of the fee will be returned.

20. In every case the Examination, whether for Only Mate, First Mate, or Master, is to commence with the problems for Second Mate.

21. In all cases of failure the candidate must be re-examined *de novo*. If a candidate fails in *Seamanship* he will not be re-examined until after a lapse of Six Months, to give him time to gain experience. If he fails three times in *Navigation* he will not be re-examined until after a lapse of Three Months.

22. As the examinations of Masters and Mates are made compulsory, the qualifications have been kept as low as possible; but it must be distinctly understood, that it is the intention of the Board of Trade to raise the standard from time to time, whenever, as will no doubt be the case, the general attainments of officers in the merchant service shall render it possible to do so without inconvenience; and officers are strongly urged to employ their leisure hours, when in port, in the acquirement of the knowledge necessary to enable them to pass their examinations; and Masters will do well to permit apprentices and junior officers to attend schools of instruction, and to afford them as much time for this purpose as possible.

#### EXAMINATION OF MASTERS AND MATES WITH REFERENCE TO THE COMMERCIAL CODE OF SIGNALS FOR THE USE OF ALL NATIONS.—INSTRUCTIONS TO EXAMINERS.

23. In transmitting the accompanying copy of the latest edition of the Commercial Code of Signals for the use of the Examiners, the Board of Trade desire to direct attention to the principal points connected with this Code as to which Candidates for examination should be questioned.

24. At the same time, as the subject is probably new to some of the Examiners themselves, the Board recommend to them a perusal of the *Report of the Signal Committee of 1855* (which will be found at the commencement of the Signal Book), and also the *first few pages of the Book*. The information therein given will be found sufficient to make the Examiners theoretically acquainted with the characteristics of the New Code, and the advantages it claims to possess over other Codes, and will enable them to appreciate and urge upon Candidates for Examination the facilities which the new System of Signalling affords for easy and rapid communication.

25. The "comprehensiveness" and "distinctness" of the Commercial Code are its chief recommendations.

26. The form of the Hoist generally indicates the nature of the Signal made, so that an observer can at sight understand the character of the Signal he sees flying.

27. The Examinations should tend to elicit a knowledge of the distinctive features of the Code above alluded to.

With this object the Examiners should make the 2, 3, and 4 Flag Signals on the Frame board which is furnished for the purpose (*always taking care first to show the Ensign and the Code Pennant at the Gaff*),\* questioning the Candidates as to the distinguishing Forms of the respective Hoists, which will be indicated according as a Burgee, or a Pennant, or a Square Flag, is uppermost.

28. The Candidate ought to know how to find in the Signal Book the communication or the inquiry he desires to make, and how to make the Signal. The Signal to be made should *invariably* be sought for by the candidate in the Vocabulary and Index, Part II, and never in Part I.

29. The Candidate ought to know how to interpret a Signal.

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\* The object of this is, of course, to distinguish the Signals from those of another Code.

The Examiner should place a Signal on the Frame board, and vary the Signal by showing a 2 or 3 Flag Signal, or a "Geographical" or a "Vocabulary" Signal, or the name of a Merchant Ship or a Ship of War.

The two latter Signals would not of course be found in the Signal Book. The Candidate ought to point them out in the *Code List of Ships*.

30. A Candidate ought to be able to read off a Signal at sight, so far as to name the Flags composing the Hoist.

31. He ought to know the use of the Code Pennant, and of the Pennants C and D, "Yes" and "No."

32. The Candidate should be practised in the use of the Spelling Table, by being made to spell his own name, or some word not in the Vocabulary of the Code.

33. As Ships of War use a different set of Code Flags, the Candidate ought to be aware of the fact, and should know that a plate of the Admiralty Flags is to be found in the Signal Book, as well as plates of the Code Flags which Foreign Ships of War will use in signalling to Merchant Vessels. He should also know that every Official Log Book contains plates of these Code Flags.

34. A knowledge of the Distant Signals should be required of the Candidate, their object, and the mode of signalling by Distant Code, which will be found at the end of the Signal Book.

For the purpose two Black Balls, two Black Square Flags, and two Black Pennants will be furnished with the Frame board, and the Candidate should be required to make one or two Distant Signals, and to read off one or two made by the Examiners.

The Ball being the distinguishing symbol of the Distant Signal, any Pennants or Flags of the Code may be employed in conjunction with it, irrespective of colour. The Black Pennants and Flags are merely sent as showing best in the light background of the Frame board.

#### SEMAPHORES.

35. We have as yet no Semaphores on our coasts. The French, however, have upwards of 110 such stations established on their coasts, at which the Commercial Code of Signals only is used.

36. A plate at the end of the Signal Book explains the method by which the arms of the Semaphore are made to represent by their position (up, down, or horizontal), the three symbols used for distant signalling, viz., a Flag, a Ball, or a Pennant. Before making Signals with the Semaphores, the Black Disc, with the white rim, should be placed on the top of the Semaphore Mast, as it properly forms a part of the Mast itself.

37. The Board of Trade think it of consequence to observe that as the Commercial Code has (in its integrity) been translated into French, and as copies of the Signal Book are furnished to all French Vessels of War and Semaphore stations, any Englishman can now, by this Code, make his wants known to them.

Other nations are now negotiating for the adoption of the Commercial Code, and from the favour with which Foreigners seem to have accepted the Code wherever it has been presented to their notice, there is every reason to believe that in a short time the Mercantile Marine of all nations will have the advantage of being able to communicate by an "Universal Language of Signals."

38. Her Majesty's Government have done all in their power to promote the use of the Commercial Code, and the Government of India and nearly all the Colonial Governments have adopted it, and a large number of Signal Books and Code Lists have already been circulated in the British Possessions abroad.

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## MASTERS' AND MATES' VOLUNTARY EXAMINATIONS IN STEAM.

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39. Arrangements have been made for giving to those Masters and First and Only Mates who are possessed of or entitled to certificates of competency, an opportunity of undergoing a voluntary examination as to their practical knowledge of the use and working of the steam

engine. These examinations are conducted on the premises, and under the superintendence of the Local Marine Boards at such times as they may appoint for the purpose; and the Examiners are selected by the Board of Trade from the Engineer Surveyors appointed under the fourth part of "The Merchant Shipping Act, 1854."

40. Any Master or Mate desiring to be examined in Steam, must deliver to the Superintendent of the Mercantile Marine Office, a statement in writing to that effect, upon the form of application (Exn. 2, late EE); if the applicant has a Certificate of Competency, such certificate must be delivered to the Shipping Master along with his statement. If he is about to pass an examination for a Certificate of Competency at the same time, the applications should be sent in together.

41. A fee of one pound must be paid by the applicant for the examination in Steam, and the Superintendent of the Mercantile Marine Office will thereupon inform him of the time and place at which he is to attend to be examined, and the examination will then and there proceed in the same manner as the other examinations. If the applicant fails, and has given in his certificate, it will at once be returned to him, but *no part of the fee he has paid will be returned.*

42. If he passes, the Report (Exn. 14, late FF) will be sent to the Board of Trade, and the Certificate of Competency with the Form (Exn. 2, late EE) to the Registrar-General of Seamen; the words "*Passed in Steam,*" with the date and place of examination, will then be entered on the certificate and its counterpart, and the certificate will be sent to the Superintendent of the Mercantile Marine Office of the port named in the Application (Exn. 2, late EE) to be delivered to the applicant in the usual manner.

43. The examination is *viva voce*, and extends to a general knowledge of the practical use and working of the steam-engine, and of the various valves, fittings, and pieces of machinery connected with it. Intricate theoretical questions on calculations of horse-power or areas of cylinders and valves, or any of the more difficult questions which appertain to steam-engines and boilers, will not be asked. The examination will in fact be confined to what a master of a steam-vessel may be called upon to perform in the case of the death, incapacity, or delinquency of the engineer.

44. If the applicant fails to answer some few of the questions, and yet, in the opinion of the Examiner, possesses such a competent knowledge of the parts of the engine generally, and such other practical knowledge of the subject as will enable him to effect the object in view, the Examiner will exercise his discretion as to whether a sufficiently high standard of knowledge has been attained, and pass him or not accordingly.

45. The Examiner will provide drawings and working sections, on a sufficiently large scale, of the various parts of the steam-engine, and of the valves and slides, &c., as may be necessary, and will require the applicant to make use of them in giving his answers to the various questions put to him; and, if an opportunity offer, the applicant will be permitted, under the guidance of the Examiner, to start and stop the engine of some vessel which may have her steam up.

#### CERTIFICATES OF SERVICE.

46. A Certificate of *Service* entitles an Officer who had served as either Master or Mate in a British Foreign-going Ship before the 1st January, 1851, or as Master or Mate in a Home Trade Passenger Ship before the 1st January, 1854, to serve in those capacities again; and it also entitles an Officer who has attained or attains the rank of Lieutenant, Master, Passed Mate, or Second Master, or any higher rank in the service of Her Majesty or of the late East India Company, to serve as Master of a British Merchant Ship, and may be had by application to the Registrar-General of Seamen, Adelaide Place, London Bridge, London, or to any Superintendent of a Mercantile Marine Office in the Outports, on the transmission and verification of the necessary certificates and testimonials.

#### LOCAL MARINE BOARD EXAMINATIONS—NOTICE TO CANDIDATES—OFFICIAL NOTICE.

1. Candidates are required to appear at the examination room punctually at the time appointed.

2. Candidates are prohibited from bringing into the examination room books or papers of any kind whatever. The slightest infringement of this regulation will subject the offender to all the penalties of a failure.

3. In the event of any Candidate being detected in defacing, blotting, writing in, or otherwise injuring any book or books belonging to the Board, the papers of such Candidate will be detained until the book or books so defaced be replaced by him. He will not, however, be at liberty to remove the damaged book, which will still remain the property of the Board.

4. In the event of any Candidate being discovered copying from another, or affording any assistance or giving any information to another, or communicating in any way with another, during the time of examination, he will subject himself to a failure and its consequences.

5. No Candidate will be allowed to work out his problem on a slate or on waste paper.

6. No Candidate will be permitted to leave the room until he has given up the paper on which he is engaged.

7. Candidates will be allowed to work out the various problems by the method and tables they have been accustomed to use, and will be allowed five hours to perform the work. At the expiration of the five hours they will, if they have not finished, be declared to have failed, unless the Local Marine Board or Examiner see fit to lengthen the period in any special case. If however, the period is lengthened in any case, the special circumstances of that case, and the reasons for lengthening the period must be reported to the Board of Trade by the Examiners at the time they send in the report on Form FF.

8. Candidates will find it more convenient, both here and at sea, to correct the declination and other elements from the Nautical Almanac by the "hourly differences" which have been given in that work in order to facilitate such calculations; they will thereby render themselves independent of any proportional or logarithmic table for such purpose.

9. The corrections by inspection from tables given in many works on navigation will not be allowed (see Tables IX, XI, and XXI, in Norie's Epitome; Tables 21 and 38 in Raper's Navigation); every correction must appear on the papers of the Candidates. The First-class and Extra Master are referred to page 519 of the Nautical Almanac, 1867, for further information on this subject.

10. Candidates are expected to bring their answers to all problems within, or not to exceed, a margin of one mile of position from a correct result.

11. In finding the longitude by chronometer the logarithms used in finding the hour-angle should be taken out for seconds of arc.

12. In all other problems the logarithms to the nearest minute will be sufficiently correct for all grades, except Extra Master, from whom a degree of precision will be required, both in the work and in the results, beyond what is demanded from the inferior grades.

THOMAS GRAY, Assistant Secretary.

Board of Trade, Marine Department, *January 1st, 1869.*

## NOTICE OF ALTERATION IN EXAMINATION PAPERS.

After the 1st day of March, 1872, all candidates presenting themselves for examination for Master's and Mate's Certificates for the first time, will be required to give short definitions of so many of the terms contained in the following list (A) as may be marked with a cross by the Examiner. These questions are, at the same time, intended to test the candidate's handwriting and spelling, to both of which special attention should be paid by him.

For the "Table of Deviations" which hitherto formed part of Form Exn. 7, the questions contained in the following list (B) have been substituted. Candidates for Certificates of Competency as Masters Ordinary will be required to answer at least twelve of such of these questions as may be marked with a cross by the Examiner. Candidates for First-class Certificates (Master Extra) will be required to answer the whole of these questions.

THOMAS GRAY.



*List A referred to in Circular.*

N.B.—The Candidate is to write a short definition against so many of the following terms as may be marked with a cross by the Examiner. The Examiner will not mark less than 10. The writing should be clear, and the spelling should not be disregarded.

- |  |   |
|--|---|
| 1. The Equator.                              | 23. Declination.                          |
| 2. The Poles.                                | 24. Polar Distance.                       |
| 3. A Meridian.                               | 25. Right Ascension.                      |
| 4. The Ecliptic.                             | 26. Dip or Depression of the Horizon.     |
| 5. The Tropics.                              | 27. Refraction.                           |
| 6. Latitude.                                 | 28. Parallax.                             |
| 7. Parallels of Latitude.                    | 29. Semi-diameter.                        |
| 8. Longitude.                                | 30. Augmentation of Moon's Semi-diameter. |
| 9. The Visible Horizon.                      | 31. Observed Altitude.                    |
| 10. The Sensible Horizon.                    | 32. Apparent Altitude.                    |
| 11. The Rational Horizon.                    | 33. True Altitude.                        |
| 12. Artificial Horizon and its use.          | 34. Zenith Distance.                      |
| 13. True course of a Ship.                   | 35. Vertical Circles.                     |
| 14. Magnetic Course.                         | 36. Prime Vertical.                       |
| 15. Compass Course.                          | 37. Civil Time.                           |
| 16. Variation of the Compass.                | 38. Astronomical Time.                    |
| 17. Deviation of the Compass.                | 39. Sidereal Time.                        |
| 18. The Error of the Compass.                | 40. Mean Time.                            |
| 19. Lee Way.                                 | 41. Apparent Time.                        |
| 20. Meridian Altitude of a Celestial Object. | 42. Equation of Time.                     |
| 21. Azimuth.                                 | 43. Hour Angle of a Celestial Object.     |
| 22. Amplitude.                               | 44. Complement of an Arc or Angle.        |
|  | 45. Supplement of Ditto.                  |

*List B. referred to in Circular.*

DEVIATION OF THE COMPASS.

The Candidate is to answer correctly at least eight of such of the following questions as are marked with a cross by the Examiner. The Examiner will not mark less than 12.

1. What do you mean by Deviation of the Compass?
2. How do you determine the deviation (a) when in port, and (b) when at sea?
3. Having determined the deviation with the Ship's head on the various points of the Compass, how do you know when it is Easterly and when Westerly?
4. Why is it necessary in order to ascertain the deviations, to bring the Ship's head in more than one direction?
5. For accuracy, what is the least number of points to which the Ship's head should be brought?
6. How would you find the deviation when sailing along a well known coast?
7. In the following table give the correct magnetic bearing of the distant object, and thence the deviation:—

| Ship's Head by Standard Compass. | Bearing of distant object by Standard Compass. | Deviation required. | Ship's Head by Standard Compass. | Bearing of distant object by Standard Compass. | Deviation required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North.                           |  |                     | South.                           |  |                     |
| N.E.                             |  |                     | S.W.                             |  |                     |
| East.                            |  |                     | West.                            |  |                     |
| S.E.                             |  |                     | N.W.                             |  |                     |

8. With the deviation as above, give the courses you would steer by the Standard Compass to make the following courses, correct magnetic.
9. Supposing you have steered the following courses by the Standard Compass, find the correct magnetic courses made from the above deviation table.
10. You have taken the following bearings of two distant objects by your Standard Compass as above; with the Ship's head at \_\_\_\_\_, find the bearings, correct magnetic.
11. Name some suitable objects by which you could readily obtain the deviation of the Compass when sailing along the coasts of the English Channel.
12. Do you expect the deviation to change; if so, state under what circumstances?
13. How often is it advisable to test the accuracy of your table of deviations?
14. State briefly what you have chiefly to guard against in selecting a position for the Compass.
15. The compasses of iron Ships are more or less affected by what is termed the heeling error; on what courses does this error vanish, and on what courses is it the greatest?
16. State to which side of the ship, in the majority of cases, is the North point of the Compass drawn in the Northern hemisphere; and what effect has it on the assumed position of the Ship when she is steering on Northerly, and also on Southerly courses?
17. The effect being as you state, on what courses would you keep away, and on what courses would you keep closer to the wind, in order to make good a given Compass course?
18. Does the same rule hold good in both hemispheres with regard to the heeling error?

### EXAMINATIONS OF EXTRA MASTERS, &c.: MINOR ALTERATIONS IN EXAMINATION PAPERS.

Some misunderstanding appears to exist as to the extent of the examination in Compass Deviation which candidates for Extra Masters' Certificates will be required to pass. Examination in the Syllabus hitherto *voluntary*, became *compulsory*, so far as Candidates for Extra Master's Certificates were concerned, on the 1st January last.

It was also announced that, in addition to the questions contained in the afore-mentioned Syllabus, they would, after the 1st March, 1872, be required to answer the whole of the elementary questions headed "Deviation of the Compass" on the revised Form Exn. 7.

Upon further consideration, these regulations have been slightly modified. Candidates for Extra Master's Certificates will still be examined in the whole of the Syllabus, but it will be sufficient if they answer *two-thirds* of the questions to the satisfaction of the Examiner; and they will *not* be required to answer the elementary questions on Exn. 7.

Any Master or Mate who wishes to pass a *voluntary* examination in the Syllabus, can at any time be examined upon payment to the Superintendent of the Mercantile Marine Office of the usual fee of two pounds. If the Candidate passes the examination successfully, an endorsement to that effect will be duly made upon the Master's or Mate's Certificate held by him. If he fail to pass, the fee will not be returned.

In addition to the alterations announced, the following minor alterations in the Examination Papers of Masters and Mates came into effect after the 1st of March, 1872:—

*Day's Work.*—(Exn. 4, No. 3.) The Deviation of the Compass will be given for the several courses in this problem, which latter will therefore require to be corrected for the same.

*Mercator Sailing.*—(Exn. 4, No. 6.) This will in future be required from all candidates for Second Mate's Certificates.

*Amplitude and Azimuth.*—(Exn. 5, No. 2, and Exn. 6, No. 1.) From the errors of the Compass as found by these problems, and the Variation which will be given, the Candidates will be required to find the deviation of the Compass for the position or direction of the ship's head at the time the observations were taken.

*Longitude by Chronometer.*—(Exn. 5, No. 3.) In this problem the rate of the Chronometer will not be given as heretofore, but the Candidate will be required to find the rate from two given errors on different dates.

THOMAS GRAY.

## NOTICE OF ALTERATIONS IN THE EXAMINATIONS OF MASTERS AND MATES.

On and after the 1st January, 1874, candidates will be required to give written answers to the questions on navigation contained in Lists A. and B., as follows, and to the question marked C. which has been added to the paper on compass deviation.

THOMAS GRAY.

### *List A.*

#### ADJUSTMENTS OF THE SEXTANT.

The applicant will answer in writing, on a sheet of paper which will be given him by the Examiner, all the following questions, numbering his answers with the numbers corresponding to the questions:—

Question.

1. What is the first adjustment of the sextant?
2. How do you make that adjustment?
3. What is the second adjustment?
4. Describe how you make that adjustment?
5. What is the third adjustment?
6. How would you make the third adjustment?
7. In the absence of a screw how would you proceed?
8. How would you find the index error by the horizon?
9. How is it to be applied?
10. Place the index at error of \_\_\_\_\_ minutes to be added, clamp it, and leave it.  
(NOTE.—The examiner will see that it is correct.)
11. The examiner will then place the zero of the vernier on the arc, not near any of the marked divisions, and the candidate will read it.

NOTE.—In all cases the applicants will name or otherwise point out the screws used in the various adjustments.

The above completes the examination of second and only Mates.

In addition to the above, first Mates and Masters will be required to state in writing:—

12. How do you find the index error by the Sun?
13. How is the same applied?
14. What proof have you that those measurements or angles have been taken with tolerable accuracy?

### *List B.*

#### EXAMINATION IN CHART.

The applicant will be required to answer in writing, on a sheet of paper which will be given him by the Examiner, all the following questions according to the grade of Certificate required, numbering his answers with the numbers corresponding with those on the question paper:—

1. A strange chart being placed before you, what should be your special care to determine, before you answer any questions concerning it, or attempt to make use of it?
2. How do you ascertain that in our British charts?
3. Describe how you would find the course by the chart between any two places, A and B.

- 
4. Supposing there to be                      points of                      variation at the first-named place, what would the course be magnetic? the true course being
  5. How would you measure the distance between those two or any other two places on the chart?
  6. Why would you measure it in that particular manner?  
The above comprises all the questions on the chart that are put to first Mates and only Mates.  
In addition to the above, the Masters are required to answer—
  7. What do you understand those small numbers to indicate that you see placed about the chart?
  8. At what time of the tide?
  9. What are the requisites you should know in order that you may compare the depths obtained by your lead line on board with the depths marked on the chart?
  10. What do the Roman numerals indicate that are occasionally seen near the coast, and in harbours?
  11. How would you find the time of high water at any place, the Admiralty tide tables not being at hand, nor any other special tables available?

All the above questions should be answered, but this does not preclude the Examiner from putting any other questions of a practical character, or which the local circumstances of the port may require.

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*C.*

The following question has been added to the examination paper on compass deviation:—  
Question.

19. Your steering compass having a large error, how would you proceed to correct that compass by compensating magnets and soft iron, in order to reduce the error within manageable limits?

N.B.—The candidate is required to construct a deviation curve upon a Napier's diagram supplied by the Examiner.

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## APPROPRIATE CERTIFICATE.

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A PERSON possessing a Master's Certificate, whether of Competency or Service, is eligible to command any vessel of whatsoever tonnage, and either Certificate is sufficient for clearance at the Custom House. But a condition in the Charter-party of vessels taken up by Government for the conveyance of troops, stores, or emigrants, and also the Regulations of the Principal Steam Packet Companies, require that the Master and principal Officer shall possess Certificates of Competency.

The First Mate may engage as Mate of any kind.

The Only Mate as Mate when there is no other; or as Second Mate when there is a First Mate.

The Second Mate is not appropriate for any superior station, and must be employed only in cases where a First Mate is also engaged.

A Certificate of Competency for a "Foreign-going Ship" is equivalent to a Certificate of equal or lower grade for a "Home Trade Passenger Ship," and entitles the holder to fill the situation of Master or Mate, as the case may be.

Certificates of Competency or Service may be either of a grade appropriate to the Stations held for the time being, or of any superior grade.

N.B.—CAUTION TO OFFICERS PROCUING CERTIFICATES OF CHARACTER FROM OWNERS AND CAPTAINS: Certificates of Character from Owners and Captains, must particularly include the word "Sobriety," as they cannot otherwise be received by the Examiners at the Local Marine Board.

TABLE A.

## EXAMINATION DAYS

AT

| PLACES.         |   | DAYS.   |
|-----------------|---|---|
|                 |   | For Masters and Mates.  |
| 1.              |   | 2.  |
| Aberdeen*       | . | First and third Friday and Saturday in each month.  |
| Belfast         | . | First and third Tuesday in each month.  |
| Bristol*        | . | Tuesday in each week.   |
| Cork            | . | Second and fourth Monday in each month.   |
| Dublin          | . | First and third Thursday in each month.   |
| Dundee*         | . | Saturday in each week.  |
| Glasgow*        | . | Thursdays and Fridays; held alternately at each place.  |
| Greenock*       | . |   |
| Hull*           | . | Second and fourth Tuesday in each month.  |
| Leith*          | . | Tuesday in each week.   |
| Liverpool*      | . | Every week—Monday and Tuesday "Foreign Trade;" Thursday and Friday "Home Trade Passenger" and "Foreign Trade."  |
| London          | . | The examination in Navigation commences every Monday, and the examination in Seamanship takes place as soon as the Navigation examination is finished; Master's voluntary examination in Steam held on Friday in each week. |
| Shields, South* | . | Every alternate Thursday.   |
| Sunderland*     | . | Every alternate Monday.   |
| Plymouth*       | . | Tuesday in each week.   |

\* At these places Masters' Extra Examinations are held.

EXERCISES  
IN THE  
SIMPLE RULES OF ARITHMETIC  
FOR  
MASTERS AND MATES OF HOME TRADE PASSENGER SHIPS.

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EXERCISES IN NOTATION AND NUMERATION.

I.—NOTATION.

1. NOTATION is the art of expressing numbers by figures or symbols, appropriated for that purpose.

2. Unit, or unity, is the name given to that quantity which is to be reckoned as *one*, when other quantities of the same kind are to be measured.

3. Number is the relation of a quantity to its unit; the notion of number being suggested by successive repetitions of the individual unit, or number, is the name by which we signify how many objects or things are considered, whether *one* or *more*. When, for instance, we speak of one ship, two steamers, three masts, or four yards, the number of things referred to will be one, two, three, or four, according to the case; and so one, two, three, four, and the rest are called numbers.

4. In the common system of arithmetic all numbers, however large or small, can be expressed by the following symbols or characters, called figures, viz. :—

|      |      |        |       |       |      |        |        |       |         |
|------|------|--------|-------|-------|------|--------|--------|-------|---------|
| 1    | 2    | 3      | 4     | 5     | 6    | 7      | 8      | 9     | 0       |
| one, | two, | three, | four, | five, | six, | seven, | eight, | nine, | nought. |

The first nine of these are called *significant figures* or *digits*,\* and sometimes represent units, sometimes tens, hundreds, or higher classes. When placed singly they denote the simple numbers subjoined to the characters; where several are placed together the first figure on the right is taken for its simple value, the next, or figure standing in the second place, expresses ten times its simple value, or signifies so many tens; thus 94 expresses ten times nine units, together with four units more; the third, or figure standing in the third place, expresses one hundred times its simple value, or signifies so many hundreds; thus 943 expresses one hundred times nine units, together with four times ten units, and also three units more, and so on by a ten-fold increase for each additional figure that follows it. The value which thus belongs to a figure in consequence of its position or place is called its *local*

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\* Names frequently throw light on the origin of *things*. It is interesting to notice that the name *digits* is plainly significant of the early rude method of counting on the *fingers*; and that the name *calculation* as plainly refers to the primitive practice of reckoning with *pebbles* (*calculus*, a pebble).

value. Therefore, all numbers have a simple or intrinsic value, and also a local value.

5. It appears, then, that in common arithmetic we proceed towards the left from units to tens of units, from tens of units to tens of tens of units, or hundreds of units, from hundreds of units to tens of hundreds of units or thousands of units; from thousands of units to tens of thousands of units; from tens of thousands of units to tens of tens of thousands of units, that is to hundreds of thousands of units, thence to tens of hundreds of thousands of units, or millions of units, thence to tens of millions of units, hundreds of millions of units, &c., till we come to millions of millions of units, which are called billions of units, and so on to trillions, quadrillions, &c.\*

The actual scale is as follows:—

|   |                                     |                   |
|---|-------------------------------------|-------------------|
| Units .....                             | a single one being written as ..... | 1                 |
| Tens .....                              | .....                               | 10                |
| Hundreds .....                          | .....                               | 100               |
| Thousands .....                         | .....                               | 1,000             |
| Tens of Thousands .....                 | .....                               | 10,000            |
| Hundreds of Thousands .....             | .....                               | 100,000           |
| Millions .....                          | .....                               | 1,000,000         |
| Tens of Millions .....                  | .....                               | 10,000,000        |
| Hundreds of Millions .....              | .....                               | 100,000,000       |
| Thousands of Millions .....             | .....                               | 1,000,000,000     |
| Tens of Thousands of Millions .....     | .....                               | 10,000,000,000    |
| Hundreds of Thousands of Millions ..... | .....                               | 100,000,000,000   |
| Billions .....                          | .....                               | 1,000,000,000,000 |

6. When any of the denominators, units, tens, hundreds, &c., is wanting, it becomes necessary to supply its place with the last sign or character, viz., 0, which is termed *cypher*, or *nothing*—the word *cypher* in the Arabic signifying *vacuity*. This character, which indicates the absence of all number, is a most important one, inasmuch as its introduction serves to preserve the proper position of the significant figure, thus the number *forty thousand three hundred and twenty* would be expressed in figures by 40320, because the denominations units and thousands are wanting, and the absence of each is indicated by the cypher which occupies its place.

## RULE I.

To write in figures a number expressed in words.—Write down a row of noughts, or cyphers, and, as if these blanks were numbers, mark off the periods by cutting off the last three, then the next three, then the next, and so on; then

\* It is worth while to remark that as regards *billions* there is a difference between the French and English practice; in French, a billion (or *milliard*) is one thousand million, in English a billion is a million of millions, and accordingly the word is seldom used in our language, for such large numbers are rarely of any practical use.

The old books use a scale of numbers of this kind—

A million of millions is a billion,

A million of billions is a trillion,

and so forth; but these names are never used in practice, and can hardly be said to belong to the language of arithmetic or to English speech. It may be worth a passing notice, too, that no distinct ideas are conveyed by any of these terms; beyond a very moderate extent our notions of the value of numbers become confused. The number of *ones* in a million even, is hard to conceive; it is a thousand thousand, and would take more than twenty-three days to count through, kept at it for twelve hours a day, and counted one every second.

commencing at the first cypher on the left, put under each the proper figure in the number proposed, taking care that it be in its proper place; if any vacancies appear under the corresponding cyphers, fill them up with noughts.

Thus, let it be required to put into figures the number five hundred and four million, eighty-two thousand and thirty-five. We know the place of millions has *six* places to the right of it, we therefore put a nought for the millions, and write six noughts after it, and, as we see, from *hundreds* being the leading word in the written expression, that the first period will be a *complete* period, we prefix two noughts more. The requisite number of noughts, divided as proposed, is as in the margin, and under them we now have to write, in their proper places, the figures 5, 4, 8, 2, 3, 5, and then fill up the gaps with noughts; we thus find the number, when written, to be 504,082,035.

#### EXAMPLES.

Ex. 1. Express in figures, five hundred thousand six hundred and four.

000,000  
500,604

Ex. 2. Express in figures, eight millions, seven thousand, seven hundred and two.

0,000,000  
8,007,702

Ex. 3. Express in figures, sixty-seven million, eight hundred thousand, five hundred and six.

00,000,000  
67,800,506

Ex. 4. Express in figures, five hundred and twenty millions, three thousand and eleven.

000,000,000  
520,003,011

#### EXAMPLES FOR PRACTICE.

Express the following numbers in Figures:—

1. Sixty-three; eighty-one; ninety-nine; forty; thirteen.
2. Two hundred; three hundred and three; five hundred and ninety-eight; eight hundred and eighty-eight.
3. Four thousand; one thousand, seven hundred and eighty-three; six thousand and eighty-three; seven thousand, nine hundred and thirty; nine thousand and nine.
4. Twenty-seven thousand, five hundred and four; eighty-nine thousand and sixty-four; thirty-three thousand.
5. One hundred thousand; six hundred and seventy-six thousand and fifty; six hundred and three thousand, two hundred and forty.
6. Twenty thousand, six hundred; ninety thousand and ninety-two; two hundred and four thousand, six hundred and forty-one; eight hundred thousand and eight hundred.
7. Three million, six thousand and four; five million, thirty thousand and forty; seven million, seven hundred thousand and six; ten million, ten thousand and ten.
8. Seven million, three thousand; eleven million, one hundred and eight thousand, one hundred and six; fifty-four million, fifty-four thousand and eighty eight; six hundred and thirteen million, twenty thousand, three hundred and three.
9. Seventy million, seven hundred and four thousand, and thirty-two; forty-five million, three hundred and eighty-seven thousand, and twenty-five; three hundred and forty-nine million, four thousand and sixty-five; one hundred million, ten thousand and one.
10. Eight hundred and forty-two million, two hundred and forty-eight thousand, four hundred and eighty-four; nine hundred and nine million, nine thousand and ninety-nine; two hundred and twenty-two million, and forty; three hundred and five million, forty thousand and eight.
11. Seven hundred million, seven hundred thousand and seven hundred; two hundred and two million, two hundred and two thousand, two hundred; nine hundred million, and nine hundred; one hundred million, ten thousand and one.



2.—NUMERATION.

7. NUMERATION is generally applied to the converse process of expressing in words a number which is already expressed in symbols.

8. To express in words the numbers denoted by a line of figures.

RULE II.

1°. Divide them into periods of three figures each, beginning at the right hand.

2°. Then, commencing at the left hand, read the figures of each period in the same manner as those of the right hand period are read, and at the end of each period pronounce the name.

NOTE.—A glance at the numeration table shows that the leading figure of each set is *hundreds* of something; that of the first set, on the right, is *hundreds* of *units*, or simply *hundreds*; that of the next set, *hundreds* of *thousands*; that of the next set, *hundreds* of *millions*, and so on. And by thus finding out the local value of the leading figure in each period, the number may be read with ease. When any of the figures is 0, a little extra care is, however, necessary.

EXAMPLES.

Ex. 1. Express in words 68547329.

The number 68547329, when divided into periods as proposed, is 68, 547, 329, pointing to the 3 you say *hundreds*, and passing to the 5 you say *hundreds* of *thousands*; the incomplete period 68, must, therefore, be 68 *millions*; and the entire number 68 millions, 547 thousand, 329, or expressing the whole in words it is, sixty-eight million, five hundred and forty-seven thousand, three hundred and twenty-nine.

Ex. 2. Express in words 460305007.

The number 460305007 being divided into periods is 460, 305, 007, and is read, four hundred and sixty millions, three hundred and five thousand and seven.

Ex. 3. Express in words 999999999.

Divided into periods this is 999, 999, 999, and is read, nine hundred and ninety-nine million, nine hundred and ninety-nine thousand, nine hundred and ninety-nine.

Ex. 4. Express in words 561234826479365.

and is read, five hundred and sixty-one billions, two hundred and thirty-four thousand eight hundred and twenty-six million, four hundred and seventy-nine thousand three hundred and sixty-five.

EXAMPLES FOR PRACTICE.

Express in words:—

|       |          |           |             |               |               |
|-------|----------|-----------|-------------|---------------|---------------|
| 1. 43 | 9. 123   | 17. 7036  | 25. 690006  | 33. 20084216  | 41. 202202200 |
| 2. 60 | 10. 407  | 18. 2000  | 26. 8047328 | 34. 5001860   | 42. 100100101 |
| 3. 88 | 11. 500  | 19. 3003  | 27. 4090300 | 35. 8080808   | 43. 275008005 |
| 4. 97 | 12. 999  | 20. 5505  | 28. 5210007 | 36. 55700005  | 44. 20084216  |
| 5. 59 | 13. 738  | 21. 37654 | 29. 6030405 | 37. 76014059  | 45. 79030184  |
| 6. 12 | 14. 837  | 22. 87078 | 30. 560075  | 38. 6006606   | 46. 408076032 |
| 7. 21 | 15. 2760 | 23. 37003 | 31. 3000006 | 39. 56700505  | 47. 401400056 |
| 8. 19 | 16. 5080 | 24. 63090 | 32. 1397475 | 40. 120015015 | 48. 908500060 |

ADDITION.

9. The process of finding a number which shall be equal to the sum of two or more numbers is called *addition*. The number found, or the answer, is called the *sum*, and numbers which are added are called *addends*.



| (17)   | (18)   | (19)   | (20)   | (21)   | (22)   | (23)   | (24)   |
|--------|--------|--------|--------|--------|--------|--------|--------|
| 987825 | 916427 | 695024 | 986257 | 985626 | 372519 | 586372 | 148537 |
| 736349 | 625736 | 538426 | 427385 | 796842 | 463726 | 477754 | 697296 |
| 856925 | 346831 | 827836 | 514986 | 915638 | 298534 | 638831 | 526438 |
| 734316 | 857936 | 735985 | 726326 | 809274 | 851372 | 951490 | 723649 |
| 827842 | 735784 | 216515 | 915827 | 444444 | 319628 | 479291 | 859698 |
| 936736 | 426467 | 859827 | 734482 | 913258 | 738543 | 863748 | 852619 |
| 842625 | 849753 | 910756 | 386912 | 872364 | 497791 | 376546 | 419648 |
| 759519 | 358358 | 683625 | 219863 | 410698 | 345345 | 356633 | 777777 |
| 846325 | 647846 | 745841 | 391285 | 742367 | 679567 | 459681 | 999999 |
| 987846 | 386921 | 526606 | 842163 | 946208 | 161514 | 453148 | 555555 |
| 333445 | 666777 | 888999 | 615827 | 807609 | 131549 | 567963 | 724483 |
| 335445 | 666777 | 888999 | 736846 | 915827 | 761346 | 313499 | 952637 |

25. Add together the addends (1) under exercises (1), (9), and (17); (2) under (2), (10), and (18); (3) under (3), (11), and (19); (4) under (4), (12), and (20); (5) under (5), (13), and (21); (6) under (6), (14), and (22); (7) under (7), (15), and (23); and (8) under (8), (16), and (24).
26. Add together three hundred and nine million, four hundred and seventeen thousand, and eighty-seven; six hundred and seventy-five thousand, and forty-nine; seven thousand and ninety-seven million, eight hundred and fourteen thousand, three hundred and five; seventy-nine million, five hundred and four thousand, and forty-nine; six thousand and seventy-eight million, four hundred and thirty-nine thousand, six hundred and forty-seven; seven thousand million, eight hundred and seventy-six thousand, four hundred and twenty-nine.

## SUBTRACTION.

12. The process of finding a number which shall be equal to the difference of two numbers is called *subtraction*. It is customary to call the quantity from which the subtraction is made, the *minuend*; the quantity to be subtracted, the *subtrahend*; and the result of the subtraction, the *difference*. Thus, then, we have, minuend — subtrahend = difference.

We may also write this as,

$$\text{minuend} = \text{subtrahend} + \text{difference},$$

which shows the connection between subtraction and addition.

The operation of SUBTRACTION is indicated or expressed by the sign —, which is read *minus* or *less by*, with the use of the sign =; thus, the excess of 7 above 3 will be expressed in the form  $7 - 3 = 4$ , which is read 7 minus 3 equals 4; where the sign — between 7 and 3 denotes the subtraction of the latter from the former, and the sign = between 3 and 4 shows the *equality* of the excess to 4.

13. The rule for simple subtraction is as follows:—

### RULE IV.

1°. Put the smaller number under the greater, taking care, as in addition, that units shall be under units, tens under tens, hundreds under hundreds, and so on.

2°. Then, beginning at the units, subtract each figure in the lower row from the figure above it, if the lower figure be not the greater of the two, and put the remainder underneath. (See the operation in Ex. 1).

3°. But if you come to a lower figure which is greater than the figure above it, add 10 to the upper figure and then subtract, putting down the remainder as before, and taking care to carry 1 to the next figure of the lower row. (See Ex. 2).

## EXAMPLES.

Ex. 1. Let it be required to subtract 42572 from 76594.

$$\begin{array}{r} \text{From } 76594 \\ \text{Subt. } 42572 \\ \hline \text{Rem. } 34022 \end{array}$$

Ex. 2. Let it be required to subtract 29385 from 86947; then placing the former number under the latter (as in the margin) we proceed thus: 5 from 7 and 2 remains; 8 from (not 4) but 14 and 6 remains, carry 1; 4 from 9 and 5 remains; 9 from 16 and 7 remains, carry 1; 3 from 8 and 5 remains.

$$\begin{array}{r} \text{From } 86947 \\ \text{Subt. } 29385 \\ \hline \text{Rem. } 57562 \end{array}$$

In the preceding example we see that 8 cannot be taken from the figure above it, because this is only 4, we therefore add 10 to the 4, converting it into 14; but the adding 10 to any figure is simply putting 1 before it, that is, it is adding 1 to the *preceding* figure, which 1, by carrying it to the next lower or subtractive figure, is taken away again at the next step. In like manner, the 6 in the upper row is converted into 16, and the 1 thus prefixed to it is afterwards taken away, by 1 being carried to the next lower figure, and 3 subtracted instead of 2. It is plain that in *subtraction* the carrying can never amount to more than 1.

Ex. 3. As another example, let 84025506 be subtracted from 130741394, then, having arranged the numbers, as in the margin, we proceed thus, 6 from 14, 8, carry 1; 1 from 9, 8; 5 from 13, 8, carry 1; 6 from 11, 5, carry 1; 3 from 4, 1; 0 from 7, 7; 4 from 10, 6, carry 1; 9 from 13, 4; therefore the remainder is 46715888.

$$\begin{array}{r} \text{From } 130741394 \\ \text{Subt. } 84025506 \\ \hline \text{Rem. } 46715888 \end{array}$$

14. **Verification of Subtraction.**—The best verification is to add the subtrahend and difference. This ought to give back the minuend, or original quantity from which the subtraction was made.

## EXERCISES IN SIMPLE SUBTRACTION.

|   |  |  |   |   |                                 |                                |                                |
|---|--|--|---|---|---------------------------------|--------------------------------|--------------------------------|
| (1)<br>706205<br><u>84694</u>                     | (2)<br>804601<br><u>265061</u>                 | (3)<br>9800001<br><u>9800000</u>           | (4)<br>600501<br><u>600492</u>                      | (5)<br>702001<br><u>26000</u>               | (6)<br>601002<br><u>46003</u>   | (7)<br>501001<br><u>20106</u>  | (8)<br>602004<br><u>11006</u>  |
| (9)<br>701628<br><u>20449</u>                     | (10)<br>508000<br><u>129</u>                   | (11)<br>403000<br><u>26001</u>             | (12)<br>393436<br><u>219050</u>                     | (13)<br>321288<br><u>213788</u>             | (14)<br>345876<br><u>123457</u> | (15)<br>206011<br><u>48605</u> | (16)<br>123456<br><u>65432</u> |
| (17)<br>36479236472<br><u>28217993216</u>         | (18)<br>3642364231<br><u>1284128417</u>        | (19)<br>7631026341<br><u>5624736794</u>    | (20)<br>3462364284<br><u>2698768796</u>             | (21)<br>23476212861<br><u>17467127437</u>   |                                 |                                |                                |
| (22)<br>32179836472<br><u>2222222222</u>          | (23)<br>347986312101<br><u>269887360189</u>    | (24)<br>7987642062<br><u>486428462</u>     | (25)<br>101100110110<br><u>10011101011</u>          | (26)<br>479863217896<br><u>241826424862</u> |                                 |                                |                                |
| (27)<br>230962083534589<br><u>187524828485771</u> | (28)<br>10100011101011<br><u>1011100110110</u> | (29)<br>378219362112<br><u>24686762421</u> | (30)<br>1270106851256158<br><u>1196398779220936</u> |   |                                 |                                |                                |

Take each subtrahend 12 times from its minuend in the following examples:—

|                                  |                                 |                                 |                                |                                 |                                |
|----------------------------------|---------------------------------|---------------------------------|--------------------------------|---------------------------------|--------------------------------|
| (31)<br><u>7432326</u><br>157689 | (32)<br><u>6677298</u><br>67527 | (33)<br><u>7213545</u><br>57636 | (34)<br><u>4362579</u><br>9873 | (35)<br><u>6002109</u><br>45108 | (36)<br><u>8100630</u><br>6156 |
|----------------------------------|---------------------------------|---------------------------------|--------------------------------|---------------------------------|--------------------------------|

37. Take two thousand and nine from ten thousand and ninety-six; three thousand and eight from seven thousand nine hundred and forty-four.
38. From three hundred and two thousand four hundred and sixty-seven take ninety-four thousand six hundred and eighty-one.
39. Take seventy-eight thousand four hundred and one from one hundred and thirty thousand.
40. Find the difference between two hundred and eighteen and one million one hundred.
41. The minuend is one hundred million one hundred and one thousand and ten, and the subtrahend is seventy million seven thousand and seven: find the remainder.
42. The population of Russia is about 67,500,000, that of France 37,050,671; how many more people in Russia than in France?

### MULTIPLICATION.

15. **Multiplication** is the finding the amount of a number repeated any number of times. The number which is repeated is called the **multiplicand**, the number denoting the repetitions is called the **multiplier**, and the amount the **product**.

**Multiplier**  $\times$  **Multiplicand** = **Product**. **Multiplicand**  $\times$  **Multiplier** = **Product**.

The multiplicand and multiplier are termed the **factors** of the product, because they are factors or makers of the product.

The operation of **MULTIPLICATION** is expressed by the sign  $\times$ , which is read *into*, or *multiplied by*; thus,  $5 \times 7 = 35$  denotes the result of the multiplication of 5 by 7 to be 35; so again,  $4 \times 5 \times 13 = 260$  expresses the continued product of 4, 5, and 13.

Let it be required to multiply 739 by the single figure 8.

Since the product of 739 by 8 is evidently equal to the sum of the products of all its parts, we have the following operation:—

| Thousands. | Hundreds. | Tens. | Units. |                        |
|------------|-----------|-------|--------|------------------------|
| 0          | 7         | 3     | 9      | 739                    |
| —          | —         | —     | —      | 8                      |
|            |           | 7     | 2      | 72 = product of 9 by 8 |
|            | 2         | 4     |        | 240 = " " 30 " 8       |
| 5          | 6         | —     | —      | 5600 = " " 700 " 8     |
| —          | —         | —     | —      | —                      |
| 5          | 9         | 1     | 2      | 5912 = " " 739 " 8     |

In practice, the partial products, 72, 240, and 5600, are not written down, but combined mentally into one sum: thus we say 8 times 9 are 72, write down 2 and reserve the 7 tens; then 8 times 3 are 24, and the reserved 7 added thereto gives 31, write down 1 and carry 3 to the sum of 7 by 8, or to 56 hundreds, and the entire number of hundreds is 59, the whole product being 5912.

16. When the multiplier is not greater than 12.

### RULE V.

*Put the multiplier under the multiplicand, units under units, and multiply each figure of the multiplicand, commencing at the unit's figure by the multiplier. Set down the right-hand figure only of the product, when it is a number of more than one figure, and carry as in addition.*

The following worked like the above example require no further explanation.

$$\begin{array}{r} 73826 \\ 8 \\ \hline 590608 \end{array}$$

$$\begin{array}{r} 9073142 \\ 9 \\ \hline 81658178 \end{array}$$

$$\begin{array}{r} 531462 \\ 12 \\ \hline 6377544 \end{array}$$

17. When the multiplier is greater than 12, we proceed as follows:—

### RULE VI.

1°. Place the multiplier under the multiplicand so that the units of the former may be under those of the latter, the tens under the tens, &c.

2°. Write down the product of the whole multiplicand by the unit's digit of the multiplier. In like manner write down the product of the multiplicand by each of the remaining figures of the multiplier, observing to place the unit of each line in the column under the figure of the multiplier from which it came.

(a) If the multiplicand contain a cypher, treat it as if it were a number, recollecting that  $0 \times 1 = 0$ ,  $0 \times 2 = 0$ , and so on.

(b) If one or more of the figures of the multiplier be 0, the corresponding partial product, or products, will be 0, cyphers, and the lines may be entirely omitted, recollecting to give its proper value to the product arising from multiplying by the next figure.

3°. Then add all these partial products together, and their sum will be the entire product of the two factors.

As before, an example will explain this rule.

Ex. 1. Let it be to multiply 4786 by 2783. That is, to take 4786 2783 times, and add them all together; or, to take it 2000 times, 700 times, 80 times, and 3 times, and add the sums together; or, to multiply it by 2000, by 700, by 80, and by 3 times, and add the products together.

$$\begin{array}{rcl} \text{Now,} & 4786 \times 3 & = 14358 \text{ (a)} \\ & 4786 \times 80 & = 382880 \text{ (b)} \\ & 4786 \times 700 & = 3350200 \text{ (c)} \\ & 4786 \times 2000 & = 9572000 \end{array}$$

And the sum of all these is 13319438 the product required.

Ordinary form.

$$\begin{array}{r} 4786 \\ 2783 \\ \hline 14358 \text{ units' product.} \\ 38288 \text{ tens' } \\ 33502 \text{ hundreds' } \\ 9572 \text{ thousands' } \\ \hline 13319438 \text{ complete } \end{array}$$

We first multiply 4786 by 3 (a); then by 8, annexing a cypher to the right of the product (b); next by 7, annexing two cyphers to the product (c); and, lastly, by 2, annexing three cyphers.

If the ordinary method of performing the operation be compared with the detailed process here given, it will be seen that in practice the cyphers on the right may be omitted, provided care be taken that the first significant figure of each partial product is made to occupy its proper place, *i.e.*, directly under the multiplying figure which supplies that product.

Ex. 2. Multiply 7680426 by 500403.

$$\begin{array}{r} 7680426 \\ 500403 \\ \hline 23041278 = 3 \text{ times.} \\ 30721704 = 400 \text{ } \\ 38402130 = 500000 \text{ } \\ \hline 3843308211678 = 500403 \text{ } \end{array}$$

Here the first figure (8) of the first partial product is set below the figure 3 in the multiplier, the first figure (4) of the second partial product below 4, the multiplying figure, and the first figure (0) of the third partial product is placed directly under 5, the multiplying figure. (This example illustrates Rule VI, 2°, (a) and (b).)

18. Any number is multiplied by 10 by annexing *one* cypher, by 100 by annexing *two* cyphers, by 1000 by annexing *three* cyphers, &c.; *e.g.*,  $85 \times 10 = 850$ , for, by annexing the cypher, the 5 *units* have become 5 *tens*, and the 8 *tens* have become 8 *hundreds*, *i.e.*, the *several parts* of the multiplicand have each received a tenfold increase, and, therefore, the whole number has been multiplied by 10. Again,  $2376 \times 100 = 237600$ , where the value of each figure is increased a hundred times by writing to the right of the multiplicand as many cyphers as there are in the multiplier.

(a) When the significant figure of the multiplier is not a unit, as for example 30, 400, or 700. Since these multipliers are the same, as 10 times 3, 100 times 4, or 1000 times 7; the multiplicand is first multiplied by the significant figure 3, 4, or 7, (by Rule V), afterwards the product is multiplied by 10, 100, or 1000 (as in Art. 18) by writing one, two or three cyphers to the right of the product. Thus to multiply 468 by 700, we have the operation in the margin.

19. Hence, if the multiplier to any proposed multiplicand consists of any one or more of the nine digits, followed by a cypher, or any number of cyphers, then multiply according to the following

#### RULE VII.

1°. Place the multiplier under the multiplicand, so that the significant figure of the multiplier shall stand under the unit's figure of the multiplicand, and multiply the successive figures of the multiplicand by the significant figure of the multiplier, according to Rule VI.

2°. Then, to the product thus obtained, place to the right the same number of cyphers as are contained in the multiplier.

#### EXAMPLE.

Multiply 123456789 by 80 and 800000.

|              |                |
|--------------|----------------|
| Multiplicand | 123456789      |
| Multiplier   | 80             |
| Product      | 9876543120     |
| Multiplicand | 123456789      |
| Multiplier   | 800000         |
| Product      | 98765431200000 |

In the first of these examples we multiply first by 8, according to Rule VI, then annex (*i.e.*, join to) to the product *one* cypher, because the multiplier contains *one* cypher, in order to preserve the product in its proper place, as the product of 8 *tens*. In the second example the same rule is followed, but five cyphers are annexed, because the multiplier contains *five* cyphers, in order to preserve the product in its proper place as 9 *hundred of thousands*.

20. If the multiplier or multiplicand, or both, end with cyphers, we may omit them in the working, and proceed according to the following

#### RULE VIII.

Multiply the significant figures of the factors, as directed in Rule V. Then, to the product, affix as many cyphers as have been omitted from the end of the multiplier or multiplicand, or both.

The principle of this annexation has been already explained (No. 18).

## EXAMPLES.

Thus, if 263 be multiplied by 6200, 570 be multiplied by 3200, and 4076800 by 307000.

$$\begin{array}{r} (1) \\ 263 \\ \times 6200 \\ \hline \end{array}$$

$$\begin{array}{r} 526 \\ 1578 \\ \hline \end{array}$$

$$1630600$$

$$\begin{array}{r} (2) \\ 570 \\ \times 3200 \\ \hline \end{array}$$

$$\begin{array}{r} 114 \\ 171 \\ \hline \end{array}$$

$$1824000$$

$$\begin{array}{r} (3) \\ 4076800 \\ \times 307000 \\ \hline \end{array}$$

$$\begin{array}{r} 285376 \\ 122304 \\ \hline \end{array}$$

$$1251577600000$$

The reason is clear: for in the first case, when we multiply by 2, we, in fact, multiply by 200; and 3 multiplied by 200, gives 600. In the second case, the 7 multiplied by 2 is the same as 70 multiplied by 200; and 70 multiplied by 200 gives 14000. In the third the product of the significant figures is  $40768 \times 307 = 12515776$ , to this *five* cyphers must be annexed, because  $100 \times 1000 = 100000$ ; and  $12515776 \times 100000 = 1251577600000$ .

21. It is sometimes advantageous to split up a multiplier which is the product of two or more numbers, and multiply by its factors; thus, if we have to multiply by 36, it is easier to multiply in this case by 6 and 6 ( $6 \times 6 = 36$ ), or by 4 and 9 ( $4 \times 9 = 36$ ), than to multiply by long multiplication, that is, by 3 tens and 6. In any case we have two rows of multiplication, but in the last case we have an addition into the bargain.

## EXAMPLE.

Multiply 57894362 by 48.

Here,  $6 \times 8 = 48$ ; or,  $4 \times 12 = 48$ , then,

$$\begin{array}{r} 57894362 \\ \times 48 \\ \hline 471154976 \\ 231577296 \\ \hline 2778929376 \end{array}$$

22. **Verification of Multiplication.—I.** By casting out nines.—Add together the figures of the multiplicand, multiplier, and product separately, not counting any 9 that may occur, rejecting also 9 whenever, in adding up, the sum amounts to 9 or more; note each result. Multiply the first two remainders, *i.e.*, the remainder arising from casting out nines in the multiplicand and multiplier, retaining, as before, only what is left after the rejection of all the nines from this product, if the sum of the digits exceed nine; then, if the remainder which thus arises is the same as that from the product of the two factors, the operation is likely to be correct, unless there be some compensation of errors, or some figure misplaced.\* Thus, in the annexed example, we say (omitting the 9) 3 and 7 are 10; then 1 and 6 are 7, which write down. Again, 2 and 8 are 10; then 1 and 3 are 4, which is also put down near the multiplier. Lastly, the product of 4 and 7 are 28, and 2 and 8 are 10, which is 1 above 9. Write, then, 1 near the product, and cast the nines out of the product thus, 188253208....r

$$\begin{array}{r} \text{Multiply } 90376 \dots 7 \\ 2083 \dots 4 \end{array}$$

$$\begin{array}{r} 271128 \\ 723008 \\ 1807520 \\ \hline \end{array}$$

\* It is plain, that if any of the figures in the product were made to exchange places, the agreement of the third and fourth results would remain, though the product would be wrong; as would also be the case if one figure were increased and another diminished by the same number; all, therefore, that we can safely infer is, that the agreement spoken of must have place if the work be correct, so that if it fail, the work is wrong.



The truth of all results in multiplication may be proved by using the multiplicand as multiplier, and the multiplier as multiplicand; if the product thus obtained be the same as the product found at first, the results are in all probability true.

EXERCISES IN SIMPLE MULTIPLICATION.

- |  |                                       |                           |
|--|---------------------------------------|---------------------------|
| 1. $342647896 \times 2$  | 5. $91823740526 \times 6$             | 9. $987654321 \times 10$  |
| 2. $654321987 \times 3$  | 6. $6521734782 \times 7$              | 10. $891237654 \times 11$ |
| 3. $376543198 \times 4$  | 7. $485868788 \times 8$               | 11. $647853291 \times 12$ |
| 4. $379865782 \times 5$  | 8. $573241789 \times 9$               | 12. $918273654 \times 12$ |
| 13. $58726341 \times 23$   | 17. $5832764985 \times 4689$          | 21. $685732 \times 15$    |
| 14. $78954236 \times 34$   | 18. $735865000 \times 30700$          | 22. $903421 \times 18$    |
| 15. $98765240 \times 57$   | 19. $958866 \times 804002$            | 23. $356628 \times 36$    |
| 16. $93876129 \times 95$   | 20. $31622777 \times 6324553$         | 24. $838777 \times 48$    |
| 25. $50014000 \times 270$  | 31. $378421896 \times 5928578$        | 37. $777838 \times 49$    |
| 26. $78965430 \times 700$  | 32. $58640987 \times 98067$           | 38. $434560 \times 56$    |
| 27. $43679854 \times 806$  | 33. $5906408 \times 90064$            | 39. $735846 \times 64$    |
| 28. $67869578 \times 903$  | 34. $6437063 \times 5006701$          | 40. $279819 \times 72$    |
| 29. $23589647 \times 678$  | 35. $38926392 \times 77$              | 41. $356718 \times 81$    |
| 30. $86483279 \times 567$  | 36. $29362983 \times 84$              | 42. $817938 \times 96$    |
| 43. $586371829 \times 6738579$   | 48. $98763210 \times 64038040$        |                           |
| 44. $95400621 \times 70030401$   | 49. $49864023 \times 708600470$       |                           |
| 45. $948375628 \times 8764853$   | 50. $275361328 \times 7462170$        |                           |
| 46. $987654321 \times 123456789$                                       | 51. $5432149 \times 8705040950$       |                           |
| 47. $4771213 \times 602059999$   | 52. $30001000300 \times 400100020000$ |                           |
| 53. $2793 \times 812358 \times 857$                                    |                                       |                           |
| 54. $744615 \times 427282 \times 15905$                                |                                       |                           |
| 55. $708421 \times 930937 \times 461762 \times 972744$                 |                                       |                           |
| 56. $1010101 \times 999999 \times 1111111 \times 9090909$              |                                       |                           |
| 57. $9998 \times 9999 \times 10000 \times 10001 \times 10002$          |                                       |                           |
| 58. $9999 \times 9999 \times 9999 \times 9999 \times 9999 \times 9999$ |                                       |                           |
| 59. $9999 \times 99980001 \times 999700029999$                         |                                       |                           |
| 60. $1234 \times 2345 \times 3456 \times 4567$                         |                                       |                           |

DIVISION.

23. The object of division is to find how many times one number is contained in another. The quantity to be divided is called the **dividend**, the quantity by which we divide is the **divisor**, the *number of times* is the **quotient**, and what remains over (if any such there be) is called the **remainder**.  
**Dividend = divisor  $\times$  quotient + remainder.**

The operation of Division is expressed by the sign  $\div$ , which is read *by or divide by*; thus,  $42 \div 7 = 6$ , implies that the result of the division of 42 by 7 is 6. The number 42 which is divided is called the dividend, that which divides, *i.e.* 7 the divisor and the result 6, the quotient. If the divisor be not contained in the dividend an exact number of times, that which remains is called the remainder.

24. The first idea of obtaining the result is to use subtraction and count the times we have to use it.

Thus to find how many times 8 is contained in 34.

$$\begin{array}{r}
 34 \\
 \underline{8} \quad (1) \\
 26 \\
 \underline{8} \quad (2) \\
 18 \\
 \underline{8} \quad (3) \\
 10 \\
 \underline{8} \quad (4) \\
 2
 \end{array}$$

We see we can take 8 away from 34 *four* times in succession, and then we leave 2. But if we had helped ourselves by the multiplication table (of *eight* times) we might have done it more shortly. For since  $5 \times 8 = 40$ , 8 will go 5 times into 40, exactly; therefore 8 will not go 5 times into 34. Again  $4 \times 8 = 32$ , and thus 8 will go 4 times into 34 and leave something over. This "something over" is evidently  $34 - 32$ , or 2.

Let it be required to divide 3168 by 27. Here the quotient will consist of three digits, and therefore there will be at least 3 separate subtractions. Now the figure in the hundreds' place cannot be more than 1, and if the product 27 hundreds, or 2700, be subtracted from the total product 3168, the remainder 468 must contain the products of the tens and units of the quotient multiplied by the divisor 27. We now inquire how often 27 is contained ten times in 468, and this is found to be only once ten times; then subtracting the partial product 27 tens or 270 from 468, the remainder is 198. Lastly, we have to divide 198 by 27 which gives 7 for a quotient and a remainder 9; and, therefore, 3168 contains 27, 100 + 10 + 7, or 117 times leaving 9 for the remainder.

It will be seen that as often as 27 is contained in 31, so many hundred times it will be contained in 3100, or in 3168; and as often as 27 is contained in 46, so many ten times it will be contained in 460, or 468, and in this manner any quotient figure is just as readily obtained as the last or unit's figure of it.

25. The preceding articles contain the principles of division, and all that remains is to apply them in the most economical manner.

#### EXAMPLE.

Suppose we have to divide 2987618 by 3605.

Operation with cyphers in full.

$$\begin{array}{r}
 3605)2987618(800 + 20 + 8 \\
 \underline{2884000} \quad \text{or } 828, \\
 103618 \\
 \underline{72100} \\
 31518 \\
 \underline{28840} \\
 2678
 \end{array}$$

Operation without annexing cyphers.

$$\begin{array}{r}
 3605)2987618(828 \\
 \underline{28140} \\
 10361 \\
 \underline{7210} \\
 31518 \\
 \underline{28840} \\
 2678
 \end{array}$$

Hence we may deduce the following rules:—

### RULE IX.

26. If the divisor be not greater than 12.

1°. Set the divisor at the left hand of the dividend and draw a line beneath which the quotient is to be written.

2°. By the multiplication table find the greatest number of times the divisor is contained in the first figure, or if necessary the first two, or first three figures of the dividend; set down the quotient and carry the remainder to the next figure of the dividend.

3°. Divide this number by the divisor, set down the result as the next figure of the quotient, carry the remainder to the next figure of the dividend, and so on till all the figures of the dividend are exhausted.

The number thus found is the quotient.

### EXAMPLES.

Ex. 1. Divide 25602 by 3.

Placing the dividend and divisor (3) as in the margin, we proceed thus:—  

$$\begin{array}{r} 3 \overline{)256020} \\ 3 \text{ is contained in } 2, \text{ no times; so that nothing is to be placed under the } 2: 3 \text{ is} \\ \text{contained in } 25, 8 \text{ times and } 1 \text{ over; } 8 \text{ and carry } 1: \text{ this } 1, \text{ regarded as} \\ \text{prefixed to the } 6, \text{ gives the number } 16: \text{ we therefore say; } 3 \text{ in } 16, 5 \text{ times and } 1 \text{ over: } 3 \text{ in} \\ \text{ } 10, 3 \text{ times and } 1 \text{ over: } 3 \text{ in } 12, 4 \text{ times: } 3 \text{ in } 0, 0 \text{ times. Therefore, the quotient is } 85340; \\ \text{and this is the complete quotient, as there is no remainder.} \end{array}$$

Ex. 2. Divide 7804623 by 5.

We say, 5 in 7, 1 and 2 over: 5 in 28, 5 and 3 over: 5 in 30, 6: 5 in 4, 0: 5 in 46, 9, and 1 over: 5 in 12, 2, and 2 over: 5 in 23, 4, and 3 over. As there is here a remainder, we annex it, with the divisor 5 under it, to the figures of the quotient and call 1560924  $\frac{3}{5}$ , the complete quotient.

$$\begin{array}{r} 5 \overline{)7804623} \\ 1560924 \frac{3}{5} \end{array}$$

### RULE X.

27. If the divisor be greater than 12.

1°. At the right hand of the dividend, draw a line for the quotient; at its left hand, and in a line with it, write the divisor.

2°. Mark off a number of figures, from the left hand side of the dividend, equal in number to those of the divisor, or one more if necessary and find the greatest number of times the divisor is contained in this number; write down this as the first figure of the quotient.

3°. Multiply the divisor by this number, and place the product under the number marked off from the dividend, and subtract.

4°. Bring down to the remainder the next figure of the dividend, and if the remainder thus increased be greater than the divisor, find the greatest number of times the divisor is contained in it, and write this number as the second figure of the quotient, but if not bring down the next figure of the dividend, or more, until it is greater—recollecting to place a cypher in the quotient for every figure of the dividend so taken except the last: find how often the divisor is contained in this number; then multiply, subtract, and bring down, &c., as before, till all the figures of the dividend are exhausted.

The number thus obtained is the quotient required.

## EXAMPLES.

Ex. 1. Let it be required to divide 256434 by 346.

Looking at the leading figure of the divisor, and also at that of the dividend, with the view of seeing whether the latter contains the former, which it does not, 3 being greater than 2; we therefore commence with the number 25, formed by the first *two* figures of the dividend, and seeing that 3 is contained in 25 8 times, we should put 8 for the first quotient figure; but bearing in mind that when the *whole* divisor is multiplied by this 8 we must attend to the *carryings*; we perceive that 8 is too great, we therefore try 7, and find 7 times 346 to be 2422, a number less than 2564 above it, so that we can *subtract*; the remainder is 142, which, when the next figure of the dividend is brought down, becomes 1423. We now take this as a dividend, and looking at the *leading figures* in this new dividend and the divisor, we see that the latter *will* go 4 times, we therefore put 4 for the second quotient figure, and multiplying and subtracting we get 39 for the second remainder, and, by bringing down another figure we get 394 for a new dividend; the divisor goes into this *once*, so that the quotient is 741, and the final remainder 48; this remainder must be annexed with the divisor underneath to the quotient figures, so that the complete quotient is 941  $\frac{48}{346}$ , which is the 346th part of 256434.

$$\begin{array}{r}
 346)256434(741 \text{ quotient.} \\
 \underline{2422} \\
 1423 \\
 \underline{1384} \\
 394 \\
 \underline{346} \\
 48
 \end{array}$$

Ex. 2. Divide 108419716214 by 5783.

$$\begin{array}{r}
 5783)108419716214(18748005 \text{ quotient.} \\
 \text{Quotient figure (1).....} \quad \underline{5783} \\
 \phantom{000000}50589 \text{ ..... 1st remainder with next figure.} \\
 \phantom{000000}\underline{46264} \\
 \phantom{0000000}43257 \text{ ..... 2nd} \quad \text{,,} \quad \text{,,} \\
 \phantom{0000000}\underline{40481} \\
 \phantom{00000000}27761 \text{ ..... 3rd} \quad \text{,,} \quad \text{,,} \\
 \phantom{00000000}\underline{23132} \\
 \phantom{000000000}46296 \text{ ..... 4th} \quad \text{,,} \quad \text{,,} \\
 \phantom{000000000}\underline{46264} \\
 \phantom{0000000000}322 \text{ ..... 5th} \quad \text{,,} \quad \text{,,} \\
 \text{☞ (0).....} \quad \underline{\phantom{0000000000}} \\
 \phantom{00000000000}3221 \text{ ..... 6th} \quad \text{,,} \quad \text{,,} \\
 \text{☞ (0).....} \quad \underline{\phantom{00000000000}} \\
 \phantom{000000000000}32214 \text{ ..... 7th} \quad \text{,,} \quad \text{,,} \\
 \phantom{000000000000}\underline{28915} \\
 \phantom{0000000000000}3299 \text{ final remainder.}
 \end{array}$$

It must be noticed that if any *dividend* formed by a remainder and a figure brought down should be less than the divisor, that the divisor will go *no times* in that dividend; so that a 0 will be the corresponding quotient figure; and that, then, a second figure must be brought down as in the operation annexed. The steps marked ☞ are inserted merely to show the principle. In practice we simply put down the two noughts in the quotient, and go at once to 32214 for the divisor.

28. Whenever the divisor can be separated into two factors, the division may be effected by the following rule:—

## RULE XI.

1°. Divide by one factor, setting down the quotient and remainder.

2°. Divide the quotient by the other factor, setting down the quotient and remainder; the second quotient thus obtained is the required quotient.

3°. The proper remainder is found by multiplying the second remainder by the first divisor, and to the product adding the first remainder.

This rule may be extended to the case of the divisor being divisible into any number of factors, as follows, always setting down as remainder the product of the partial remainder by all the previous divisors increased by the previous remainder.

## EXAMPLES.

Ex. 1. Divide 569736869 by 15.

Here the remainder 2 in the first quotient is 2 units of the upper line; but the remainder 4 in the second line consists of 4 units of the second line; and as each unit in the second line is three times as great as each unit in the upper line, the remainder 4 is equal to  $3 \times 4$  units of the upper line, i.e., is equal to 12 ordinary units, hence the whole remainder is  $2 + 12$ , or is 14.

Ex. 2. Divide 8327965 by 72 and 99.

$$72 \left\{ \begin{array}{l} 8 \mid 8327965 \\ 9 \mid 925329 \dots 4 \\ \hline 115666 \dots 1 \end{array} \right.$$

$$99 \left\{ \begin{array}{l} 9 \mid 8327965 \\ 11 \mid 925329 \dots 4 \\ \hline 84120 \dots 9 \end{array} \right.$$

To deduce the remainders which would have been left had the divisions been performed by 72 and 99 in the usual way, we may observe that the first partial remainder 4 must be units; but the second dividend being so many collections of 9 units each, the second remainder must be regarded as so many collections of 9 units each; hence the true remainders in these examples are respectively

$$1 \times 9 + 4 = 13, \text{ and } 9 \times 9 + 4 = 85.$$

Ex. 3. Divide 2671998 by 192.

$$192 \left\{ \begin{array}{l} 4 \mid 2671998 \\ 6 \mid 667999 \dots 2 \\ 8 \mid 111333 \dots 1 \\ \hline 13916 \dots 5 \end{array} \right. \quad \begin{array}{l} 1 \times 4 + 2 = 6 \\ 5 \times 6 \times 4 + 6 = 126 \end{array}$$

Ans.—Quotient = 13916  
Remainder = 126

29. Division may also be abridged where the divisor is terminated by a cypher or cyphers; we proceed as follows:—

## RULE XII.

1°. Cut off the cyphers from the divisor, and as many figures from the right hand of the dividend as there are cyphers so cut off at the right hand end of the divisor, then proceed with the remaining figures in the usual manner (Rule X or XI), and if there are anything remaining after the division annex those figures which are cut off from the dividend; otherwise, the figures cut off will be the remainder.

## EXAMPLES.

Ex. 1. Divide 3704196 by 20.

$$\begin{array}{r} 2,0 \overline{) 370419,6} \\ \underline{185209} \quad \frac{18}{20} \end{array}$$

Ex. 2. Divide 31086901 by 7100.

$$\begin{array}{r} 71,00 \overline{) 310869,01} (4378 \frac{7101}{7100} \\ \underline{284} \\ 268 \\ \underline{213} \\ 556 \\ \underline{497} \\ 599 \\ \underline{568} \\ 31 \end{array}$$

In the first of these examples you mark off with a turned comma the cypher or 0 in the divisor, and the first figure 6 to the right in the dividend; this is equivalent to dividing both divisor and dividend by 10. You next divide the remaining figures 370419, to the left in the dividend, by the divisor 2, according to Rule IX; thus is obtained the quotient 185209, and remainder 1; to this remainder you annex the figure 6, which was cut off, and you have the complete remainder 16. The quotient may now be correctly represented thus, 185209 $\frac{1}{2}$ .

In the second example you follow the same rule; that is, you cut off two cyphers in the divisor and two figures in the dividend, and obtain the quotient in the usual way, which is 4378, and remainder 31; to this 31 annex the two figures cut off from the dividend, and you have the complete remainder 3101.

30. **Verification of Division.**—(1.) Multiply the quotient by the divisor, or the divisor by the quotient, and to the product add the remainder, if there be one. The result ought to be the same as the dividend; because we are only adding the divisor the same number of times, as it was subtracted in the operation of division.

(2.) Subtract the remainder, if any, from the dividend, and divide the difference so obtained by the quotient. The result should be equal to the divisor, if the working be correct.

#### EXERCISES IN SIMPLE DIVISION.

- |                                   |                                    |                           |
|-----------------------------------|------------------------------------|---------------------------|
| 1. 135792695 $\div$ 2             | 5. 400678493 $\div$ 6              | 9. 254096146 $\div$ 10    |
| 2. 584697386 $\div$ 3             | 6. 276586437 $\div$ 7              | 10. 1101182267 $\div$ 11  |
| 3. 399345884 $\div$ 4             | 7. 6947421006 $\div$ 8             | 11. 1095137170 $\div$ 12  |
| 4. 298244760 $\div$ 5             | 8. 2470263075 $\div$ 9             | 12. 59437955312 $\div$ 12 |
| 13. 6489275432689467 $\div$ 14    | 18. 987654321012345 $\div$ 66      |                           |
| 14. 598432789648320758 $\div$ 22  | 19. 9357864837986496 $\div$ 70     |                           |
| 15. 56983475689268 $\div$ 36      | 20. 483795864973206789 $\div$ 120  |                           |
| 16. 9357864837986496 $\div$ 50    | 21. 3591321391621911 $\div$ 132    |                           |
| 17. 5986432685946896 $\div$ 63    | 22. 4902550716552769 $\div$ 144    |                           |
| 23. 987654321670 $\div$ 3000      | 26. 27410012221749999 $\div$ 37009 |                           |
| 24. 17932810740000 $\div$ 2600    | 27. 149778007923526 $\div$ 618934  |                           |
| 25. 14710962989869 $\div$ 1709    | 28. 42243968241835 $\div$ 872169   |                           |
| 29. 31415926536 $\div$ 648        | 34. 6345670000000 $\div$ 45630425  |                           |
| 30. 100000000000000 $\div$ 11111  | 35. 6680943744279021 $\div$ 467896 |                           |
| 31. 4895300478 $\div$ 5678        | 36. 4842315713782 $\div$ 570634    |                           |
| 32. 655650751827 $\div$ 396218    | 37. 815240906170 $\div$ 763054     |                           |
| 33. 33201610691892 $\div$ 7043628 | 38. 34939053124326 $\div$ 8431072  |                           |

39. Divide 31415926536 into 100 . . . . with as many noughts added as may be necessary to give ten figures in the quotient.

- 
- Express in figures, ten thousand and four.
  - $29483 + 7648 + 32479 + 586 + 298364 + 98765 + 897 + 789 + 5678 + 99$ .
  - From 6794006897 take 3985160534.
  - Multiply 94785830 by 78060.
  - Divide 5688208152 by 594.
  - Express in figures, one hundred million, one hundred thousand and one hundred.
  - Add together 90473, 9456, 268, 59, 45694, 5437, 87668497, 2837, 9865, 3652, 999, and 8888.
  - Find the difference between 10000000000 and 87649786.
  - Multiply 326904678 by 3060900.
  - Divide 236487698743 by 85409.
  - Express in figures, one hundred and three million, eighty thousand, two hundred and seven.

12. Add together 69074, 6745, 723, 29, 931648, 9005, 76245, 54267, 47096, and 7777.
13. From 78600070000 take 6974208506.
14. Multiply 167409678 by 768900.
15. Divide 60000007006490088805 by 98706543.
16. Express in words and in figures how much greater the value of one 5 is than the other in the number 658457.
17. Multiply 129847 by 468. If, in the process, you shift all the figures resulting from the multiplication of the multiplicand by 4 two places farther to the left and then add, of what two numbers will the result be the product?
18. What number subtracted from 850967 will leave 3946?  
The 365th part of a number is 101001, what is the number?
19. The digits in the units' and millions' places of a number are 4 and 6 respectively, what will be the digits in the same places when 99999 is added to the number.
20. What number must be added to sixty-nine thousand four hundred and twenty-seven to produce three hundred and twenty-five millions, seven thousand and twenty-one?
21. Find the sum, difference, and product of 12345678 and 288144412.  
Find the sum, difference, and product of 1234567 and 4321089.
22. 15996 tons of coal are exported in 43 ships: how many tons does each ship on the average carry?
23. How many years of 365 days each in 46355 days?
24. How often can you subtract 6 from 47112?
25. How many ships, each carrying 673 men, can transport an army of 22882 men?
26. By what number must you divide 7460020 in order that the quotient may be 52907 and the remainder 133?
27. 2036809 divided by a certain number gives a quotient 2031 with a remainder of 1747: find the dividing number?
28. A ream of paper contains 20 quires of 24 sheets each; on each page there is room for 34 lines of writing: how many may be written in the ream?
29. What is the number of holes in a sheet of perforated zinc, containing 1519 square inches, if there be 85 in the square inch.
30. What will remain after subtracting 213 as often as possible from 83216?
31. The product of two numbers is 1270374 and half of one of them is 3129: what is the other number?
32. Find the sum, difference, product, and quotient of 1653125 and 13225.
33. Find the sum, difference, product, and quotient of 9765625 and 78125.

## DECIMAL FRACTIONS.

31. ARITHMETICAL operations become lengthy and troublesome if they involve many vulgar fractions of different denominations; it becomes necessary, therefore, to devise a method of expressing fractions in such a manner that they may be easily reduced to the same denomination. To effect this all fractions are reduced to others having for denominators 10, 100, 1000, &c. Such fractions are called decimal fractions.

32. Decimals occur so frequently in all computations relating to Nautical Astronomy, that it becomes absolutely necessary to have a knowledge of their application and their relation to Vulgar Fractions.

33. In the Notation of Integers or common numbers, the actual value of each figure depends upon its position with respect to the place of units, its value in any one position being one-tenth of what it would be if it stood one place further to the left; thus the number 1111 denotes one thousand, one

hundred, one ten, and one unit, or  $1000 + 100 + 10 + 1$ , where the second unit beginning with the right hand one is ten times the first, the third is ten times the second, the fourth ten times the third, and so on; or beginning with the first on the left, the second is the tenth part of the first, the third the tenth part of the second, and so on, till we come down to the last unit, which is merely one; or in other words, the figures decrease in a tenfold ratio from left to right.

34. Now we may evidently extend this principle still further, and on the same plan may represent one-tenth of *one*, one-tenth of *this*, or one-hundredth of one, one-thousandth of *one*, and so on, by simply putting some mark of separation between the *integers* and these *fractions*. The mark actually used is a *dot* or *full stop*, and is called the *decimal point*, thus  $1111'1111$ .\* The unit (or 1) next the dot, on the left, is 1; the unit one place from this on the left is 10; the next is 100; the next 1000, and so on. In like manner, the unit next the decimal point, on the right, is  $\frac{1}{10}$ , the next  $\frac{1}{100}$ , the next  $\frac{1}{1000}$ , and so on. In other words, any figure one place to the right of the unit's place will be one-tenth of what it would be if it were in the unit's place, and will thus really denote a decimal fraction; any figure two places to the right of the unit's place will be one-hundredth of what its value would be if it were in the unit's place, and so on for any number of figures, as in the following table, which may be regarded as an extension of the numeration table.

|           |                        |                    |            |           |       |        |   |         |             |              |                  |                      |             |                 |
|-----------|------------------------|--------------------|------------|-----------|-------|--------|---|---------|-------------|--------------|------------------|----------------------|-------------|-----------------|
| 7         | 6                      | 5                  | 4          | 3         | 2     | 1      | . | 2       | 3           | 4            | 5                | 6                    | 7           | 8               |
| millions. | hundreds of thousands. | tens of thousands. | thousands. | hundreds. | tens. | units. |   | tenths. | hundredths. | thousandths. | ten thousandths. | hundred thousandths. | millionths. | ten millionths. |

35. This being agreed upon, it follows that a decimal may either be considered as the sum of as many fractions as it contains digits, or as a single fraction; thus:—

$$.567 = \frac{5}{10} + \frac{6}{100} + \frac{7}{1000} = \frac{567}{1000}.$$

$$.0305 = \frac{0}{10} + \frac{3}{100} + \frac{0}{1000} + \frac{5}{10000} = \frac{0305}{10000}.$$

$$18.204 = 18 + \frac{2}{10} + \frac{0}{100} + \frac{4}{1000} = \frac{18204}{1000}.$$

36. Hence, a decimal is always equivalent to the vulgar fraction whose numerator is the decimal considered as integral, that is, the number itself, when the decimal point is suppressed, and whose denominator is 1 followed by as many cyphers as there are decimal places in it.

37. We generally speak of any figure in a decimal as being in *such a place of decimals*; thus, for instance, in  $3.14159$ , we should say that the 5 is in the fourth place of decimals, the 9 in the fifth place, and so on, reckoning from left to right.

38. The figures 1, 2, 3, 4, 5, 6, 7, 8, 9, in a decimal are sometimes called *significant figures* or *digits*; thus, in such a decimal as  $.0002345$ , we should

\* The decimal point should be put at the top of the line of figures, thus— $5.7$ , because  $5.7$  with a stop at the bottom is used in most works to mean  $5 \times 7 = 35$ .



say that 2 is a significant digit, because it is the first figure which indicates a number, the cyphers only serving to fix the place in which the 2 occurs.

39. Numbers made up of whole numbers and fractions, either vulgar or decimal, are called mixed numbers; for instance,  $368\frac{4}{10}$  is a mixed number, the figures which precede the decimal point (the 3, the 6, and the 8) are whole numbers or integers, while those which follow the point ( $\frac{4}{10}$ ) are decimals.

40. To read off, or express in words, decimal fractions, *read the decimal figures as if whole numbers, and to the last figure add the name of the order determined by the place it occupies*; thus,  $\cdot 734$  is read *seven hundred and thirty-four thousandths*;  $58\cdot 64327$  is read *fifty-eight, together with sixty-four thousand three hundred and twenty-seven hundred-thousandths*;  $\cdot 080905$  is read *eighty thousand nine hundred and five millionths*.

In reading decimals as well as whole numbers, the *unit's* place should always be made the *starting* point. It is advisable for the learner to apply to every figure the name of its order, or the place which it occupies, before attempting to read them. Beginning at the unit's place he should proceed towards the right, thus—*units, tenths, hundredths, thousandths, &c.*, pointing to each figure as he pronounces the name of its order. In this way he will be able to read decimals with as much ease as he can whole numbers.

41. The value of the decimal figures depending entirely on the place they occupy with respect to the point which separates the units from the tenths, any number of cyphers on their right may be annexed or effaced, without altering the value of the *significant* figures. For instance,  $0\cdot 7$  is the same as  $0\cdot 70$ , because the number that expresses the decimal fraction becomes ten times greater while its parts become hundredths, and are therefore diminished ten times,

$$\text{thus } \frac{7}{10} = \frac{70}{100} = \frac{700}{1000}, \text{ \&c.}$$

and hence it is evident that annexing cyphers to the right hand of decimals does not change their value, for we only multiply both numerator and denominator by 10, 100, &c., and consequently does not alter their value at all. Again, take a decimal such as  $\cdot 56$ , which, as already explained, means 5 tenths 6 hundredths, it will follow that  $\cdot 560$  means 5 tenths, 6 hundredths, no thousandths; whence the addition of the cypher to the right-hand has made no alteration in the value of the decimal. In fact,

$$\cdot 56 = \frac{56}{100} \text{ and } \cdot 560 = \frac{560}{1000} = \frac{56}{100}.$$

Similarly  $\cdot 23$ ,  $\cdot 230$ , and  $\cdot 2300$ , are all of equal value, for expressed as fractions they are respectively  $\frac{23}{100}$ ,  $\frac{230}{1000}$ , and  $\frac{2300}{10000}$ .

42. But placing cyphers between the decimal point and the other decimal figures does alter the value of the decimal, because this alters the place of the significant digits, the value being diminished ten times for each cypher that is prefixed,

$$\text{thus } \cdot 7 = \frac{7}{10}, \cdot 07 = \frac{7}{100}, \cdot 007 = \frac{7}{1000}, \text{ and so on.}$$

We infer from this, that as the value of a decimal is *decreased* ten-fold for every cypher added to the left-hand, we do in fact *divide* a decimal by 10, by 100, by 1000, &c., as we shift the decimal point one, two, three, &c., places to the *left*; and that conversely by shifting the decimal point one, two, three, &c., places to the *right*, we multiply the decimal by 10, by 100, by 1000, &c. For instance, the expression  $56\cdot 789$  is divided by 10 if written  $5\cdot 6789$ , is

divided by 100 if written .56789, and is divided by 1000 if written .056789; whereas the expression .00723 is multiplied by 10 if written .0723, is multiplied by 100 if written .723, and is multiplied by 1000 if written 7.23.

### EXAMPLES FOR PRACTICE.

Express as decimals—

1.  $\frac{3}{10}$ ,  $\frac{3}{100}$ ,  $\frac{3}{1000}$ , and  $\frac{33}{10}$ ; also  $\frac{7}{10}$ ,  $\frac{117}{100}$ ,  $\frac{33}{1000}$ , and  $\frac{1015}{1000}$ .
2.  $\frac{1}{100}$ ,  $\frac{21}{10000}$ ,  $\frac{117}{100000}$ ,  $\frac{3}{1000000}$ ,  $\frac{1}{10}$ ,  $\frac{53}{100}$ ,  $\frac{700}{1000}$ ,  $\frac{11}{10000}$ , and  $\frac{13700}{1000000}$ .
3.  $\frac{301}{10}$ ,  $\frac{40001}{100}$ ,  $\frac{5300415}{100000}$ ,  $\frac{60000101}{1000000}$ ,  $\frac{441}{10000000}$ ,  $\frac{331}{100000000}$ ,  $\frac{601}{1000000000}$ .
4.  $\frac{0178}{10000}$ ,  $\frac{0178}{100}$ ,  $\frac{0178}{100000}$ ,  $\frac{01}{1000000}$ ,  $\frac{0}{10000000}$ ,  $\frac{6203}{100000000}$ ,  $\frac{90}{1000000000}$ .
5.  $\frac{30142}{100000}$ ,  $\frac{672819}{1000000}$ ,  $\frac{672819}{10000000}$ ,  $\frac{67281900}{100000000}$ .
6. In the following mixed numbers write the fractional parts in decimals :—  
 $7\frac{60}{10000}$ ,  $43\frac{2145}{100000}$ ,  $9\frac{7823457}{100000000}$ ,  $1\frac{1}{10000000}$ , and  $35\frac{721341}{100000000}$ .
7.  $53\frac{9}{10}$ ,  $47\frac{73}{100}$ ,  $6\frac{60}{10000}$ ,  $3\frac{7000}{100000}$ ,  $9\frac{400637}{100000000}$ ,  $902\frac{30401}{100000000}$ .
8. Express as decimal fractions the following :—  
 Seventy-three *thousandths*; one hundred and ninety-seven *ten thousandths*; one *millionth*; two hundred and sixty-one *hundred thousandths*; one thousand and one *ten millionths*.
9. Express as decimals the following :—  
 One, and fifty-four *hundredths*; twenty-four, and seventy-nine *thousandths*; three hundred and fifteen, eight *thousandths*, and fifty *millionths*; eleven hundred *millionths*; nine *thousandths*, and three hundred *thousandths*.
10. One tenth; three hundredths; five thousandths; one hundred and five thousandths; two millionths; sixty millionths; forty-one and eight hundredths; one thousand and one thousandth; thirty and six millionths; one hundred thousandth; two thousand three hundred and seventy-five hundred millionths.
11. Express as vulgar fractions—  
 .7, .07, .007, .000007, .327, 3.27, 32.7, .45697, 456.97, .893, .0000893.
12. Express in words the following decimals and mixed numbers :—  
 .283, .5321, .74895, .821056, 27.8354, 34.0009, 43.101007, 23.75, 2.375, .2375, .00002375.
13. Express as vulgar fractions, and reduce to the lowest terms :—  
 .0000001024, .00000000576, .9241, 67.09, .5064919, and .0000000000000065536.
14. Express in words the following :—  
 .6, .92, .5498, 7.07, 26.405, .000001, .00037, 11.101101, .0440308, .82344, .13236.
15. Write in words 9.0457; 4004.0000345; 3.400; 524000634.0008034; .000003705; .000024056; 7005.000000674; 100000.0000001; 10.001; 9.000028; 1.0006003.
16. 1.0000001; .10000001; .000000001; 1.13004; 9.203167; 4.3008004; 27.4627350.

### ADDITION.

43. Decimals, or integers and decimals mixed, may be added together precisely as in whole numbers, care being taken so to arrange the figures that all the decimal points fall exactly under one another. This will ensure that *tenths* fall under *tenths*, *hundredths* under *hundredths*, &c. The reason of this arrangement will appear from the following consideration: if this rule were *not* observed, tenths would fall under hundredths, or hundredths under thousandths, as the case might be; and we should be attempting to add together fractions which had not common denominators. But if we arrange the decimal points all exactly beneath one another, tenths fall under tenths, hundredths under hundredths, &c., in other words, by so arranging them we at once bring the several fractions to a common denominator, and can proceed to add them together. The decimal point, in the answer, will fall exactly beneath the decimal points in the quantities to be added. When the sum of any figures exceeds 10, 20, &c., *carrying* to the next denominator will be performed exactly as in whole numbers, whether the given quantities are all decimals, or are mixed integers or decimals. For as the value of each figure decreases tenfold as we proceed from left to right, the rules of ordinary addition are immediately applicable.

We have, therefore, the following rule for addition:—

### RULE XIII.

1°. Place the quantities so that their decimal points shall be in the same vertical line; for then the quantities of the same denomination will stand together.

2°. Then proceed as in addition of whole numbers.

### EXAMPLES.

For instance, let it be required to add together .8, .78, and .678.

Where we see that after writing in the answer 8 in the place of *thousandths*, that 7 *hundredths* and 8 *hundredths* added together make 15 *hundredths*; but 15 *hundredths* are 1 *tenth* and 5 *hundredths*, writing 5 in the place of *hundredths*, and carrying one to the place of *tenths*, we obtain 22 *tenths*; but 22 *tenths* are properly written as 2 *integers* and 2 *tenths*.

Again, where integers and decimals are mixed

Where writing 5 in the place of *ten thousandths*, the sum of 7 *thousandths* and 7 *thousandths* is 14 *thousandths*; writing 4 in the place of *thousandths*, and carrying 1 to the place of *hundredths*, we obtain 10 as the sum in the *hundredths* place; but 10 *hundredths* are 1 *tenth*, carrying 1 to the place of *tenths*, we have 10 *tenths*; but as 10 *tenths* are 1 *unit*, we carry 1 to the

place of *integers*, and write 6 in the place of *units*, and 4 in the place of *tens*.

Ex. 3. Add together 0.35, 47.4, and 9.12.

$$\begin{array}{r} 0.35 \\ 47.4 \\ 9.12 \\ \hline 56.87 \end{array}$$

Ex. 4. Add together 23.628, 4.1056, .0137, and .0042.

$$\begin{array}{r} 23.628 \\ 4.1056 \\ .0137 \\ .0042 \\ \hline 27.7515 \end{array}$$

Ex. 5. Add together 1234.6789, 13, 170, .0054, .5, and 87.142.

$$\begin{array}{r} 1234.6789 \\ 13 \\ 170 \\ .0054 \\ .5 \\ 87.142 \\ \hline 1505.3263 \end{array}$$

Ex. 6. Add together 66199.3226, .301, 54.5, .00632, 1000, .07, and 32745.80008.

$$\begin{array}{r} 66199.3226 \\ .301 \\ 54.5 \\ .00632 \\ 1000 \\ .07 \\ 32745.80008 \\ \hline 100000 \end{array}$$

### EXAMPLES FOR PRACTICE.

Find the value of

1. 225, 3.086, 12.17, .0051, and 729.54; 2.63, .263, .0263, and .000263.
2. 8.1, 40.652, 98.51, 695.7, and 43.9706; 69.75, 0.97, 0.059, 673.5, 4.8, and 932.6.
3. 897.4, 63.18, 400.03, 7.9, 63.9, and 5.0079; .00162, .1701, 325, 2.7031, and 3.000701.
4. 3608.26, 360.826, 36.0826, 3.60826, and .22314; 467.3004, 28.78249, 1.29468, and 3.78241.
5. 36.053, .0079, .000952, 417, 85.5803, and .0000501.
6. 87.1 + 0.376 + .0056 + 49 + 3.009 + .709; 293.0072, 89.00301, 29.84567, 924.00369, and 72.39602.
7. .8 + .046 + 9.1 + 3.09 + 8.6409 + 32; 1.721341, 8.620047, 51.720345, 2.684 and 62.304607.
8. 1 + .1 + .01 + .001 + .0001; 4.07 + .6201 + .936 + 29.08 + 1.0101 + 7.
9. 1 + .2 + .03 + .004 + .0005; .7, 50.08, 312.907, .4093, 494.5, and 87.003.

What is the sum of

10. Eighteen hundredths; seven hundred and forty-five hundred thousandths; nine thousandths; forty-three millionths; five hundred and eight thousandths; one hundred and thirty-two thousandths; one thousand and forty-four ten millionths; twenty-five hundredths; five tenths; and six hundred and five thousandths?

11. Add together 9 tenths, 92 hundredths, 162 thousandths, 489 thousandths, and 92 millionths.

12. Add together 1 tenth, 2 hundredths, 16 thousandths, 7 millionths, 26 thousandths, 95 ten millionths, and 7 ten thousandths.

## SUBTRACTION.

44. In subtraction of decimals, or of integers and decimals mixed, for reasons precisely similar the decimal points must be arranged to fall exactly beneath one another; and then the smaller quantity can be subtracted from the larger in the same manner as in whole numbers, *thousandths* being taken from *thousandths*, *hundredths* from *hundredths*, and *tenths* from *tenths*. The decimal point in the answer will fall exactly beneath the decimal points in the subtrahend and minuend, cyphers may be added (or supposed to be added) to the *right* of the decimal figures in the minuend, as this will not alter the value (see page 32), and the subtraction may proceed as in whole numbers.

We have, therefore, the following rule for subtraction:—

### RULE XIV.

1°. *Place the quantities so that their decimal points shall be in the same vertical line.*

2° *Next proceed as in subtraction of whole numbers.*

### EXAMPLES.

Ex. 1. Subtract '756 from '897.

$$\begin{array}{r} .897 \\ -.756 \\ \hline .141 \end{array}$$

Here the difference between 6 *thousandths* and 7 *thousandths* is 1 *thousandth*, between 9 *hundredths* and 5 *hundredths* is 4 *hundredths*, between 8 *tenths* and 7 *tenths* is 1 *tenth*.

Ex. 3. From 98765'4321 take 99'99.

$$\begin{array}{r} 98765'4321 \\ -99'99 \\ \hline 98665'4421 \end{array}$$

Ex. 5. Subtract '0000999 from '01.

$$\begin{array}{r} .01 \\ -.0000999 \\ \hline .0099001 \end{array}$$

Ex. 2. From 37'6 take '907.

In this instance 37'6 may be written 37'600.

$$\begin{array}{r} 37\ 600 \\ -.907 \\ \hline 36'693 \end{array}$$

Ex. 4. Subtract '97658 from 5'1394.

$$\begin{array}{r} 5'1394 \\ -.97658 \\ \hline 4'16282 \end{array}$$

In subtracting 8, 0 is supposed to occupy the place above it as 5'13940 = 5'1394.

Ex. 6. From 1 take '47712.

$$\begin{array}{r} 1 \\ -.47712 \\ \hline .52288 \end{array}$$

In examples of this kind (Ex. 5, 6, and 8) when the number of decimal figures in the lower line exceeds the number of figures in the upper, it is advisable to mentally supply cyphers to make up the deficiency in the upper line. This may be done without altering the value of the upper line.

Ex. 7. Subtract 247'258746 from 347'258745.

$$\begin{array}{r} 347'258745 \\ 247'258746 \\ \hline 99'999999 \end{array}$$

Ex. 8. From 1 take '000001.

$$\begin{array}{r} 1 \\ '000001 \\ \hline '999999 \end{array}$$

### EXAMPLES FOR PRACTICE.

#### Subtract

1. 3'07 from 6'501; '79999 from 9; 2'9989 from 3; '999999 from 9.
2. '0090806 from 39'857; '00032 from 32; '876534 from 8'21314; 364'3123 from 456'0546.
3. '99 from 1; '00000099 from 99; '000001 from 10; 3'29 from 999; 25'6050 from 567'392.
4. '9682347 from 65'00001; '79999 from 9; 9'163 from 81'6823401.
5. '000001 from '0001; '000004 from '0004; '00032 from 32; '87623 from 24681.
6. From 700 take 7 hundredths; from '0001 take '0000001.
7. From 42 hundredths take 42 thousandths; 154 millionths from 6231 hundred thousandths.
8. From 96 thousandths take 909 ten thousandths; 92 thousandths from 29 thousand.

### MULTIPLICATION.

45. We have stated that for every place we shift the decimal point to the *right* we increase the value of the decimal *ten-fold*, for every place we shift it to the *left* we decrease it *ten-fold*. Now, in multiplying two decimals together, since the law of *local value* hold with regard to the digits comprising the decimals, the process of multiplication will be performed exactly as in ordinary whole numbers; the only matter requiring consideration will be the proper position of the decimal point.

Suppose we have to multiply 4'935 by 6'28, and let us suppose the decimal point in each case removed to the extreme right. Then (Art. 42, page 33) we have multiplied the number 4'935 by 1000, and the number 6'28 by 100, and we have obtained the numbers 4935 and 628 respectively. Now,  $4935 \times 628 = 3099180$ , but as we increased our original numbers one thousand and one hundred fold respectively, it is evident our product is increased  $1000 \times 100$ , or one hundred thousand fold. Dividing, therefore, the above result, 3099180 by 100000, or what is the same thing (Art. 42, page 33), writing it 3099180 and removing the decimal point 5 places to the left, we get for the product of the numbers 4'935 and 6'28, the result 30'99180. It will be seen that the number of decimal places on the product, namely, 5, is the sum of the numbers of the decimal figures in the two given numbers.

We have, therefore, the following rule for multiplication:—

#### RULE XV.

*Multiply the numbers together, as whole numbers, and point off as many decimal places in the product (beginning at the right) as there are decimal places in the multiplier and multiplicand together.*

When the decimal places to be pointed off are more in number than the figures of the product, make up the proper number by prefixing cyphers to the product.

#### EXAMPLES.

Ex. 1. Multiply 34'11 by 3'72.

$$\begin{array}{r} 34'11 \\ 3'72 \\ \hline 6822 \\ 23877 \\ 10233 \\ \hline 126'8892 \end{array}$$

Ex. 2. Multiply 236000 by '48.

$$\begin{array}{r} 236000 \\ '48 \\ \hline 1888 \\ 944 \\ \hline 113280'00 \end{array}$$

In 34'11 are two decimals; in 3'72 are two; therefore four decimal places are pointed off.

The product of 236 by '48 is 11328; in 236000 are no decimals; in '48 are two decimals; therefore two places are pointed off in the product.

Ex. 3. Multiply  $56\cdot3$  by  $\cdot08$ .

$$\begin{array}{r} 56\cdot3 \\ \cdot08 \\ \hline 4504 \end{array}$$

In  $56\cdot3$  is one decimal; in  $\cdot08$  are two; therefore three places are pointed off in the product.

Ex. 5. Multiply  $\cdot0048$  by  $\cdot000012$ .

$$\begin{array}{r} \cdot0048 \\ \cdot000012 \\ \hline \cdot0000000576 \end{array}$$

The product of 48 by 12 is 576; in  $\cdot0048$  are four decimals; in  $\cdot000012$  are six decimals; therefore the product must contain ten decimals (four and six), and seven cyphers are prefixed to 576, whence the product is  $\cdot0000000576$ , as above.

Ex. 4. Multiply  $5\cdot63$  by  $\cdot00005$ .

$$\begin{array}{r} 5\cdot63 \\ \cdot00005 \\ \hline 0\cdot0002815 \end{array}$$

In  $5\cdot63$  are two decimals; in  $\cdot00005$  are five; therefore three cyphers must be prefixed to the product 2815, and seven decimals marked off.

Ex. 6. Find the value of  $1\cdot005 \times \cdot005 \times \cdot0064$ .

$$\begin{array}{r} 1\cdot005 \\ \cdot005 \\ \hline 005025 \\ \cdot0064 \\ \hline 20100 \\ 300150 \\ \hline 0000321600 \end{array}$$

## EXAMPLES FOR PRACTICE.

Find the value of

- $2\cdot5 \times 4$ ;  $\cdot25 \times 40$ ;  $2\cdot5 \times 476$ ;  $2\cdot5 \times 4\cdot76$ ;  $\cdot0025 \times 4\cdot76$ ;  $\cdot025 \times 0476$ .
- $\cdot0002 \times \cdot00101$ ;  $90\cdot01 \times 0\cdot034$ ;  $\cdot0008 \times \cdot00014$ ; and  $\cdot6005 \times \cdot0035$ .
- $\cdot0783 \times 461$ ;  $2764 \times 96$ ;  $\cdot06948 \times \cdot0087$ ; and  $\cdot00043 \times 4700$ .
- $21\cdot56 \times \cdot0035$ ;  $24\cdot35 \times \cdot074$ ;  $35\cdot85 \times 2\cdot09$ ; and  $\cdot004716 \times \cdot22240656$ .
- $1\cdot075 \times \cdot0101$ ;  $8\cdot004 \times \cdot004$ ;  $\cdot0006 \times \cdot00012$ ; and  $\cdot923521 \times \cdot28629151$ .
- $100\cdot0008 \times \cdot000306$ ;  $7535060 \times 62\cdot3906$ ; and  $31\cdot50301 \times 17\cdot0352$ .
- $\cdot000713 \times 2\cdot30561$ ;  $42\cdot10062 \times 3\cdot821013$ ; and  $1\cdot0142034 \times \cdot0620034$ .
- $25067823 \times \cdot0000001$ ;  $394\cdot2003 \times \cdot00000003$ ; and  $\cdot834567834 \times \cdot000000008$ .
- $47\cdot83$  by 10, 100, 1000,  $\frac{1}{10}$ ,  $\frac{1}{100}$ ,  $\frac{1}{1000}$ ;  $\cdot5 \times 1000$ ;  $\cdot75 \times 100000$ .
- $22\cdot5 \times \cdot0241 \times \cdot0024$ ;  $\cdot0003 \times \cdot01 \times 500000$ ;  $\cdot006 \times \cdot00012$ .
- $2\cdot7 \times 27 \times \cdot027 \times 270$ ;  $\cdot2 \times \cdot04 \times \cdot008 \times 64000$ ;  $8\cdot004 \times \cdot004$ .
- $1\cdot1 \times \cdot011 \times 1\cdot01 \times \cdot0101$ ;  $\cdot013 \times 1\cdot6 \times \cdot007 \times 3\cdot05$ ;  $1003 \times 6\cdot12$ .

## DIVISION.

46. Let it be required to divide  $37\cdot015$  by  $6\cdot73$ .

By shifting the decimal point to the right of the dividend and divisor so as to turn both into whole numbers, we increase the number 1000-fold, and the divisor 100-fold. The former of these alterations will have the same effect as multiplying the quotient by 1000, the latter the same as dividing by 100; so that the quotient will be 10 times too great, and must be further divided by 10, *i.e.*, one decimal place must be pointed off to give a correct result.

Had it been required to divide  $370\cdot15$  by  $6\cdot73$  where there is the *same* number of decimal places in both dividend and divisor, by shifting the decimal points so as to make both whole numbers, we should increase the dividend 100-fold, and the divisor 100-fold; this would not affect the value of the result, and the quotient would be a whole number requiring no decimal point at all.

If the given quantities had been  $370\cdot15$  by  $\cdot673$ , so that there had been fewer decimal places in the dividend than in the divisor, by converting both into whole numbers we should have increased the dividend 100-fold and the divisor 1000-fold. This would have decreased the divisor 10-fold, and to obtain the correct result we should have had to multiply the quotient by 10.

We can hence determine the following practical rule for the division of decimals:—

RULE XVI.

*Divide as in whole numbers, and point off in the quotient as many decimal figures as the decimal places in the dividend exceed those in the divisor, that is, the quotient and divisor together must contain as many decimals as the dividend.*

EXAMPLES.

Ex. 1. Divide  $17\cdot68$  by  $3\cdot4$ .

$$\begin{array}{r} 3\cdot4)17\cdot68(5\cdot2 \\ \underline{170} \\ 68 \\ \underline{68} \end{array}$$

Here  $17\cdot68$  contains two decimals;  $3\cdot4$  contains one; therefore  $52$  must contain the remaining one required, and be written  $5\cdot2$ .

Ex. 3. Divide  $4\cdot784$  by  $9\cdot2$ .

$$\begin{array}{r} 9\cdot2)4\cdot784(5\cdot2 \\ \underline{460} \\ 184 \\ \underline{184} \end{array}$$

Here  $4\cdot784$  contains three decimals, and  $9\cdot2$  one, the remaining two required must therefore be obtained by pointing off both figures, thus,  $\cdot52$ .

(a) *When the dividend has no decimals, cyphers must be annexed, preceded by the decimal point.*

Ex. 5. Divide  $38$  by  $\cdot08$ .

$$\begin{array}{r} \cdot08)38\cdot00 \\ \underline{475} \end{array}$$

Annex two cyphers to  $38$ ; then the dividend contains two cyphers, and the divisor also two, and the quotient is therefore an integer.

(b) *When the number of figures in the quotient is not sufficient to make up the required number of decimals, cyphers must be prefixed.*

Ex. 7. Divide  $\cdot30285$  by  $67\cdot3$ .

$$\begin{array}{r} 67\cdot3)\cdot30285(45 \\ \underline{2692} \\ 3365 \\ \underline{3365} \end{array}$$

Here  $\cdot30285$  contains five decimals, and  $67\cdot3$  contains only one; the quotient  $45$  contains only two, and four are required; hence two cyphers must be prefixed, and the quotient written as  $\cdot0045$ .

Ex. 2. Divide  $547\cdot8$  by  $66$ .

$$\begin{array}{r} 66)547\cdot8(8\cdot3 \\ \underline{528} \\ 198 \\ \underline{198} \end{array}$$

Here  $547\cdot8$  contains one decimal;  $66$  none; hence  $83$  must contain one, and be written  $8\cdot3$ .

Ex. 4. Divide  $1353\cdot6$  by  $37\cdot6$ .

$$\begin{array}{r} 37\cdot6)1353\cdot6(36 \\ \underline{1128} \\ 2256 \\ \underline{2256} \end{array}$$

Here the dividend has one decimal, and the divisor also one, or as many, and the quotient is therefore an integer.

Ex. 6. Divide  $132$  by  $\cdot07$ .

$$\begin{array}{r} \cdot07)132\cdot00000 \\ \underline{1885714} \end{array}$$

Annexing five cyphers (decimals) gives quotient  $1885714$ . Then the number which added to one decimal in  $\cdot07$  to make up five is four. *Ans.* :  $188\cdot5714$ .

Ex. 8. Divide  $4\cdot784$  by  $92$ .

$$\begin{array}{r} 92)4\cdot784(52 \\ \underline{460} \\ 184 \\ \underline{184} \end{array}$$

Here  $4\cdot784$  contains three decimals, and  $92$  none; the quotient therefore must contain three, and becomes  $\cdot052$ .

(c) When the number of decimal places in the *dividend* is *less* than the number in the *divisor*, annex as many *cyphers* to the dividend as will make the number equal to the number in the divisor, and then proceed as in whole numbers.

Ex. 9. Divide 14.4 by .0012.

The divisor contains *four* decimal places and the dividend only *one*, annex *three* cyphers to the dividend, so as to make the number of decimal places in both divisor and dividend equal, and then divide by 12, and the work will stand thus:—

$$\begin{array}{r} .0012 \overline{) 14.4000} \\ \underline{12000} \phantom{00} \\ 24000 \phantom{00} \\ \underline{24000} \phantom{00} \\ 0000 \phantom{00} \end{array}$$

As the number of decimal figures in the dividend is equal to that of the divisor, we have none to cut off in the quotient. The answer is therefore 12000, an integer.

Ex. 10. Divide 3028.5 by .673.

In this instance the divisor contains *three* decimal places and the dividend only *one*; therefore *two* cyphers are annexed to make the number of decimal places in each equal.

$$\begin{array}{r} .673 \overline{) 3028.500} \\ \underline{2692} \phantom{00} \\ 3365 \phantom{00} \\ \underline{3365} \phantom{00} \\ 0000 \phantom{00} \end{array}$$

The number of decimal figures in the dividend and divisor being equal, we have none to cut off in the quotient. The answer 4500, is therefore an integer.

The division may always be carried to any degree of accuracy by annexing cyphers to the dividend, as seen in example 6 (a).

47. The decimal point may be removed altogether from both the divisor and dividend, by continually multiplying each by 10; for the quotient will thus remain unaltered. The first decimal in the quotient will then appear only with the first cypher annexed to carry on the division.

EXAMPLE.—Divide 55.80 by 0.04. Multiplied by 10 they become 558 and 0.4 multiplied again they become 5580 and 4, the quotient of which is 1395.

This easy process furnishes a complete security against wrongly placing the decimal point in the quotient.

#### EXAMPLES FOR PRACTICE.

1. Divide 99.12105 by 5, 7, 9, 36, and 88.
2. " 6.66816 by 4, 6, 8, 25, and 630.
3. " .6052158 by 3, 6, 9, 24, and 6400.
4. " 6541.234567 by 21; 7461.30765 by 112; 2188.054 by 983.
5. " 236.041 by 1.75; 67234 by 85; 60.0001 by 1.01; 300.402 by 12.1.
6. " 325.67543 by 20.02; 684234.6 by 2682; 73.8243 by .061; .00006 by .003.
7. " 34.82725 by 39.5275; 897.25 by .98725; 42.9365 by 387.25; and 3.1415926 by 180, true to seven decimal places.
8. " 17.084522 by .024; 1237.0519 by .5425; 762.151 by .00325.
9. " .00033 by .011; 140.02564 by 1.871; 4.32067 by .001; .59 by 80000; 167342 by .002; .001024 by 30517578125; 1001 by 16384.
10. " 992 by .37; .1599 by 4100; .019 by 190; 1 by .152; .2 by 23.2.
11. " 1.95 by .00013; 9.614 by .0000019; .25 by 31.25; 8.92 by 237.6567.
12. " .03679 by 2.83; 165.434 by 36.2; .027472 by 3.434; 61000 by .825.
13. " 17.171717 by 343.4; 1255 by 1.004; 12.55 by 1004; 7.231068 by .12.
14. " .012550 by 1004000; 12.55 by .01004; 1255 by 10.04; 4 by .00001.
15. " .001255 by 1004; .01 by 1000; 202 by .01; 6821091.97627 by 88.03.
16. " 13099.52 by .0011008; .005868 by .036, and arrange the divisor, dividend, and quotient in order of magnitude.
17. " .6 by 6; 6 by .6; .06 by 60; .006 by .6; 600 by .6; 600 by .06; and .006 by 600.
18. " .00636056 by .86; 6100 by .825; 23 by .000579; 37.69416 by .156; .0016 by .000008; 6 by .0000001; .8 by .0000002; .000054 by 9; 4000 by .000125.



19. „ 36 by 10000; 9'3 by 10; 52'306 by 100; 8 by 10000; 2'0076364 by 1000000.  
 20. „  $\frac{1'5}{17}$  to 10 decimal places;  $\frac{19'5}{1130}$  to 12 decimal places;  $\frac{0'001}{10'01}$  to 25 decimal places.  
 21. „  $\frac{0'0001}{1111}$  to 25 decimal places;  $\frac{06'561}{531441}$  to 15 decimal places;  $\frac{0009840018}{159'282}$  to 7 decimal places.

## REDUCTION.

48. The great convenience of decimals makes it often desirable to reduce vulgar fractions to the decimal form.

To reduce a vulgar fraction to a decimal.

We have to change the fraction to another equivalent fraction whose denominator is of the form 10, 100, 1000, &c. To do this we multiply the numerator and denominator of the fraction by 10, 100, 1000, &c., as may be necessary, *i.e.* we add a certain number of cyphers (the same to each); we then divide the numerator and denominator by the original denominator. These operations will not alter the value of the fraction. If the numerator by the addition of the cyphers becomes divisible by the denominator, without remainder, the required decimal is found; if not, a circulating or recurring decimal is produced as is shown in the following examples:—

Ex. 1. To reduce  $\frac{5}{8}$  to a decimal.

$$\frac{5}{8} = \frac{5000}{8000} \div 8 = \frac{625}{1000} = .625.$$

Here we multiply numerator and denominator by 1000 and divide them by 8. The resulting fraction  $\frac{625}{1000}$  represented as a decimal is .625.

Ex. 2. To reduce  $\frac{123}{625}$  to a decimal.

$$\frac{123}{625} = \frac{1230000}{6250000} = \frac{1968}{10000} = .1968.$$

Here we multiply numerator and denominator by 10000, and then divide them by 625. The resulting fraction  $\frac{1968}{10000}$  represented as a decimal is .1968.

$$625 \overline{)1230000} \cdot 1968$$

$$\begin{array}{r} 625 \\ 6050 \\ 5625 \\ \hline 4250 \\ 3750 \\ \hline 5000 \\ 5000 \end{array}$$

The work is shortened thus:—we put down the numerator 123 as dividend, and denominator 625 as a divisor, and adding cyphers as often as required, we obtain as a quotient the significant digits of the decimals; and the number of cyphers added to the dividend will be the number of places to be marked off in the question.

Hence to convert vulgar fractions into decimals we proceed by the following rule.

## RULE XVII.

*Annex a cypher to the numerator, and then divide by the denominator; if there be a remainder, annex another cypher, and continue the division, still annexing a cypher, either till the division terminates without a remainder, or till as many decimals as are considered necessary are obtained: the quotient, with a decimal point before it, will be the value of the fraction in decimals.*

## EXAMPLES.

Ex. 1. Reduce  $\frac{1}{5}$  to a decimal fraction.

$$\begin{array}{r} 5 \overline{)1\cdot0} \\ \underline{0\cdot2} \end{array}$$

Dividing 10 by 5 (the cypher being added) we find that  $\frac{1}{5}$  is  $= 0\cdot2$ . That  $\frac{1}{5} = 0\cdot2$  is easily proved, for  $\frac{1}{5} = \frac{2}{10}$ ; consequently, by dividing both the numerator and denominator by 5, we have  $\frac{1}{5} = \frac{2}{10} = \cdot2$

Ex. 3. Reduced  $\frac{3}{10}$  to a decimal fraction.

$$\begin{array}{r} 3 \overline{)1\cdot0000} \\ \underline{\phantom{0}3333}, \text{ \&c.} \end{array}$$

Dividing 10 by 3 gives 3, the next cypher added gives another 3, and so on, continually.

Ex. 5. Reduce  $\frac{25}{100}$  to a decimal.

$$36 = 4 \times 9 \quad 36 \left\{ \begin{array}{l} 4 \overline{)25\cdot00} \\ 9 \overline{)6\cdot25} \end{array} \right. \begin{array}{l} \\ \underline{\phantom{0}694444}, \text{ \&c.} \end{array}$$

Hence  $\frac{25}{100} = \cdot694$  which is called a *mixed recurring* or *circulating* decimal, consisting of the non-recurring part 69 and the recurring part 444, and usually written with a point or dot above the figure which is repeated.

Ex. 7. Convert  $\frac{8}{113}$  into a decimal.

$$\begin{array}{r} 113 \overline{)8\cdot00007079}, \text{ \&c.} \\ \underline{791} \\ 900 \\ \underline{791} \\ 1090 \\ \underline{1017} \\ 73, \text{ \&c.} \end{array}$$

When the 0 is annexed to the 8, the divisor 113 will go *no time*; therefore the first decimal place is to be occupied with a cypher. Annexing now a second 0, the next decimal figure is 7, and the work proceeds as above. The quotient shows that  $\frac{8}{113} = \cdot07079$ , &c.; the decimals may be carried out to any extent.

Ex. 10. Reduce  $\frac{1}{512}$  to a decimal.

$$\frac{1}{512} = \cdot001953125.$$

Ex. 2. Convert  $\frac{3}{8}$  into a decimal fraction.

$$\begin{array}{r} 8 \overline{)3\cdot000} \\ \underline{\phantom{0}2400} \\ 375 \end{array}$$

That  $\frac{3}{8} = \cdot375$  is proved thus,  $\frac{3}{8} = \frac{3000}{8000}$ ; consequently, dividing the numerator and denominator by 8, (the denominator of the fraction), we have  $\frac{3}{8} = \frac{375}{1000} = \cdot375$ .

Ex. 4. Reduce  $\frac{6}{11}$  to a decimal.

$$\begin{array}{r} 11 \overline{)6\cdot0} \\ \underline{\phantom{0}55} \\ 5454 \end{array}$$

It is plain from the remainder that 54 would recur continually, so that  $\frac{6}{11}$  is equal to a *recurring* decimal; 54 being the *recurring* period.

Ex. 6. Reduce  $\frac{3}{14}$  to a decimal.

$$14 = 2 \times 7 \quad 14 \left\{ \begin{array}{l} 2 \overline{)3\cdot000} \\ 7 \overline{)1\cdot500} \end{array} \right. \begin{array}{l} \\ \underline{\phantom{0}2142857} \end{array}$$

Hence  $\frac{3}{14} = \cdot2142857$ ; the recurring part 142857 having a point above its first and last figures being called its period. If the whole decimal recurs, it is called a *pure circulator*.

Ex. 8. Reduce  $\frac{1}{128}$  to a decimal.

$$\begin{array}{r} 128 \overline{)1\cdot0000078125} \\ \underline{896} \\ 1040 \\ \underline{1024} \\ 160 \\ \underline{128} \\ 320 \\ \underline{256} \\ 640 \\ \underline{640} \end{array}$$

Ex. 9. Reduce  $\frac{101}{8102}$  to a decimal.

$$\frac{101}{8102} = \cdot0123291015625.$$

Ex. 11. Reduce  $\frac{7}{512}$  to a decimal.

$$\frac{7}{512} = \cdot013671875.$$

Ex. 12. Reduce  $\frac{48}{953}$  to a decimal.

$$\frac{48}{953} = \cdot0451206715634837355718782791185729275970619.$$

## EXAMPLES FOR PRACTICE.

1. Change into equivalent decimals  $\frac{7}{10}$ ,  $\frac{11}{15}$ ,  $\frac{13}{20}$ ,  $\frac{11}{32}$ ,  $\frac{3}{10}$ ,  $\frac{5}{60}$ ,  $\frac{7}{25}$ , and  $\frac{11}{40}$ .
2. Reduce to decimals  $\frac{7}{13}$ ,  $\frac{11}{17}$ ,  $\frac{13}{19}$ ,  $\frac{5}{27}$ ,  $\frac{129}{530}$ ,  $\frac{113}{550}$ ,  $\frac{37}{79}$ , and  $\frac{3}{280}$ , carrying interminants to seven decimal places.

49. It becomes important to observe what fractions will produce terminating decimals. Suppose a fraction in its lowest terms; then in reducing it to a decimal we multiply the numerator by 10, 100, 1000, &c. Now the numerator contains no factor common to the denominator, and by this multiplication we introduce the factors 2 and 5 as often as we please and no others. Unless, then, the denominator contains no other factor except twos and fives, this multiplication cannot render the numerator divisible by it. Hence the only fractions which will produce terminating decimals are those whose denominators contain only 2 and 5 as prime factors. All other fractions will produce circulating decimals, though in many cases the period is so long that it would be tedious to find it.

50. Decimals are most frequently used to make calculations on numbers that have been obtained by observations of some kind, by measuring, for instance, or weighing; and it is very seldom indeed that the accuracy of these observations can be relied on to within one five-thousandth part of the unit employed. Now if we cannot rely on the measurement beyond three decimal places, it is needless to carry the result derived from it any farther. In all operations with decimals, then, whether terminating or repeating, we may usually stop at the third or fourth place, and need very rarely go beyond the fifth or sixth. We may, however, attain any degree of exactness that may be required, by carrying the decimal far enough.

With respect to repeating decimals, if perfect accuracy be necessary, they must in most cases be reduced to vulgar fractions before they are added, subtracted, multiplied, or divided. In almost all the applications of decimals, however, an approach to accuracy is sufficient, and this is attained by carrying the decimal only to a moderate number of digits, and omitting the rest. If, in converting a vulgar fraction into a decimal, we stop after the third digit, for instance, adding unity to that digit, if the next be 5 or upwards, it does not differ from its exact value by more than one five-thousandth part of the unit employed. Thus,  $\cdot 172$  differs from  $172437$  by  $\cdot 0004372$ , which is less than  $\cdot 0005$ . Similarly,  $983$  differs from  $\cdot 98276$  by  $\cdot 0002317$ , which is also less than  $\cdot 0005$ .

51. To reduce any quantity or fraction of one denomination to the decimal of another denomination.

## RULE XVIII.

*Reduce the number of the lowest denomination to a decimal of the next higher denomination, prefix to this decimal the number of its denomination given in the question, if any, and reduce this also to a decimal of the next higher order, and so on till all the numbers of the given denominations are exhausted, and the decimal of the required denomination has been obtained: the last result will be the answer.*

## EXAMPLES.

Ex. 1. Let it be required to express 17s.  $5\frac{1}{2}$ d. as the decimal of £1.

The process will be first to express the fractional part of a penny as a decimal of a penny; placing the 5 as a whole number before this decimal, to divide that result by 12, in order to reduce it to the decimal of a shilling; placing the 17 as a whole number before this decimal, to divide that result by 20 in order to reduce it to the decimal of a pound. This will be written as follows:—

$$\begin{array}{r} 4) 1' \\ \hline 12) 5'25 \text{ pence} \\ \hline 20) 17'4375 \text{ shillings} \\ \hline .871875 \text{ of a pound.} \end{array}$$

It will be seen from this, that whatever we should divide by in whole numbers in order to bring pence into shillings, or shillings into pounds, that we must likewise divide by in this case, only marking off correctly the decimal results.

Ex. 3. Find what decimal of an hour is 40<sup>m</sup>.

There are 60 minutes in an hour; hence 1 minute is  $\frac{1}{60}$  of an hour, and 40 minutes is  $\frac{40}{60}$  of 1 hour, which gives 0.66 of 1 hour.

$$\begin{array}{r} 60) 40'00 \\ \hline 0'66 \text{ of an hour.} \end{array}$$

Ex. 5. Find what decimal of 1 degree is 3' 37".

37" are  $\frac{37}{60}$  of 1', or 0.61 of 1'; then 1' is  $\frac{1}{60}$  of 1°; hence 8' 61 are  $\frac{8.61}{60}$  of 1°, or 0°.143.

$$\begin{array}{r} 60) 37'' \\ \hline 60) 8'616 \\ \hline 0'143 \text{ of a degree.} \end{array}$$

Ex. 7. Find what decimal of 1 mile (nautical) is 700 feet.

There are 6080 feet nearly in a nautical mile; hence 1 foot is  $\frac{1}{6080}$  of a mile, and 700 feet are  $\frac{700}{6080}$  of 1 mile, which gives 0.115 of 1 mile nearly.

$$\begin{array}{r} 6080) 700'0(0'115 \\ 6080 \\ \hline 9200 \\ 6080 \\ \hline 31200 \\ 30400 \end{array}$$

Ex. 2. Express as decimals of a degree 27° 18' 35".

$$\begin{array}{r} 60 \mid 35'' \\ 60 \mid 18'5833 \\ 27'30972 \end{array}$$

Here for convenience of arrangement we write the 35' uppermost, and the 18' and 27° directly under it, and draw a vertical line to the left of the line opposite these numbers write for divisors the number of that denomination which makes one of the next higher—namely, 60 opposite the seconds, since 60" = 1', and 60 opposite the minutes, because 60' = 1°. Then dividing 35 by 60 we get .583, which we write after the minutes, which gives 18' 583; this again divided by 60, the number of minutes in a degree, gives the quotient .30972, which being annexed to the degrees 27° gives the answer 27°.30972.

Ex. 4. Find what decimal of an hour is 15<sup>m</sup>.

Here 1 minute is  $\frac{1}{60}$  of 1 hour, 15 minutes is  $\frac{15}{60}$  of 1 hour; hence  $\frac{15}{60}$  gives 0.25 of 1 hour.

$$\begin{array}{r} 60) 15'00 \\ \hline 0'25 \text{ of an hour.} \end{array}$$

Ex. 6. Find what decimal of 1 day is 3<sup>h</sup> 42<sup>m</sup>.

42<sup>m</sup> are  $\frac{42}{60}$  of 1 hour, or 0<sup>h</sup>.7; and 1<sup>h</sup> is  $\frac{1}{24}$  of 1 day; hence 3<sup>h</sup>.7 is  $\frac{3.7}{24}$  of 1 day, or 0<sup>d</sup>.154166, &c.

$$\begin{array}{r} 60) 42^m \\ \hline 24) 3'7 \\ \hline 0'154166 \end{array}$$

Ex. 8. Find what decimal of 1 foot is 8 $\frac{3}{4}$  inches.

First,  $\frac{3}{4}$  is 0.75 of 1 inch; hence 8 $\frac{3}{4}$  inches are 8.75 inches. Then, 1 inch is  $\frac{1}{12}$  of 1 foot; hence 8.75 inches are  $\frac{8.75}{12}$ , or 0.729 of 1 foot.

$$\begin{array}{r} 12) 8'75 \\ \hline 0'729 \end{array}$$

52. Or, reduce the given quantities to the lowest denominations when there are more than one, and also the integer to which it is referred, to the same denomination; then divide the given quantity by the integer thus reduce.

Ex. 1. (Ex. 7 above). The given quantity 700 feet, being all of one denominator requires no further reduction. The integer 1 mile, reduced to the same denomination, is 6080 feet; then 700 divided by 6080 gives 0.115.

Ex. 2. (Ex. 8 above). 8 inches and 3 quarters are 35 quarters, and 1 foot reduced to the same denomination is 48 quarters; then 35 divided by 48 gives 0.729.

### EXAMPLES FOR PRACTICE.

- Express as decimals of an hour  $17^m$ ;  $29^m$ ;  $42^m$ ;  $25^m$ ;  $48^m$ ; and  $58^m$ .
- Reduce  $5^d 12^h 25^m 39^s 92$  to decimals of a week.
- Reduce  $29^d 12^h 44^m 28^s 82$  to decimals of a day.
- Add together 2.095 hours, .07 days, .05 weeks, and express the same as the decimal of 365.25 days.
- A nautical mile is 6082.66 feet, and an imperial mile is 5280 feet; express each of these miles as decimals of the other. Also find how near the results are to the decimal values of  $\frac{3}{8}$  and  $\frac{2}{3}$ .
- A sidereal day is  $23^h 56^m 4^s 09$ ; express this as a decimal of a common day—that is, of  $24^h$ —and give the result to nine decimal places.
- Express as decimals of a day the following quantities:— $12^d 14^h 13^m 12^s$ ;  $29^d 17^h 11^m 45^s$ ;  $15^d 17^h 48^m 54^s$ ; and  $119^d 5^h 19^m 15^s$ .
- Express as decimals of a degree the following quantities:— $8^\circ 11' 15''$ ;  $19^\circ 40' 45''$ ;  $104^\circ 16' 7\frac{1}{2}''$ ; and  $82^\circ 19' 30''$ .
- If 90 degrees correspond to 100 French grades, how many degrees are there in the sum of  $41.45$  degrees and  $41.45$  grades.
- A mètre is 39.37079 English inches, a kilomètre is 1000 mètres; express as decimals of each other a kilomètre and an English mile.
- If the length of a degree of latitude is 365000 feet, and a mètre one ten-millionth of 90 degrees: find its length in feet.
- Express in figures thirty-four and two thousandths, and by it divide 28255662. What alteration must be made in the quotient if the decimal part in the dividend be moved eight places to the left?
- The sidereal year being  $365^d 6^h 9^m 9^s 6$ , and the tropical year  $365^d 5^h 48^m 49^s 7$ : reduce their difference to the decimal of a tropical year.
- Supposing the velocity of electricity be 288,000 miles per second, and the earth's circumference to be 25,000 miles: calculate to seven places of decimals the time of transmission of an electric telegraph to the antipodes.
- A French mètre is 39.37 inches nearly: show that a foot is equal to .304 mètres nearly.

To find the value in a lower denomination of any decimal of a higher denomination.

### RULE XIX.

1°. Note the number of parts which the unit or integer of the given quantity contains of the next inferior denomination, and multiply the given decimal by this number; the product is the given quantity expressed in that denomination.

2°. If this product has a decimal part, multiply this decimal by the number of parts which the unit of the present denomination contains of the next inferior denomination to that just before employed; this product is the quantity which the given decimal contains of the next denomination.

3°. Proceed (if there still be decimals), in like manner, to the lowest denomination in which the decimal is required to be expressed.

## EXAMPLES.

Ex. 1. Find the number of feet in  $0.115$  of a mile.

The next inferior denomination to that of miles is here feet, }  $0.115$   
 of which the number in one mile is ..... }  $\times 6082$

---

$230$   
 $920$   
 $6900$

*Ans.* (in the lowest denomination required)  $699.430$  feet.Ex. 2. Find the number of seconds in  $0.7$  of a minute.

The next inferior denomination to that of minutes is seconds }  $0.7$   
 of which the number in a minute is ..... }  $\times 60$

---

*Ans.*  $42.0$  seconds.Ex. 3. Find the number of inches and eighths in  $0.48$  of a foot.

The next inferior denomination to that of feet is inches, of }  $0.48$   
 which the number in a foot is ..... }  $\times 12$

---

$5.76$  inches.

The next proposed inferior denomination to inches is eighths, }  $\times 8$   
 of which the number in an inch is ..... }

---

$6.08$  eighths.

Ex. 4. What is the value of  $.625$  of a cwt.?

The next inferior denomination to that of a cwt. is qrs., of }  $.625$   
 which the number in a cwt. is ..... }  $\times 4$

---

$2500$  qrs.

The next inferior denomination to qrs. is lbs., of which the }  $\times 28$   
 number in a quarter is ..... }

---

$14.0$  lbs.

## EXAMPLES FOR PRACTICE.

What is the value of

- |                       |                       |                        |
|-----------------------|-----------------------|------------------------|
| 1. $.7768$ tons.      | 4. $.225$ tons.       | 7. $.2957795$ degrees. |
| 2. $.785425$ degrees. | 5. $.3625$ tons.      | 8. $.165625$ tons.     |
| 3. $.643825$ degrees. | 6. $.108725$ degrees. | 9. $.530588715$ days.  |

Find the length of a tropical year which contains  $365.242218$  days.

## ON LOGARITHMS.

53. Logarithms are numbers arranged in Tables for the purpose of facilitating arithmetical computations. They are adapted to the natural numbers, 1, 2, 3 . . . . in such a manner that by means of them

|  |
|--|
| the operation of Multiplication is changed into that of Addition ; |
| . . . Division . . . . . Subtraction ;                             |
| . . . Involution . . . . . Multiplication ;                        |
| . . . Evolution . . . . . Division ; *                             |

\* No proof can here be offered that numbers must exist possessing the properties under which we call them logarithms; neither can any account be here given of the methods of computing such logarithms. The reader will accept the statement that if such numbers exist, bearing the properties aforesaid, they are called logarithms. He must also accept the

54. Take any whole numbers, as 18, 813, 6489; the first consists of two, the second of three, and the third of four figures or *digits*. Again, in the mixed number  $739.815$ , the whole number or integral part (739) consists of three *digits*.

55. By multiplying a number by itself, *one, two, three, &c.*, times successively, we obtain the *second, third, fourth, &c.*, powers of that number; hence, a *power of a number is the number arising from successive multiplication by itself*. Thus,  $3 \times 3 = 9$  is the square or second power of 3; and  $5 \times 5 \times 5 = 125$ , the cube or third power of 5; and so on.

These operations are denoted by means of *Indices*, or small figures placed on the right of the numbers, a little above the line; thus,  $2^2 = 2 \times 2 = 4$ ,  $3^3 = 3 \times 3 \times 3 = 27$ , and  $2^5 = 2 \times 2 \times 2 \times 2 \times 2 = 32$ , where the *Index* or *exponent* denotes the number of factors employed.

56. When there are a series of numbers, such that each is found from the previous one by the addition or subtraction of the same number, they are said to be in arithmetical progression. 1, 3, 5, 7, 9, 11, &c., are in arithmetical progression.

57. Again, the numbers 3, 6, 12, 24, &c., are in geometrical progression, for each number is formed from the one immediately preceding by multiplying by 2. If we take the following series of powers,  $3^1, 3^2, 3^3, 3^4, 3^5$ , &c., we find that the exponents proceed in arithmetical progression, and the quantities themselves in geometrical progression.

58. DEF.—Logarithms are a series of numbers in *arithmetical* progression answering to another series in *geometrical* progression, so taken that 0 in the former corresponds with 1 in the latter.

Thus, 0, 1, 2, 3, 4, 5, 6, &c., are the logarithms or *arithmetical* series, and 1, 2, 4, 8, 16, 32, 64, &c., are the numbers or *geometrical* series, answering thereto—the latter being called the *natural number*.

Or, 0, 1, 2, 3, 4, 5, the logarithms,  
and 1, 5, 25, 125, 425, 5125, the corresponding numbers.

Or, 0, 1, 2, 3, 4, 5, the logarithms,  
and 1, 10, 100, 1000, 10000, 100000, the corresponding numbers.

In which it will be seen, that by altering the common ratio of the geometrical series, the same arithmetical series may be made to serve as

tables which are published, recording logarithms for the several numbers to which they profess to belong, though he cannot at present verify the computation of these several logarithms; and he will be informed how he may use these tables to effect with comparative ease many calculations which would otherwise be most laborious.

The truth is, though it requires for its demonstration higher algebra than this work presupposes the reader to be acquainted with, that not only has every number a logarithm, but it has an infinite variety of logarithms, constructed, as the term is, on different scales or bases. The base of any system of logarithms is defined by the fact that in that system *unity* is its logarithm.

Any number *might* be used as a base; but in fact there are only two numbers which are ever really used.

The one is an unterminating decimal,  $2.7182818 \dots$ , denoted generally by the letter *e*. This is the base of what is called the natural or Napierian system; and the advantage of it consists in the ease with which logs. are computed, to this base; but which we cannot here explain.

The other is 10, which is the base in ordinary use, and with this base  $\log. 10 = 1$ . Logarithms to this base are the only ones which will now be considered in their practical use.

logarithms of any series of numbers. As above, when the common ratio of the geometrical series are 2, 5, and 10 respectively.

59. The common ratio in the geometrical series corresponding to the common difference of 1 in the arithmetical series is called the base of the system. Thus, the base of the first specimen exhibited is 2, the base of the second is 5, and the base of the third is 10.

In the specimens just exhibited we have, in each, taken two ascending progressions, but they might equally well have been two descending progressions, or the one descending and the other ascending. Logarithms, however, as now used in practice, are limited to the case of two progressions, either both ascending or both descending—the former giving the logarithms of integers, the latter of fractional numbers.

But a better way of considering logarithms is as follows:—

60. DEF.—The logarithm of a number to a given base is the index of the power to which the base must be raised to give the number.

For instance, if the base of a system of logarithms be 2, 3 is the logarithm of 8, because  $8 = 2^3 = 2 \times 2 \times 2$ .

And if the base be 5, then 3 is the logarithm of the number 125, because  $125 = 5^3 = 5 \times 5 \times 5$ .

There may thus be as many different systems of logs. as we please; but, for practical use, it is necessary to select and adhere to one. That usually employed now is called *Briggs' system*.

61. We now proceed to describe what is called the **common system of logarithms**. In the common system of logarithms unity is assumed to be the logarithm of 10; that is, 10 is the constant base. All the logarithms registered in the Tables commonly used, are indices of the radix or base 10; a Table of logarithms of numbers is in fact nothing more than a Table of the exponents of 10 placed against the several numbers themselves. Accordingly—

|   |                |            |                |
|---|----------------|------------|----------------|
| 0 | is the log. of | 1, because | $1 = 10^0$     |
| 1 | "              | 10, "      | $10 = 10^1$    |
| 2 | "              | 100, "     | $100 = 10^2$   |
| 3 | "              | 1000, "    | $1000 = 10^3$  |
| 4 | "              | 10000, "   | $10000 = 10^4$ |
|   | "&c.,          |            | &c.            |

Now, if the above Tables were amplified by the insertion of the logarithms of all the numbers between 1 and 10, between 10 and 100, &c., we should have a Table of logarithms of all numbers from 1 to 10000; and whatever may be the difficulty of determining the intermediate logarithms, it is at once easily seen that the logarithms of all numbers between 1 and 10 will be 0 + a fraction, that is, a decimal less than 1; of all numbers between 10 and 100 will be 1 + a fraction, or a decimal between 1 and 2; of all between 100 and 1000 will be 2 + a fraction, and so forth; or the integral part of each intermediate logarithm will be *one less* than the number of integral figures in the quantity of which it is the logarithm. Thus, the logarithms of 2, 3, 4, &c., to 9, have 0 as the integral part; those of 10, 11, 12, &c., to 99, have 1 as the integer; those of 100, 101, 102, &c., to 999, have 2 as the integer; and so forth. Hence Tables of logarithms usually supply only the fractional or decimal part; the integral part is always known from the number of



integers in the value whose logarithm is wanted. Very few logs. can be expressed in terminating decimals, but this causes little inconvenience since a log. carried to six or seven decimal places is sufficiently exact for all common purposes.

62. The integers 1, 2, 3, 4, &c., which are the logarithms of 10 and its powers (see 61), are chief indices, and the logarithms intermediate to these, as for instance 1.778151 (which is the logarithm of 60) consisting of an integer and a decimal fraction, though they are also indices, are usually referred to as consisting of an *index*\* and *mantissa*†, the integral part being specially termed the *index* or *characteristic*, because it indicates, by being *one less*, how many integral places are in the corresponding natural number, and the annexed decimal being called the *mantissa*.

EXAMPLE.—In the log. 4.616339, the figure (4) standing to the left of the decimal point is the *characteristic* or *index*, and the remaining portion (.616339) is the *mantissa* or *decimal part*.

63. To find the characteristic of the logarithm of any number greater than unity, we have, therefore, the following rule:—

#### RULE XX.

*The characteristic of the logarithm of a number greater than unity, i.e., of a whole or mixed number, is one less than the number of the digits of its integer part.*

Thus: the characteristic of the logarithm of 849 is 2; for the number 849 is an integer consisting of three digits (that is a number between 100 and 1000) and 1 less than 3 is 2. Also, the index of the log. of 264.96 (which is a mixed number) is 2, since the integral part of the number, namely 264 is a number between 100 and 1000, or consists of 3 digits, and one less than 3 is 2. Again, 3 is the characteristic of the logarithm of 3847.216, since this number has 4 integral digits; while 0 is the characteristic of the logarithm of 3.847216, since this number has one integral digit.

Again, the characteristic of the log. of a number of *one* place of integers (such as 5 or 5.08, or 5.0801) is 0. Again, every number with *two* places of integers (such as 50, or 50.8, or 50.813) is 1. Again, every number with *three* places of integers (such as 508, or 508.2, or 508.25) has for its characteristic 2, and so on.

#### EXAMPLES FOR PRACTICE.

Write down the characteristics of the logarithm of the following numbers:—

|           |           |             |              |
|-----------|-----------|-------------|--------------|
| 1. 365    | 6. 69710  | 11. 474000  | 16. 473.908  |
| 2. 4.8    | 7. 45.82  | 12. 4256.45 | 17. 54793000 |
| 3. 643.75 | 8. 8640   | 13. 3.9     | 18. 21256.8  |
| 4. 28.9   | 9. 75     | 14. 8       | 19. 2.14006  |
| 5. 6      | 10. 7.265 | 15. 18      | 20. 50.7406  |

64. It has been shown that in the common system of logarithms (Briggs') the log. of 1 is 0; consequently, if we wish to extend the application of logs. to fractions, we must establish a convention by which the logs. of numbers

\* In order to avoid confusion from the use of the word "index" to signify two things, we shall throughout this work employ the term *characteristic* when speaking of logarithms, and *index* when speaking of roots or powers.

† *Mantissa*, a Latin word signifying an additional handful; something over and above an exact quantity.

wholly decimal, *i.e.*, less than unity, may be represented by numbers less than zero, *i.e.*, by *negative numbers*.

*Extending*, therefore, the above principles to negative exponents, since

|                             |            |     |                                       |        |
|-----------------------------|------------|-----|---------------------------------------|--------|
| $10^0 = 1$                  | $= 1$      | 0   | is the logarithm of 1 in this system. |        |
| $10^{-1} = \frac{1}{10}$    | $= 0.1$    | 1   |                                       |        |
| $10^{-2} = \frac{1}{100}$   | $= 0.01$   | 2   | "                                     | 01 "   |
| $10^{-3} = \frac{1}{1000}$  | $= 0.001$  | 3   | "                                     | 001 "  |
| $10^{-4} = \frac{1}{10000}$ | $= 0.0001$ | 4   | "                                     | 0001 " |
| &c.,                        |            | &c. |                                       |        |

It follows from this, that when the number is a decimal with all its digits significant, in value between 1 and  $\frac{1}{10}$ , its log. is negative, yet not so small as the log. of  $\frac{1}{10}$ , which is  $-1$ . Its log. therefore will be something between 0 and  $-1$ , or  $-1$  with some positive decimal added. Hence  $-1$  is its characteristic. When the number is a decimal with zero as its first digit, in value therefore below  $\frac{1}{10}$  but not so low as  $\frac{1}{100}$ , its log. is less than  $-1$ , but not so small as  $-2$ , and so will be  $-2$  with some positive decimal attached. Thus  $-2$  is the characteristic. The log. of a decimal between  $.01$  and  $.001$  is some number between  $-2$  and  $-3$ , and its characteristic is  $-3$ ; of a number between  $.001$  and  $.0001$  its log. is between  $-3$  and  $-4$ , and its characteristic is 4; and generally, following this reasoning it will appear that the characteristic of a decimal fraction may be known from its denoting the place of the first significant figure of the decimal, as being the 1st, 2nd, 3rd, &c., place after the point.

65. To find the characteristic of any number less than unity, *i.e.*, of a decimal.

The characteristics of the logarithms of all numbers less than unity are negative, and may be found by

#### RULE XXI.

*The characteristic of the logarithm of a number less than unity, and reduced to the decimal form, is negative and one more than the number of cyphers following the decimal point.*

A negative characteristic is denoted by writing over it the negative sign ( $-$ ), thus  $\bar{1}$ ,  $\bar{2}$ ,  $\bar{3}$ , &c.\*

Thus the characteristic of the logarithm of  $.00521$  is  $\bar{3}$ , since the number of cyphers following the decimal point increased by 1 is 3.

|                                |              |    |           |
|--------------------------------|--------------|----|-----------|
| Similarly the index of log. of | '156         | is | $\bar{1}$ |
| "                              | " '0156      | is | $\bar{2}$ |
| "                              | " '00046     | is | $\bar{4}$ |
| "                              | " '000000721 | is | $\bar{7}$ |

66. But in order to avoid the confusion that might arise by the addition and subtraction of *negative* indices, the following rule is frequently used.

#### RULE XXII.

*Add 1 to the number of cyphers between the decimal point and the first significant figure, and subtract from 10; the remainder is the index required.*

\* The negative sign ( $-$ ) is written *above* the characteristic, thus  $\bar{2}$ , instead of before it, to show that it affects only the characteristic and not the mantissa, which remains positive. If it were written in front of the complete logarithm it would signify that the entire logarithm was negative, but such logarithms are never employed in the operations connected with navigation.

Thus the characteristic of the log. of  $\cdot 04$  is  $\bar{2}$  or 8, since 1 added to the number of cyphers following the decimal point is 2, then 2 from 10 is 8.

|  |    |    |
|--|----|----|
| Similarly the index of log. of $\cdot 140$ | is | 9. |
| „ „ „ $\cdot 0149$                         | is | 8. |
| „ „ „ $\cdot 00064$                        | is | 6. |
| „ „ „ $\cdot 00000721$                     | is | 3. |

(a) If the characteristic of a vulgar fraction is required, it must first be reduced to an equivalent decimal fraction, and then the index is found by the rule.

|   |                        |                    |
|---|------------------------|--------------------|
| Thus, the index of log. $\frac{1}{8}$ , | or of log. $\cdot 125$ | is $\bar{1}$ or 9. |
| „ of log. $\frac{1}{25}$ ,              | or of log. $\cdot 04$  | is $\bar{2}$ or 8. |
| „ of log. $24\frac{3}{5}$ ,             | or $24\cdot 6$         | 1.                 |

### EXAMPLES FOR PRACTICE.

Write down the characteristics of the logarithms of the following decimal fractions:—

|                 |                    |                     |                          |
|-----------------|--------------------|---------------------|--------------------------|
| 1. $\cdot 045$  | 6. $\cdot 0000001$ | 11. $\cdot 4537$    | 16. $\cdot 037299$       |
| 2. $\cdot 9$    | 7. $\cdot 01$      | 12. $\cdot 009$     | 17. $\cdot 00000052018$  |
| 3. $\cdot 0004$ | 8. $\cdot 0003127$ | 13. $\cdot 0000008$ | 18. $\cdot 000000205379$ |
| 4. $\cdot 6798$ | 9. $\cdot 02803$   | 14. $\cdot 000064$  | 19. $\cdot 5$            |
| 5. $\cdot 0062$ | 10. $\cdot 7007$   | 15. $\cdot 000485$  | 20. $\cdot 000000000382$ |

67. The characteristic may also be found as follows:—

### RULE XXIII.

*Place your pen between the first and second figure, (not cypher), and count one for each figure or cypher, until you come to the decimal point, the number thus given will be the characteristic: but observe that if you count to the left you must subtract the number found from 10, and consider the remainder as the characteristic.*

Thus, in finding the log. of  $4\cdot 6017$ , if you place your pen between the first figure (4) and second (6), it falls on the decimal point; in this case the characteristic is 0. Next, in the case of log. of  $4601\cdot 7$ , place your pen between 4 and 6, and count  $4\frac{601\cdot 7}{123}$ ; the characteristic is 3. Next, in the case  $4601700$ , here the decimal point falls behind the last cypher (No. 5). Hence, counting as before, we have  $4\frac{601700}{123456}$  and the characteristic is 6.

Again, in the case of log.  $\cdot 00046017$  the first significant figure is 4. Hence, counting, we have  $\cdot 0\frac{0046017}{4321}$ , but here we count to the left, so that the characteristic is negative, or  $\bar{4}$ , which taken from 10 is 6. Again, in the case of log. of  $46017$ , we have  $4\frac{6017}{1}$ , and the characteristic is  $\bar{1}$ , or 9.

68. The mantissa of the logarithm depends entirely on the relative value of the figures composing the quantity whose logarithm it is, and not at all upon the numerical value of that quantity: thus, the mantissa of the log. of 13 is  $\cdot 113943$ , which is also the mantissa of 13, or 130, or 1300, for in each case the 1 and the 3 have the same relative value. So the mantissa of a logarithm is always the same, if the significant figures remain the same, and is not altered by the addition of cyphers to the right or left of these figures, or what is equivalent, by the multiplication or division of the quantity by 10, or any power of 10; it is only the characteristic which alters its value by an

alteration in the position of the decimal point, 1 being added to the characteristic for every place the decimal point is removed to the right, that is, for every 10 by which the quantity is *multiplied*; or, 1 is *subtracted* from the characteristic for every place the decimal point is removed to the left, that is, divided by 10.

|                  |          |       |          |
|------------------|----------|-------|----------|
| The logarithm of | 745800   | being | 5.872622 |
| that of          | 74580    | is    | 4.872622 |
| "                | 7458     | "     | 3.872622 |
| "                | 745.8    | "     | 2.872622 |
| "                | 74.58    | "     | 1.872622 |
| "                | 7.458    | "     | 0.872622 |
| "                | .7458    | "     | T.872622 |
|                  |          | or    | 9.872692 |
| "                | .07458   | "     | 2.872622 |
|                  |          | or    | 8.872622 |
| "                | .007458  | "     | 3.872622 |
|                  |          | or    | 7.872622 |
| "                | .0007458 | "     | 4.872622 |
|                  |          | or    | 6.872622 |

### ON TABLES OF LOGARITHMS OF NUMBERS.

69. In Raper's, Norie's, and the collection of nautical tables intended to accompany this work, the Tables of the Logarithms of Numbers are arranged so as to give the mantissæ of the natural numbers from 1 to 10000. If the reader will open an ordinary table of logarithms, such as is contained in the above mentioned works, he will find a short table of logs. from 1 to 100 immediately preceding the general table, and giving the entire logarithm; following which is the general table, on opening which he will find a vertical column on the left side of the page containing three digits and ten columns of logarithms headed by the digits 0, 1, 2, . . . 9. These last are fourth digits to be attached to the former three, so that the table thus embraces numbers from 1,000 up to 9,999. Opposite to every such number is a number with six places of figures. This is a decimal, though to save printing the decimal point is not printed, and it is the decimal part, or mantissa, of the logarithm of the number to which it corresponds. The characteristics are never printed, but are prefixed according to the rules XX and XXI. Hence, from such a table we can take out the logarithm of any number with any four significant digits.

70. If the number be given, its logarithm may be found as follows:—

To find the logarithm of a number consisting of not more than two digits, *i.e.*, which does not exceed 100, using the short table of logarithms, from 1 to 100, preceding the general table.

### RULE XXIV.

*Seek for the number proposed, considered as a whole number, in the column at the top of which is No., and the logarithm will be found opposite to it in the next column to the right hand.* Prefix the proper characteristic (by changing it if necessary) to the mantissa, see Rules XX and XXI, pages 49 and 50. The result is the logarithm sought.

NOTE.—It may be observed here, once for all, that the proposed number must be considered a whole number, and in case a decimal point occurs in the given number, no notice is taken

of it till we come to the insertion of the characteristic; and should cyphers occur *between the decimal point and the first significant figure*, these, also, are disregarded in entering the table, being only taken into account when determining the characteristic.

Ex. 1. Required the logarithm of 21, 2'1, '21, and '021.

In the first page of the Table, and in one of the vertical columns marked *No.*, we find 21, against which stands 1'322219, the logarithm sought. Since the mantissa of the logarithm of any number consisting of the same figures is the same whether the number be integral, fractional, or mixed, the logarithms of the numbers 2'1, '21, and '021 will have the same decimal part as 21, the characteristic only being changed, consequently the logarithm of 2'1 is 0'322219, the logarithm of '21 is 9'322219, and the logarithm of '021 is 8'322219.

Ex. 2. To find the logarithm of 52, 5'2, '52, and '00052:—

In the Tables we find the log. of 52 is 1'716003, and, therefore, simply changing the index, the log. of 5'2 is 0'716003, '52 is 9'716003, and the log. of '00052 is  $\bar{4}$ ·6716003 or 6'716003.

| No. | Nat. No. | No. | Nat. No. | No. | Nat. No.             | No. | Nat. No.         |
|-----|----------|-----|----------|-----|----------------------|-----|------------------|
| 1.  | 5        | 7.  | 41       | 13. | 94                   | 19. | '0091            |
| 2.  | 9        | 8.  | '004     | 14. | $\frac{1}{2}$ or '5  | 20. | 25'0             |
| 3.  | '009     | 9.  | 2'4      | 15. | $\frac{3}{4}$ or '75 | 21. | '024             |
| 4.  | '01      | 10. | 24       | 16. | 2'5                  | 22. | '000035          |
| 5.  | '0001    | 11. | '24      | 17. | $\frac{1}{4}$ or '25 | 23. | '000057          |
| 6.  | 14       | 12. | '0021    | 18. | '09                  | 24. | $\frac{1}{2000}$ |

71. To find the logarithm of a number consisting of not more than three places of figures (from 100 to 1000).

### RULE XXV.

*Find the given number in the left-hand column of the Table, and opposite it, in the next column, will stand the mantissa or decimal part of the logarithm.* Prefix the characteristic according to Rules XX and XXI. The result is the logarithm sought.

NOTE.—When we say “three figures” we mean independently of cyphers either to the right or to the left. Thus we should include 6340, 73200, and '00265 under the head of this problem.

NOTE.—If the number is less than three figures make up three by placing cyphers, if not already present (or by supposing them placed), on the right of the number, cyphers so added being regarded as decimal; then proceed as directed in the above Rule XXV. Thus the logarithm of 75 is the same as that of 75'0; the logarithm of 8 is the same as of 8'00; and that of '035 is the same as of '0350.

Ex. 1. Required the log. of 476, 4'76, and '00476.

We seek in the left-hand column of the Table for 476, against which in the column marked 0 at the top, stands the mantissa corresponding thereto; and this part by the rule is the same for each of the above numbers. Now prefixing the index according to the number of integral figures in the natural number, we find the log. of 476 is 2'677607; of 4'76 is 0'677607; and of '00476 is 7'677607.

Again, the logarithm of 576 is 2'760422; that of 39'4 is 1'595496; that of '0253 is  $\bar{2}$ ·403121.

| No. | Nat. No. | No. | Nat. No. | No. | Nat. No. | No. | Nat. No. |
|-----|----------|-----|----------|-----|----------|-----|----------|
| 1.  | 100      | 5.  | 673      | 9.  | 8'96     | 13. | '0147    |
| 2.  | 145      | 6.  | 794      | 10. | 1'47     | 14. | 424      |
| 3.  | 2'94     | 7.  | 982      | 11. | '147     | 15. | '0000448 |
| 4.  | 361      | 8.  | 4'80     | 12. | '901     | 16. | 448000   |

72. If the number contains four places of figures, exclusive of final cyphers, or cyphers included between the decimal point and the first significant figure.

### RULE XXVI.

*Find the first three figures in the vertical column on the left marked No., and the fourth in the horizontal column at the top of the page. Under this last, and opposite the three figures, will be found the mantissa of the logarithm sought. Prefix the index according to Rules XX and XXI. The result is the logarithm sought.*

Ex. 1. Required the logarithms of 4587 and of 0.0004587.

The first three figures (viz. 458) being found in the column to the left marked No., and the fourth (7) in the line of digits at the top of the page, the decimal part of logarithm (.661529) is found in the same horizontal line as the three first figures of the given number, and in the same column as the fourth. The characteristic is 3, being one less than the number of integers in the whole number; whence the completed logarithm is 3.661529. The logarithm of .0004587 is 7.661529, the characteristic being negative, and one more than the number of prefixed cyphers.

Again, the logarithm of 3470 is 3.541330; that of 3.492 is 0.543074; and that of 0.3468 is 7.540079; that of 74.39 is 1.871515; that of 325600 is 5.512648, in which case the mantissa of 3256 is taken out since it is the same as the mantissa of 3256000.

| No. | Nat. No. | No. | Nat. No. | No. | Nat. No. | No. | Nat. No. |
|-----|----------|-----|----------|-----|----------|-----|----------|
| 1.  | 1000     | 4.  | 5432     | 7.  | .01012   | 10. | 987.6    |
| 2.  | 1234     | 5.  | 26.06    | 8.  | 94.87    | 11. | .06843   |
| 3.  | 25.65    | 6.  | 2.606    | 9.  | 7.777    | 12. | .002784  |

NOTE.—The foregoing rule may be used not only in the case of numbers consisting of four places of figures, but may be made to include all numbers consisting of less than four significant digits, and so enable us to dispense with the Rules XXIV and XXV. Thus, if the number consists of less than four figures, make up four by placing cyphers, if not already placed (or by supposing them placed), on the right of the number; cyphers so added being regarded as decimals. Then proceed to find the mantissa of the log. by the foregoing rule.

Thus, the log. 75 is the same as the log. of 75.00; the log. of 8 is the same as the log. of 8.000; and that of .035 the same as that of .03500 (3500 in the tables).

Although the tables in Raper, Norie, and the "Nautical Tables" accompanying this work are constructed so that the mantissæ corresponding to more than four figures cannot be taken out directly, yet the mantissæ of numbers containing five or six figures can be found from them without much trouble.

73. If the number consists of more than four figures other than final cyphers, or if the number be a decimal fraction, cyphers immediately following the decimal point, we use

### RULE XXVII.

1°. *Cut off the first four figures and consider the rest as a decimal.*

2°. *Find the mantissa corresponding to the first four figures (Rule XXVI).*

3°. *Multiply the tabular difference by the decimal cut off, i.e., by the remaining figures of the given number, and cut off from the right-hand as many figures as there are in the multiplier, but at the same time adding unity if the highest figure thus cut off is not less than 5.*

4°. *Add the integer part of this product to the figures of the mantissa just found.*

The result is the mantissa of the required logarithm.

The characteristic or index is found by Rules XX and XXI, pages 49 and

Ex. 1. Required the logarithm of 28434.

|                  |  |
|------------------|--|
| Tab. diff.       | Mantissa of 2843 = 453777              |
| 153              | Tab. diff. $153 \times 4 = 612 = + 61$ |
| $\times 4$       | Characteristic 4                       |
| <u>612 or 61</u> | The log. of 28434 = 4.453838           |

We seek in the left hand column of the Table for 284 (the first three digits) and also at the top of the page in one of the horizontal columns we find 3 (the fourth figure), then in a line with the former and in the column with the latter at the top we have 453777, which is the mantissa of 2843. In a line with the quantity in the right hand column marked Diff., stands tab. diff. 153; which multiplied by 4, the remaining digit of the given number, produces 612; then cutting off one digit from this (since we have multiplied by only *one* digit) it becomes 61, which being added to 453777 (the mantissa of 2843) makes 453838, and, with the characteristic, 4.453838 the required logarithm.

The logarithm of 28434 is 4.453838, and the log of .028434 is 2.453838 or 8.453838.

Ex. 2. Required the logarithm of 12806.

|                    |  |
|--------------------|--|
| Tab. diff.         | Mantissa of 1280 = 107210                |
| 338                | Tab. diff. $338 \times 6 = 2028 = + 203$ |
| $\times 6$         | Characteristic 4                         |
| <u>2028 or 203</u> | The log. of 12806 = 4.107413             |

Ex. 3. Find the logarithm of 873457.

|                   |   |
|-------------------|---|
| Tab. diff.        | Mantissa of 8734 = 941213               |
| 50                | Tab. diff. $50 \times 57 = 2850 = + 29$ |
| $\times 57$       | Characteristic 5                        |
| <u>2850 or 29</u> | The log. of 873457 = 5.941242           |

The mantissa of the first four figures is found thus:—opposite the 873 and under 4 stands 941213; then in the right hand column in a line with this stands the diff. 50, which being multiplied by 57, the remaining digits of the given number, makes 2850; from this we cut off *two* digits to the right (since we have multiplied by *two* digits), when it becomes 18; but as the highest digit cut off is 5, we add unity, which makes 29. Then 5.941212 (the logarithm of 8734) + 29 = 5.941242 is the required logarithm.

Ex. 4. Required the logarithm of 628007.

|                                       |                 |
|---------------------------------------|-----------------|
| Mantissa of 6280 = 797960             | Tab. diff.      |
| Tab. diff. $69 \times 07 = 483 = + 5$ | 69              |
| Characteristic = 5                    | $\times 07$     |
| <u>The log. of 628007 = 5.797965</u>  | <u>483 or 5</u> |

The log. of 628067 is 5.798006, and the log. of .00628067 is 3.798006 or 7.798006. The Mantissa of the log. of each of these numbers being the same, the index only being varied.—(See Rules XX and XXI.)

|          |               |             |             |
|----------|---------------|-------------|-------------|
| 1. 38475 | 7. 43560      | 13. 200000  | 19. 365152  |
| 2. 38475 | 8. 78604      | 14. 056214  | 20. 9971370 |
| 3. 12345 | 9. 22055      | 15. 0098563 | 21. 321908  |
| 4. 54321 | 10. 078362    | 16. 643786  | 22. 1032764 |
| 5. 66666 | 11. 10000     | 17. 112906  | 23. 1000125 |
| 6. 92448 | 12. 000800073 | 18. 998095  | 24. 596423  |

74. To find the natural number corresponding to a given logarithm.—If the logarithm be given, the number which corresponds to it may be found by the following rules, which are the converse of those last given for finding the logarithm when the number is given.

Since the characteristic denotes how many places the first significant figure stands to the right or left of the unit's place; conversely, therefore, if logs. be given having for characteristics 1, 2, 3, ....  $\bar{1}$ ,  $\bar{2}$ ,  $\bar{3}$ , .... there are in the integral parts of the number to which these logs. belong, 2, 3, 4, .... 0,  $\bar{1}$ ,  $\bar{2}$ , ... digits respectively. In illustration of these remarks take the following:—

|   |       |                   |      |
|---|-------|-------------------|------|
| Log. 4'589950 (in which characteristic 4) gives 38900 |       |                   |      |
| 3'589950  | ..... | 3 ..              | 3890 |
| 2'589950  | ..... | 2 ..              | 389  |
| 1'589950  | ..... | 1 ..              | 38'9 |
| 0'589950  | ..... | 0 ..              | 3'89 |
| $\bar{1}$ '589950 }                                   | ..... | $\bar{1}$ or 9 .. | 389  |
| or 9'589950 }   | ..... |                   |      |
| $\bar{2}$ '589950 }                                   | ..... | $\bar{2}$ or 8 .. | 0389 |
| or 8'589950 }   | ..... |                   |      |
| &c.   |       | &c.               |      |

In which it will be observed that the first answer must consist of five integers, because the index of the given logarithm is 4; that the second answer must contain four integers, because the index of the given logarithm is 3; that the third answer must contain three integers, because the index of the logarithm is 2, &c., &c.; and that the sixth answer must be a decimal fraction having the first significant figure in the place of tenths, because the logarithmic index is  $\bar{1}$ ; and lastly, that the seventh answer must be a decimal fraction having the first significant figure in the place of hundredths, because the logarithmic index is  $\bar{2}$ .

75. From the foregoing it is evident that when the figures of the natural number have been found, we must place the decimal point so that the number of integral figures may be one more than the characteristic denotes. Cyphers must be supplied to the right, if necessary, to make up the number.

If the characteristic is negative place the decimal point to the left of the natural number found, along with as many cyphers as may remove the first significant figure to that place of decimals which the index expresses; that is, one cypher fewer than the number denoted by the characteristic, whence, to find the place of the decimal point proceed as follows:—

#### RULE XXVIII.

*Add 1 to the characteristic of the given logarithm, and mark off to the left the number of figures for whole numbers; the rest (if any) will be decimals.*

#### RULE XXIX.

*The number corresponding to a logarithm with a negative index is wholly decimal, and the number of cyphers following the decimal point is one less than the characteristic of the logarithm.*

But instead of the negative characteristic its *arithmetical complement* is sometimes used, in which case we proceed by

#### RULE XXX.

*Add 1 to the index, and subtract the number thus found from 10; the remainder is the number of cyphers to be prefixed to the figures taken out of the Tables. Place the dot before the first cypher.*



76. To find the natural number corresponding to any given logarithm.

When the mantissa or decimal part of the logarithm can be found exactly in the Table, we proceed by

### RULE XXXI.

1°. *Seek out the mantissa, and take from the column No. the three figures in the same horizontal row.*

2°. *From the head of the column take the fourth figure.*

3°. *From the characteristic find by the rules already given the position of the decimal point, and so adjust the local value of the figures. (Rules XXVIII, XXIX, and XXX, No. 75, page 56.)*

(a) When the characteristic of the given logarithm requires a greater number of digits to the left of the decimal point than there are in the number found by the above rule, the deficiency is made up by adding a sufficient number of cyphers to the right.

(b) If the natural number is a decimal fraction, and the final figure or figures are cyphers, they need not be written down.

### EXAMPLES.

Given the logarithm  $2.698970$  to find the natural number.

Entering the Table with the decimal part  $.698970$ , we find the natural number corresponding to it to be 5, or 50, or 500, or 5000, &c., but as the index of the logarithm is 2, the natural number must contain three integral figures. Hence the natural number of  $2.698970$  is 500.

Given the logarithm  $3.539954$  or  $7.539954$ : find the number.

Entering the Table with the decimal part, we find the corresponding number is 3467; to this we prefix two cyphers, since the index is 3; or adding 1 to 7 (8), and subtract 8 from 10, we have 2, the number of cyphers to be prefixed, and then the decimal point; hence the number corresponding to  $7.539954$  is  $.0034567$ .

When number corresponds the logarithm  $4.214314$ .

The decimal part of the log. being found opposite 163 and under the figure 8 at the top of the page; therefore the digits of the required number are 1638. But as the characteristic is 4, there must be in it 5 places of integers. A cypher is annexed (see Rule XXXI, (a)). Hence the required number is 16380.

Required the natural numbers corresponding to logs.  $0.176091$  and  $4.176091$ .

(1). The mantissa  $.176091$  stands in the Table opposite 150, and the column with 0 at the top; and the characteristic 0 shows that one of these is integral, whence the number sought is 1500 or 15 (see Rule XXVIII, page 56).

(2). The mantissa of second log. being the same as that of the first, the corresponding number will consist of the same significant figures, but the characteristic 4 shows that the first significant figure (1) must occupy the fourth place to the right of the decimal point, whence the number sought is  $.00015$ . (See Rule XXIX or XXX, page 56.)

Required the natural numbers whose logarithms are respectively  $1.813514$ ,  $0.303412$ ,  $4.996993$ ,  $2.299943$  or  $8.299943$ ,  $4.000000$ ,  $4.000000$ ,  $7.816109$ , we shall find them to be as follows:—

|               |   |         |           |
|---------------|---|---------|-----------|
| $1.813514$    | = | log. of | $65.09$   |
| $.303412$     | = | ..      | $2.011$   |
| $4.996993$    | = | ..      | $99310$   |
| $2.299943$    | = | ..      | $.01995$  |
| or $8.299943$ | = | ..      | $.01995$  |
| $4.000000$    | = | ..      | $10000$   |
| $4.000000$    | = | ..      | $.00001$  |
| $7.816109$    | = | ..      | $6548000$ |

Where it will be observed that the first answer must contain only two integers, as the index of the given logarithm is 1; that the second must contain only one integer as the characteristic is 0; that the third must consist of five integers, because the index of the given logarithm is 4, and therefore to 9931, the number found in the Table, a cypher is annexed, (see Rule XXXI, (a); and that the fourth answer must be a decimal, having the first significant figure two places to the right of the decimal point because the characteristic is 2; the fifth answer must consist of five integral figures (a cypher being annexed to make up the number) since the characteristic is 4; the mantissa of the sixth log., or .000000, gives the corresponding natural number 1000, but adjusting the decimal punctuation, or the local value of the figures, the characteristic 4 denotes that the first significant figure (1) must stand in the fourth decimal place, and, therefore, three cyphers must be prefixed, and the natural number will be .0001—the three final cyphers not being written down. Finally, the mantissa of last log. being found in the table gives the natural number corresponding as 6548, to which annex four cyphers; the characteristic 7 determines the number to consist of 8 integral figures.

| No. | Log.     | No. | Log.     | No. | Log.     | No. | Log.     |
|-----|----------|-----|----------|-----|----------|-----|----------|
| 1.  | 0.477121 | 11. | 3.091315 | 21. | 2.990561 | 31. | 7.991093 |
| 2.  | 0.903090 | 12. | 3.898506 | 22. | 4.541579 | 32. | 7.903524 |
| 3.  | 0.041393 | 13. | 2.538574 | 23. | 4.722522 | 33. | 2.621488 |
| 4.  | 1.301030 | 14. | 1.394977 | 24. | 1.744058 | 34. | 9.901349 |
| 5.  | 0.973128 | 15. | 3.845098 | 25. | 1.501196 | 35. | 3.662758 |
| 6.  | 1.161368 | 16. | 7.000000 | 26. | 7.875061 | 36. | 4.851258 |
| 7.  | 0.812245 | 17. | 5.825426 | 27. | 6.602062 | 37. | 6.778151 |
| 8.  | 2.767898 | 18. | 5.602060 | 28. | 8.845098 | 38. | 6.913761 |
| 9.  | 0.394452 | 19. | 4.698970 | 29. | 3.605197 | 39. | 0.004321 |
| 10. | 1.478422 | 20. | 5.000027 | 30. | 3.444669 | 40. | 5.868527 |

77. When, as usually happens, the mantissa cannot be found exactly in the Tables, but lies between two successive records in the Tables, and it is proposed to find the corresponding number correct to six places of figures, other than final cyphers immediately following a decimal point, the number is to be found by the method of proportional parts, on the supposition that, between two successive records in the table, the number advances in proportion to the increase of the logarithm.

78. To find the natural number corresponding to a given logarithm, when more than four figures are required. We proceed by

### RULE XXXII.

1°. Having found the next lower mantissa in the Tables, note the four figures which correspond to it.

2°. From the given logarithm subtract that taken out of the Tables, divide the remainder (annexing as many cyphers as there are digits required above four) by the tabular difference,\* and reduce the quotient to the form of a decimal.

3°. To the four figures already found, add this decimal, and shift the decimal point to suit the characteristic of proposed logarithm.

The result will be the required number.

NOTE.—It is needless to annex many cyphers to the dividend. We cannot with safety carry the natural number to more than six figures when the tabular difference contains three, or to more than five when the tabular difference contains only two.

\* The tabular difference (Diff.) spoken of here is given at the end of every line in the table, and is the difference of the successive logarithms in that part of the table.

Given the logarithm 3.543027 to find the natural number.

Given logarithm 3.543027  
Mantissa next lower in Table 542950 which corresponds to 3491.

$$\begin{array}{r} \text{Tab. diff.} = 124)7700(.62 \\ \underline{744} \\ 260 \\ \underline{248} \end{array}$$

Attaching this (.62) to the four figures, we have 349162, &c. The decimal punctuation or local value of the figures of the number can now be adjusted, and as the index is 3, we obtain, by pointing off four figures to the left, 3491.62 the natural number sought.

Given the logarithms 5.654329 and 2.654273 to find the natural numbers.

Given logarithm 5.654329  
Mantissa next less in Table 654273 which corresponds to 4511.

$$\begin{array}{r} \text{Tab. diff.} = 96)5600(58 \\ \underline{480} \\ 800 \\ \underline{768} \\ 32 \end{array}$$

*Ans.* 451158.

654273, which corresponds with the natural number 4511, is the logarithm next less than the given one; therefore the first *four* digits of the required number are 4511. Adding two cyphers to 56, the difference between 654273 and the given logarithm, it becomes 5600, which being divided by 96, the *tabular difference* corresponding with 4511, gives 58 as quotient and 32 as remainder. The *integers* of the required number (one more than 5, the characteristic) are, therefore, 451158. The mantissa of the second log. being the same as the first one, the natural number will contain the same significant figures, viz., 451158, but the characteristic 2 shows that the first significant figure of the nat. no. (4) must stand in the second place to the right of the decimal point; therefore, the nat. no. corresponding to 2.654273 is .0451158.

Let it be required to find the number of which the logarithm is 3.104831.

Given logarithm 3.104831  
Mantissa next lower in Table 104828 which corresponds to 1273.

$$\begin{array}{r} \text{Tab. diff.} = 341)3000(.008 \\ \underline{2728} \\ 272 \end{array}$$

Therefore, 3.104831 = log. of 1273.009 nearly. In dividing by tab. diff. we take remainder 3 and a cypher, then 341 in 30 goes no times, which we place down in the quotient, then taking another cypher we have 300, which contains 341 no times, lastly, 341 goes into 3000 eight times with 272 for remainder. The remainder 272 being more than half the quotient the last figure of the quotient (8) is increased by 1 or unity.

| No. | Log.     | No. | Log.     | No. | Log.        | No. | Log.        |
|-----|----------|-----|----------|-----|-------------|-----|-------------|
| 1.  | 2.931214 | 10. | 4.994603 | 19. | 0.230449    | 25. | 6.246631    |
| 2.  | 3.625343 | 11. | 4.925936 | 20. | 1.217845    | 26. | 1.998813    |
| 3.  | 4.851906 | 12. | 5.091512 | 21. | 3.984671    |     | or 9.998813 |
| 4.  | 4.361730 | 13. | 2.535224 |     | or 7.984671 | 27. | 1.895090    |
| 5.  | 1.725364 | 14. | 3.744726 | 22. | 4.463726    |     | or 9.895090 |
| 6.  | 1.972521 | 15. | 5.831835 |     | or 6.463726 | 28. | 4.932847    |
| 7.  | 5.659707 | 16. | 2.415671 | 23. | 2.241877    |     | or 6.932847 |
| 8.  | 5.734968 | 17. | 4.841989 |     | or 8.241877 | 29. | 5.565942    |
| 9.  | 5.823904 | 18. | 4.092561 | 24. | 6.371000    |     | or 5.565942 |

79. To find the arithmetical complement\* of the logarithm of a number.

The arithmetical complement of a number is the number by which it falls short of the units of the next higher denominator. (If  $x$  is any number whatever, then the arithmetical complement of  $x = 10 - x$ .) It is abbreviated into *ar. co.*

The most expeditious way of finding the arithmetical complement is as follows:—

### RULE XXXIII.

*Begin from the left; subtract every figure from 9 up to the lowest significant figure, which subtract from 10. Repeat the cyphers at the end, if any.*

(a) When the characteristic is negative it must be added to 9.

#### EXAMPLES.

Ex. 1. Find the ar. co. of 1.97043

(a) Ar. co. log. required 8.02957

(a) Thus we say, beginning at the left hand, 1 from 9, 9 from 9, 7 from 9, 0 from 9, 4 from 9, and 3 from 10.

The ar. co. of 3.607218 is 6.392782  
 . . . 0.714000 .. 9.286000  
 . . . 5.631642 .. 4.368358

Ex. 2. Find the ar. co. of .9086540

(b) Ar. co. log. required 0.913460

(b) In this example we proceed as before; thus 9 from 9, 0 from 9, 8 from 9, 6 from 9, 5 from 9, and as the next figure, 4, is the lowest significant figure (see Rule), we take it from 10, which leaves 6; lastly, the cypher at the end is repeated.

The ar. co. of 2.170630 is 7.829370  
 . . . 7.217034 .. 10.782966  
 . . . 3.178680 .. 12.821320

80. A subtractive quantity is, by this means, made additive. The process is equivalent to subtracting the number from 10, and the reason of it is evident on considering that to add 3 and subtract 10 is the same as to subtract 7. In like manner, instead of subtracting  $42^m 10^s$  for example, we may add  $17^m 50^s$  (the complement of  $60^m$ ), provided we subtract  $1^h$  (or  $60^m$ ); and thus any number of quantities, of which some are additive and some subtractive, may be rendered all additive, provided that the larger numbers which are employed in taking the complements be themselves subtracted.

### MISCELLANEOUS.

81. We here insert a collection of numbers, the logarithms of which are to be taken out of the Tables.

|          |            |             |             |                |
|----------|------------|-------------|-------------|----------------|
| 1. 8     | 11. 63.5   | 21. 8.44.4  | 31. 93.7654 | 41. 10000000   |
| 2. 0.1   | 12. 6390   | 22. .92096  | 32. 52790   | 42. .000000062 |
| 3. 4.9   | 13. .1463  | 23. .0899   | 33. 50000   | 43. 30000.9    |
| 4. 38    | 14. 3.874  | 24. 10000   | 34. 700090  | 44. 10000.9    |
| 5. 380   | 15. 6754   | 25. 4800    | 35. 264000  | 45. 594500     |
| 6. 100   | 16. .0876  | 26. 9080.8  | 36. 404007  | 46. 88590000   |
| 7. .0001 | 17. .3467  | 27. .00058  | 37. 500909  | 47. 287.642    |
| 8. 24.6  | 18. 1.083  | 28. .035872 | 38. 48.627  | 48. 0.003564   |
| 9. 3.88  | 19. 0.125  | 29. .000448 | 39. 93.514  | 49. .000856736 |
| 10. 900  | 20. 0.0009 | 30. 4480000 | 40. .032764 | 50. 65480000   |

82. Required the natural number of the following logarithms:

|             |              |              |              |              |
|-------------|--------------|--------------|--------------|--------------|
| 1. 2.309630 | 10. 0.565021 | 19. 7.954243 | 28. 5.606389 | 37. 7.883030 |
| 2. 3.676968 | 11. 0.778441 | 20. 3.959041 | 29. 5.000000 | 38. 3.625343 |
| 3. 0.954243 | 12. 2.769504 | 21. 4.705864 | 30. 2.881955 | 39. 1.725364 |
| 4. 1.698970 | 13. 5.774152 | 22. 0.415974 | 31. 7.167317 | 40. 2.627407 |
| 5. 0.000000 | 14. 5.421604 | 23. 7.000000 | 32. 7.875061 | 41. 3.686216 |
| 6. 2.000000 | 15. 3.000000 | 24. 3.954243 | 33. 0.000186 | 42. 0.400573 |
| 7. 2.564494 | 16. 6.394452 | 25. 7.160003 | 34. 6.947385 | 43. 5.002559 |
| 8. 3.563362 | 17. 1.415674 | 26. 5.654243 | 35. 2.963081 | 44. 4.321547 |
| 9. 2.621754 | 18. 1.188591 | 27. 0.434294 | 36. 0.763947 | 45. 0.875061 |

\* A very curious and valuable artifice, discovered by GUNTER about 1614.

83. Finally, we recommend the student to commit to memory the following table of logarithms to two places :—

| No. | Log. | No. | Log. | No. | Log. |
|-----|------|-----|------|-----|------|
| 1.  | 00   | 4.  | 60   | 7.  | 85   |
| 2.  | 30   | 5.  | 70   | 8.  | 90   |
| 3.  | 48   | 6.  | 78   | 9.  | 95   |

### MULTIPLICATION BY LOGARITHMS.

84. In multiplication we proceed by

#### RULE XXXIV.

1°. *Find the logarithms of the numbers, the product of which is required.* (For the method of taking out the log. of a number see pages 52 to 55.)

NOTE.—If any of the quantities is a decimal, either the negative characteristic of that quantity or its arithmetical complement is to be used (Rules XXXI and XXXII, page 50.)

2°. *Add these together, the sum will be the logarithm of the product.*

3°. *Find from the Tables the corresponding number.* (For the method of finding the corresponding number to a log., see pages 57 to 58.)

This will be required product.

NOTE 1. When the characteristics are negative and subtracted from 10 (see Rule XXX, page 56), if the sum of such characteristic exceeds the sum of tens borrowed, the product will be a whole number; otherwise it will be a decimal.

NOTE 2. When the characteristics of the logarithms to be added are all positive, it is evident that their sum will be positive.

NOTE 3. *If the characteristics are all negative, their sum diminished by the figure—if any—carried from the sum of the mantissa or positive decimal parts will be negative.*

NOTE 4. *If some characteristics are positive and the others negative, find the sum of the positive characteristics together with any figure which may be carried from the decimal part of the logarithm; also add the negative characteristics together; subtract the less of these quantities from the greater and prefix to the difference the sign belonging to the greater. But if a positive and a negative characteristic are exactly equal to each other, cancel both; this is done in practice by simply drawing the pen through them.*

#### EXAMPLES.\*

1. Multiply 77 by 100. The log. of 77 and 100 being taken from the table, we have

77 log. 1.886491  
100 log. 2.000000

7700 log. 3.886491

We have here added the logs. of the given factors, and having sought in the Table for the mantissa .886491, we have found the figures of the nat. no. corresponding to be 7700; the index 3 determines four of these to be integral; hence the product is 7700 (Rule XXVIII, page 56).

3. Multiply 378 by 50.

378 log. 2.577492  
50 log. 1.698970

18900 log. 4.276462

The mantissa of log., viz., .276462, is found *exactly* in the Table in a line with 189, and under 0; but as the characteristic 4 requires 5 digits in the integer part, we therefore add a cypher (0), which gives 18900 as the nat. no. corresponding to the proposed log. This is according to Rule XXXI (a), page 56.

2. Multiply 97 by 83. The log. of 97 and 83 being taken from the Table, we have

97 log. 1.986772  
83 log. 1.919078

8051 log. 3.905850

We add the logs. of the given factors, and then seek in the Table for the mantissa .905850, which corresponds to the natural number 8051; the index 3 determines four of these to be integral; hence the product is 8051 (Rule XXVIII, page 56).

4. Multiply 3456 by 500.

3456 log. 3.538574  
500 log. 2.698970

1728000 log. 6.237544

The characteristic 6 requires 7 digits in the integer part of product, we therefore annex 3 cyphers which gives 1728000 as the nat. no. required. (See Rule XXXI, (a), page 56).

\* In these examples, and for several of the subjoined Exercises, the logarithmic is more tedious than the ordinary method of calculation; the purpose here intended being simply to make the student familiar with the process of finding products logarithmically. It must be remembered too, that by the logarithmic process, we generally obtain only an approximate value of the required result.

5. Multiply 963 by 48.9 by common logarithms. The log. of 963 and 48.9 being taken from the Table, we have

$$\begin{array}{r} 963 \text{ log. } 2.983626 \\ 48.9 \text{ log. } 1.689309 \\ \hline \text{log. } 4.672935 \\ \text{(next lower in Table) } 4.672929 \text{ gives } 4709 \\ \hline \text{Product } 47090.7 \quad 92)6.00(06 \\ \quad \quad \quad 552 \\ \quad \quad \quad \hline \quad \quad \quad 48 \end{array}$$

We have here added the logs. of the given factors together, and having sought for the given mantissa 672935, which is not to be exactly found in the Tables, we obtain the next less mantissa 672929, which we subtract from the given mantissa; the difference is 6, to which two cyphers are annexed, and then we divide by the tabular difference 92, whence we obtain 07 nearly; the remainder, 48, being more than half the divisor, 1 is added to the last figure in the quotient (0); attaching these to the four figures obtained previously, we have 470907; the characteristic 4 determines five of these to be integral; hence the product is 47090.7 (Rule XXVIII, page 56). The multiplier containing one decimal place, the product is worked out to one place of decimals.

8. Multiply 29.42 by 8.6 by common logarithms.

$$\begin{array}{r} 29.42 \text{ log. } 1.468643 \\ 8.6 \text{ log. } 0.934498 \\ \hline 2.403141 \\ \text{(next lower in Tab.) } 403120^* \text{ gives } 2530 \\ \hline \text{Product } 253.012 \quad 171)2.100(12+ \end{array}$$

In this instance the characteristic of the log. of the product is 2, hence the integral part of the natural number must contain 3 figures; but since there are decimals in both factors, there must be decimals in the product—as many decimal places as there are in both the multiplier and multiplicand together. In 29.42 are two decimal places, and in 8.6 one; hence in the product three decimal places are required, making, with the three integral figures, in all six places. Now the next lower mantissa found in the table gives the four corresponding figures 2530, leaving two figures to be found. (See Rule XXXII, page 58.)

\* This log. is taken from Norie, and is incorrect in the last decimal figure, which ought to be 1, as given in Raper's table; the true log. being 40312052.

10. Multiply 99.9 by 8.63.

$$\begin{array}{r} 99.9 \text{ log. } 1.999565 \\ 8.63 \text{ log. } 0.936011 \\ \hline 862.136 \text{ log. } 2.935576 \\ \quad \quad \quad 558 \\ \hline 5,0)180,0 \\ \quad \quad \quad \hline \quad \quad \quad 36 \end{array}$$

6. Multiply 734 by 23.

$$\begin{array}{r} 734 \text{ log. } 2.865696 \\ 23 \text{ log. } 1.361728 \\ \hline \text{log. } 4.227424 \\ \text{(Next lower mantissa) } 4.227372 \text{ corresponds} \\ \hline \text{Product } 16882 \quad 258)520(2 \\ \quad \quad \quad 516 \end{array}$$

7. Multiply 498 by 376.

$$\begin{array}{r} 498 \text{ log. } 2.697229 \\ 376 \text{ log. } 2.575188 \\ \hline 187248 \text{ log. } 5.272417 \\ \quad \quad \quad 306 \\ \hline \text{Diff. } 232)11100(48 \text{ nearly} \end{array}$$

9. Multiply .0567 by .00339.

Both multiplier and multiplicand being decimals, the characteristics of these factors will be negative, but instead we use their arithmetical complements, thus:—

$$\begin{array}{r} .0567 \text{ log. } 8.753583 \\ .00339 \text{ log. } 7.530200 \\ \hline .0001922 \text{ log. } 6.283783 \end{array}$$

Here 10 is borrowed to find the characteristic both of the multiplicand .0567, and the multiplier .00339 (See Rule XXII, page 50). The sum of the characteristics, including the 1 carried from the decimal part of the log., amounts to 16; reject 10 and write down 6 for the index of the log. of product. Then, seeking in the Table for the decimal part, viz., 283783, the natural number corresponding to it is found to be 1022; and since the sum of the indices 16 is 4 less than the 20 borrowed, (see Rule XXXIV, Note 1, page 61) the product is a decimal fraction and the first significant digit must stand in the fourth decimal place; hence the product is .0001922.

Or thus—using negative indices:

$$\begin{array}{r} .0567 \text{ log. } \bar{2}.753583 \\ .00339 \text{ log. } \bar{3}.530200 \\ \hline .0001922 \text{ log. } \bar{4}.283783 \end{array}$$

In adding, when we come to the places of tenths, the process is 5 and 7 are 12, 2 to put down and 1 to carry, and since the characteristics are both negative (2) and (3), we diminish their sum (5) by the number carried (1), which leaves 4 for the index (see Rule XXXIV, Note 3, page 61). We prefix 3 cyphers because the index being 4 the first significant figure of product must stand in the fourth place from the decimal point.

11. Multiply 436 by 19.7.

$$\begin{array}{r} 436 \text{ log. } 2.639486 \\ 19.7 \text{ log. } 1.294466 \\ \hline 8589.2 \text{ log. } 3.933952 \\ \quad \quad \quad 43 \\ \hline 51)90(2 \text{ nearly} \end{array}$$

12. Find the product of  $\cdot 073$  by  $\cdot 00028$  by logarithms.

$$\begin{array}{r} \cdot 073 \log. 8^{\circ}863323 \\ \cdot 00028 \log. 6^{\circ}447158 \\ \hline \end{array}$$

$$\cdot 00002044 \log. 5^{\circ}310481$$

Or, using negative characteristics, thus:—

$$\begin{array}{r} \cdot 073 \log. 2^{\circ}863323 \\ \cdot 00028 \log. 4^{\circ}447158 \\ \hline \end{array}$$

$$\cdot 00002044 \log. 5^{\circ}310481$$

In adding, when we come to the place of tenths, the process is 5 and 8 are 13, 3 to put down and 1 to carry; and this 1 being a positive quantity. Hence, in the above, +1, -2, and -4 are to be algebraically added together to form the new characteristic. The sum of the two characteristics (both negative) viz., -2 and -4 is -6, which diminished by +1 leaves -5 for the new characteristic. We prefix four cyphers, because the characteristic being 5 shows that the first significant figure must stand in the fifth decimal place. (Rule XXXIX page 56).

14. Multiply  $\cdot 0172$  by  $\cdot 00214$ .

$$\begin{array}{r} \cdot 0172 \log. 8^{\circ}235528 \\ \cdot 00214 \log. 7^{\circ}330414 \\ \hline \end{array}$$

$$\cdot 000036808 \log. 5^{\circ}565942$$

In this instance 10 is borrowed, in finding the index of the log. both of the multiplier and multiplicand, and 10 is rejected from the sum, which sum (15) being 5 less than the amount borrowed (20), indicates that the product must be a decimal fraction, and the first significant digit stands in the fifth decimal place; hence the product is  $\cdot 000036808$ . This is according to Rule XXXIV, Note 1, page 61.

Or thus—using negative indices: Ex. 14.

$$\begin{array}{r} \cdot 0172 \log. 2^{\circ}235528 \\ \cdot 00214 \log. 3^{\circ}330414 \\ \hline \end{array}$$

$$\cdot 000036808 \log. 5^{\circ}565942$$

The characteristics of both logs. being negative, the sum of them is taken, and this, with the negative sign over it, is put down as the characteristic of the log. of product. We prefix four cyphers to the number taken out of the table, since the characteristic being 5, the first significant figure of the product must stand in the fifth place from the decimal point.

13. Multiply 24000 by  $\cdot 000783$ .

$$\begin{array}{r} 24000 \log. 4^{\circ}380211 \\ \cdot 000783 \log. 6^{\circ}893762 \\ \hline \end{array}$$

$$18^{\circ}7919 + \log. 1^{\circ}273973$$

Here 10 was borrowed in determining the index of the log. of  $\cdot 000783$ , and since the sum of the indices (including 1 carried from the decimal part of log.) is eleven, we reject or pay back the 10 borrowed, which leaves 1 for the index, and the nat. number corresponding is found to be 187919, and we mark off to the right two figures (1 more than the characteristic) whence the answer is 187919+.

Or thus—using negative indices: Ex. 13.

$$\begin{array}{r} 24000 \log. 4^{\circ}380211 \\ \cdot 000783 \log. 4^{\circ}893762 \\ \hline \end{array}$$

$$18^{\circ}7919 + \log. 1^{\circ}273973$$

Here the 1 which is carried after adding 1, 8, and 3 (in the place of tenths), instead of increasing the 4 leaves 3. This is according to Rule XXXIV, Note 4, page 61.

15. Required the product of  $17^{\circ}25$ ,  $0^{\circ}82$ , and  $0^{\circ}65$ .

$$\begin{array}{r} 17^{\circ}25 \log. 1^{\circ}236789 \\ 82 \log. 9^{\circ}913814 \\ 65 \log. 8^{\circ}812913 \\ \hline \end{array}$$

$$0^{\circ}919425 \log. 9^{\circ}963516$$

Here 10 is borrowed, to find the characteristics of log. both of the second and third factors, and subtracting the sum of the indices 19 from 20 leaves 1; the sum being less than the number borrowed, the product is a decimal, and hence the first significant figure must occupy the first place to the right of the decimal point. (See Rule XXXIV, Note 1, page 61.)

Or thus:—

$$\begin{array}{r} 17^{\circ}25 \log. 1^{\circ}236789 \\ 82 \log. 9^{\circ}913814 \\ 65 \log. 8^{\circ}812913 \\ \hline \end{array}$$

$$0^{\circ}919425 \log. 9^{\circ}963516$$

Here we have 1 to carry from the mantissa, which added to the positive characteristic 1 (characteristic of log.  $17^{\circ}25$ , see above) makes positive 2. Now the sum of the negative indices is 3 (negative 3), and, therefore, since where one is positive and the other is negative the difference is the characteristic; we have +2 from 3 leaves 1 for the characteristic; (see Rule XXXIV, Note 4, page 61) and the first significant figure of the quotient must occupy the first place to the right of the decimal point (Rule XXVIII, page 56).

### EXAMPLES FOR PRACTICE.

- Multiply by logs. 85 by 70; 39 by 27; 100 by 10; and 369 by 9.
- Multiply 538 by  $1^{\circ}74$ ; 601 by 18; 250 by  $12^{\circ}5$ ; and 3964 by 7.
- Multiply  $20^{\circ}42$  by  $0^{\circ}5$ ;  $3^{\circ}646$  by  $0^{\circ}75$ ;  $2^{\circ}745$  by  $0^{\circ}24$ ; and  $5^{\circ}792$  by  $6^{\circ}5$ .
- Multiply 5671 by  $4^{\circ}7$ ; 517 by 659;  $60^{\circ}609$  by 72;  $1^{\circ}955$  by  $10^{\circ}04$ ; and  $758875$  by 8.
- Multiply 127 by 304; 476 by 100;  $80^{\circ}08$  by  $5^{\circ}98$ ; 5760 by 30; and 970 by 630.
- Multiply  $37^{\circ}6$  by 249;  $44^{\circ}4$  by  $22^{\circ}2$ ;  $182^{\circ}7$  by 250;  $2807$  by 200; and  $63^{\circ}055$  by 84.
- Multiply  $280054$  by 50; 30967 by 90; 23716 by 350; and 45670 by 690.
- Multiply  $82^{\circ}33$  by  $15^{\circ}3$ ;  $47^{\circ}6$  by  $6^{\circ}82$ ; 10000 by 10; and  $4^{\circ}02674$  by  $0^{\circ}123456$ .
- Multiply 78960 by 400;  $756^{\circ}875$  by 8;  $94^{\circ}055$  by 74; and 1975 by  $10^{\circ}76$ .
- Multiply 732 by 543;  $58^{\circ}7$  by  $66^{\circ}4$ ; 3000 by  $100^{\circ}14$ ; and 60060 by 700.
- Multiply  $543^{\circ}29$  by  $3800^{\circ}62$ ;  $90^{\circ}43$  by  $712^{\circ}2$ ;  $87^{\circ}305$  by  $4^{\circ}09$ ; and  $209^{\circ}36$  by 46.
- Multiply  $348^{\circ}25$  by  $7^{\circ}125$ ;  $498^{\circ}256$  by  $41^{\circ}2467$ ;  $56^{\circ}3426$  by  $0^{\circ}23579$ ;  $123456$  by  $26813^{\circ}9$ .
- Multiply  $\cdot 0001468$  by  $\cdot 000395$ ;  $0^{\circ}0006$  by  $10^{\circ}0004$ ;  $\cdot 605$  by  $\cdot 00000091$ ; and  $35^{\circ}691$  by  $\cdot 0048$ .

14. Multiply  $\cdot 00146$  by  $\cdot 039$ ;  $5900$  by  $\cdot 00071$ ;  $4\cdot 189$  by  $\cdot 00071$ ; and  $247\cdot 55$  by  $56\cdot 72$ .  
 15. Multiply  $527\cdot 45$  by  $1\cdot 6938$ ;  $10\cdot 5526$  by  $317\cdot 145$ ;  $\cdot 007461$  by  $\cdot 3351767$ ; and  $\cdot 0700379$  by  $\cdot 0086752$ .  
 16. Multiply  $\cdot 1$  by  $\cdot 1$ ;  $\cdot 0001$  by  $\cdot 00001$ ;  $\cdot 011$  by  $1\cdot 01$  and  $\cdot 00101$ ; and  $1000$  by  $100$ .

## DIVISION BY LOGARITHMS.

85. In division we proceed by

## RULE XXXV.

1°. Find the logarithms of the numbers the quotient of which is required.

NOTE. If the dividend or divisor, or both, are decimals, the negative characteristic of of that quantity, or its arithmetical complement is to be used.

2°. Subtract the logarithm of the divisor from that of the dividend, (adding 10 to the characteristic of this last, if required); the difference will be the logarithm of the quotient.

3°. Find from the Tables the corresponding number.

This will be the required quotient.

NOTE 1. When the divisor is greater than the dividend, the characteristic of the logarithm of the quotient will come out negative—the quotient itself being, evidently, a decimal; but if we wish to avoid the use of negative characteristics it will be necessary to add 10 to the characteristic of the dividend when subtracting the logarithm of the divisor, and the characteristic of the remainder is the arithmetical complement of the negative characteristic of the quotient. (See Ex. 4, 5.)

NOTE 2. If, for the sake of convenience, the line containing the quantity to be subtracted, when the quantities have been written down one under the other, is called the take line and the quantity from which it is to be subtracted the *from* line, then subtracting in the usual way until we come to the characteristics; if their signs are alike take the difference of them, and if the *from* line is the *greater*, prefix to the remainder the *given sign*; but if the *take* line is the *greater* prefix the *contrary* of the given sign. If the signs are different, take the *sum* of the characteristics and prefix the sign of the *from* line. The figure borrowed when subtracting the decimal part of the logarithm, when carried to the characteristic, is always to be added, and therefore make a negative characteristic less, thus 2 carried to 5 makes it  $\bar{3}$ .

NOTE 3. Otherwise, if one or both of the given terms are decimals, remove the decimal points till the factors contain whole numbers, and the dividend the greatest; then if the dividend be more places removed than the divisor, remove the decimal point of the quotient as many places to the *left hand*, but if the divisor be more places removed, then remove the decimal point of the quotient as many places to the *right hand*. If the dividend and divisor be equally removed, the quotient is not to be altered.

## EXAMPLES.

1. Divide 3192 by 76.

The log. of 3192 is taken out according to Rule XXVI, page 54, and the log. of 76 by Rule XXIV, page 52.

$$\begin{array}{r} 3192 \text{ log. } 3\cdot 504063 \\ 76 \text{ log. } 1\cdot 8810814 \\ \hline \text{Quotient } 42\cdot 0 \text{ log. } 1\cdot 633249 \end{array}$$

3. Divide 579416 by 4324.

$$\begin{array}{r} \text{Log. of } 5794 = 762978 \quad \text{Tab. diff. } 75 \\ \text{Parts for } 16 \quad + 12 \quad \times 16 \\ \hline \text{Log. of } 579416 = 5\cdot 762990 \quad 450 \\ \quad \quad \quad \quad \quad 75 \\ \hline \quad \quad \quad \quad \quad 12,00 \\ 579416 \text{ log. } 5\cdot 762990 \\ 4324 \text{ log. } 3\cdot 635886 \\ \hline 134\cdot 0 \text{ log. } 2\cdot 127104 \end{array}$$

2. Divide 830772 by 982.

The log. of 830772 is taken out by Rule XXVII, page 54. We seek in the left hand column of the Table (No.) for 830 (the first three digits), and also at the top of the page in one of the horizontal columns for the fourth figure 7, then in a line with the first and under the latter we have 919444. In a line with this quantity and in the right hand column marked *Diff.* stands 52, which multiplied by the remaining figures of the nat. number, viz. 72, produces 3744; then cutting off two digits from these (since we multiplied by two digits) it becomes 37, which being added to 919444, the mantissa of 8307, makes 919481, and with the characteristic 5, is 5919481. The work will stand thus:—

$$\begin{array}{r} \text{Log. } 8307 = 919444 \quad \text{Tab. diff. } 52 \\ \text{Diff. for } 72 + 37 \quad \times 72 \\ \hline \quad \quad \quad 919481 \quad 104 \\ \quad \quad \quad \quad \quad 364 \\ \hline \quad \quad \quad \quad \quad 37,44 \\ 830772 \text{ log. } 5\cdot 919481 \\ 982 \text{ log. } 2\cdot 992111 \\ \hline \text{Quotient } 846\cdot 0 \text{ log. } 2\cdot 927370 \end{array}$$



## 4. Divide 34 by 582.

$$\begin{array}{r} 34 \log. 1.531479 \\ 582 \log. 2.764923 \\ \hline \end{array}$$

Quotient  $\cdot 05842 \log. 8.766556$ 

In this instance 10 is added to the characteristic of the dividend to enable the subtraction of the log. of divisor to be made, and to avoid negative characteristics; the quotient therefore is a decimal.

Or thus, using negative characteristic.

$$\begin{array}{r} 34 \log. 1.531479 \\ 582 \log. 2.766923 \\ \hline \end{array}$$

Quotient  $\cdot 05842 \log. 2.766556$ 

In this example, when carrying 1 to the characteristic 2, we have to subtract 3 from 1 which gives  $-2$  (negative 2); or, according to Note 2, the characteristics having like signs (+) their difference is taken, and the take line being the greater, prefix to the remainder a contrary sign ( $-$ ) to the given one.

## 5. Divide 3672 by 51000.

$$\begin{array}{r} 3672 \log. 3.564903 \\ 51000 \log. 4.707570 \\ \hline \end{array}$$

Quotient  $\cdot 072 \log. 8.857333$ 

Here 10 is added to the characteristic of the dividend before subtracting log. of divisor. The divisor being greater than the dividend the quotient is evidently a decimal.

Or thus, using negative characteristics:—

$$\begin{array}{r} 3672 \log. 3.564903 \\ 51000 \log. 4.707570 \\ \hline \end{array}$$

Quotient  $\cdot 072 \log. 2.857333$ 

In this instance, when carrying 1 to the characteristic 4, we have to subtract 5 from 3, which gives  $-2$  (negative 2); or by Note 2—Take the difference of characteristics, as they are of the same sign (+), and prefix a contrary sign ( $-$ ) to the remainder, the take line being the greater.

6. Find the quotient of  $\cdot 09983 \div \cdot 67$ 

$$\begin{array}{r} \cdot 09983 \log. 8.999261 \\ \cdot 67 \log. 9.826075 \\ \hline \cdot 149 \log. 9.173186 \end{array}$$

Before subtracting the log. of divisor from that of the dividend 10 must be added to the characteristic of the dividend; or, using negative characteristics the work will stand thus:—

$$\begin{array}{r} \cdot 09983 \log. 2.999261 \\ \cdot 67 \log. 7.826075 \\ \hline \cdot 149 \log. 7.173186 \end{array}$$

In this instance both characteristics are of the same sign ( $-$ ), the from line the greater: the characteristic of log. of quotient is marked with sign ( $-$ ).

7. Divide  $\cdot 01958$  by  $\cdot 4828$ .

$$\begin{array}{r} \cdot 01958 \log. 8.291813 \\ \cdot 4828 \log. 9.683687 \\ \hline \cdot 04056 \log. 8.608126 \end{array}$$

Here 10 has to be borrowed in subtracting the log. of divisor from that of dividend; or using negative characteristics the work will stand thus:—

$$\begin{array}{r} \cdot 01958 \log. 2.291813 \\ \cdot 4828 \log. 7.683687 \\ \hline \cdot 04056 \log. 2.608126 \end{array}$$

To obtain the characteristic of the quotient ( $2$ ) the 1 that is carried, and which is positive, is added to the 7 producing 8, which has then to be subtracted from 2, leaving 2.

8. Divide  $18.792$  by  $\cdot 000783$ .

$$\begin{array}{r} \text{Log. } 18.792 = 273927 \quad \text{Diff. } 232 \\ \text{Diff. for } 2 = + 46 \quad \quad \quad 2 \\ \hline \end{array}$$

$$\text{Log. } 18.792 = 1.273973 \quad 46,4$$

$$\text{Log. } 18.792 = 1.273973$$

$$\text{Log. } \cdot 000783 = 6.893762$$

$$\text{Log. } 24000 = 4.380211$$

Or, using the negative characteristic of divisor.

$$\text{Log. } 18.792 = 1.273973$$

$$\text{Log. } \cdot 000783 = 4.893762$$

$$\text{Log. } 24000 = 4.380211$$

In the subtraction it will be seen that carrying 1 to the 4, we say 1 and 4 make 5, and 3 taken from 1 leaves + 4. The characteristics being of different names, + and  $-$ , their sum is taken, and the remainder takes the same sign as the from line—in this case it is positive (+). In writing down the result the + is left out.

9. Divide  $26843$  by  $\cdot 03010$ .

$$\begin{array}{r} \text{Log. } 2684 = 428782 \quad \text{Tab. diff. } 162 \\ \text{Diff. for } 3 = + 49 \quad \quad \quad \times 3 \\ \hline \end{array}$$

$$\text{Log. } 26843 = 428831 \quad 48,6$$

$$26843 \log. 4.428831$$

$$\cdot 03010 \log. 8.478566$$

$$891794 \log. 5.950265$$

$$219$$

$$49)4600(94 \text{ nearly.}$$

Or thus:—

$$26843 \log. 4.428831$$

$$\cdot 03010 \log. 2.478566$$

$$891794 \log. 5.950265$$

Here the characteristic of the second log. is 2, but following the rule, we have changed it to positive 2. The characteristic of first log. being positive 4, the two are added, the sum being positive 6, but having borrowed 1, the correct characteristic is 5, and being positive, the quotient will contain 6 integral figures.

10. Divide .8 by .0000002.

$$\begin{array}{r} .8 \log. 9.903090 \\ .0000002 \log. 3.301030 \\ \hline 4000000 \log. 6.602060 \end{array}$$

The divisor being *less* than the dividend, the quotient is evidently an integer, and the characteristic denotes that it is a whole number consisting of seven places of figures; cyphers are therefore annexed to make up the required number.

$$\begin{array}{l} \text{Or, Log. } .8 = 7.903090 \\ \text{Log. } .0000002 = 3.301030 \end{array}$$

$$\text{Log. } 4000000 = 6.602060$$

The characteristics are both negative, take their difference, and prefix to the remainder the contrary sign to the given one, as the *take* one is the greater.

12. Divide 469.76 by .937.

$$\begin{array}{r} 469.76 \log. 2.671877 \\ .937 \log. 9.971740 \end{array}$$

$$\text{Quotient } 501.345 \log. 2.700137$$

$$\begin{array}{l} \text{Or, } 469.76 \log. 2.671877 \\ .937 \log. 9.971740 \end{array}$$

$$501.345 \log. 2.700137$$

14. Divide .012550 by 1004000.

$$\begin{array}{r} .012550 \log. 8.098644 \\ 1004000 \log. 6.001734 \end{array}$$

$$.0000000125 \log. 2.096910$$

$$\begin{array}{l} \text{Or, } .012550 \log. 8.098644 \\ 1004000 \log. 6.001734 \end{array}$$

$$.0000000125 \log. 8.096910$$

The characteristic of the dividend is 8, that of the divisor positive 6; then according to Note 2, the signs being *unlike*, take the *sum* of the characteristics, prefixing the sign of the *from* line (—).

11. Divide .00815 by .000275.

$$\begin{array}{r} .00815 \log. 7.911158 \\ .000275 \log. 6.439333 \end{array}$$

$$\text{Quotient } 29.6363 \log. 1.471825$$

$$\begin{array}{l} \text{Or, } .00815 \log. 7.911158 \\ .000275 \log. 6.439333 \end{array}$$

$$29.6363 \log. 1.471825$$

The index of the divisor 7 being supposed changed to positive 4, the difference between which and 3 leaves positive 1 for index of quotient. Or, proceeding according to Note 2—Since the characteristics have *like* signs, take their difference; the remainder takes a positive sign, or a contrary sign to the *take* line, which is the greater.

13. Divide 6 by .0000001.

$$\begin{array}{r} 6 \log. 0.778151 \\ .0000001 \log. 3.000000 \end{array}$$

$$60000000 \log. 7.778151$$

The divisor is *less* than the dividend, the quotient, therefore, is a whole number, and the characteristic 7 indicates that it consists of 8 places of figures; annex cyphers to make up the number.

$$\begin{array}{l} \text{Or, } 6 \log. 0.778151 \\ .0000001 \log. 3.000000 \end{array}$$

$$60000000 \log. 7.778151$$

15. Divide .027472 by 3.434.

$$\begin{array}{r} \text{Log. } 2747 = 438859 \quad \text{Diff. } 158 \\ \text{Diff. for } 2 = + 32 \quad \times 2 \end{array}$$

$$\text{Log. } 2747 = 438891 \quad 31,6$$

$$\text{Log. } .02747 = 8.438891$$

$$\text{Log. } 3.434 = 0.535800$$

$$\text{Log. } .008000 = 7.903091$$

Or, using negative characteristics, thus:—

$$\text{Log. } .02747 = 8.438891$$

$$\text{Log. } 3.434 = 0.535800$$

$$\text{Log. } .008 = 7.903091$$

### EXAMPLES FOR PRACTICE.

1. Divide 6391 by 77; 21636 by 36; 6384 by 76; and 93750 by 750.
2. Divide 9504000 by 98; 45000 by 9; 6071000 by 8; and 58469 by 981.
3. Divide 382.746 by 593; 218432 by 495; 300360 by 10012; and 365.55 by 5.5.
4. Divide 783254 by 250689; 79632 by .019354; .0092852 by .0003461; and .654831 by .474586.
5. Divide .0008464 by .0002852; .05826 by .95381; .019354 by .79632; .0003461 by .0092852; .00005 by 2.5, by 25, and by .0000025.
6. Divide 77000000 by 9999; 680300 by 681500; 100.002 by 1.0012; and 75759.6 by 13.062.
7. Divide 1.32704 by .0358; .7156 by 2.68878; 87.641 by .000368; and .563426 by .023574.
8. Divide 999999 by 10101; 57634.1 by 276.4; 69.7565 by .97564; and 352740 by 56780.
9. Divide 40048000 by 800; 11123100 by 340; 1869210 by 90; and 1875000 by 15000.
10. Divide 75.2484 by 8.59; 147392 by 440; 1962820 by 10.04; and 888888 by 88000.

11. Divide 248·25 by 364·87; 235316 by 293·864; 5·6949 by 53·058; 3876000 by 1200; and 42 by ·00007.
12. Divide 2064840 by 3800·62; 33248100 by 830000; 13·5056 by ·734; and 674·80 by ·0763.
13. Divide ·06314 by ·0007241; ·004728 by 0·2382; 36·49 by 192·24; ·048869 by ·0071698.
14.  $19 \div 72$ ;  $19 \div \cdot 72$ ;  $19 \div \cdot 72$ ;  $19 \div \cdot 0072$ ;  $6 \div \cdot 0000003$ ; and  $9 \div \cdot 0000003$ .
15.  $\cdot 01237 \div \cdot 10846$ ;  $28\cdot 7642 \div \cdot 083456$ ;  $\cdot 010011 \div \cdot 0993$ ; and  $\cdot 048869 \div \cdot 0071698$ .
16.  $\cdot 1 \div \cdot 0004572$ ;  $1 \div \cdot 0011636$ ;  $11\cdot 2221 \div 111$ ;  $4000 \div \cdot 000125$ ; and  $\cdot 562625 \div 52643$ .
17.  $\cdot 0001 \div \cdot 0001$ ;  $1000000 \div \cdot 0000001$ ;  $10 \div 100$ ;  $\cdot 00000001 \div \cdot 000001$ ;  $1000 \div \frac{1}{18}$ .

86. When it is proposed to find the value of an expression in which both multiplication and division are signified, the sum of the logarithms of the factors of the dividend, diminished by the sum of the logarithms of the factors of the divisor will be the logarithm of the value required.

$$\begin{array}{r} \text{Thus: to find the value of } \frac{209 \times 573 \times 63}{287 \times 2101} \\ \begin{array}{r} 209 \log. 2\cdot 320146 \\ 573 \log. 2\cdot 758155 \\ 63 \log. 1\cdot 799341 \\ \hline 6\cdot 877642 \\ 5\cdot 780308 \\ \hline 1\cdot 097334 \end{array} \end{array}$$

Ans.: 12·5122 log. 1·097334

87. It is very often expedient to transform the logarithm of a divisor into that of a multiplier, and it is customary, in such calculations, to avoid not only negative logarithms, but negative indices also, by substituting for a subtraction logarithm its arithmetical complement (*See No. 79, page 60*). This makes the operation consist of a single addition; only we must diminish the result by subtracting 10 for every arithmetical complement that has been used. By this means the process of division is less open to error from mistakes when logarithms with negative characteristics would be subtracted.\*

To apply this method to the example above: Having found in the table the log. of the divisor 287, we may at once transform it into the addition logarithm 7·542118, and similarly, for the log. of 2101 we may write 6·677574, and then the calculation will proceed continuously as follows:—

$$\begin{array}{r} \begin{array}{r} 209 \log. 2\cdot 320146 \\ 573 \log. 2\cdot 758155 \\ 63 \log. 1\cdot 799341 \\ 287 \text{ ar. co. } 7\cdot 542118 - 10 \\ 2101 \text{ ar. co. } 6\cdot 677574 - 10 \\ \hline 1\cdot 097334 \end{array} \quad \text{Ans.: } 12\cdot 5122. \\ \begin{array}{r} 13. \quad \frac{7 \times 8\cdot 73}{\cdot 54963} \quad \frac{84 \times \cdot 00769 \times 683}{598\cdot 00 \times \cdot 00146 \times \cdot 039} \quad \frac{8\cdot 4 \times \cdot 0769 \times \cdot 00683}{59\cdot 8 \times \cdot 0000146 \times \cdot 0039} \\ 14. \quad \frac{67\cdot 038 \times \cdot 010705 \times 4\cdot 1525}{\cdot 7854 \times 3\cdot 1416 \times \cdot 086725} \quad \frac{28\cdot 045 \times 1\cdot 3564 \times \cdot 0942537}{48\cdot 375 \times 2\cdot 71828 \times 52359} \end{array} \end{array}$$

15. Divide ·06314 × 7438 × 102367 by ·007241 × 12·9476 × 496523, and compare the result with the product of 8·71979 × ·057447 × ·0206168.

\* To divide by any number  $n$  is the same in effect as to multiply by its reciprocal  $\frac{1}{n}$  (that is, the quotient of unity by that number). Therefore to subtract  $\log. n$  is the same in effect as to add  $\log. \frac{1}{n} = 0 - \log. n$ .

88. **Degree of Dependence.**—The number of places of figures which may be obtained in a result derived from any table of logarithms, is the same usually, rejecting prefixed cyphers, as the number of decimals to which the logarithms are carried. But towards the end of the Table the last place thus obtained cannot always be depended upon within a unit, that is, provided the mantissa of log. is greater than .9388. Thus, for instance, the log. 3.7575 corresponds to the no. 5721 and the log. 3.7576 to 5722, nearly.

This remark should be kept in mind, because it is mere waste of time to employ more figures than are required to insure a certain degree of precision in the result.

## TRIGONOMETRICAL TABLES.

89. There are two kinds of trigonometrical tables; the first, called the *Table of Natural Sines, Cosines, &c.*, contains the numerical values of the sines, cosines, tangents, &c., that is, of the trigonometrical ratios for each given value of the angle; the second, called the *Table of Logarithmic Sines, &c.*, contains the logarithms of the numbers in the first Table.\*

### TABLE OF NATURAL SINES, &c.

90. The trigonometrical functions or ratios are numbers which are capable of being calculated from geometrical principles, and accordingly certain series have been investigated, and certain algebraic expedients devised for the general purpose of determining the trigonometrical ratios. With such aid the sines, cosines, &c., of all angles from  $0^\circ$  to  $90^\circ$  (*i.e.* for all values of  $A$ , from  $A = 0$  up to  $A = 90$ ) have been computed to several places of decimals and arranged in tables called *Tables of Natural Sines, Cosines, &c.* In some tables the angles succeed each other at intervals of  $1''$ , in others at intervals of  $10''$ ; but in ordinary tables (as Table XXVI, Norie) at intervals of  $1'$ , and to the last mentioned we shall refer.

91. The statement of the method by which such tables are constructed is unsuitable to the pages of the present work. The mode of using them in computation we shall now proceed to explain.

92. The arrangement of this table will be understood from a simple inspection. It contains the sines, cosines, &c., of angles between zero and  $90^\circ$ , generally for every minute, and the fluctuations of angles containing a number of degrees, minutes, and seconds, have to be found by interpolations similar in their nature to those that are required to be used in tables of logarithms of numbers. This interpolation is based upon the supposition that the differ-

\* The usual trigonometrical tables are given in conjunction with tables of logarithms, and they more frequently give logarithms only than sines, cosines, &c., themselves. When logarithms were invented they were called *artificial* numbers; and the originals for which logarithms were computed, were accordingly called *natural* numbers. Thus, in speaking of a table of sines, to express that it is not the logarithms of the sines which are given, but sines themselves, that table would be called a table of *natural* sines; and the logarithms of these would be called not *logarithms of sines* but *logarithmic sines, &c.*

ences of the sines, &c., are proportional to the differences of the angles, and this proportion, though theoretically inexact, gives, in general, a sufficient approximation, provided the difference of the angles of the table are sufficiently small.

93. Referring to the Tables (Table XXVI, Norie), it will be seen that the degrees are given at the *top* of the column, and the minutes down the *left* hand side of the page, for the sines.

And, for the cosines, the degrees are given at the *bottom* of the page, and the minutes up the *right* hand side of the page.

The difference of the trigonometrical ratios for 100" are given at the foot

94. In using these Tables, we have either to find the sine, cosine, &c., of an angle whose value is given in degrees (°), minutes (′), and seconds (″); or to find the corresponding angle in degrees, minutes, and seconds. of each column.

95. If the value of the angle be given in degrees and minutes only, the sine, cosine, &c., is found directly from the Tables, in which are registered the values of the trigonometrical ratios.

All the numbers contained in such Tables as Norie's Table XXVI must be understood as decimals.

|                 |         |         |
|-----------------|---------|---------|
| Thus, nat. sine | 7° 7′ = | .123890 |
| „ sine          | 59 40 = | .863102 |
| „ cosine        | 15 30 = | .963631 |
| „ cosine        | 71 12 = | .322266 |

96. As the sines, cosines, &c., pass through all their possible *numerical* values while the angle varies from 0° to 90°, the tables are not extended beyond 90°; such computations would be superfluous, for the sine or cosine of an angle between one and two right angles, viz., of an angle greater than 90° is the same in numerical value as the sine, cosine, &c., of an angle as much below 90°, and is known from the recorded sine or cosine of its supplement.\*

Whence also

|           |            |        |           |         |
|-----------|------------|--------|-----------|---------|
| Nat. sine | 136° 42′ = | sine   | 43° 18′ = | .395546 |
| „ cosine  | 108 48 =   | cosine | 71 12 =   | .322266 |
| „ sine    | 104 16 =   | sine   | 39 44 =   | .639215 |
| „ cosine  | 140 16 =   | cosine | 39 44 =   | .769028 |

97. If the angle contains seconds, we must proceed by the *method of proportional parts*, as in the following examples:—

### RULE XXXVI.

1°. Find from the Table the nat. sine, cosine, &c., which corresponds to the degrees and minutes. (Norie, Table XXVI.)

2°. Multiply the difference by the seconds, and divide by 100.

NOTE.—To divide by 100 we have merely to cut off the two right hand figures.

3°. If the required quantity be a nat. sine, tangent, or secant, add the result to the last figures obtained in 1°; if it be a cosine, cotangent, or cosecant, subtract. The result will be the required sine, cosine, &c.

\* Def.—The supplement of an angle is the result when the angle is subtracted from 180°. In other words, an angle and its supplement together make 180°, or two right angles, thus, 23° 19′ is the supplement of 156° 41′, and 156° 41′ is the supplement of 23° 19′.

NOTE 1.—The reason of this rule is founded on the principle that for a small interval, such as one minute, the increase of the sine is proportional to the increase of the angle.

NOTE 2.—It is necessary to bear in mind that the sine, tangent, and secant (under  $90^\circ$ ) for which the tables are constructed increase as the arc increases, whilst the cosine, cotangent, and cosecant decrease as the arc increases. This will require the corrections connected with a sine, a tangent, or a secant to be added, and those connected with a cosine, a cotangent, or a cosecant to be subtracted whether arcs or their functions be sought from the tables.

## EXAMPLES.

1. Find the nat. sine of  $12^\circ 44' 27''$ .

$$\text{Nat. sine } 12^\circ 44' = 220414$$

$$\text{Tab. diff. } \frac{473 \times 27}{100} = + 128$$

$$\text{Ans. : Nat. sine } 12^\circ 44' 27'' = 220542$$

To obtain the parts for the seconds we multiply the tabular difference by the number of seconds and divide by 100, thus:—

$$\text{Tab. diff. } 473$$

$$\text{No. of seconds } \times 27$$

$$\frac{3311}{946}$$

$$\frac{127,71}{128 \text{ nearly.}}$$

2. Find the nat. cosine of  $31^\circ 28' 42''$ .

$$\text{Nat. cosine } 31^\circ 28' = 852944$$

$$\text{Tab. diff. } \frac{253 \times 42}{100} = - 106$$

$$\text{Ans. : Nat. cosine } 31^\circ 28' 42'' = 852838$$

$$\text{Tab. diff. } 253$$

$$\text{Seconds } \times 42$$

$$\frac{506}{1012}$$

$$\frac{106,26}{106}$$

## EXAMPLES FOR PRACTICE.

To find the nat. sine of

- |                        |                        |                        |                       |
|------------------------|------------------------|------------------------|-----------------------|
| 1. $34^\circ 48' 15''$ | 3. $71^\circ 20' 43''$ | 5. $46^\circ 22' 37''$ | 7. $53^\circ 7' 49''$ |
| 2. $60^\circ 7' 18''$  | 4. $21^\circ 44' 21''$ | 6. $76^\circ 57' 49''$ | 8. $86^\circ 3' 17''$ |

To find the nat. cosine of

- |                        |                        |                        |                        |
|------------------------|------------------------|------------------------|------------------------|
| 1. $14^\circ 15' 3''$  | 3. $80^\circ 22' 22''$ | 5. $46^\circ 31' 41''$ | 7. $38^\circ 31' 10''$ |
| 2. $70^\circ 47' 40''$ | 4. $5^\circ 22' 10''$  | 6. $29^\circ 40' 48''$ | 8. $8^\circ 19' 17''$  |

98. If the value of the sine, cosine, &c., be given, and it is required to find the angle, we use the following rule:—

## RULE XXXVII.

1°. Find in the Tables the next lower nat. sine, nat. cosine, &c., and note the corresponding degrees and minutes.

2°. Subtract this from the given sine, cosine, &c., multiplying the difference by 100; divide by the tabular difference, and consider the result as seconds.

3°. If the given value be that of a sine, tangent, or secant, add these seconds to the degrees and minutes found in 1°; if it be that of a cosine, cotangent, &c., subtract. The result will be the required angle.

NOTE.—In taking out the angle for a natural cosine we may take out the next greater natural cosine, and subtract the given natural cosine from it; and having found the seconds (") as above they are additive. The trigonometrical ratio corresponding to the next less angle being written down in every case, confusion will be avoided as the additional seconds will always be additive.

EXAMPLES.

1. Given the natural sine =  $0.732156$ : find the angle.

Given nat. sine  $732156$

Sine  $47^{\circ} 4' = 732147$  next lower in table XXVI, Norie.

Tab. diff. =  $327 \quad 327)900(3''$  nearly (additional seconds for nat. sine).  
 $981 \quad \text{Ans. : } 47^{\circ} 4' 3''.$

The log.  $732156$  is sought for in Table XXVI, Norie, but as it cannot be found exactly, the next less is taken which corresponds to  $47^{\circ} 4'$ . The difference of the logs. is then found, two cyphers added (which is equivalent to multiplying by 100), and the product divided by the tabular difference; the quotient is the additional seconds.

2. Given the natural cosine  $853267$ : find the angle.

Given nat. cosine  $853267$

Cosine  $31^{\circ} 26' = 853248$  next lower in Table XXVI, Norie.

Tab. diff. =  $253 \quad 253)1900(7''$  (to be subtracted).  
 $1771$   
 $129 \quad \text{Ans. : } 31^{\circ} 25' 53''.$

3. Find the angle whose natural cosine is  $728713$ .

Proceeding according to Note, page 70.

Here nat. cosine of required angle =  $728713$

Nat. cosine of next less angle or  $43^{\circ} 13' = 728769$

Tab. diff. =  $334$

$334)5600(17''$  nearly, to be  
 $334$  added.

$2260$   
 $2338$

Hour angle required =  $43^{\circ} 13' 17''$ .

EXAMPLES FOR PRACTICE.

Given the nat. sines, to find the angle.

- |              |              |             |                                     |             |
|--------------|--------------|-------------|-------------------------------------|-------------|
| 1. $.898002$ | 3. $.8$      | 5. $.444$   | 7. $.740912$                        | 9. $.75214$ |
| 2. $.370383$ | 4. $.920411$ | 6. $.20389$ | 8. $\frac{1.03}{30.8}$ or $.529221$ | 10. $.96$   |

Given the nat. cosine, to find the angle.

- |              |              |              |              |               |               |
|--------------|--------------|--------------|--------------|---------------|---------------|
| 1. $.448807$ | 3. $.726998$ | 5. $.514841$ | 7. $.769388$ | 9. $.817726$  | 11. $.999000$ |
| 2. $.948397$ | 4. $.702017$ | 6. $.914237$ | 8. $.974822$ | 10. $.215515$ | 12. $.6$      |

## TABLES OF LOGARITHMS OF TRIGONOMETRICAL RATIOS.

99. The Trigonometrical Ratios being numbers have logarithms that correspond to them. In practice the logarithmic are generally far more useful than the natural sines, &c., though the latter are often necessary, or in some simple kinds of calculation, preferable.

100. As the sines and cosines of all angles, and the tangents of angles less than  $45^{\circ}$ , are less than radius or unity, the logarithms of the values of these quantities, properly, have negative characteristics. In order to avoid the inconvenience of printing negative logarithms, and for other reasons, 10 is added to the characteristic before it is registered in the table of logarithmic sines, &c., so that we find the characteristic 9 instead of  $\bar{1}$ , 8 instead of  $\bar{2}$ , &c.

Thus on referring to the Table of Natural Sines (Table XXVI, Norie), we find natural sine of  $16^\circ = .275637$ . If we calculate the logarithm of  $.275637$ , we find its value is  $\overline{7}.440338$ , if to this 10 is added we find that

$$\text{Log. sine } 16^\circ = 9.440338.$$

To preserve uniformity, the characteristics of the logarithms of all the other ratios, namely, of the log. tangents, cotangents, secants, and cosecants are increased by 10. In trigonometrical operations this is convenient, but principally because the extraction of roots very seldom occurs.

It may be observed here that the uniform addition of 10 to the characteristic gives the logarithm of 10000 *million* times the natural number.

Thus,  $9.599327$  is the log. of  $3979486000$ , and this latter number is the natural sine corresponding to a radius of 10000 *millions*, instead of a radius of unity.

101. The table of logarithmic sines, cosines, tangents, cotangents, secants, and cosecants, contain all arcs from zero ( $0^\circ$ ) through all magnitudes up to  $90^\circ$ , the log. of radius as just stated being 10. At the top of the page is placed the number of degrees, and in the left hand column each minute of the degree, opposite to which are arranged the numerical values of the log. sine, cosine, &c., of the corresponding angle in those columns, at the *top* of which those terms are placed. The headings of the columns run along the *top*, thus, as far as  $44^\circ$ . The degrees from  $45^\circ$  to  $90^\circ$  are placed at the bottom of the page, and the minutes of the degree arranged in a right hand column, so that the angles read off on the right hand side are complementary to those read off at the points exactly opposite on the left hand side, the values of the sines, cosines, tangents, &c., being found in the columns at the *bottom* of which those terms are found. This arrangement is rendered practicable by the circumstance of every angle between  $45^\circ$  and  $90^\circ$  being the complement of another between  $45^\circ$  and  $0^\circ$ , every sine of an angle less than  $45^\circ$  is the cosine of another greater than  $45^\circ$ , every tangent is a cotangent, &c.; the sines, tangents, &c., of angles being respectively equal to the cosines, cotangents, &c., of the complements of the same angle.

The following shows the usual arrangement of such tables:—

| M | Sin. | D. | Cosec. | Tan. | D. | Cot. | Sec.   | D. | Cos. | M |
|---|------|----|--------|------|----|------|--------|----|------|---|
| M | Cos. | D. | Sec.   | Cot. | D. | Tan. | Cosec. | D. | Sin. | M |

Besides the columns headed "sine, tangent," &c., are three smaller columns headed "Diff." They contain, in most tables, the differences between the values of the consecutive logarithms in the contiguous columns on either side, but corresponding to a change of  $100''$  in the arc; and it must be kept in mind that the same difference is common to the sine and cosecant, to the tangent and cotangent, and to the secant and cosine. They are inserted for the convenience of finding the values of the sines and cosines, &c., of angles which are expressed in degrees, minutes, and seconds.

102. The above, as just stated, is the usual arrangement of most tables, but in the earlier editions of Norie and some other works the arrangement is somewhat different.



The columns are arranged thus:—

|   |         |       |         |       |           |       |           |           |           |   |
|---|---------|-------|---------|-------|-----------|-------|-----------|-----------|-----------|---|
| M | Sine.   | Diff. | Cosine. | Diff. | Tangent.  | Diff. | Cotangent | Secant.   | Cosecant. | M |
| M | Cosine. | Diff. | Sine.   | Diff. | Cotangent | Diff. | Tangent.  | Cosecant. | Secant.   | M |

Since the same difference is common to the sine and cosecant, to the tangent and cotangent, in this arrangement, then, it must be particularly borne in mind, that the first “Diff.” column (from the left) belongs to the first column of logarithms on the left hand of the page and to the first column on the right of the page; that the second column of “Diff.” belongs the second column of logarithms from the right or left of the page; and that the third column of “Diff.” belongs to the third column from either the right or the left.

102. In the use of these Tables, as in that of the natural sines, two questions present themselves:—First, having given the angle in degrees, minutes, and seconds, required the log. sine, log. cosine, &c. Second, having given the log. sine, log. cosine, &c., required the value of the angle in degrees, minutes, and seconds.

103. When an angle is presented in degrees and minutes only, the tabular logarithm of its sine, tangent, &c., will be found simply by inspection, according to the following:—

### RULE XXXVIII.

1°. If the angle or arc is less than 45°. Find the degrees at the top of the page, and the minutes in the left-hand marginal column, then opposite the minutes, and in the column which is marked at the top with the name of the ratio, will be found the logarithm sought.

2°. If the angle be greater than 45°. Look for the degrees at the bottom of the page, and for the minutes in the right-hand column; the logarithm of the proposed function of the angle will be found opposite the minutes in the column marked at the foot with the name of the ratio whose logarithm is sought.

### EXAMPLES.

Ex. 1. Find the log. sine of 37° 47'.

As the arc is less than 45°, by looking at the top of the table for the degrees (37°), and in the first column on the left for the minutes (47'), we find in the column having at its top the word sine, the figures 9·787232, which is the log. sine of the arc required.

Ex. 2. Find the log. tang. of 75° 34'.

Here, as the arc is greater than 45°, looking at the bottom of the tables for the degrees (75°), and in the last or right hand column for the minutes (34'), we find in the column having tang. at the bottom 10·589431, which is the log. tangent of 75° 34'.

|                   |           |           |                   |           |           |
|-------------------|-----------|-----------|-------------------|-----------|-----------|
| Log. sine of      | 40° 4' is | 9·808669  | Log. sine of      | 57° 5' is | 9·924001  |
| Log. cosine of    | 21 38 „   | 9·968278  | Log. cosine of    | 79 51 „   | 9·246066  |
| Log. tangent of   | 84 13 „   | 10·994466 | Log. tangent of   | 21 50 „   | 9·602761  |
| Log. cotangent of | 55 58 „   | 9·829532  | Log. cotangent of | 27 45 „   | 10·278911 |
| Log. secant of    | 7 20 „    | 10·472954 | Log. secant of    | 44 59 „   | 10·150389 |
| Log. cosecant of  | 8 35 „    | 10·826092 | Log. cosecant of  | 69 54 „   | 10·027291 |

## EXAMPLES FOR PRACTICE.

Take out the logarithms of the following trigonometrical ratios.

|                 |        |                 |         |
|-----------------|--------|-----------------|---------|
| 1. Log. sine    | 9° 10' | 7. Log. cos.    | 53° 28' |
| 2. Log. cosec.  | 40 40  | 8. Log. sine    | 51 49   |
| 3. Log. cosine  | 12 48  | 9. Log. sec.    | 60 34   |
| 4. Log. tang.   | 37 26  | 10. Log. cotang | 79 19   |
| 5. Log. cotang. | 8 25   | 11. Log. cosec. | 45 45   |
| 6. Log. sec.    | 43 1   | 12. Log. sine   | 53 56   |

104. If the value of the angle be given in degrees, minutes, and seconds, we proceed by

## RULE XXXIX.

1°. Find from the table the sine, tangent, secant, cosine, &c., which corresponds to the degrees and minutes; also take out the number in the contiguous column headed "Diff." on the same line (See Nos. 101 and 102, page 72.)

2°. Multiply the tabular difference ("Diff.") by the seconds, reject the last two figures of the product for the division by 100, and the remaining figures will furnish the proper correction for seconds.

NOTE 1.—If the value of the two figures cut off is not less than fifty, one must be added to the first right hand figure left.

3°. If the required quantity be a sine, tangent, or secant, add the result to the last figures obtained in 1°; if it be a cosine, cotangent, or cosecant subtract.\*

The result will be the required sine, tangent, secant, cosine, &c.

NOTE 2.—The process above is sufficiently accurate unless for the sines and tangents of very small angles, and for the tangents and secants of angles very near 90°. When an angle of degrees, minutes, and seconds, and of less magnitude than 3°, occurs in calculation, neither the logarithmic sine nor the logarithmic tangent will be found very accurately from the ordinary Tables. In some books, as Hutton's "Mathematical Tables," a special Table is given, containing the logarithmic sines and tangents to every second in the first two degrees of the quadrant. By that Table we should find the correct log. tang. of 1° 25' 45" to be 2.3970503, whereas, by using the tab. diff. for 1° 25' and 1° 26' in the ordinary Table, we should get the less accurate result, 2.3970448, because for such small angles, the successive tabular differences for one minute shows too rapidly a wide departure from equality. When an angle of degrees, minutes, and seconds, and within less than 3° of 90° occurs in calculation, we cannot, for the reason just stated, obtain very accurately from the ordinary Tables either the logarithmic or the natural tangent. Thus, the true log. tang. of 88° 4' 15" is 1.6029497; but by the ordinary Tables we would get for the last three figures 552. Norie gives the log. sin. and log. tang. to every ten seconds of the first two degrees of the quadrant, and Raper gives the log. sines to every second up to 1° 30', and to every ten seconds up to 4° 30'.

\* In some tables, these differences are those due to 1 minute, or 60 seconds, and are got by simply subtracting the greater of the logarithms from the less. The difference  $d$ , due to any smaller number ( $a$ ) of seconds is found from such tables by the proportion  $60 : a :: D : d$ , so that  $d = \frac{D \cdot a}{60}$ . But as before observed the differences usually given in the tables are those due not to 60 seconds but to 100 seconds, so that in these tables,  $d = \frac{D \cdot a}{100}$ ; and thus  $d$  is found somewhat more readily.

EXAMPLES.

1. Find the log. sine of  $6^{\circ} 36' 27''$ .

Here the given number of degrees ( $6^{\circ}$ ) being less than  $45^{\circ}$ , look for them in the head line at the top of the page, turning over the leaves till the proper page is found, then in that page look in the second line for the name of the column wanted, viz., the sine; and in the left hand vertical column marked M at the top, find the number of minutes ( $36'$ ); having found the minutes, then in the same line and under sine is found  $9^{\circ}060460$ , which is the log. sine corresponding to  $6^{\circ} 36'$ . Now this log. being found in the first column on the left, the tabular difference must be taken out of the first "diff." column from the left. It will be noticed that there is no diff. exactly opposite to  $36'$  but between  $36'$  and  $37'$  will be found the diff. 1817, which multiplied by the seconds ( $27''$ ) gives 49059, and rejecting the two last figures from this product (for the division by 100) gives quotient 490, which being increased by 1, since the figures cut off exceed 50 (see Note 1, page 74) gives 491 as the correction of the logarithm for the seconds. The work will stand thus:—

$$\begin{array}{r} \text{Log. sine } 6^{\circ} 36' = 9^{\circ}060460 \\ 27'' \text{ gives } \quad \quad + \quad 491 \\ \hline 9^{\circ}060951 \end{array}$$

$$\begin{array}{r} \text{Tab. diff. } 1817 \\ \times 27 \\ \hline 12719 \\ 3634 \\ \hline 49059 \end{array}$$

or 491

$$\text{Ans.: Log. sine } 6^{\circ} 36' 27'' = 9^{\circ}060951.$$

2. Find the log. cosine of  $13^{\circ} 5' 32''$ .

The log. cosine of  $13^{\circ} 5'$  is  $9^{\circ}988578$ , and the tabular difference corresponding to the log. cosine of the given degrees and minutes is 50; this being multiplied by 32 (the given number of seconds), and pointing off *two figures* to the right, is 16 to be *subtracted*, because the cosine is a *decreasing* log.; therefore—

$$\begin{array}{r} \text{Log. cosine } 13^{\circ} 5' = 9^{\circ}988578 \\ 32'' \text{ gives } \quad \quad - \quad 16 \\ \hline 9^{\circ}988562 \end{array}$$

$$\begin{array}{r} \text{Tab. diff. } 50 \\ \times 32 \\ \hline 100 \\ 150 \\ \hline 1600 \end{array}$$

or 16

$$\text{Ans.: Log. cosine } 13^{\circ} 5' 32'' = 9^{\circ}988562.$$

3. Find the log. tangent of  $72^{\circ} 59' 8''$ .

The log. tangent of  $72^{\circ} 59'$  is  $10^{\circ}514209$ , and the tab. diff. corresponding to the given degrees and minutes is 753; this being multiplied by 8 (the number of seconds), and pointing off *two figures* to the right is 60, which is additive; thus:—

$$\begin{array}{r} \text{Log. tang. } 72^{\circ} 59' 0'' = 10^{\circ}514209 \\ \text{Parts for } \quad \quad 8'' = + \quad 60 \\ \hline \end{array}$$

$$\begin{array}{r} \text{Tab. diff. } 753 \\ \times 8 \\ \hline \end{array}$$

$$\text{Log. tang. } 72^{\circ} 59' 8'' = 10^{\circ}514269$$

$$60,24$$

4. Find the log. cotangent  $73^{\circ} 21' 7''$ .

The log. cotangent of  $73^{\circ} 21'$  is  $9^{\circ}475763$ , and the tab. diff. corresponding to the cotangent of the given degrees and minutes is 767; this being multiplied by 7 (the given number of seconds), and pointing off *two figures* to the right is 54; which is to be *subtracted* in this instance, being a *colog.*

$$\begin{array}{r} \text{Log. cotang. } 73^{\circ} 21' 0'' = 9^{\circ}475763 \\ \text{Parts for } \quad \quad 7'' = - \quad 54 \\ \hline \end{array}$$

$$\begin{array}{r} (\text{Tab. diff. } 767) \times 7 = 5369 \\ \hline 100 \quad \quad \text{or } 54 \end{array}$$

$$\text{Log. cotang. } 73^{\circ} 21' 7'' = 9^{\circ}475709$$

The parts for the seconds are subtracted in this instance *being a colog.* (See Rule XXXIX, 3<sup>o</sup>).

5. Take out log. sine  $1^{\circ} 5' 34''$ .

Here the angle whose log. sine is sought being less than  $2^{\circ}$ , it must, therefore, be taken out of the special part of the Table (see Table XXV, page 107, *NOTE*). The next less angle to be found in the Table is  $1^{\circ} 5' 30''$ , the log. sine of which 8.279941, and the corresponding tabular, "Diff" (for  $10''$  in this part of the Table) is 1104, which multiplied by 4, the seconds over 30, gives 4416, and cutting off one figure from the right, for the division by 10 gives the correction 442, to be added to the logarithm taken out of the Table; thus the work stands as follows:—

|           |                                |            |                |
|-----------|--------------------------------|------------|----------------|
| Log. sine | $1^{\circ} 5' 30'' = 8.279941$ | Tab. diff. | 1104           |
| Parts for | $4 = + 442$                    |            | 4              |
| Log. sine | $1^{\circ} 5' 34'' = 8.280383$ |            | 441,6          |
|           |                                |            | or 442 nearly. |

6. Required the cosecant of  $3^{\circ} 7' 21''$ .

|               |                                 |            |        |
|---------------|---------------------------------|------------|--------|
| Log. cosecant | $3^{\circ} 7' 0'' = 11.264646$  | Tab. diff. | 3857   |
| Parts for     | $21 = - 810$                    |            | 21     |
| Log. cosecant | $3^{\circ} 7' 21'' = 11.263836$ |            | 3857   |
|               |                                 |            | 7714   |
|               |                                 |            | 809,97 |

105. For the functions\* of an angle between  $90^{\circ}$  and  $180^{\circ}$  we may take the same functions of its supplement; hence to find the logarithm of a trigonometrical ratio of an angle greater than  $90^{\circ}$ , *i.e.*, of an obtuse angle, we have the following

#### RULE XL.

*Subtract the angle from  $180^{\circ}$  and look for the remainder, which is called its supplement in the Tables.*

#### EXAMPLES.

Ex. 1. Find the log. sine of  $110^{\circ} 24'$ .

Subtract it from  $180^{\circ}$ .

|           |                                |
|-----------|--------------------------------|
| From      | $180^{\circ} 00'$              |
| Subtract  | $110^{\circ} 24'$              |
| Remainder | $69^{\circ} 36'$ (Supplement.) |

Look for the log. sine of remainder (namely  $69^{\circ} 36'$ ), which is 9.971870; or log. sine  $110^{\circ} 24' = 9.971870$ .

Ex. 2. Find the log. secant of  $95^{\circ} 43'$ ; also the log. cosecant of the same.

|                    |                  |
|--------------------|------------------|
| From $180^{\circ}$ | $0'$             |
| Take $95^{\circ}$  | $43'$            |
| Supplement         | $84^{\circ} 17'$ |

Look for the log. secant of  $84^{\circ} 17'$ , which is 11.001701;  $\therefore$  log. secant of  $95^{\circ} 43'$  is 11.001701.

Again, look for the cosecant of  $84^{\circ} 17'$ , which is 10.002165;  $\therefore$  log. cosecant of  $95^{\circ} 43'$  is 10.002165.

\* By the *functions of angles*, sometimes called their *trigonometrical* or *goniometrical functions*, are meant their sines, tangents, secants, versed sines, and chords; the word *function* signifying any quantity that is dependent on another, changing as it changes.

Ex. 3. Find the log. tangent of  $128^{\circ} 55' 47''$ .

|  |      |           |                  |
|--|------|-----------|------------------|
| From   | 180° | 00'       | 00"              |
| Subtract   | 128  | 55        | 47               |
| Remainder  | 51   | 4         | 13 (Supplement.) |
| ∴ Supplement of the given angle = $51^{\circ} 4' 13''$ . |      |           |                  |
| Log. tangent $51^{\circ} 4'$                             | =    | 10.092664 | Tab. diff. 431   |
| Parts for $13''$   | =    | + 56      | × 13             |
| Log. tangent $51^{\circ} 4' 13''$                        | =    | 10.092720 | 1293             |
|  |      |           | 431              |
|  |      |           | 56,03            |
|  |      |           | or 56            |

∴ Log. tangent  $128^{\circ} 55' 47'' = 10.092720$ , *Ans.*

106. But a readier way, and the better practical method, is to proceed as follows:—

### RULE XLI.

*Diminish the given angle by  $90^{\circ}$ , and look out the remainder in the tables, observing that if the trigonometrical ratio have "co" prefixed to drop the "co," but if it have not "co," prefix it, then find the logarithm corresponding to the new ratio. Or,*

*If A denote any angle less than  $90^{\circ}$ , then*

|             |                   |          |                 |
|-------------|-------------------|----------|-----------------|
| For sine    | .....( $90 + A$ ) | take out | ..... cosine A  |
| „ tangent   | ....( $90 + A$ )  | —        | .. cotangent A  |
| „ secant    | .....( $90 + A$ ) | —        | .... cosecant A |
| „ cosine    | .... ( $90 + A$ ) | —        | ..... sine A    |
| „ cosecant  | ....( $90 + A$ )  | —        | ..... secant A  |
| „ cotangent | .. ( $90 + A$ )   | —        | .... tangent A  |

This rule may easily be remembered by observing that to the sine, tangent, and secant, *co* is prefixed, while from the cosine, cosecant, and cotangent the *co* is dropped, and in each case the excess of  $90^{\circ}$  of the angle is used.

### EXAMPLES.

Find the log. cosine of  $110^{\circ}$ .

To find the log. cosine of  $110^{\circ}$ , or log. cosine ( $90 + 20$ ), take out the log. sine  $20^{\circ}$ , which is 9.534052.

To find the log. secant of  $160^{\circ} 12'$ , take out the cosecant  $70^{\circ} 12'$  which is 10.026465.

|                  |                   |   |             |                  |             |
|------------------|-------------------|---|-------------|------------------|-------------|
| Log. cosine of   | $143^{\circ} 24'$ | = | Log. sine   | $53^{\circ} 24'$ | is 9.904617 |
| Log. cosecant of | 99 37             | = | Log. secant | 9 37             | „ 10.006146 |
| Log. sine of     | 109 2             | = | Log. cosine | 19 2             | „ 9.975583  |

Find the log. cosecant of  $131^{\circ} 45' 19''$ .

Subtracting  $90^{\circ}$  from  $131^{\circ} 45' 19'' = 41^{\circ} 45' 19''$ .

Log. cosecant  $131^{\circ} 45' 19'' =$  log secant  $41^{\circ} 45' 19''$ .

|             |                       |   |           |                |
|-------------|-----------------------|---|-----------|----------------|
| Log. secant | $41^{\circ} 45' 0''$  | = | 10.127228 | Tab. diff. 188 |
| Parts for   | + 19                  | = | + 36      | × 19           |
| Log. secant | $41^{\circ} 45' 19''$ | = | 10.127264 | 1692           |
|             |                       |   |           | 188            |
|             |                       |   |           | 35,72          |

In this instance "co" is prefixed to the given trigonometrical ratio, then, according to rule, "co" is dropped, and the log. corresponding to the new ratio is taken out for the remainder resulting from the given angle when diminished by  $90^{\circ}$ .

Ex. 3. Required the log. tangent  $99^{\circ} 32' 58''$ .

Log. tangent  $99^{\circ} 32' 58'' = \text{cotangent } 9^{\circ} 32' 58''$ .

|                |                                 |            |              |
|----------------|---------------------------------|------------|--------------|
| Log. cotangent | $9^{\circ} 32' 0'' = 10.774844$ | Tab. diff. | 1288         |
| Parts for      | $+ 58 = 747$                    |            | 58           |
| Log. cotangent | $9 32 58 = 10.774097$           |            | <u>10304</u> |
|                |                                 |            | <u>640</u>   |
|                |                                 |            | 747,04       |

#### EXAMPLES FOR PRACTICE.

Required the log. sine, tangent, secant, cosine, cotangent, and cosecant corresponding the following arcs:—

|                         |                          |                         |                            |
|-------------------------|--------------------------|-------------------------|----------------------------|
| 1. $6^{\circ} 53' 56''$ | 4. $56^{\circ} 54' 17''$ | 7. $1^{\circ} 49' 47''$ | 10. $115^{\circ} 34' 41''$ |
| 2. $24 9 30$            | 5. $10 10 6$             | 8. $87 28 45$           | 11. $119 40 48$            |
| 3. $37 49 14$           | 6. $70 47 40$            | 9. $1 0 40$             | 12. $101 40 19$            |

Take out of the Table the following:—

|                  |                      |                  |                        |
|------------------|----------------------|------------------|------------------------|
| 13. Log. sine    | $2^{\circ} 40' 10''$ | 22. Log. cosec.  | $127^{\circ} 30' 40''$ |
| 14. Log. sine    | $170 30 39$          | 23. Log. cosec.  | $141 16 51$            |
| 15. Log. sine    | $1 49 47$            | 24. Log. sine    | $2 0 53^*$             |
| 16. Log. cosine  | $89 59 19$           | 25. Log. cotang. | $89 23 37$             |
| 17. Log. cosine  | $88 40 56$           | 26. Log. cosine  | $87 23 27$             |
| 18. Log. cosine  | $108 40 6$           | 27. Log. cosine  | $88 50 29$             |
| 19. Log. tang.   | $1 8 7$              | 28. Log. tang.   | $1 2 18$               |
| 20. Log. cotang. | $3 7 8$              | 29. Log. sec.    | $101 8 7$              |
| 21. Log. tang.   | $114 9 30$           | 30. Log. sine.   | $110 11 18$            |

107. If the value of the log. sine, log. cosine, &c., *i.e.*, the logarithm of a trigonometrical ratio, be given, and it is required to find the corresponding angle in degrees and minutes, we use

#### RULE XLII.

*Look for the logarithm in the several columns of the Table marked at the top or bottom, with the name of the given trigonometrical ratio, which being found exactly or the nearest to it, will give the degrees and minutes answering to the given logarithm, being careful to observe that when the name of the given ratio is found at the top of the Table, then the degrees are to be taken from the top and the minutes from the left hand marginal column; but if the name of the ratio is found at the bottom of the Table, take the degrees from the bottom and the minutes from the right hand side of the page.*

NOTE.—In using the Table *inversely*, for example, in searching for the angle which has 9.611294 for the logarithm of its sine, the student must not distinguish sine from cosine, nor tangent from cotangent, but must consider *sines* and *cosines* as one table, *tangents* and *cotangents* as one table, and must cast an eye on both, and get to 9.611294 as fast as he can. For want of this caution some beginners will turn over page after page until they come to  $45^{\circ}$ , and then back again to the very page that was first opened.

Ex. 1. Required the angle corresponding to the log. sine 9.729223.

In page 142, Table XXV, Norie, under the word "Sine," and opposite 25' in left hand marginal column, are the exact figures, the degree (being sought at the head of the page, because the column in which the figures are found is named at the head) is  $32^{\circ}$ ; therefore, the angle is  $32^{\circ} 25'$ .

\* When the tabular difference is considerable, as in this instance, the log. is easier reduced from the log. of the nearest minute.

If the angle for the cosine of the same logarithm be required, the degrees are found at the bottom, and the minutes in the right hand column, and is  $57^{\circ} 35'$  accordingly.

|            |                             |              |                            |
|------------|-----------------------------|--------------|----------------------------|
| Log. sine  | 9.731009 = $32^{\circ} 34'$ | Log. cosine  | 9.995555 = $8^{\circ} 11'$ |
| Log. sine  | 9.871073 = 48 0             | Log. cosec.  | 10.030580 = 68 45          |
| Log. tang. | 9.787036 = 31 29            | Log. cotang. | 10.508820 = 17 13          |
| Log. tang. | 10.047850 = 48 9            | Log. cosine  | 9.718497 = 58 28           |
| Log. sec.  | 10.043673 = 25 16           | Log. cosec.  | 10.307885 = 29 29          |
| Log. sec.  | 10.566325 = 74 15           | Log. cotang. | 11.197235 = 3 38           |

108. If the value of the log. sine, log. cosine, &c., be given, and it is required to find the corresponding angle, in degrees, minutes, and seconds, we use

### RULE XLIII.

1°. Find in the Tables (XXV, Norie) the next lower log. sine, log. cosine, &c., and note the corresponding degrees and minutes; also, take the number from the corresponding part of the adjoining column of "Diff."

2°. Subtract this from the given log. sine, log. cosine, &c., multiply the difference by 100, i.e., annex two cyphers, divide by the tabular difference, and consider the result as seconds.

3°. If the given value be that of a log. sine, log. tangent, or log. secant, add these seconds to the degrees and minutes found in 1°; if it be that of a log. cosine, log. tangent, or log. cosecant, subtract.

The result will be the required angle.

NOTE.—If the given log. be a cosine, cosecant, or cotangent, we may seek out the next greater to the given log.: then proceed by 2° to find the seconds, which add to the degrees and minutes as found by 1°.

### EXAMPLES.

1. Given log. sine = 9.422195 (or 7.422195): find the angle.

We take out 9.421857, the log. sine of  $15^{\circ} 19'$ , as it is the logarithm next less than the given one, which we take, as the logarithms in the columns increase with the angle. The difference of these logarithms is 338, and if two cyphers be affixed to the difference, and the number then divided by 768, taken from the column of Diff. in the Table, we have 44 for the number of seconds to be added to the degrees and minutes before taken out. The work will stand thus:—

$$\begin{array}{r}
 \text{Given log. sine} \quad 9.422195 \\
 \text{Tab. log. sine next less } 9.421857 = \text{log. sine } 15^{\circ} 19' \\
 \hline
 \text{Tab. diff. for } 100'' = 768 \cdot 33800(44'' \text{ additional seconds.}) \\
 \quad 3072 \\
 \hline
 \quad 3080 \\
 \quad 3072 \\
 \hline
 \end{array}$$

Therefore 9.422195 = log. sine of  $15^{\circ} 19' 44''$ .

2. Given log. cosine = 9.873242 (or 7.873242): find the angle.

Here we take out 9.873223, the log. cosine of  $41^{\circ} 41'$ , as it is the log. cosine in the Table next less than 9.873242. The difference between these two logarithms is 19; and if two cyphers be affixed to the difference we get 1900; whence 1900 divided by 187, the number from the column of "Diff." gives 10 for the number of seconds to be subtracted. Hence the required angle is  $41^{\circ} 40' 50''$ . The work will stand thus:—





109. It is also necessary to have a distinct conception of the limits to which the Trigonometrical Ratios tend when the angles become right angles. The following are the Trigonometrical Ratios for the angles  $0^\circ$  and  $90^\circ$  :—

|        |                      |        |                     |
|--------|----------------------|--------|---------------------|
| Sin.   | $0^\circ = 0$        | Sin.   | $90^\circ = 1$      |
| Cos.   | $0^\circ = 1$        | Cos.   | $90^\circ = 0$      |
| Tang.  | $0^\circ = 0$        | Tang.  | $90^\circ = \infty$ |
| Cot.   | $0^\circ = \infty$ * | Cot.   | $90^\circ = 0$      |
| Sec.   | $0^\circ = 1$        | Sec.   | $90^\circ = \infty$ |
| Cosec. | $0^\circ = \infty$   | Cosec. | $90^\circ = 1$      |

And the following, therefore, are the Logarithms of their Trigonometrical Ratios :—

|             |                     |             |                      |
|-------------|---------------------|-------------|----------------------|
| Log. sin.   | $0^\circ = -\infty$ | Log. sin.   | $90^\circ = 0$       |
| Log. cos.   | $0^\circ = 0$       | Log. cos.   | $90^\circ = -\infty$ |
| Log. tang.  | $0^\circ = -\infty$ | Log. tang.  | $90^\circ = \infty$  |
| Log. cot.   | $0^\circ = \infty$  | Log. cot.   | $90^\circ = -\infty$ |
| Log. sec.   | $0^\circ = 0$       | Log. sec.   | $90^\circ = \infty$  |
| Log. cosec. | $0^\circ = \infty$  | Log. cosec. | $90^\circ = 0$       |

110. When these values occur amongst others requiring to be added to or subtracted from them, the learned must be careful to remember *that the addition to or subtraction from them of finite numbers cannot alter them.* Hence the explanation of the results in the following :

#### EXAMPLES.

Ex. 1. Add together log. cot.  $0^\circ$  and log. sine  $20^\circ$ .

$$\begin{array}{rcl} \text{Log. cot. } 0^\circ & = & \infty \\ \text{Log. sine } 20^\circ & = & 9.534032 \\ \hline \text{Ans.} & & \infty \end{array}$$

Ex. 2. Add together log. cos.  $90^\circ$  and log. tang.  $45^\circ$ .

$$\begin{array}{rcl} \text{Log. cos. } 90^\circ & = & -\infty \\ \text{Log. tang. } 45^\circ & = & 10.000000 \\ \hline \text{Ans.} & & \infty \end{array}$$

Ex. 3. From log. cos.  $0^\circ$  take log. sine  $62^\circ 48'$ .

$$\begin{array}{rcl} \text{Log. cos. } 0^\circ & = & \infty \\ \text{Log. sine } 62^\circ 48' & = & 9.949105 \\ \hline \text{Ans.} & & \infty \end{array}$$

Ex. 4. From log. tang.  $21^\circ 48' 30''$  take log. cot.  $90^\circ$ .

$$\begin{array}{rcl} \text{Log. tang. } 21^\circ 48' 30'' & = & 9.602212 \\ \text{Log. cot. } 90^\circ & = & -\infty \\ \hline \text{Ans.} & & \infty \end{array}$$

111. In the event of a bad or obliterated figure in the table, it may be convenient to know that the tangents are found by subtracting the cosines from the sines, adding always 10, or the radius; the cotangents are found by subtracting the tangents from 20, or the double radius, and the secants are found by subtracting the cosines from 20, the double radius.

\* This mathematical symbol is called *infinity*.

# NAVIGATION.

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## DEFINITIONS.

112. Navigation is a general term denoting that science which treats of the determination of the place of a ship on the sea, and which furnishes the knowledge requisite for taking a vessel from one place to another. The two fundamental problems of navigation are, therefore, the finding at sea the present position of the ship, and the determining the future course.

113. The place of a ship is determined by either of two methods, which are independent of each other:—1st. By referring it to some other place, as a fixed point of land, or a previous defined place of the ship herself. 2nd. By astronomical observations.

114. It has been customary to employ the term NAVIGATION in a restricted sense to the first of these methods; the second is usually treated of under the head of NAUTICAL ASTRONOMY.

Navigation and Nautical Astronomy are the two great co-ordinate divisions of the "*Art of Sailing on the Sea*," as the old writers quaintly worded it. The first branch of the art is accomplished by means of the Mariner's Compass, which shows the *direction* of the ship's track; the Log, which with the help of sand-glasses for measuring small intervals of time, gives the velocity or the rate of sailing, and thence the distance run in any interval; and also a Chart of appropriate construction; in short, this branch of the art relates to the directing the ship's course under the varying forces of winds and currents, and the estimation of her change of place. The second division is that branch of practical astronomy by which the situation of the observer on the globe is ascertained by a *comparison of the position of his Zenith with relation to the heavens with the known position of the Zenith of a known place at the same moment*. The principal instruments are the sextant for measuring the altitudes and taking the distances of heavenly bodies; and a chronometer to tell us the difference in time between the meridian of the ship and the first meridian; also a pre-calculated astronomical register, such as the Nautical Almanac, the *Connaissance de Temps* of France, &c. The solution of problems in nautical astronomy requires the use of spherical trigonometry, which is therefore characteristic of this method of navigation.

115. A **Sphere** is a solid body bounded by a surface, every point of which is equally distant from a fixed point within it; this fixed point is called the **centre**; the constant distance is called the **radius**.

Every section of a sphere by a plane is a circle.

116. A **Great Circle** of a sphere is a section of the surface by a plane which passes through its centre. A **Small Circle** of a sphere is a section of the surface by a plane which does not pass through its centre.

Or, a *great circle* is a circle of the sphere having for its centre the centre of the sphere, thus dividing the sphere into two equal parts; no greater circle can be traced upon its surface. All other circles are called *small circles*.

All great circles of a sphere have the same radius. All great circles bisect each other.

117. The extremities of that diameter of a sphere which is perpendicular to the plane of a circle are called the *poles* of that circle. In the case of a small circle, the poles are distinguished as the *adjacent* and *remote* pole.

All parallel circles have the same poles. The distance of every point in the circumference of a circle from either of its poles is the same. The poles of a great circle are  $90^\circ$  distant from every point of the circle.

118. Regarding any great circle as a *primary* circle, all great circles which pass through its poles are called its *secondaries*.

All secondaries cut their primary at right angles.

The arc of a great circle is measured by the angle subtended by it at the centre of the sphere, which is also the same as the angle of inclination, at its pole, of two secondaries drawn through its extremities.

119. The earth is nearly a globe or sphere.

The ordinary proofs of this are of the following nature—1st. When a vessel is seen at a considerable distance on the sea, in any part of the world, the hull is entirely or partly concealed by the water, though the masts are visible. 2nd. Ships have actually and repeatedly made the circuit of the globe; that is, by sailing from a port in a westerly direction they have returned to it in an easterly direction. 3rd. When we travel a considerable distance from north to south, a number of new stars appear, successively, in the heavens, in the quarter to which we are advancing, and many of those in the opposite quarter gradually disappear, which would not happen if the earth were a plane in that direction. 4th. In an eclipse of the moon, which is caused by the intervention of the body of the earth between the sun and moon, the shadow of the earth thrown on the moon is found in all cases, and in every position of the earth, to be a circular figure; the earth therefore, which casts that shadow, must be a round body.

120. The earth, however, is not a perfect sphere, but of the figure of an oblate spheroid very nearly, that is, a figure traced out by an ellipse revolving round its shortest axis, being flattened in at the poles, and bulging out in a corresponding degree at the equatorial regions—the curvature being less as we recede from the equator to the poles; such a figure, in fact, as would be produced if a hoop were slightly flattened by pressure, and then made to revolve about the shortest diameter thus produced.

The shortest diameter (that which joins the poles) being 7899 statute miles, and that of the fullest parts (about the equator) being nearly  $26\frac{1}{2}$  more.

We can, of course, in a work like this give no intelligible account of the refined mathematical processes by which the most probable values of the flattening in, and of the absolute dimensions have been obtained. It is sufficient to say, that from a combination of the measurements of ten arcs of the meridian, BESSEL has deduced the following results:—\*

|  |                                   |
|--|-----------------------------------|
| Greater, or equatorial diameter . . . . .              | 41,847,192 feet = 7925.604 miles. |
| Lesser, or polar diameter . . . . .                    | 41,707,324 " = 7899.114 "         |
| Difference of diameter, or polar compression . . . . . | 139,768 " = 26.471 "              |

Proportion of diameters, as 299.15 to 298.15.

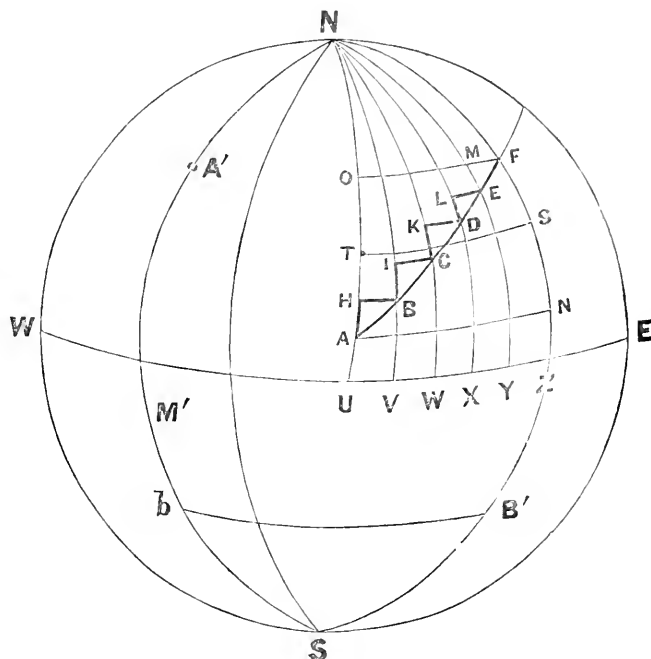
And from the result it follows that the polar diameter is shorter than the equatorial by about  $\frac{1}{3100}$  (one three hundredth) part. This quantity is technically called the *compression*.†

\* Astronomische Nachrichten, No. 438.

† The best values for its dimensions, however, appear to be those given by Capt. Clarke.

|                               |                                  |
|-------------------------------|----------------------------------|
| Equatorial diameter . . . . . | 41847662 feet = 12754937 mètres. |
| Polar axis . . . . .          | 41707536 " = 12712227 "          |

121. The **Axis of the Earth** is that diameter about which it is supposed to turn round once in twenty-four hours. The direction of this rotation is from west to east, thus causing all the heavenly bodies to have an apparent motion from east to west.



122. **Poles.**—The two extremities of the axis of the earth are called the *poles* of the earth, distinguished respectively as the *North Pole* and *South Pole*—N. S. (see fig.) The former being that to which we in Europe are nearest. As they are the extremities of a diameter they are  $180^\circ$  apart.

123. **Equator** (from Latin *æquare* to divide into equal parts), called also by seamen the *Line*, is a great circle circumscribing the earth, every point of which is equally distant from the poles, being  $90^\circ$  from each, as *W M' E*; and dividing the globe into two equal parts called hemispheres; that towards the north pole is called the northern hemisphere, as *N W E*, and the other the southern hemisphere, as *S W E*. (See figure above).

If a plane be supposed to pass through the centre of the earth at right angles to its axis, it will intersect its surface in a great circle called the **EQUATOR**.

The equator is chosen as the primary circle for co-ordinates. At all places on this circle the sun rises at 6<sup>h</sup> A.M., and sets at 6<sup>h</sup> P.M., all the year round; the days and nights are therefore equal, being 12<sup>h</sup> each.

124. The **Meridian** of any place is a semi-circle passing through that place and the poles, and therefore cutting the equator at right angles, as *N M' S*, *N W S*, *N Z S*. (See figure.) The other half of the circle is called the *opposite meridian*. Every point on the surface of the earth may be con-

ceived to have a meridian passing through it; hence there may be as many meridians as there are points in the equator. Of all these innumerable meridians one is always selected as the *Initial Circle of Longitude*, or, as it is commonly called, the *First Meridian*; it is a matter of arbitrary choice amongst different nations; thus the first meridian with us is that of Greenwich, whilst the French refer to Paris, &c.

Meridians (*L. Meridies*, from *medius dies* mid-day) are so called because they mark all places which have noon at the same instant, for when any one of the meridians is exactly opposite the sun it is mid-day with all places situated on that meridian; and with the places situated on the *opposite* meridian it is consequently midnight. They are secondaries to the Equator, and on them Latitudes are reckoned North and South from their primitive. They also mark out all places which have the same longitude, and are hence called "*Circles of Longitude*."

Every portion of the meridian lies north and south; and places lying north and south of each other are said to be on the same meridian.

The direction of the meridian towards the north pole is called *north*, and marked N.; the opposite direction is called *south*, marked S. Directions at right angles to the meridians are called *east* and *west*; the right hand looking to the north *east*, the left hand *west*: they are marked E. and W.

125. **Latitude** is the distance from the equator, measured in degrees ( $^{\circ}$ ), minutes ( $'$ ), and seconds ( $''$ ),\* on the meridian of the place, or its angular distance from the equator measured by the arc of the meridian intercepted (cut off), between the place and the equator, or by the corresponding angle at the centre of the sphere; it is marked *north* (N.), or *south* (S.), according as the place is to the north or south of the equator. Thus, the arc A' M' (fig., page 84), is the latitude of a place A' (supposed Greenwich), and is marked N., because A' is to the north of W M' E; and the latitude of B' is M' B', and is marked S., because the place B' is to the south of the equator; whilst O U, or its equal F Z, is the latitude of O, or of F.

As the latitude begins at the equator (lat.  $0^{\circ}$ ), and is reckoned thence to the poles (lat.  $90^{\circ}$ ), where it terminates, therefore the greatest latitude a place can have is  $90^{\circ}$ , and all other places must have their latitude intermediate between  $0^{\circ}$  and  $90^{\circ}$ .

126. **Parallels of Latitude** are small circles of the sphere parallel to the equator, that is, equidistant from it in every point, and hence all the places of the same latitude being at the same distance from the equator, are said to be on the same parallel: thus (fig., page 84) A N, T S, O F, and b B' are portions of parallels of latitude, and all places on O F, and b B', &c., have the same latitude, being on the same parallel.

127. **Co-Latitude** is the complement of the latitude to  $90^{\circ}$ ; thus the co-latitude of A' (fig., page 84) is A N, of B' is B' S.

128. **The Difference of Latitude** (abbreviated *diff. lat.*) between two places, or of the parallels O F and T S, or of any places on those parallels, is the arc of a meridian included between their parallels of latitude, showing how far one of them is to the northward or southward of the other; thus

\* All circles, great or small, are supposed to be divide into 360 equal parts called degrees ( $^{\circ}$ ) 60' (minutes) make one degree, and 60" (seconds) make one minute.

(fig., page 84)  $A'b$  is the difference of latitude of the two places  $A'$  and  $B'$ ;  $FS$  between the places  $F$  and  $T$ , or  $O T$ . The difference of latitude between two places can never exceed  $180^\circ$ .

The difference of latitude of the ship is therefore the distance made good in a north or south direction. This is also called her "*northing*" or "*southing*," these names being indicated by the initials  $N.$  and  $S.$

129. It is evident that when two places are on the *same* side of the equator their diff. lat. is found by subtracting the less latitude from the greater; and that when they are on *opposite* sides of the equator, that is, when one place is in north latitude and the other in south latitude, the *sum* of their latitudes is the *diff.* lat. Thus the diff. of lat. of  $A'$  and  $B'$ , which is  $A'b$ , is the sum of the north lat.  $A'M'$ , and of the south lat.  $ZB'$ , or  $M'B'$ .

130. **Meridional Parts.**—At the Equator a degree of longitude is equal to a degree of latitude; but as we approach the poles, while (upon the supposition that the earth is a sphere) the degrees of latitude remain the same, the degrees of longitude become less and less. In the chart, on Mercator's projection, the degrees of longitude are made everywhere of the same length, and, therefore, to preserve the proportion that exists at every part of the earth's surface between the degrees of latitude and the degrees of longitude, the former must be increased from their natural lengths, more and more as we recede from the equator. The lengths of small portions of the meridian thus increased, expressed in minutes of the equator, are called meridional parts; and the *meridional parts for any latitude* is the line, expressed in minutes (of the equator), into which the latitude is thus expanded. The meridional parts computed for every minute of latitude from  $0^\circ$  to  $90^\circ$ , from the *Table of meridional parts*, which is chiefly used for finding the meridional difference of latitude in solving problems in Mercator's sailing, and for constructing charts on Mercator's projection.

131. **The Meridional difference of Latitude** is the quantity which bears the same ratio to the difference of latitude that the difference of longitude bears to the departure. It is the projection of the difference of latitude on the Mercator's chart, and takes its name from the meridional parts, by the use of a table of which parts it is found.

132. **Middle Latitude.**—When the two places are situated on the *same* side of the equator, the middle latitude is the latitude of the parallel passing midway between them; its value is therefore half the sum of the latitudes of the two places. When the two places are situated on *opposite* sides of the equator, the simple "middle latitude" is replaced by the two half latitudes of each of the places. (See Raper's Navigation, page 98.)

133. **Longitude** is the arc of the equator intercepted between the first meridian and the meridian of the place, and is, therefore, the measure of the angle between the two meridians; thus (fig., page 84), take  $NA'M'bS$  as the meridian of Greenwich, then, the longitude of  $A'$ , or of any place on the meridian  $NA'M'bS$  is  $O$ , and taking  $NU$  as the meridian of  $T$ , then the arc of the equator  $M'U$  reckoned in degrees ( $^\circ$ ), minutes ( $'$ ), and seconds ( $''$ ), or the angle  $M'NU$ , which  $M'U$  measures, is the longitude of  $T$  from  $M'$ , the

meridian of Greenwich; the arc  $M'Z$ , or the angle  $M'NZ$  is the longitude of the points  $Z$ ,  $N$ ,  $S$ , and  $F$ , or of any place on the meridian  $NZ$ ; the arc  $WM'$ , or the angle  $WNM'$ , which  $WM$  measures, is the longitude of the meridian  $NWS$ , or of any place on that meridian.

Longitude is reckoned from the first meridian, both eastward and westward, till it meets at the opposite point of the equator, therefore the longitude can never exceed  $180^\circ$ .

It will be evident that the latitude alone will be insufficient for the determination of the position of a place. If we state that a certain place is  $45^\circ$  north of the equator, it will be impossible to ascertain certainly the place in question, inasmuch as there is a circle of points on the earth, all of which are  $45^\circ$  north of the equator. If we suppose a circle drawn round the surface of the northern hemisphere parallel to the equator, at the distance from the equator of  $45^\circ$ , every point of such circle will be equally characterized by the latitude of  $45^\circ$ . But if we state its latitude and longitude, we can fix at once and unequivocally, the position of the place. Thus, let us suppose that its latitude is  $50^\circ$  north, its longitude  $30^\circ$  east of Greenwich; its position will be found by imagining a circle parallel to the equator, drawn upon the northern hemisphere at a distance of  $50^\circ$  from the equator; then supposing a meridian drawn through Greenwich intersecting this parallel, and another drawn so as to cross the equator at a point  $30^\circ$  east of the former; the place in question will be upon the line parallel to the equator first drawn, inasmuch as it will be  $50^\circ$  north of the equator, and it will also be in the meridian last drawn, inasmuch as it will be  $30^\circ$  east of Greenwich. Since, then, it will be at the same time upon both these lines, it will necessarily be at the point where they cross each other at the east of the standard meridian of Greenwich. The place of a ship on the apparently indefinable and trackless face of the ocean can, in this manner, be as accurately marked down and discussed as any known and visible spot on the stable land.

134. **Difference of Longitude** between two places is the arc or portion of the equator included between their meridians, or, which is the same thing, the corresponding angle at the pole. To measure, therefore, the diff. of longitude of two places, we must follow down their meridians to the equator, and then take the included portion of the equator itself. It is named East or West, according to the direction in which the ship is proceeding; thus, if we take  $A$  and  $F$  (fig., page 84) to represent two places on the surface of the globe, the arc  $UZ$ , or the angle  $UNF$ , is diff. of long. between  $A$  and  $F$ , and is East, the arc  $UZ$  being the difference of  $HK$ , and  $HO$  is the difference of the longitudes of  $PK$  and  $PO$ , or of any two places on those meridians, and  $WZ$ , the sum of  $WM'$ , and  $M'Z$  is the difference of the longitudes of the meridians  $NWS$  and  $NZB'S$ .

135. **Horizon**.—The remote bounding circle which, to an eye elevated above the surface of the ocean, appears to unite sea and sky is called the *visible* or *sea-horizon*. A plane conceived to touch the surface of the earth at any place, and to be extended to the heavens, is called the *sensible horizon* of that place. And a plane parallel to this, but passing through the centre of the earth, is called the *rational horizon* of that place.

136. When a ship in sailing from one place another, preserves the same angle with the meridians, as she crosses them in succession, she is said to sail on a **Rhumb Line**. Thus, a ship in sailing from  $A$  to  $F$  (fig., page 84) is supposed to describe on the sea a curve  $AF$ , which cuts the meridians  $NA$ ,  $NB$ ,  $NC$ , &c., at the same angle; that is, the angles  $NAF$ ,  $NBF$ ,  $NCF$  are supposed to be equal. The rhumb line coincides with the meridian when

the course is due N. or S., or with a parallel of latitude when the course is due E. or W. On any other course but these the rhumb line is a spiral, approaching nearer and nearer to one of the poles at every convolution, but never reaching it.

Such a curve is appropriately called the *Equiangular Spiral*, and the *Loxodromic Curve*; and also because, in sailing on it, we keep on the same rhumb or point of the compass, it is called the rhumb curve. That such a curve may be drawn through any two given points will appear from this consideration,—that from one of the points an infinite number of these curves can be drawn, making different angles with the meridian, and on some one of these the second point must lie. It is evident also that only one of these curves can pass through the two points. It is the track used ordinarily in navigation, for when out of sight of land the compass determines the ship's track, and hence the selection of that track which makes a constant angle with the meridian, the advantages of such a selection being that the seaman is not required to alter his course. It would seem desirable to take the shortest route on the voyage, and this is the arc of a great circle; but the great circle drawn between two places—except it happens to be on the equator, or a meridian itself—cuts successive meridians at different angles, as a little consideration will show. When in sight of his port the compass is no longer needed, and the rhumb line is given up, and the port is made for on the great circle. When accurately following the compass course, we are, in strictness, only approximating, though very closely approximating, to a rhumb line, on account of the continuous change in the variation, due to the magnetic pole and the pole of the earth not being coincident.

137. The Course from one point of the earth's surface to another is the constant angle which the rhumb curve joining the two points makes with the meridians, or it is the direction in which a ship sails from one place to another, this direction being referred to the meridian, which lies truly north or south, or to the north or south line of the compass by which the ship is steered. The former is distinguished as the *True Course*, the latter as the *Compass Course*.

The course *steered* is the angle between the meridian and the ship's head.

The course *made good* is the angle between the meridian and the ship's real track on the surface of the sphere.

The course is reckoned from the north towards the east or west, when the ship's head is less than eight points from the north; and similarly from the south point.

The course is measured in *points* of  $11^{\circ} 15'$  each, or in degrees and minutes.

138. The Distance between two places is the arc of the rhumb line joining them, expressed in nautical miles of 60 to the degree of latitude. Thus (fig., page 84), the length of line A F, expressed in minutes of a great circle of the earth, is called the *distance*.\*

It must never be lost sight of that the distance is not necessarily nor generally the *shortest* distance between the two places, that is, the distance as the "crow flies." On a Mercator's Chart the rhumb curve is represented by a straight line, but it must be borne in mind, that equal parts of any such line do not represent equal distances on the earth.

The Meridian Distance between two places is the arc of a parallel of latitude between them.

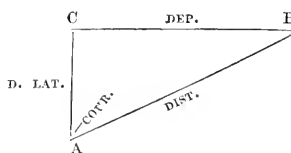
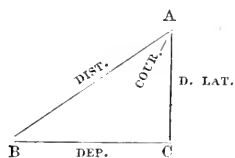
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\* Minutes of a great circle are usually called *nautical miles*, or simply miles.



140. **Departure** is the sum of all the intermediate meridian distances made in going from one place to another, computed on the supposition that the distance is divided into indefinitely small equal parts. It is the distance, in nautical miles, made good towards the east or west, and such departure is expressed in *miles*, and not like the longitude, in *arc*. When the two places are on the same parallel, the departure is identical with the distance. When the places do not differ much in latitude, and are on the same side of the equator, an approximation to the departure is found in the arc of the parallel of middle latitude included between the meridians of the two places.

If the subjoined right angled plane triangles be taken to illustrate the terms defined above (Nos. 137 to 140), A B will represent the distance sailed, that is, the length of A F on the globe (see fig. 1); A C drawn N. and S., or in the meridian, shows the angle C A B the *course*; A C will represent A O (fig. 1), while B C drawn E. and W. will represent the sum of all the small departures H B, I C, K D, &c., from the successive meridians which it crosses.



141. If a ship's course be due north or south, she sails on a meridian, and therefore makes no departure; hence the distance sailed will be equal to the difference of latitude.

If a ship sails either due east or due west, she sails on a parallel of latitude; in which case she makes *no difference of latitude*, and the departure is identical with the distance.

When the course is 4 points, or 45 degrees, the difference of latitude and departure are equal.

When the course is *less* than 4 points, or 45 degrees, the difference of latitude exceeds the departure; but when it is *more* than 4 points, or 45 degrees, the departure exceeds the difference of latitude.

142. **Magnetic Course** is the angle which the ship's track makes with the magnetic meridian; such an angle can only be shown by a compass not affected with deviation; but since the compasses of all iron ships have more or less deviation, and any course steered by such compass is magnetic in a certain sense, it has been deemed necessary to distinguish these when *corrected for deviation* as *correct magnetic courses*.

143. **Compass Course** is the angle which the track of the ship makes with the north and south line of the compass card; such a course is affected with deviation and variation; applying the deviation the result is the *correct magnetic course*; applying both the deviation and the variation it becomes the *true course*.

144. The True Bearing\* of an object or place is the angle contained between the meridian and the direction of the object, and is the same thing as the course towards it. It is thus qualified to distinguish it from the "Compass" and "Correct Magnetic Bearing."

145. Correct Magnetic Bearing.—The "correct magnetic bearing" of an object is the angle which its direction makes with the magnetic meridian; such an angle can only be found by a compass not affected with deviation. It is the bearing observed with the azimuth compass after being corrected for local deviation.

A magnetic bearing as given in "sailing directions" and on charts is the *correct* magnetic bearing—in respect to a compass affected with deviation.

146. Compass Bearing.—The bearing of an object as taken by the compass. It is the angle between the direction of the needle of the standard compass on board the ship of the observer and the direction of the object, it is therefore affected by the deviation and variation of the compass; but the deviation to be applied in this case is that due to the azimuth (direction) of the ship's head, *not that on the point of bearing*; when this correction is applied it becomes the *correct* magnetic bearing, and if, further, the correction for variation be applied, the true bearing or azimuth is deduced; E. deviation and variation to the right, W. deviation and variation to the left.

Taking a bearing of an object is called setting it.

The bearings of two objects, taken from the same place constitutes **cross bearings**, the lines of direction of the two objects intersecting or crossing each other at the place of the observer.

147. The Tropics of Cancer and Capricorn are the parallels of latitude  $23^{\circ} 28'$  N. and S. The Sun is vertical at noon twice in the year to every place between the tropics, and never to any place outside of them.

The space between the tropics is called the *Torrid Zone*.

148. The parallel of latitude which is  $23^{\circ} 28'$  from the north pole is called the *Arctic Circle*; and that which is at the same distance from the South pole is called the *Antarctic Circle*. Within these circles the sun does not set during part of the summer, nor rise during part of the winter.

The spaces within these circles are called the *Frigid Zones*.

The spaces between the tropics and the polar circles are called the *Temperate Zones*.

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\* Before the introduction of iron in such large quantities into the construction and equipment of steamers and iron sailing ships, bearings and courses were deemed to be sufficiently well defined when spoken of as true and magnetic—the latter qualifying term being used simply to indicate the *direction by compass as affected by variation only*, according to the locality. But, on board an iron ship, compass bearings and compass courses though magnetic, inasmuch as they are the indications of a magnetic needle, are no longer such in the old sense of the term, since they are affected by deviation. Under these circumstances it has been found necessary, especially in respect to this class of ships, to adopt a modification of the old nomenclature, and so "bearing" or "course" admits of an additional qualifying term not previously recognised, viz., *correct magnetic*.

## PRELIMINARY RULES IN NAVIGATION.

149. DEF.—The latitude and longitude of the place left are called the *latitude from* and *longitude from*; the latitude and longitude of the place arrived at are called the *latitude in* and *longitude in*.

150. Given the latitude from and latitude in or to, to find the true difference of latitude.

To find the difference of latitude. (For definition, &c., see Nos. 128 and 129, pages 85 and 86.)

### RULE XLIV.

1°. When the latitudes have *like* names—*Subtract the less latitude from the greater, and multiply the degrees in the remainder by 60, adding in the minutes.* The result is the true difference of latitude.

2°. When the latitudes have *unlike* names—*Take the sum of the two latitudes, reduce it to minutes.* The result is the true difference of latitude.

3°. To name the diff. lat.—*If the latitude to is North of the latitude from, mark the diff. of latitude North (N.); but if latitude to is South of latitude from, mark diff. latitude South (S.)*

Latitudes are reckoned North and South of the Equator. If these different directions are considered the one positive and the other negative, the difference of latitude of two places is always found by taking the *algebraic* difference of their latitudes.

### EXAMPLES.

Ex. 1. Find the diff. of lat. between Tynemouth Light, in lat.  $55^{\circ} 1' N.$ , and the Naze of Norway, in lat.  $57^{\circ} 58' N.$

|                |                     |
|----------------|---------------------|
| Lat. Tynemouth | $55^{\circ} 1' N.$  |
| Lat. Naze      | $57^{\circ} 58' N.$ |
|                | <hr/>               |
|                | 2 57                |
|                | 60                  |
|                | <hr/>               |
|                | 177 N.              |

The lat. *from* (Tynemouth) and lat. *to* (Naze) being of the *same* name, that is, both North, the *difference* of them is taken for the diff. lat., and since we have to pass from the lower North lat. to a higher, the diff. lat. is marked North (N.)

Ex. 3. A ship from lat.  $32^{\circ} 40' N.$ , sails to lat.  $20^{\circ} 47' N.$ : what is the diff. of lat. made?

|           |                     |
|-----------|---------------------|
| Lat. from | $32^{\circ} 40' N.$ |
| Lat. to   | $20^{\circ} 47' N.$ |
|           | <hr/>               |
|           | 11 53               |
|           | 60                  |
|           | <hr/>               |
| D. lat.   | 713 S.              |

The ship here passes from a *higher* N. lat. to a *lower* N. lat., and to do so must evidently sail S.; whence we mark diff. lat. S.

Ex. 2. Required the diff. of lat. between Cape Formosa, in lat.  $4^{\circ} 15' N.$ , and St. Helena, in lat.  $15^{\circ} 55' S.$

|                 |                     |
|-----------------|---------------------|
| Lat. C. Formosa | $4^{\circ} 15' N.$  |
| Lat. St. Helena | $15^{\circ} 55' S.$ |
|                 | <hr/>               |
|                 | 20 10               |
|                 | 60                  |
|                 | <hr/>               |
| D. lat.         | 1210 S.             |

The lat. *from* (C. Formosa) is *North*, and the lat. *to* (St. Helena) is *South*, it is evident that the ship must sail South in order to pass from North lat. into South; whence we put South (S.) to the diff. of lat.

Ex. 4. Required the diff. of lat. between Port Natal, in lat.  $29^{\circ} 53' S.$ , and Akyab, in lat.  $20^{\circ} 8' N.$

|                 |                     |
|-----------------|---------------------|
| Lat. Port Natal | $29^{\circ} 53' S.$ |
| Lat. Akyab      | $20^{\circ} 8' N.$  |
|                 | <hr/>               |
|                 | 50 1                |
|                 | 60                  |
|                 | <hr/>               |
| D. lat.         | 3001 N.             |

As the ship (Port Natal) is in S. hemisphere and Akyab is in the N. hemisphere, to pass from the former into the latter the ship must sail N.

## Preliminary Rules in Navigation.

Ex. 5. A ship from lat.  $50^{\circ}$  S. arrives in lat.  $45^{\circ} 29'$  S.: what is the diff. of lat?

Lat. from  $50^{\circ} 0' \text{ S.}$   
Lat. in  $45^{\circ} 29' \text{ S.}$

D. lat.  $4^{\circ} 31' = 271 \text{ N.}$

Here the ship passes from a *higher* to a *lower* S. lat., and to do so must evidently sail N.; whence the diff. lat. is marked N.

Ex. 6. A ship from lat.  $13^{\circ} 45' \text{ S.}$ , arrives in lat.  $26^{\circ} 15' \text{ S.}$ : required diff. lat.

Lat. from  $13^{\circ} 45' \text{ S.}$   
Lat. in  $26^{\circ} 15' \text{ S.}$

$12^{\circ} 30' = 750 \text{ S.}$

Here the ship passes from a *lower* to a *higher* S. lat., and to do so must evidently sail S.; whence S. is marked against the diff. of lat.

(a) When one of the places has no latitude, or is on the Equator, the latitude of the other place is equal to the difference of latitude.

Ex. 7. A ship from a place A, lat. 0, is bound to a place B, lat.  $25^{\circ}$  S.; required the diff. lat.

Since lat. is reckoned from the Equator lat. 0° (N. or S.) to pass from 0° to  $25^{\circ}$  S., the ship must evidently sail S.; whence the lat. of B ( $25^{\circ}$ ) is diff. of lat., and is marked S.

Ex. 8. A ship from a place A, in lat.  $10^{\circ}$  N., arrives at a place B, in lat. 0°: required the diff. lat. made.

One place being on the Equator, and the other in  $10^{\circ}$  N., the diff. of lat. is evidently  $10^{\circ}$  or 600' and is named S., because it is evident the ship must sail South to pass from  $10^{\circ}$  N. to 0° N.

### EXAMPLES FOR PRACTICE.

Required the difference of latitude between the place A and the place B in each of the following examples:—

1. Lat. A  $55^{\circ} 0' \text{ N.}$   
B  $58^{\circ} 23' \text{ N.}$

4. Lat. A  $3^{\circ} 42' \text{ S.}$   
B  $1^{\circ} 48' \text{ N.}$

7. Lat. A  $10^{\circ} 10' \text{ N.}$   
B  $0^{\circ} 0'$

2. Lat. A  $50^{\circ} 38' \text{ N.}$   
B  $42^{\circ} 48' \text{ N.}$

5. Lat. A  $13^{\circ} 15' \text{ S.}$   
B  $0^{\circ} 0'$

8. Lat. A  $49^{\circ} 52' \text{ S.}$   
B  $42^{\circ} 13' \text{ S.}$

3. Lat. A  $58^{\circ} 24' \text{ S.}$   
B  $63^{\circ} 17' \text{ S.}$

6. Lat. A  $0^{\circ} 0'$   
B  $2^{\circ} 37' \text{ S.}$

9. Lat. A  $0^{\circ} 17' \text{ N.}$   
B  $1^{\circ} 17' \text{ N.}$

151. To find the meridional difference of latitude, having given the latitude from and latitude in. (For definition, see page 86, Nos. 130 and 131).

### RULE XLV.

*Take the meridional parts for the two latitudes from the Table of meridional parts; take the difference if the latitudes are of the same name, but their sum if the names are unlike. The result is the meridional difference of latitude.*

#### EXAMPLES.

Ex. 1. Lat. A  $49^{\circ} 10' \text{ N.}$ , lat. B  $27^{\circ} 40' \text{ N.}$ : find the mer. diff. of lat.

Lat. A  $49^{\circ} 10' \text{ N.}$  M. parts 3397  
B  $27^{\circ} 40' \text{ N.}$  „ 1729

Mer. d. lat. 1668

Ex. 3. Lat. left  $29^{\circ} 53' \text{ S.}$ , and lat. to  $20^{\circ} 8' \text{ N.}$ : required mer. diff. of lat.

Lat. left  $29^{\circ} 53' \text{ S.}$  M. parts 1880  
Lat. to  $20^{\circ} 8' \text{ N.}$  „ 1234

Mer. d. lat. 3114

Ex. 2. Lat. left  $49^{\circ} 58' \text{ S.}$ , and lat. bound to  $32^{\circ} 42' \text{ S.}$ : find mer. diff. of lat.

Lat. left  $49^{\circ} 58' \text{ S.}$  M. parts 3471  
Lat. to  $32^{\circ} 42' \text{ S.}$  „ 2078

Mer. d. lat. 1393

Ex. 4. Lat. from  $46^{\circ} 40' \text{ N.}$ , and lat. to  $34^{\circ} 22' \text{ S.}$ : find the mer. diff. of lat.

Lat. left  $46^{\circ} 40' \text{ N.}$  M. parts 3173  
Lat. to  $34^{\circ} 22' \text{ S.}$  „ 2198

Mer. d. lat. 5371

### EXAMPLES FOR PRACTICE.

Find the meridional difference of latitude in each of the following examples:—

1. Lat. from  $34^{\circ} 40' \text{ N.}$  Lat. in  $33^{\circ} 20' \text{ N.}$   
2. „  $24^{\circ} 12' \text{ S.}$  „  $15^{\circ} 18' \text{ N.}$   
3. „  $49^{\circ} 10' \text{ S.}$  „  $52^{\circ} 47' \text{ S.}$

4. Lat. from  $15^{\circ} 44' \text{ N.}$  Lat. in  $4^{\circ} 20' \text{ S.}$   
5. „  $60^{\circ} 20' \text{ S.}$  „  $67^{\circ} 10' \text{ S.}$   
6. „  $0^{\circ} 0'$  „  $4^{\circ} 20' \text{ N.}$

152. To find the latitude in, having given the latitude from and true difference of latitude.

# RULE XLVI.

1°. When the latitude from and true difference of latitude have a *like* name—*To the latitude from add the true difference of latitude (turned into degrees, minutes, and seconds, if necessary): the sum will be the latitude in, of the same name as the latitude from.*

2°. When the latitude from and true difference of latitude have *unlike* names—*Under the latitude from, put the true difference of latitude (in degrees and minutes, if necessary); the remainder marked with the name of the greater is the latitude in.*

## EXAMPLES.

Ex. 1. A ship from lat.  $59^{\circ} 27' S.$ , sails South, until the diff. lat. is 374 miles: required the lat. come to.

|                            |   |
|----------------------------|---|
| $6,0)37,4$                 | Lat. from $59^{\circ} 27' S.$                   |
| $\underline{\hspace{1cm}}$ | D. lat. $\underline{\hspace{1cm}} 6 \ 14 \ S.$  |
| $6^{\circ} 14' S.$         | Lat. in $\underline{\hspace{1cm}} 65 \ 41 \ S.$ |

Ex. 2. A ship from lat.  $2^{\circ} 25' N.$  sails South, 180 miles: what lat. is she in?

|                            |  |
|----------------------------|--|
| $6,0)18,0$                 | Lat. from $2^{\circ} 25' N.$                   |
| $\underline{\hspace{1cm}}$ | D. lat. $\underline{\hspace{1cm}} 3 \ 0 \ S.$  |
| $3^{\circ} 0'$             | Lat. in $\underline{\hspace{1cm}} 0 \ 35 \ S.$ |

In this example it is evident that as the diff. lat. is more than the lat. left, the ship must have crossed the Equator, and consequently has come into South lat.

Ex. 3. A ship from lat.  $55^{\circ} 1' N.$  sails North, 94 miles: find the lat. in.

|                            |   |
|----------------------------|---|
| $6,0)9,4$                  | Lat. from $55^{\circ} 1' N.$                    |
| $\underline{\hspace{1cm}}$ | D. lat. $\underline{\hspace{1cm}} 1 \ 34 \ N.$  |
| $1^{\circ} 34'$            | Lat. in $\underline{\hspace{1cm}} 56 \ 35 \ N.$ |

Ex. 4. A ship from lat.  $28^{\circ} 39' N.$  sails South, 131 miles: required the lat. in.

|                            |   |
|----------------------------|---|
| $6,0)13,1$                 | Lat. from $28^{\circ} 39' N.$                   |
| $\underline{\hspace{1cm}}$ | D. lat. $\underline{\hspace{1cm}} 2 \ 11 \ S.$  |
| $2^{\circ} 11'$            | Lat. in $\underline{\hspace{1cm}} 26 \ 28 \ N.$ |

Ex. 5. A ship from lat.  $0^{\circ} 49' S.$  sails North, 83 miles: required the lat. in.

|                            |  |
|----------------------------|--|
| $6,0)8,3$                  | Lat. from $0^{\circ} 49' S.$                   |
| $\underline{\hspace{1cm}}$ | D. lat. $\underline{\hspace{1cm}} 1 \ 23 \ N.$ |
| $1^{\circ} 23'$            | Lat. in $\underline{\hspace{1cm}} 0 \ 34 \ N.$ |

Ex. 6. A ship from lat.  $3^{\circ} 12' N.$  sails South, 192 miles: required the lat. arrived at.

|                            |   |
|----------------------------|---|
| $6,0)19,2$                 | Lat. from $3^{\circ} 12' N.$                    |
| $\underline{\hspace{1cm}}$ | D. lat. $\underline{\hspace{1cm}} 3 \ 12 \ S.$  |
| $3^{\circ} 12'$            | On the Equator $\underline{\hspace{1cm}} 0 \ 0$ |

## EXAMPLES FOR PRACTICE.

Find the latitude in, in each of the following examples:—

|                                  |                   |                                |                   |
|----------------------------------|-------------------|--------------------------------|-------------------|
| 1. Lat. from $31^{\circ} 10' N.$ | D. lat. $172' N.$ | 6. Lat. from $0^{\circ} 8' N.$ | D. lat. $182' S.$ |
| 2. " $29 \ 38 \ N.$              | " $104 \ S.$      | 7. " $0 \ 39 \ N.$             | " $59 \ S.$       |
| 3. " $3 \ 2 \ S.$                | " $190 \ N.$      | 8. " $3 \ 58 \ N.$             | " $238 \ S.$      |
| 4. " $2 \ 56 \ S.$               | " $357 \ N.$      | 9. " $4 \ 48 \ S.$             | " $288 \ N.$      |
| 5. " $0 \ 0$                     | " $168 \ S.$      | 10. " $35 \ 25 \ S.$           | " $229 \ S.$      |

153. To find the middle latitude, having given the latitude from and latitude in. (For definition see No. 132, page 86.)

# RULE XLVII.

The name being supposed *alike*, that is, both *North* or both *South*—*Add together the true latitudes, and take half the sum; the result is the middle latitude.*

NOTE.—When the names are unlike, the middle latitude (which is seldom required but for obtaining the departure) should be found by means of a table; but in this case, it may perhaps be as well to avoid the use of the middle latitude in any of the common problems of navigation.

## EXAMPLES.

Ex. 1. Find the mid. lat., having given the lat. from  $50^{\circ} 25' N.$ , and lat. in  $47^{\circ} 12' N.$

Lat. from  $50^{\circ} 25' N.$   
Lat. in  $47^{\circ} 12' N.$

$\begin{array}{r} 2)97\ 37 \\ \hline \end{array}$

Mid. lat.  $48\ 48$

Ex. 2. Lat. from  $6^{\circ} 28' S.$ , lat. in  $14^{\circ} 50' S.$ : required the mid lat.

Lat. from  $6^{\circ} 28' S.$   
Lat. in  $14\ 50\ S.$

$\begin{array}{r} 2)21\ 18 \\ \hline \end{array}$

Mid. lat.  $10\ 39$

## EXAMPLES FOR PRACTICE.

Required the middle latitude in each of the following examples:—

- |                                  |                   |                               |                            |
|----------------------------------|-------------------|-------------------------------|----------------------------|
| 1. Lat. from $16^{\circ} 10' S.$ | D. lat. $138' S.$ | 4. Lat. A $63^{\circ} 53' S.$ | Lat. B $59^{\circ} 10' S.$ |
| 2. „ $1\ 40\ S.$                 | „ $61\ S.$        | 5. „ $56\ 10\ N.$             | „ $50\ 15\ N.$             |
| 3. „ $36\ 22\ N.$                | „ $90\ S.$        | 6. „ $67\ 20\ S.$             | „ $61\ 42\ S.$             |

154. To find the difference of longitude, having given the longitude from and longitude to. (For definition see No. 134, page 86).

## RULE XLVIII.

1°. When the longitudes are of the same name—Take their difference and reduce the same to minutes, place E. or W. against the remainder, according as the longitude to is East or West of longitude from.

2°. When the longitudes are of contrary names—Take the sum of the two longs., which sum, if less than  $180^{\circ}$ , is the diff. of long., and attach E. or W., according as the long. to is East or West of long. from; but when the sum exceeds  $180^{\circ}$  subtract it from  $360^{\circ}$ , for the diff. of long., and reduce the remainder thus found to minutes, attaching to it the contrary name to that found in the usual way.

Longitudes are reckoned East or West of the first meridian. If these different directions are considered one positive and the other negative, the difference of longitude of two places is always found by taking the algebraic difference of their longitudes.

## EXAMPLES.

Ex. 1. Find the diff. of long., having given the long. from  $89^{\circ} 42' W.$ , and long. in  $79^{\circ} 42' W.$

Long. from  $89^{\circ} 42' W.$   
Long. in  $79\ 42\ W.$

$\begin{array}{r} 10\ 0 \\ 60 \\ \hline \end{array}$

D. long.  $600\ E.$

The ship here passes from a high W. long. to a lower, and diff. long. must be E. to do so.

Ex. 3. A ship from Cape Bajoli, long.  $3^{\circ} 48' E.$ , is bound to Cape Sicie, in long.  $5^{\circ} 51' E.$ : required the diff. of long.

Long. Cape Bajoli  $3^{\circ} 48' E.$   
Long. Cape Sicie  $5\ 51\ E.$

$\begin{array}{r} 2\ 3 \\ 60 \\ \hline \end{array}$

D. long.  $123\ E.$

The long. to Cape Sicie is E. of long. from Cape Bajoli, therefore, diff. of long. is marked E. The ship must evidently sail E.

Ex. 2. Required the diff. of long., having given the long. from  $12^{\circ} 20' E.$ , and long. in  $2^{\circ} 45' W.$

Long. from  $12^{\circ} 20' E.$   
Long. in  $2\ 45\ W.$

$\begin{array}{r} 15\ 5 \\ 60 \\ \hline \end{array}$

D. long.  $905\ W.$

The ship here passes from E. long. to W. long., and in order to do so diff. long. must be W.

Ex. 4. A ship from Tynemouth, in long.  $1^{\circ} 25' W.$ , is bound to long.  $7^{\circ} 12' E.$ : required the diff. of long.

Long from  $1^{\circ} 25' W.$   
Long. to  $7\ 12\ E.$

$\begin{array}{r} 8\ 37 \\ 60 \\ \hline \end{array}$

D. long.  $517\ E.$

The ship here is about to cross the meridian of Greenwich (long.  $0^{\circ}$ ) and pass from W. long. to E. long., whence the diff. of long. must be E. to do so.

Ex. 5. Find the diff. long. between Acapulco, long.  $99^{\circ} 54' W.$ , and Pellew Island, long.  $134^{\circ} 21' E.$

|                     |                      |
|---------------------|----------------------|
| Long. Acapulco      | $99^{\circ} 54' W.$  |
| Long. Pellew Island | $134^{\circ} 21' E.$ |

|                                  |                      |
|----------------------------------|----------------------|
| Being greater than $180^{\circ}$ | $234^{\circ} 15' E.$ |
| it is subtracted from            | $360^{\circ} 0'$     |

|                   |                      |
|-------------------|----------------------|
| Diff. of long. is | $125^{\circ} 45' W.$ |
|                   | $60$                 |

D. long.  $7545 W.$

By going E. and W. from Greenwich, the two places in this example will be found to be  $234^{\circ} 15'$  asunder, but as both places are for our purpose upon one circle, the smaller arc of the circle must be taken to find how far apart the places Acapulco and Pellew Island are separated; so that the sum  $234^{\circ} 15'$  is subtracted from  $360^{\circ}$ , the whole circumference of a circle, for the required answer.

Ex. 7. A ship from long.  $5^{\circ} 12' W.$  is bound to a port in long.  $90^{\circ} W.$ : what diff. of long. must she make?

|                               |
|-------------------------------|
| Long. from $5^{\circ} 12' W.$ |
| Long. to $90^{\circ} W.$      |

|                  |
|------------------|
| $84^{\circ} 48'$ |
| $60$             |

D. long.  $5088 W.$

The ship here passes from a *less* to a *greater* W. long.: and therefore the diff. of long. must be W. to do so.

Ex. 6. A ship from long.  $177^{\circ} 50' E.$  arrives in long.  $178^{\circ} 10' W.$ : what diff. of long. has she made?

|            |                      |
|------------|----------------------|
| Long. left | $177^{\circ} 50' E.$ |
| Long. in   | $178^{\circ} 10' W.$ |

|                                  |                     |
|----------------------------------|---------------------|
| Being greater than $180^{\circ}$ | $356^{\circ} 0' W.$ |
| it is subtracted from            | $360^{\circ} 0'$    |

|                   |                   |
|-------------------|-------------------|
| Diff. of long. is | $4^{\circ} 0' E.$ |
|                   | $60$              |

D. long.  $240 E.$

Ex. 8. A ship from long.  $165^{\circ} E.$  is bound to a place in long.  $72^{\circ} 12' E.$ : what diff. of long must she make?

|            |                     |
|------------|---------------------|
| Long. left | $165^{\circ} 0' E.$ |
| Long. to   | $72^{\circ} 12' E.$ |

|                  |
|------------------|
| $92^{\circ} 48'$ |
| $60$             |

D. long.  $5568 W.$

The ship in this example sails from a *greater* to a *less* long. (E. long.), the diff. long. is therefore, of a different name to the long. left.

### EXAMPLES FOR PRACTICE.

Required the difference of longitude between a place A and a place B in each of the following examples:—

- |                               |                             |                               |                           |
|-------------------------------|-----------------------------|-------------------------------|---------------------------|
| 1. Long. A $9^{\circ} 29' W.$ | Long. B. $4^{\circ} 29' W.$ | 7. Long. A $0^{\circ} 55' E.$ | Long. B $7^{\circ} 3' E.$ |
| 2. " 1 $25 W.$                | " 7 $2 E.$                  | 8. " 40 $10 E.$               | " 33 $10 E.$              |
| 3. " 6 $11 E.$                | " 5 $45 W.$                 | 9. " 178 $30 W.$              | " 178 $30 E.$             |
| 4. " 0 $0$                    | " 4 $20 W.$                 | 10. " 176 $34 E.$             | " 176 $34 W.$             |
| 5. " 4 $20 W.$                | " 0 $10 E.$                 | 11. " 38 $32 W.$              | " 8 $43 E.$               |
| 6. " 7 $2 E.$                 | " 0 $0$                     | 12. " 5 $12 W.$               | " 25 $12 W.$              |

155. To find the longitude in, having given the longitude from and the difference of longitude.

### RULE XLIX.

1°. When the longitude from and the difference of longitude have *like* names—*To the longitude from add difference of longitude (turned into degrees, if necessary); the sum, if not more than  $180^{\circ}$ , will be the longitude in, of the same name as the longitude from; but if the sum exceed  $180^{\circ}$ , subtract it from  $360^{\circ}$ , and the remainder is the long. in and of a contrary name to long. from.*

2°. When the longitude left and difference of longitude have *unlike* names—*Under longitude from, put difference of longitude (in degrees and minutes, if necessary); take the less from the greater; the remainder, marked with the name of the greater, is the longitude in.*

## EXAMPLES.

Ex. 1. A ship from long.  $5^{\circ} 12' W.$  makes diff. long.  $113'$  W.: required the long in.

$$\begin{array}{r} \text{Long. from } 5^{\circ} 12' W. \\ 6,0)11,3 \quad \text{D. long. } 1 \ 53 \ W. \\ \hline 1^{\circ} 53' W. \quad \text{Long. in } 7 \ 5 \ W. \end{array}$$

Ex. 3. A ship from long.  $0^{\circ} 57' E.$  sails W. until her diff. of long. is  $201'$ : find the long. in.

$$\begin{array}{r} \text{Long. from } 0^{\circ} 57' E. \\ 6,0)20,1 \quad \text{D. long. } 3 \ 21 \ W. \\ \hline 3^{\circ} 21' W. \quad \text{Long. in } 2 \ 24 \ W. \end{array}$$

Ex. 5. Long. from  $3^{\circ} 40' W.$ , diff. of long.  $220'$  E.: required the long. in.

$$\begin{array}{r} \text{Long. from } 3^{\circ} 40' W. \\ 6,0)22,0 \quad \text{D. long. } 3 \ 40 \ E. \\ \hline 3^{\circ} 40' E. \quad \text{Long. in } 0 \ 0 \\ \text{On the meridian of Greenwich.} \end{array}$$

Ex. 2. A ship from long.  $1^{\circ} 25' W.$  sails E. until her diff. of long. is  $177'$ : required her long. in.

$$\begin{array}{r} \text{Long. from } 1^{\circ} 25' W. \\ 6,0)17,7 \quad \text{D. long. } 2 \ 57 \ E. \\ \hline 2^{\circ} 57' E. \quad \text{Long. in } 1 \ 32 \ E. \end{array}$$

Ex. 4. Let the long. left be  $174^{\circ} 4' W.$ , and the diff. of long.  $797'$  W.: required the long. in.

$$\begin{array}{r} \text{Long. from } 174^{\circ} 4' W. \\ 6,0)79,7 \quad \text{D. long. } 13 \ 17 \ W. \\ \hline 13^{\circ} 17' W. \\ \text{Being greater than } 180^{\circ} \quad 187 \ 21 \ W. \\ \text{subtract from} \quad \underline{360 \ 0} \\ \text{Long. in } 172 \ 39 \ E. \end{array}$$

Ex. 6. A ship from long.  $177^{\circ} 40' W.$  makes  $140'$  diff. of long. to the W.: required the long. arrived at.

$$\begin{array}{r} \text{Long. from } 177^{\circ} 40' W. \\ 6,0)14,0 \quad \text{D. long. } 2 \ 20 \ W. \\ \hline 2^{\circ} 20' W. \quad \text{Long. in } 180 \ 0 \ W. \\ \hline \text{or, } 180 \ 0 \ E. \end{array}$$

## EXAMPLES FOR PRACTICE.

Required the longitude in, or arrived at, in each of the following examples:

- |   |  |
|---|--|
| 1. Long. from $5^{\circ} 48' W.$ D. long. $110' W.$ | 7. Long. from $41^{\circ} 29' W.$ D. long. $139' E.$ |
| 2. " " $0 \ 59 \ W.$ " " $137 \ E.$                 | 8. " " $94 \ 4 \ E.$ " " $115 \ W.$                  |
| 3. " " $29 \ 10 \ E.$ " " $114 \ E.$                | 9. " " $98 \ 54 \ E.$ " " $302 \ E.$                 |
| 4. " " $3 \ 10 \ E.$ " " $220 \ W.$                 | 10. " " $178 \ 13 \ E.$ " " $201 \ E.$               |
| 5. " " $2 \ 47 \ W.$ " " $242 \ E.$                 | 11. " " $177 \ 6 \ W.$ " " $237 \ W.$                |
| 6. " " $3 \ 12 \ E.$ " " $237 \ W.$                 | 12. " " $179 \ 59 \ W.$ " " $2 \ W.$                 |

13. Define meridian of the earth, equator, parallel of latitude. Which of these are great circles, and why?

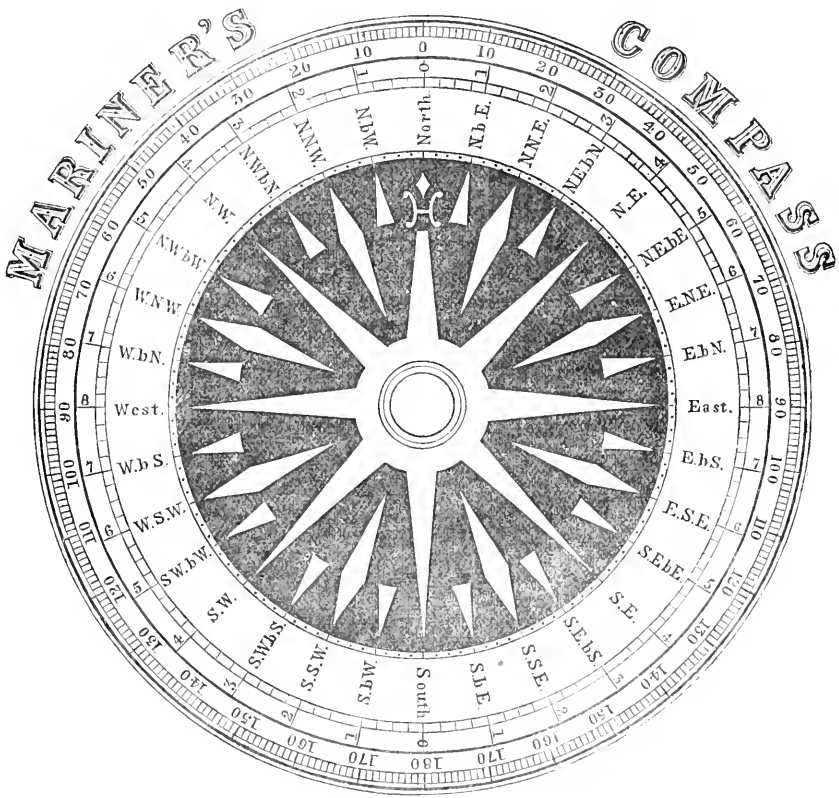


## THE COMPASS.

156. **The Compass\*** is simply an instrument which utilises the directive power of the magnet. A magnetised bar of steel, apart from disturbing forces and free to move, points in a definite direction, and to this direction all others may be referred, and a ship guided on any desired course.

There are various adaptations of the instrument, according to the use it is specially intended for. The compass intended for use on board ship is called the "**Mariner's Compass**," and according to the purposes it is intended for it is named **The Steering Compass**, **The Standard Compass**, and **The Azimuth Compass**.

157. **The Mariner's Compass** consists of a circular card, which represents the horizon of the observer; the circumference or edge of the card being divided according to two systems of notation into points and degrees.



\* The origin of the compass is very obscure. The ancients were aware that the loadstone attracted iron, but were ignorant of its directing property. The instrument came into use in Europe sometime in the course of the thirteenth century.

1. **By Points.**--There are 32 *points*; and each of those divisions is again sub-divided into four parts called *quarter points*. A point of the compass being therefore the 32nd part of the circumference of a circle is equal to  $11^{\circ} 15'$ . The four principal points, or, as they are called, the *cardinal points*, are the North (represented by N), South (S), East (E), West (W), the East being to the right and West to the left when facing the North.

All the points of the compass are called by names composed of these four terms.

Thus, the points half-way between the cardinal points are called after the two adjacent cardinal points; hence the point midway between the North and East is called North-east, and represented by N.E.; so midway between South and East is called South-east (written S.E.); in like manner we get South-west (written S.W.), and North-west (written N.W.)

A point half-way between one of these last and a cardinal point is called, in like manner, by a name composed of the nearest cardinal point and the adjacent points, N.E., N.W., S.E., and S.W. Thus, the point half-way between N. and N.E. is called North-north-east (written N.N.E.); the point between E. and N.E. is called East-north-east (written E.N.E.); and so we have E.S.E., S.S.E., W.S.W., W.N.W., and N.N.W. The remaining sixteen points are reckoned from the cardinal or secondary point to which each is adjacent, the name of which it takes qualified by the name of the succeeding cardinal point towards which it lies. Thus, the point next to N., on the east side, is called North by East (written N. by E.); that next N.E., towards the north, is called North-east by North (N.E. by N.); and so we have N.E. by E., E. by N., E. by S., S.E. by E., S.E. by S., S. by E., S. by W., S.W. by S., S.W. by W., W. by S., W. by N., N.W. by W., N.W. by N., N. by W.

The points of the compass are frequently spoken of with reference to their position to the right or left of the cardinal point towards the spectator is looking; thus, N.N.E. is said to be "two points" to the right-hand of North; W.N.W. six points to the left of North.

A *half-point*, which is the middle division between two points, is called after that one of its adjacent points which is either a cardinal point or is the nearest to a cardinal point. Thus, the middle division between N. and N. by E. is called North-half-east (written N.  $\frac{1}{2}$  E.) Half-points near N.E., N.W., S.E., and S.W., take their name from these points. Thus, we say, N.E.  $\frac{1}{2}$  N., N.E. by E.  $\frac{1}{2}$  E.

The same holds for a quarter and for three-quarters as for a half-point, all of which are named upon the same principle as the subordinate points.

In choosing the name to use we must be guided by circumstances. In some problems it is convenient always to reckon uniformly from North or South, but generally the simpler name will be the preferable one; and similarly for quarters and three-quarters of a point.

2. **By Degrees.**--The whole circumference is divided into three hundred and sixty degrees ( $360^{\circ}$ ), each degree into sixty minutes ( $60'$ ). This furnishes

a notation for the compass more minute than points, half points, and quarter points. We still reckon from the cardinal points; thus, to indicate a division which has  $72^{\circ} 48'$  to the east of North we write N.  $72^{\circ} 48'$  E.

The name of the opposite point to any proposed point is known at once, without referring to the compass, by simply reversing the names or the letters which compose it—thus, the opposite of N. being S. and of E. being W., the opposite point to N.E. by N. is at once known to be S.W. by S., the opposite of W.  $\frac{3}{4}$  S. is E.  $\frac{3}{4}$  N. and so on.

158. Repeating the points in any order is called *boxing the compass*; to do this is, of course, one of the first things a seaman learns.

159. As the ship's course, which is sometimes expressed in points and sometimes in degrees, is always reckoned from the North or South point, the seaman has to refer at once, in using the Tables, to the *number of points* or *degrees* in any course given by *name*. The following table, which exhibits the degrees, minutes, and seconds in each quarter point of the compass, will be convenient for reference.

### A TABLE OF THE ANGLES,

which every Point and Quarter Point of the Compass makes with the Meridian.

| NORTH      |            | Points | 0 | 1  | 2  | Points | SOUTH |   |
|------------|------------|--------|---|----|----|--------|-------|---|
|            |            | 0      | 1 | 2  | 48 | 45     | 0     | 1 |
|            |            | 0      | 0 | 5  | 37 | 30     | 0     | 0 |
|            |            | 0      | 0 | 8  | 26 | 15     | 0     | 0 |
| N. by E.   | N. by W.   | 1      | 1 | 11 | 15 | 0      | 1     | 1 |
|            |            | 1      | 1 | 14 | 3  | 45     | 1     | 1 |
|            |            | 1      | 1 | 16 | 52 | 30     | 1     | 1 |
| N.N.E.     | N.N.W.     | 1      | 1 | 19 | 41 | 15     | 1     | 1 |
|            |            | 2      | 2 | 22 | 30 | 0      | 2     | 2 |
|            |            | 2      | 2 | 25 | 18 | 45     | 2     | 2 |
|            |            | 2      | 2 | 28 | 7  | 30     | 2     | 2 |
|            |            | 2      | 2 | 30 | 50 | 15     | 2     | 2 |
| N.E. by N. | N.W. by N. | 3      | 3 | 33 | 45 | 0      | 3     | 3 |
|            |            | 3      | 3 | 36 | 33 | 45     | 3     | 3 |
|            |            | 3      | 3 | 39 | 22 | 30     | 3     | 3 |
|            |            | 3      | 3 | 42 | 11 | 15     | 3     | 3 |
| N.E.       | N.W.       | 4      | 4 | 45 | 0  | 0      | 4     | 4 |
|            |            | 4      | 4 | 47 | 48 | 45     | 4     | 4 |
|            |            | 4      | 4 | 50 | 37 | 30     | 4     | 4 |
|            |            | 4      | 4 | 53 | 26 | 15     | 4     | 4 |
| N.E. by E. | N.W. by W. | 5      | 5 | 55 | 15 | 0      | 5     | 5 |
|            |            | 5      | 5 | 58 | 3  | 45     | 5     | 5 |
|            |            | 5      | 5 | 61 | 52 | 30     | 5     | 5 |
|            |            | 5      | 5 | 64 | 41 | 15     | 5     | 5 |
| E.N.E.     | W.N.W.     | 6      | 6 | 67 | 30 | 0      | 6     | 6 |
|            |            | 6      | 6 | 70 | 18 | 45     | 6     | 6 |
|            |            | 6      | 6 | 73 | 7  | 30     | 6     | 6 |
|            |            | 6      | 6 | 75 | 56 | 15     | 6     | 6 |
| E. by N.   | W. by N.   | 7      | 7 | 78 | 45 | 0      | 7     | 7 |
|            |            | 7      | 7 | 81 | 33 | 45     | 7     | 7 |
|            |            | 7      | 7 | 84 | 22 | 30     | 7     | 7 |
|            |            | 7      | 7 | 87 | 11 | 15     | 7     | 7 |
| East.      | West.      | 8      | 8 | 90 | 0  | 0      | 8     | 8 |

160. The card is laid upon a magnetic needle, which is a small steel bar magnetised, the north end being attached to the north end or *pole* of the needle.\* The whole is then balanced on a sharp centre or pivot rising from

\* Some compass cards carry on their lower surface, one, two, four, or more parallel magnets with similar poles pointing in similar directions. The object of using several magnets is to increase the magnetic moment of a given weight of steel.

the bottom of a brass bowl, and covered with glass. The bowl having a weight fixed to it below, is placed in *gimbals*, which are brass hoops or rings, so arranged as to admit of motion about two independent horizontal axis at right-angles to each other, *i.e.*, each turning upon two pivots at opposite points of the hoop next greater in size; by this means the loaded bowl remains nearly horizontal during the confused and irregular motion of the ship. The pivots of the outer ring fit into bearings in the binnacle (a turret shaped case fitted with panes of glass and a lamp) and constitutes the **Steering Compass**.

161. The helmsman steers the ship so that a line parallel to the keel passes over the centre of the card, and the point prescribed as the course. Care is taken to place the box so that the *lubber's point* in the bowl and the centre of the card are in a line fore-and-aft, or parallel to the keel; but as lubber's point deviates a little from its proper position when the ship is heeled over, seamen do not implicitly depend upon it, as, indeed, the name implies.

162. The **Azimuth Compass** is a compass of superior construction, particularly adapted to observe bearings. It is mounted on a stand, and is fitted with two small frames carrying vertical wires, called *sight-vanes*, for the purpose of observing objects elevated above the horizon. In one of these vanes there is a long and very narrow slit, and in the other is an opening of the same kind, but wider, and having a wire up and down the middle of it, exactly opposite the slit.

163. In the best modern instruments, a horizontal ring is expressly provided to carry the vertical wire frame, and instead of having a wire next the eye, a glass prism, acting by internal reflection, is placed there, so arranged that one half of the pupil of the eye can observe the wire on the further side of the horizontal ring and the distant object, and the other half of the pupil can see the graduations of the compass card by internal reflection in the prism. This prism is a solid piece of glass, whose sides are parallelograms and ends triangles. The compass card is very carefully and minutely graduated; besides the points and quarter points being marked, the circumference over which the prism passes is graduated in degrees, and usually cut to every 20', and this graduation is arranged so that we may read off the bearing at once, and is reckoned in more ways than one, for facilitating taking bearings from different cardinal points. The card can be brought to rest by a stop. There is also a contrivance for throwing the card off its centre when the instrument is not in use, to prevent the fine pivot being worn, and the sensibility of the compass impaired. This instrument is known as the **Prismatic Azimuth Compass**.

164. In observing bearings on board ship the card should never be stopped, but two or more bearings being read off as quickly as convenient, the mean should be used; for, as the vessel, and consequently the compass-card, have always some motion, the card may not therefore be stopped exactly in the middle of its vibration, which as may be supposed to vibrate equally on both sides of the line of direction of the object, is essential to the true result.

165. **Standard Compass.**—The Standard Compass on board ship is the one placed on a particular spot on deck, or above it, where the local deviation is nothing, or very small. Such a compass will show magnetic bearings correct, or of ascertained errors, and the deviation of the Steering Compass can at any time be determined by a comparison with it—all other compasses employed being in fact simply considered as auxiliaries to it. It should be fitted with an azimuth circle. This circle should be graduated so as to show the angle between the ship's head and any heavenly body, as measured on the horizon, without using the compass card; the sight-vanes and reading prism should be fitted to the azimuth circle in such a way as to turn freely in azimuth, without moving the compass bowl or disturbing the card.

#### SELECTION OF BEST POSITION FOR COMPASSES.

166. **Standard Compass.**—The Standard Compass should be placed in the middle of the ship, and fixed on a permanent and secure pillar or support, raised at such a height as to permit amplitudes of the sun and bearings of the land to be conveniently observed by it. It should also be in a position as far as possible removed from any considerable mass of iron—at least 5 feet from iron deck beams—and should not be within 10 feet of the extremity of any elongated iron mass, especially if vertical, such as funnels, stanchions, or the spindle of the wheel; and it should be received as a general rule that no iron, subject to occasional removal, is to be placed within 15 feet of this compass, either on the same deck or that below it.

167. **Steering Compasses** being placed according to the requirements of the ship, the moderate and uniform amount of deviation generally attainable at the Standard Compass by selection of position, cannot always be secured. Still we should do the best we can, for if, as frequently happens, the steering wheel is placed near an iron stern-post or rudder-head, and further fitted with an iron spindle—near which, of necessity, the steering compass is fitted—then large and perplexing deviations may be expected, defying even approximate correction by magnets, causing much inconvenience to the helmsman, and possibly a total loss of the services of the compass on the ship proceeding into southern latitudes.

The following rules to avoid the inconvenience and even danger just pointed out, have been recommended in selecting a place for steering compasses:—"Not to be within half the width of the ship from the stern-post or rudder-head; the spindle of the steering wheel and the foremost support on which the wheel works *not* to be of iron; avoid vertical iron." The needle should be at least 3ft. 6in. from iron deck beams, and as much higher as can be made convenient to the helmsman.

In addition to the rules already given for the guidance of seamen, the following (given by Capt. Evans, Superintendent of the Admiralty Compass Department) are worthy the attention of the Naval Architect and those superintending the equipment of the ship:—

1. In all designs for the construction of iron ships, a place to be prepared for the Standard Compass, and to be shown in the plan.
2. The Standard Compass not to be within half the breadth of the ship

from the rudder-head and stern-post or iron cased screw well, not to be nearer an iron deck or iron deck beams than five feet.

3. In ships built near *North*, the Standard Compass to be as far *forward* as the requirements of the ship will permit. In ships built head near *South*, to be as far aft as the requirements of the ship will permit, subject to Rule 2. In ships built nearly *East* or *West*, the Standard Compass not to be near either extremity of the vessel

4. To be as far as possible from transverse iron bulkheads.

5. As far as possible, no masses of iron—as boilers, engines, bulkheads, or stanchions—should be placed below the compass, or within  $55^\circ$  of the vertical line through the centre, the angle being drawn from the compass as centre to the centre of the mass in question.\*

168. There is no advantage in having a large number of compasses in a ship: since unlike the mean results of a number of chronometers, for example, the mean results of any number of compasses need not necessarily be near the truth, as they may all be largely in error, and that error may be all in one direction. Hence the necessity of depending upon one compass alone, but that compass should be in the best position in the ship, of the best manufacture, and the constant attention of the navigator should be devoted to ascertain its errors.

NOTE.—“Comparative Merits of Large and Small Compasses.—Of late years much diversity in practice has prevailed as to the size of compasses for use on board ship. The Admiralty Standard Card, for example, is fitted with needles, the maximum lengths of which are  $7\frac{1}{2}$  inches, while in large passenger steam vessels the needles are frequently 12 to 15 inches, and even longer. The chief object in the employment of large compasses is to enable the helmsman to steer to degrees, and a more accurate course is presumed to be preserved.

“With reference to this increased size it must be observed that competent authorities limit the length of efficient compass needles to 5 or 6 inches; beyond this limit an increase of length is alone accompanied by an increase of directive power in the same proportion, and if the thickness of the needle be preserved, the weight, and consequently the friction, increases in the same ratio. No advantage of directive power is therefore gained by increase of length, but with the increased weight of the card and appendages, the increase of friction probably far exceeds the increase of directive force; sluggishness is the result, which is further exaggerated by the extreme slowness of oscillation of long needles compared with short ones.

“Large cards, however convenient in practice, are therefore not without danger, for the course steered may deceive the seaman by seeming right to the fraction of a degree, but which avails little if the card itself is wrong half a point, and the ship in consequence

\* Investigation has shown that the effect of a sphere of iron within this cone is prejudicial by diminishing the directive force and increasing the heeling error to windward—when without the cone it would be beneficial in both respects. Hence the recommendation.

With reference to the magnetic character of boilers, or tanks, it has been stated that the effect is the same as if they were solid bodies, on the assumption that magnetism exists entirely on the surface of iron masses. This is not the case; it is, however, true that the effect of hollow masses of iron increases very rapidly with the increase of the thickness of the iron, so that the limit of thickness is speedily reached when the effect of the body is sensibly the same as if it were solid; for example, in a tank 4 feet in diameter and  $\frac{1}{10}$ th of an inch thick, the effect is about  $\frac{1}{2}$  of a solid mass of the same size; in a similar sized tank  $\frac{1}{4}$  of an inch thick, the effect would be about half that of a solid mass.—See a valuable investigation by Mr. Archibald Smith, in the Phil. Trans. for 1865, pages 304—318.

hazarded. In the opinion of the writer, the present Admiralty Standard Card is as large as should be used for the purposes of *navigation*, and that as regards safety in the long, steady, and fast ship; the choice is really between the Admiralty Card and a smaller one. In short, the question may be thus stated:—the smaller a card the more correctly it points, the larger a card the more accurately it is read.”—*Manual of the Deviation of the Compass*, by Capt. Evans, R.N.

#### ADJUSTMENTS OF THE COMPASS.

169. (1.) The direction of the magnetism of the needle or the “magnetic axis” should be in a line along *the middle of the needle itself*, otherwise the needle will not point with exactness to the magnetic North and South. To examine whether this is the case reverse the needle on the card. If after this reversion the N. and S. points of the card are also found to be reversed, the adjustment is good.

As this error obviously affects all points of the compass alike, it may be included in the total variation of the particular compass as found by observation and therefore need not be made the subject of special examination.

(2.) *The pivot must be in the centre of the graduated circumference of the card.* If it is not, the difference of bearing of two objects will not be the same when measured on different parts of the edge. This adjustment is generally good.

(3.) *The line joining the eye-vane and the object-vane, called the “line of sight” of the Azimuth Compass, must pass directly over the pivot.* This condition is examined by noting carefully the bearing of a distant object, and then turning the compass half round, so as to reverse the vane and the slit, and then repeating the observation with an object eight points from the first. The bearings taken directly should be identical with those taken by reversion. The effects of this error, if any, may be eliminated by taking the mean of the direct and reversed bearings every time the instrument is used.

(4.) *The sight vanes must be vertical, i.e., the eye-vane and the object-vane must each be vertical.*

This can be examined only on shore, by observing whether the wires coincide through their length with a plumb line, or any vertical edge. When this adjustment is not perfect, or when the bowl is not maintained in a strictly horizontal position, bearings are most correctly obtained when the object is low.

## CORRECTING COURSES.

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170. The corrections of the compass are those quantities which must be applied to the indications of the instrument to obtain the reading that would be given if the north point of the compass-card always corresponded to the north point of the horizon. Three corrections are sometimes necessary to be applied to the course steered by compass, to reduce it to the true course; and the converse. These are called

1. The Leeway.
2. The Variation of the Compass.
3. The Deviation of the Compass.

### 1. LEEWAY.

171. The angle included between the direction of the fore-and-aft line or keel of a ship, and that in which she moves through the water, as indicated by her wake, is called the **Leeway**.

A ship is said to be **on the port tack** when the wind is on her port side, that is, on the left hand side of a person looking forward; and **on the starboard tack** when the wind is on her starboard side, that is, on the right hand side of a person looking forward.\*

When the ship is not going before the wind, she will not only be forced forward in the direction of her head, but, in consequence of the wind pressing against her sideways, her actual course will be to "*leeward*" of the apparent course she is lying. The amount of leeway differs in different ships; depending on their construction, on the sails set, the velocity forward, and other circumstances. Experience and observation are required to judge what amount of leeway to allow in each case. The correction for *leeway* is necessary to deduce the course made good from the course steered, and it is one of the corrections to be applied in reducing the compass course to the true course in the day's work; the correction being allowed according to

### RULE I.

*When the ship is on the port tack, allow the leeway to the right of the course steered; but when on the starboard tack, allow it to the left, the observer looking from the centre of the compass towards the point the ship is sailing upon.*

### EXAMPLES.

Ex. 1. The course steered is N.W. by W., the wind N. by E., leeway  $1\frac{1}{4}$  points.

The ship has the starboard tacks on board; therefore, the leeway ( $1\frac{1}{4}$  points) allowed to the left of N.W. by W., gives corrected Course W. by N.  $\frac{3}{4}$  N.

Ex. 2. Course by Compass S. by E., wind E. by S., leeway  $2\frac{3}{4}$  points.

The ship is on the port tack, then  $2\frac{3}{4}$  points allowed to the right of S. by E., is S. by W.  $\frac{3}{4}$  W., the Course corrected for leeway.

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\* A ship is said to be *on the tack* of the side from which the wind comes: even if it be on the quarter.



Ex. 3. Course N.E. by N., the wind N.W. by N., the leeway 1 point.

The ship being on the *port* tack, 1 point to the *right*, of N.E. by N. is N.E., the corrected *Course*.

Ex. 4. Course steered W. by S., the wind N.W. by N., leeway  $3\frac{1}{2}$  points.

The ship is on the *starboard* tack,  $3\frac{1}{2}$  points to the *left* of W. by S. is S.W.  $\frac{1}{2}$  S., the Compass Course made good.

172. The points of the compass are frequently treated with reference to their position to the right or left of the cardinal point towards which the spectator is looking, thus N.N.E. is said to be "two points to the right of North;" W.N.W. "six points to the left of North." Adopting this notation the work in the above Examples will stand thus:—

Ex. 1.  
Course steered N.W. by W. is 5 pts. L of N  
Leeway carries ship  $1\frac{1}{4}$  „ L of N  
Sum is corrected course  $6\frac{1}{4}$  „ L of N  
or W. by N.  $\frac{3}{4}$  N.

Ex. 3.  
Course steered N.E. by N. is 3 pts. R. of N.  
Leeway carries ship 1 „ R. of N.  
Sun is corrected course + „ R. of N.  
or N.E.

Ex. 2.  
Course steered S. by E. is 1 pt. L of S  
Leeway carries ship  $2\frac{3}{4}$  „ R of S  
The difference is  $1\frac{3}{4}$  „ R of S  
S. by W.  $\frac{3}{4}$  W.

Ex. 4.  
Course steered W. by S. is 7 pts. R. of S.  
Leeway carries ship  $3\frac{1}{2}$  „ L. of S.  
The diff. is corrected course  $3\frac{1}{2}$  „ R. of S.  
or S.W.  $\frac{1}{2}$  S.

### EXAMPLES FOR PRACTICE.

Correct the following courses for leeway:—

|    | Course Steered.         | Wind.                 | Leeway.        |    | Course Steered.       | Wind.      | Leeway.        |
|----|-------------------------|-----------------------|----------------|----|-----------------------|------------|----------------|
| 1. | S.S.W.                  | S.E.                  | $1\frac{1}{2}$ | 4. | E. $\frac{3}{4}$ N.   | N. by E.   | $1\frac{3}{4}$ |
| 2. | S.W. $\frac{1}{2}$ W.   | W.N.W.                | $2\frac{1}{4}$ | 5. | N.W. $\frac{3}{4}$ N. | N.E. by E. | $1\frac{3}{4}$ |
| 3. | N. by E.                | E. by N.              | $\frac{1}{4}$  | 6. | S.W. by W.            | S. by E.   | $2\frac{3}{4}$ |
| 4. | N.N.E. $\frac{1}{2}$ E. | N.W. $\frac{1}{2}$ N. | 2              | 7. | N.E. $\frac{1}{4}$ E. | N. by W.   | $1\frac{1}{2}$ |

(a) *When the ship is hove-to, take the middle point between that to which she comes up and that to which she falls off for the compass course, and correct this for leeway.*

### EXAMPLES.

Ex. 1. A ship lying-to under her main-sail, with her starboard tacks aboard, comes up E. by S., and falls off to N.E. by E., making 5 points leeway. What compass course does she make good?

The middle point between E. by S. and N.E. by E. is E. by N., then 5 points to the *left* hand gives N.N.E., the compass course made good.

Ex. 3. A ship lying-to comes up S. by E. and falls off to S.E. by E., the wind being S.W., making 5 points leeway: required the compass course.

The middle point between S. by E. and S.E. by E. is S.E. by S., then 5 points to the *left* hand (the ship having starboard tacks on board) is East, the compass course made good.

Ex. 2. A ship lying-to under a close-reefed main-topsail, with her port (larboard) tacks on board, comes up to S.S.W. and falls off to S.W. by W., making  $2\frac{1}{2}$  points leeway. What compass course does she make?

The middle point between S.S.W. and S.W. by W. is S. W.  $\frac{1}{2}$  S., then  $2\frac{1}{2}$  points to the *right* hand is W.S.W.

Ex. 4. A ship lying-to with port tacks on board, comes up W. by S. and falls off N.W. by W., making 5 points leeway. What course does she make good?

The middle point between W. by S. and N.W. by W. is W. by N., then 5 points to the *right* hand is N.N.W., the compass course made good.

## 2. THE VARIATION OF THE COMPASS

173. The needle points to the magnetic north, which in few parts of the world agrees with the true north, the difference between them is called the *Variation of the Compass*.\*

The variation is said to be *easterly* when the north end of the needle is drawn to the eastward, and *westerly* when drawn to the westward of the true north; thus, when the north end of the needle points to that part of the horizon, which is true N.N.W.  $\frac{1}{2}$  W., the variation is said to be  $2\frac{1}{2}$  points west; but when it points to the N. by E. part of the horizon, the variation is said to be 1 point east.

174. The variation is different in different places,† and it is also subject to a slow change in the same place, and becomes alternately east and west.‡ It also changes slightly at different times of the day.§ Its value for each locality is indicated on charts, and always to be found by easy methods.

175. Variation is one of the “corrections” in deducing the true course and bearing from the course and bearing observed with the compass. It is given on the charts used in navigation.

The method of correcting Compass Courses or Bearings for Variation will be readily understood by means of an example.

Suppose the variation of the compass is found to be two points east—That is, the needle is directed two points to the right of the north point of the heavens—that is, points N.N.E.

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\* This is the term commonly employed by nautical men; but among men of science the term “Magnetic Declination” is usually substituted for “Magnetic Variation.”

† At Greenwich, at the present time, the variation is  $20^{\circ}$  W., or the North end of the magnetic needle does not point exactly North, but  $20^{\circ}$  W., of North. In the West Indies the variation is 0; at Cape Farewell,  $53^{\circ}$  W.; at Cape Horn,  $23^{\circ}$  E.; at Hobart Town,  $10^{\circ}$  E.; at Canton  $1^{\circ}$  E.; and Cape of Good Hope,  $29\frac{1}{2}^{\circ}$  W. Generally in Europe, Africa and the Atlantic, the variation is westerly, while in America, and the Pacific, it is easterly.

‡ “The system of Magnetic Meridians has undergone considerable changes in the times of modern accurate science. The southern point of Africa received from the Portuguese voyagers in the fifteenth century the name of L’Agulhas (the needle), because the direction of the compass needle or the Local Magnetic Meridian, coincided with the Geographical Meridian: it now makes with it an angle of about  $30^{\circ}$  W. In the sixteenth century, the compass-needle in Britain pointed east of north: it now points from  $20^{\circ}$  to  $30^{\circ}$  (in different parts of the British isles) west of north. At the present time, a change of the opposite character is going on: in 1819 the westerly declination at Greenwich was about  $24^{\circ} 23'$ , which was probably its maximum; in the last 30 years it has diminished from  $23\frac{1}{2}^{\circ}$  to  $20^{\circ}$  nearly. It is believed that the magnetic poles are rotating round the geographical poles from East to West.”—*A Treatise on Magnetism*, designed for the use of Students in the University. By George Biddell Airy, M.A., L.L.D., D.C.L.

§ Besides the gradual changes which occur in terrestrial magnetism, both as regards direction and intensity of force, in the course of long periods of time, there are minute fluctuations continually traceable. To a certain extent these are dependent on the varying positions of the sun, and, to a much smaller extent, of the moon, with respect to the place of observation; but over and above all regular and periodic changes, there is a large amount of irregular fluctuations, which occasionally become so great as to constitute what is called a *magnetic storm*. These variations occur with great rapidity, causing deflections to the right and left comparable in their rate or period of alternation with ordinary telegraphic signalling; accidental variations of  $70'$  have been observed. “Magnetic storms” are not connected with thunder-storms, or any other known disturbance of the atmosphere; but are invariably connected with exhibitions of aurora borealis, and with spontaneous galvanic currents in the telegraphic wires, and this connection is found to be so certain, that upon remarking the display of one of the three classes of phenomena, we can at once assert that the other two are observable (the aurora borealis sometimes not visible here, but certainly visible in a more northern latitude).

instead of N.; then the N.N.W. point of the compass card will evidently point to the true north, and every other point on the card will be shifted round two points. If, therefore, a ship is sailing *by compass* N.N.W., or, as it is usually expressed, her compass course is N.N.W., her true course will be north; that is, *two points to the right of the compass course*. In a similar manner it may be shown that when the variation is two points westerly, the true course will be *two points to the left of the compass course*.

176. To find the true course, the compass course being given.

RULE LI.

*Allow easterly variation to the right of the compass course.*

westerly           ,,         left           ,,         ,,

looking from the centre of the card over the point to be corrected.\*

### EXAMPLES.

Taking the courses between North and South round by east.

Ex. 1. Course steered N.E. by E. variation  $2\frac{3}{4}$  points *West*, to find the true course.

Here the compass course is N. 5 points E., and the variation is westerly, and hence must be applied to the *left*, thereby bringing it  $2\frac{3}{4}$  points nearer to the North (N. 5 E.— $2\frac{3}{4}$ =N.  $2\frac{1}{4}$  E.), that is, within  $2\frac{1}{4}$  points of North; the true course is therefore N.N.E.  $\frac{1}{4}$  E.

Ex. 3. Course by compass N.N.E., variation  $2\frac{1}{4}$  points *West*, the *true course*  $2\frac{1}{4}$  points to the left hand of N.N.E., or N.  $\frac{1}{4}$  W.

Ex. 5. Compass course S.E., variation  $1\frac{1}{4}$  points *East*, then the *true course* (allowing the variation to the *right*) will be S.S.E.  $\frac{3}{4}$  E., or S.  $2\frac{3}{4}$  points E.

Ex. 7. Compass course East, variation 2 points *West*, then allowing 2 points to the left gives *true course* E.N.E.

Now proceeding to the courses between North and South round by West.

Ex. 9. Course by compass N.W.  $\frac{1}{2}$  W., variation 2 points *West*, then the *true course* (allowing the variation to the *left*) will be W. by N.  $\frac{1}{2}$  N., or N.  $6\frac{1}{2}$  points W.

Ex. 11. Again, compass course S.W. by S., variation  $2\frac{3}{4}$  points *West*, the *true course* (allowing variation to the *left*) will be S.  $\frac{1}{4}$  W.

Ex. 13. Compass course S.S.W., variation  $3\frac{1}{2}$  West, then allowing  $3\frac{1}{2}$  W. to the left of S.S.W. gives S. by E.  $\frac{1}{2}$  E., or  $1\frac{1}{2}$  points E.

Ex. 2. Course steered the same, viz., N.E. by E., variation  $1\frac{3}{4}$  points East.

Here the compass course is N. 5 points E., and the variation Easterly, and hence must be applied to the *right*, thereby carrying the course *away from the North towards the East*, that is,  $6\frac{1}{2}$  points to the Eastward of North (N. 5 E. +  $1\frac{1}{2}$  E. = N.  $6\frac{1}{2}$  E.); the true course is therefore E. by N.  $\frac{1}{2}$  N.

Ex. 4. Compass course S. by E. variation  $2\frac{1}{4}$  East,  $2\frac{1}{4}$  points allowed to right of S. by E. is S. by W.  $\frac{1}{4}$  W., or S.  $1\frac{1}{4}$  W.

Ex. 6. But compass course S.E., variation  $2\frac{1}{2}$  points *West*, then the *true course* (allowing the variation to the *left*) will be E. by S.  $\frac{1}{2}$  S., or S.  $6\frac{1}{2}$  points E.

Ex. 8. Compass course E., variation  $2\frac{3}{4}$  points *East*, then the *true course* (allowing the variation to the right hand) is S.E. by E.  $\frac{1}{4}$  E.

Ex. 10. Taking the same compass course, viz., N.W.  $\frac{1}{2}$  W., when the variation is  $1\frac{1}{2}$  points *East*, the *true course* (allowing the variation to the *right*) will be N.W. by N., or N.  $\frac{3}{4}$  points W.

Ex. 12. Compass course S.W. by S. (as before) variation  $1\frac{3}{4}$  East, the *true course* (allowing the variation to the *right*) will be S. W.  $\frac{3}{4}$  W., or S.  $4\frac{3}{4}$  points W.

Ex. 14. Compass course W., variation  $2\frac{1}{2}$  E., then the *true course* (allowing  $2\frac{1}{2}$  points to the *right*) is N.W. by W.  $\frac{1}{2}$  W., or N.  $5\frac{1}{2}$  points W.

\* The learner must be careful to remember when correcting his courses that he is to suppose himself *looking from the centre of the card over the point to be corrected*. When he places the compass card before him, mistakes very frequently occur in the application of the variation between the *east* and *west* points round by *south*; thus—taking the compass with the north point placed before or from the observer, while an error could scarcely arise when correcting courses in the N.E. and N.W. quadrants, it would be different with the S.E. and S.W. quadrants, unless he bore in mind, that in the latter instance the compass card should be placed before him, as if he were facing the south. From what has been said it will be seen that in correcting courses, the significance of *RIGHT* on the face of a compass card, is *as the hands of a watch move over the dial*, and *LEFT* the contrary direction.

Ex. 15. But with compass course West, and variation  $3\frac{1}{2}$  *West*, then allowing  $3\frac{1}{4}$  points to the left of W., the true course is S.W.  $\frac{3}{4}$  W., or S.  $4\frac{3}{4}$  points W.

Ex. 16. Compass course N.N.W.  $\frac{1}{2}$  W., variation  $3\frac{1}{2}$  points *East*, then  $3\frac{1}{4}$  points to the right of N.N.W.  $\frac{1}{2}$  W., is N.  $\frac{3}{4}$  E.

177. The learner should so familiarise himself with the compass card as to be able entirely to dispense with its use in correcting courses, and when he has acquired such knowledge, he will find the following rule serviceable, in which the points of the compass are treated numerically.

### RULE LII.

1°. Put down the points and quarter points which the compass course is to the right or left of North or South, marking them R. or L. accordingly.

2°. Underneath put the variation, marking it also R. or L., accordingly as it is E. or W.

3°. If the names are alike, take the sum, with that name, for the true course.

(a) When the sum amounts to 8 points, it is either E. or W.

(b) When the sum exceeds 8 points, take it from 16 points; the remainder is the true course to be reckoned from the opposite point to that which the compass course is reckoned from.

That is, it is to be reckoned from the North if it had previously been reckoned from S., but marked S. if previously marked N.; also, if marked L (left) change to R (right); but if marked R change to L.

4°. If the names are unlike, take the difference, and mark it the same name as the greater.

(c) If the variation being subtractive, exceeds the amount from which it is to be subtracted, take the points of the course from the variation, and name it the course towards West if it had previously been Easterly, but towards the East if it had been Westerly.

(d) Also bear in mind that 0 points is either North or South as the case may be.

The following are examples of this method of applying the variation, and the numbers and letters in brackets refer to the rule as given above:—

1. Compass Courses:—S.S.W.; N. by E.  $\frac{1}{2}$  E.; W.S.W.; and E. by N. Variation  $3\frac{1}{2}$  points Easterly. Required the True Courses.

| S.S.W.  | N. by E. $\frac{1}{2}$ E. | W.S.W.                                       | E. by N.                    |
|---|---------------------------|--|-----------------------------|
| S.S.W. = 2 R. of S.   | $1\frac{1}{2}$ R. of N.   | 6 R. of S.                                   | 7 R. of N.                  |
| Var. $3\frac{1}{2}$ R. [3°]                                       | $3\frac{1}{2}$ R. [3°]    | $3\frac{1}{2}$ R. [b]                        | $3\frac{1}{2}$ R. [b]       |
| Sum $5\frac{1}{2}$ R. of S.                                       | 5                         | $9\frac{1}{2}$ R. of S.                      | $10\frac{1}{2}$ R. of N.    |
|   |                           | 16   | 16                          |
| S.W. by W. $\frac{1}{2}$ W.                                       | N.E. by E.                | $6\frac{1}{2}$ L. of N.                      | $5\frac{1}{2}$ L. of S.     |
| Here the sum is taken for the true course, the names being alike. |                           | Here the names being alike the sum is taken. |                             |
|   |                           | (See No. 3°)                                 |                             |
|   |                           | W. by N. $\frac{1}{2}$ N.                    | S.E. by E. $\frac{1}{2}$ E. |

2. Compass Courses:—N.N.W.; S. by E.; W.  $\frac{1}{2}$  N.; and E. by S. Variation  $2\frac{1}{2}$  W.

| N.N.W.                  | S. by E.                | W. $\frac{1}{2}$ N.     | E. by S.                  |
|-------------------------|-------------------------|-------------------------|---------------------------|
| 2 L. of N.              | 1 L. of S.              | $7\frac{1}{2}$ L. of N. | 7 L. of S.                |
| $2\frac{1}{2}$ L. [3°]  | $2\frac{1}{2}$ L. [3°]  | $2\frac{1}{2}$ L. [b]   | $2\frac{1}{2}$ L. [b]     |
| $4\frac{1}{2}$ L. of N. | $3\frac{1}{2}$ L. of S. | 10 L. of N.             | $9\frac{1}{2}$ L. of S.   |
|                         |                         | 16                      | 16                        |
| N.W. $\frac{1}{2}$ W.   | S.E. $\frac{1}{2}$ S.   | 6 R. of S.              | $6\frac{1}{2}$ R. of N.   |
|                         |                         | W.S.W.                  | E. by N. $\frac{1}{2}$ N. |

3. Compass Courses:—N.E.  $\frac{1}{2}$  E.; S.W.  $\frac{3}{4}$  W.; N. by E.; and S. by W. Variation  $2\frac{1}{4}$  points West.

|                         |                         |                           |                           |
|-------------------------|-------------------------|---------------------------|---------------------------|
| N.E. $\frac{1}{2}$ E.   | S.W. $\frac{3}{4}$ W.   | N. by E.                  | S. by W.                  |
| $4\frac{1}{2}$ R. of N. | $4\frac{3}{4}$ R. of S. | 1 R. of N.                | 1 R. of S.                |
| $2\frac{1}{4}$ L. [4°]  | $2\frac{3}{4}$ L. [4°]  | $2\frac{1}{4}$ L. [c]     | $2\frac{1}{4}$ L. [c]     |
| $2\frac{1}{4}$ R. of N. | $2\frac{3}{4}$ R. of S. | $1\frac{1}{4}$ L. of N.   | $1\frac{1}{4}$ L. of S.   |
| N.N.E. $\frac{1}{4}$ E. | S.S.W. $\frac{1}{2}$ W. | N. by W. $\frac{1}{4}$ W. | S. by E. $\frac{1}{4}$ E. |

4. Compass Courses:—N.W. by W.; S.E. by E.; N. by W.  $\frac{1}{2}$  W.; and S. by E. Variation  $3\frac{1}{4}$  points East.

|                           |                           |                           |                         |
|---------------------------|---------------------------|---------------------------|-------------------------|
| N.W. by W.                | S.E. by E.                | N. by W. $\frac{1}{2}$ W. | S. by E.                |
| 5 L. of N.                | 5 L. of S.                | $1\frac{1}{2}$ L. of N.   | 1 L. of S.              |
| $3\frac{1}{4}$ R. [4°]    | $3\frac{1}{4}$ R. [4°]    | $3\frac{1}{4}$ R. [c]     | $3\frac{1}{4}$ R. [c]   |
| $1\frac{3}{4}$ L. of N.   | $1\frac{3}{4}$ L. of S.   | $1\frac{3}{4}$ R. of N.   | $2\frac{1}{4}$ R. of S. |
| N. by W. $\frac{3}{4}$ W. | S. by E. $\frac{3}{4}$ E. | N. by E. $\frac{3}{4}$ E. | S.S.W. $\frac{1}{4}$ W. |

5. N.N.E., Variation 2 points W.; S. by E., Variation 1 point E.; W. by S., Variation 1 point E.; and E.S.E., Variation 2 points W.

|                   |                     |                     |                   |
|-------------------|---------------------|---------------------|-------------------|
| N.N.E., Var. 2 W. | S. by E., Var. 1 E. | W. by S., Var. 1 E. | E.S.E., Var. 2 W. |
| 2 R. of N.        | 1 L. of S.          | 7 R. of S.          | 6 L. of S.        |
| 2 L.              | 1 R.                | 1 R.                | 2 L.              |
| 0 [d]             | 0 [d]               | 8 R. of S. [a]      | 8 L. of S. [a]    |
| N.                | S.                  | W.                  | E.                |

6. North, Variation 2 points E.; South, Variation 2 points W.; West, Variation 2 points W.; and East, Variation 2 points E.

|                 |                 |                 |                 |
|-----------------|-----------------|-----------------|-----------------|
| N., Var. 2 E.   | S., Var. 2 W.   | W., Var. 2 W.   | E. Var. 2 E.    |
| 0 = N.          | 0 = S.          | 8 R. of S.      | 8 L. of S.      |
| 2 R. of N.      | 2 L. of S.      | 2 L.            | 2 R.            |
| 2 R. of N. [3°] | 2 L. of S. [3°] | 6 R. of S. [4°] | 6 L. of S. [4°] |
| N.N.E.          | S.S.E.          | W.S.W.          | E.S.E.          |

178. If the learner has carefully gone through the preceding examples, he will have noticed that *Easterly* variation in its application to Compass Courses *increases* them in the *N.E.* and *S.W.* quarters of the compass; and *decreases* them in the *N.W.* and *S.E.* quarters. *Westerly* variation *decreases* the courses in the *N.E.* and *S.W.* quadrants, and *increases* it in the *N.W.* and *S.E.*; we have, therefore,

### RULE LIII.

Westerly variation is — from all points between N. and E. .... S. and W.  
 Easterly variation is + to all points between N. and E. .... S. and W.  
 Westerly variation is + to all points between N. and W. .... S. and E.  
 Easterly variation is — from all points between N. and W. .... S. and E.

We shall now proceed to illustrate the foregoing rule, which is very generally used in the correcting of courses.

1. Compass Courses: N.N.E.; S. by W.  $\frac{1}{2}$  W.; W.N.W.; S.E.  $\frac{1}{2}$  E. Var.  $3\frac{1}{4}$  E.
- |                             |                       |                         |                           |
|-----------------------------|-----------------------|-------------------------|---------------------------|
| N. 2 E.                     | S. $1\frac{1}{2}$ W.  | N. 6 W.                 | S. $4\frac{1}{2}$ E.      |
| + $3\frac{1}{4}$ E.         | + $3\frac{1}{4}$ E.   | — $3\frac{1}{4}$ E.     | — $3\frac{1}{4}$ E.       |
| N. $5\frac{1}{4}$ E.        | S. $4\frac{3}{4}$ W.  | N. $2\frac{3}{4}$ W.    | S. $1\frac{1}{4}$ E.      |
| N.E. by E. $\frac{1}{4}$ E. | S.W. $\frac{3}{4}$ W. | N.N.W. $\frac{3}{4}$ W. | S. by E. $\frac{1}{4}$ E. |
2. Compass Courses:—E.N.E.; W. by S.; N.N.W.; S. by E. Var.  $3\frac{1}{4}$  E.
- |                           |                             |                           |                         |
|---------------------------|-----------------------------|---------------------------|-------------------------|
| N. 6 E.                   | S. 7 W.                     | N. 2 W.                   | S. 1 E.                 |
| + $3\frac{1}{4}$ E.       | + $3\frac{1}{4}$ E.         | — $3\frac{1}{4}$ E.       | — $3\frac{1}{4}$ E.     |
| N. $9\frac{1}{4}$ E.      | S. $10\frac{1}{4}$ W.       | N. $1\frac{1}{4}$ E.      | S. $2\frac{1}{4}$ W.    |
| 16                        | 16                          | N. by E. $\frac{1}{4}$ E. | S.S.W. $\frac{1}{4}$ W. |
| S. $6\frac{3}{4}$ E.      | N. $5\frac{3}{4}$ W.        |                           |                         |
| E. by S. $\frac{3}{4}$ S. | N.W. by W. $\frac{3}{4}$ W. |                           |                         |
3. Compass Courses:—N.E.; S.W.  $\frac{1}{2}$  S.; N.W.  $\frac{1}{2}$  N.; S.E.  $\frac{1}{2}$  S. Var.  $2\frac{1}{4}$  W.
- |                           |                           |                      |                      |
|---------------------------|---------------------------|----------------------|----------------------|
| N. 4 E.                   | S. $3\frac{1}{2}$ W.      | N. $3\frac{1}{2}$ W. | S. $3\frac{3}{4}$ E. |
| — $2\frac{1}{4}$ W.       | — $2\frac{1}{4}$ W.       | + $2\frac{1}{4}$ W.  | + $2\frac{1}{4}$ W.  |
| N. $1\frac{3}{4}$ E.      | S. $1\frac{1}{4}$ W.      | N. $5\frac{3}{4}$ W. | S. 6 E.              |
| N. by E. $\frac{3}{4}$ E. | S. by W. $\frac{1}{4}$ W. |                      |                      |
4. Compass Courses:—N. by E.; S. by W.  $\frac{1}{4}$  W.; W.  $\frac{1}{2}$  N.; E. by S. Var.  $2\frac{1}{4}$  W.
- |                      |                      |                      |                      |
|----------------------|----------------------|----------------------|----------------------|
| N. 1 E.              | S. $1\frac{1}{4}$ W. | N. $7\frac{1}{2}$ W. | S. 7 E.              |
| — $2\frac{1}{4}$ W.  | — $2\frac{1}{4}$ W.  | + $2\frac{1}{4}$ W.  | + $2\frac{1}{4}$ W.  |
| N. $1\frac{3}{4}$ W. | S. 1 E.              | N. $9\frac{3}{4}$ W. | S. $9\frac{1}{4}$ E. |
|                      |                      | 16                   | 16                   |
|                      |                      | S. $6\frac{1}{4}$ W. | N. $6\frac{3}{4}$ E. |
5. Compass Courses:—N.N.W.  $\frac{3}{4}$  W.; S.S.E.  $\frac{3}{4}$  E.; N.E. by E.  $\frac{1}{4}$  E.; S.W. by W.  $\frac{1}{4}$  W.; Variation  $2\frac{3}{4}$  E.
- |                      |                      |                      |                      |
|----------------------|----------------------|----------------------|----------------------|
| N. $2\frac{3}{4}$ W. | S. $2\frac{3}{4}$ E. | N. $5\frac{1}{4}$ E. | S. $5\frac{1}{4}$ W. |
| — $2\frac{3}{4}$ E.  | — $2\frac{3}{4}$ E.  | + $2\frac{3}{4}$ E.  | + $2\frac{3}{4}$ E.  |
| o                    | o                    | N. 8 E.              | S. 8 W.              |
| North.               | South.               | East.                | West.                |

## EXAMPLES FOR PRACTICE.

Correct the following Compass Courses for Variation:—

| COMPASS COURSE.                | VAR.              | COMPASS COURSE.            | VAR.              | COMPASS COURSE.             | VAR.              |
|--------------------------------|-------------------|----------------------------|-------------------|-----------------------------|-------------------|
| 1. N.N.E.                      | 2 E.              | 6. S.S.E.                  | 2 W.              | 12. N.N.E.                  | $2\frac{1}{4}$ W. |
| 2. S.E. $\frac{1}{2}$ S.       | $1\frac{1}{2}$ E. | 7. S.W. $\frac{1}{4}$ S.   | $1\frac{3}{4}$ W. | 13. S.S.W. $\frac{3}{4}$ W. | $2\frac{3}{4}$ E. |
| 3. S.W. $\frac{1}{4}$ W.       | $1\frac{3}{4}$ E. | 8. N.N.W. $\frac{3}{4}$ W. | $2\frac{1}{4}$ W. | 14. E.N.E.                  | $3\frac{1}{2}$ E. |
| 4. N.W. by W. $\frac{1}{4}$ W. | $1\frac{1}{4}$ E. | 9. E. $\frac{1}{2}$ N.     | 3 E.              | 15. E. $\frac{1}{2}$ S.     | $2\frac{1}{2}$ W. |
| 5. N.E. $\frac{1}{2}$ N.       | $1\frac{1}{2}$ W. | 10. N.W. by N.             | $3\frac{3}{4}$ E. | 16. W. by N.                | $2\frac{1}{2}$ W. |
|                                |                   | 11. S.W. $\frac{1}{2}$ S.  | $4\frac{1}{4}$ W. |                             |                   |

179. The learner may now proceed to correct the courses steered for the combined effect of leeway and variation, and in doing so we proceed by

## RULE LIV.

*When they are both to be applied in the same direction, take their sum and apply it in the same way; but when these corrections are to be applied in opposite*

*directions take their difference, and apply the remainder in the same direction as the greater correction is to be applied; the result in either case is the true course.*

### EXAMPLES.

Ex. 1. A ship sails N.E. by E.  $\frac{1}{4}$  E. on the port tack and makes  $1\frac{1}{2}$  points leeway, the variation is  $2\frac{1}{2}$  points East: required the true course.

|  |  |
|--|--|
| Here the ship's course being N.E. by E. $\frac{1}{4}$ E. is                | $5\frac{1}{4}$ points right of North.                                |
| The ship being on the port tack the leeway is applied to the right, and is | $1\frac{1}{2}$ points right of North.                                |
| The variation being East is applied to the right and hence is              | $2\frac{1}{2}$ points right of North.                                |
| <hr/>  |  |
| The names being alike we take the sum                                      | $9\frac{1}{4}$ points right of North.                                |
| This being greater than 8 points we take it from                           |  |
| 16 points  | 16   |
| <hr/>  |  |
| And we get true course   | $6\frac{3}{4}$ points left of South.<br>or E. by S. $\frac{1}{4}$ S. |

Ex. 2. Course by compass S.W. by S., the wind W. by N., leeway 2 points. Variation 3 points East.

|   |                          |
|---|--------------------------|
| Here the course steered being S.W. by S. is                                   | 3 points right of South. |
| The ship being on the starboard tack the leeway is applied to the left and is | 2 points left of South.  |
| <hr/>   |                          |
| The names being unlike the difference is taken                                | 1 point right of South.  |
| The variation being 2 points East is applied to right and is                  | 3 points right of South. |
| <hr/>   |                          |
| The names being alike the sum is taken and is                                 | 4 points right of South. |
| <hr/>   |                          |
| True course S.W.  |                          |

180. Sometimes it may be desirable to express the Variation in degrees, in which case we proceed as follows:—

### RULE LV.

1°. *Correct the compass course for leeway as before directed, and convert the number of points thus found in degrees, marking them R or L, according as they are right or left of N. or S.*

2°. *Underneath write the variation, marking it R or L, according as it is E. or W. Take the sum with the common name, if the names are alike, and the difference with the name of the greater, if the names are unlike. The result will be the number of degrees the true course is from N. or S. according as the course, as corrected for leeway, is reckoned from the N. or S.*

(a) *If, in taking the sum the number of degrees exceed  $90^\circ$  take the supplement to  $180^\circ$ , and reckon the true course from the opposite point to that from which the course corrected for leeway is reckoned; also change the letter R or L.*

## EXAMPLES.

| COMPASS COURSE.                                 | WINDS.                    | LEE-WAY.          | VAR.            | TRUE COURSE.                                  |
|---|---------------------------|-------------------|-----------------|---|
| S.W. $\frac{1}{2}$ S.                           | W. by N. $\frac{1}{2}$ N. | $\frac{3}{4}$     | $23^{\circ}$ W. | S. $8^{\circ}$ W.                             |
| N. by E.  | E. by N.                  | $3\frac{1}{4}$    | $20^{\circ}$ E. | N. $5^{\circ}$ W.                             |
| W. $\frac{3}{4}$ N.                             | S. W. by S.               | 1                 | $25^{\circ}$ W. | S. $85^{\circ}$ W.                            |
| S.W. $\frac{1}{2}$ S. = $3\frac{1}{2}$ R. of S. | N. by E. = 1 pt. R. of N. |                   |                 | W. $\frac{3}{4}$ N. = $7\frac{1}{4}$ L. of N. |
| Leeway $3\frac{1}{4}$ R. of S.                  | 1 R. of N.                | $3\frac{1}{4}$ L. |                 | $7\frac{1}{4}$ L. of N.                       |
| $2\frac{3}{4}$ R.                               | $2\frac{3}{4}$ L.         |                   |                 | 1 L.  |
| or $31^{\circ}$ R. of S.                        | or $25^{\circ}$ L. of N.  |                   |                 | $6\frac{1}{4}$                                |
| Var. $23$ L.                                    | $20$                      |                   |                 | or $70^{\circ}$ L.                            |
| $8$ R. of S.                                    | $5$ L. of E.              |                   |                 | $25$ L.                                       |
| S. $8^{\circ}$ W.                               | N. $5^{\circ}$ W.         |                   |                 | $180$   |
|   |                           |                   |                 | $95$ L. of N.                                 |
|   |                           |                   |                 | $85$ R. of S.                                 |
|   |                           |                   |                 | S. $85^{\circ}$ W.                            |

## RULE LVI.

181. To find the compass course, the true course and variation being given.  
 Easterly variation is allowed to the left.  
 Westerly                   "                   "                   right.

## EXAMPLES.

Taking the courses between North and South round by East.

Ex. 1. Let the true course be N.E. by E., where the variation is  $1\frac{1}{4}$  points west, the compass course (allowing westerly variation to the right) will be E.N.E.  $\frac{1}{4}$  E.

Ex. 3. Suppose the true course to be S.E. by E., where the variation is  $2\frac{1}{4}$  points easterly, the compass course (allowing variation to the right) will be S.S.E.  $\frac{3}{4}$  E.

Taking the courses between North and South round by West.

Ex. 5. Let the true course be N.W. by W., where the variation is  $2\frac{1}{2}$  points west, then the compass course (allowing westerly variation to the right) will be N.N.W.  $\frac{1}{2}$  W.

Ex. 7. With the true course West, and the variation 2 points west, then the compass course (allowing 2 points to the right) will be W.N.W.

Ex. 9. With the true course S.W.  $\frac{1}{2}$  S., where the variation is  $2\frac{1}{4}$  points west, then the compass course (allowing westerly variation to the right) will be S.W. by W.  $\frac{3}{4}$  W.

Ex. 2. Taking the same course, viz., N.E. by E., where the variation is  $1\frac{1}{4}$  points east, and then the compass course (allowing easterly variation to the left) will be N.E.  $\frac{1}{4}$  N.

Ex. 4. But the same course, viz., S.E. by S., where the variation is  $2\frac{3}{4}$  points easterly, will give the compass course (allowing easterly variation to the left) S.E. by E.  $\frac{3}{4}$  E.

Ex. 6. Suppose the course to be the same, viz., N.W. by W., where the variation is  $2\frac{1}{2}$  points easterly, the compass course (allowing easterly variation to the left) will be W.  $\frac{1}{2}$  N.

Ex. 8. Taking the same course West, suppose the variation to be 2 points east, then the compass course (allowing 2 points to the left) is W.S.W.

Ex. 10. But with the same course, viz., S.W.  $\frac{1}{2}$  S., where the variation is  $1\frac{1}{2}$  points east, the compass course (allowing easterly variation to the left) will be S.S.W.

182. Treating the points of the compass numerically, we proceed according to the following

## RULE LVII.

Proceed according to Rule LII, page 108, in every particular, except that the variation is to be allowed the opposite way to that of correcting compass courses, viz., WESTERLY variation is to be allowed to the right and marked R; and EASTERLY variation is to be allowed to the left and marked L.



EXAMPLES.

1. True Courses:—N.N.E.; S. by W.  $\frac{1}{2}$  W.; E. by N.  $\frac{1}{2}$  N.; W. by S. Var.  $2\frac{1}{2}$  W.

|                         |                           |                           |                           |
|-------------------------|---------------------------|---------------------------|---------------------------|
| N.N.E.                  | S. by W. $\frac{1}{2}$ W. | E. by N. $\frac{1}{2}$ N. | W. by S.                  |
| 2 R. of N.              | $1\frac{1}{2}$ R. of S.   | $6\frac{1}{2}$ R. of N.   | 7 R. of S.                |
| $2\frac{1}{2}$ R.       | $2\frac{1}{2}$ R.         | $2\frac{1}{2}$ R.         | $2\frac{1}{2}$ R.         |
| $4\frac{1}{2}$ R. of N. | 4 R. of S.                | 9 R. of N.                | $9\frac{1}{2}$ R. of S.   |
| N.E. $\frac{1}{2}$ E.   | S.W.                      | 16                        | 16                        |
|                         |                           | 7 L. of S.                | $6\frac{1}{2}$ L. of N.   |
|                         |                           | E. by S.                  | W. by N. $\frac{1}{2}$ N. |

2. True Courses:—N.E. by E.  $\frac{1}{4}$  E.; S.W. by W.; E. by S.  $\frac{1}{4}$  S.; N.W. by W. Variation  $3\frac{1}{4}$  E.

|                             |                           |                           |                         |
|-----------------------------|---------------------------|---------------------------|-------------------------|
| N.E. by E. $\frac{1}{4}$ E. | S.W. by W.                | E. by S. $\frac{1}{4}$ S. | N.W. by W.              |
| $5\frac{1}{4}$ R. of N.     | 5 R. of S.                | $6\frac{3}{4}$ L. of S.   | 5 L. of N.              |
| $3\frac{1}{4}$ L.           | $3\frac{1}{4}$ L.         | $3\frac{1}{4}$ L.         | $3\frac{1}{4}$ L.       |
| 2 R. of N.                  | $1\frac{3}{4}$ R. of S.   | 10 L. of S.               | $8\frac{1}{4}$ L. of N. |
| N.N.E.                      | S. by W. $\frac{3}{4}$ W. | 16                        | 16                      |
|                             |                           | 6 R. of N.                | $7\frac{3}{4}$ R. of S. |
|                             |                           | E.N.E.                    | W. $\frac{1}{4}$ S.     |

3. True Courses:—N. by W.  $\frac{1}{2}$  W. and S. by E.; Variation  $3\frac{1}{2}$  W. S. by W. and N. by E.; Variation  $3\frac{3}{4}$  E.

|                           |                         |                         |                         |
|---------------------------|-------------------------|-------------------------|-------------------------|
| N. by W. $\frac{1}{2}$ W. | S. by E.                | S. by W.                | N. by E.                |
| $1\frac{1}{2}$ L. of N.   | 1 L. of S.              | 1 R. of S.              | 1 R. of N.              |
| $3\frac{1}{4}$ R.         | $3\frac{1}{4}$ R.       | $3\frac{3}{4}$ L.       | $3\frac{3}{4}$ L.       |
| $1\frac{3}{4}$ R. of N.   | $2\frac{1}{4}$ R. of S. | $2\frac{3}{4}$ L. of S. | $2\frac{3}{4}$ L. of N. |
| N. by E. $\frac{3}{4}$ E. | S.S.W. $\frac{1}{4}$ W. | S.S.E. $\frac{3}{4}$ E. | N.N.W. $\frac{3}{4}$ W. |

183. To convert true course into compass course, we may proceed according to the following

RULE LVIII.

Westerly variation is + to all points between N. and E. ....S. and W.  
 Easterly variation is — from all points between N. and E. ....S. and W.  
 Westerly variation is — from all points between N. and W. ....S. and E.  
 Easterly variation is + to all points between N. and W. ....S. and E.

## DEVIATION OF THE COMPASS.

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184. The large quantity of iron now used in the construction and equipment of steamers, iron sailing vessels, and sometimes of wooden sailing vessels, produces a deviation from the magnetic north, which interferes seriously with the navigation of such vessels; and it is highly important that the officers of the Mercantile Marine should have a thorough acquaintance with the subject of *local attraction*, and with the correct method of applying to the different points of the compass, the "deviation," which is the effect of that attraction.

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### GENERAL STATEMENT OF FACTS AND LAWS OF MAGNETISM.

185. **Magnets, Natural and Artificial.**—Natural magnets, or *loadstones*, are exceedingly rare, although a closely allied ore of iron, capable of being strongly acted upon by magnetic forces, and hence called *magnetic-iron-ore*, is found in large quantities in Sweden and elsewhere. Artificial magnets are usually pieces of steel which have been permanently endowed with magnetism by the action of other magnets. The needle, or bar of steel, in the Mariner's compass is an artificial magnet.

186. **Poles, Neutral lines, and Axis.**—The property of attracting iron is very unequally manifested at different points of the surface of a magnet. If, for example, an ordinary bar-magnet be plunged in iron-filings, these become arranged round the ends of the bar in feathery tufts, which decrease towards the middle of the bar, where there are none. The name *poles* is used, in a somewhat loose sense, to denote the two terminal portions of a magnet, or to denote two points, not very accurately defined, situated in these portions. The middle portion to which these filings refuse to adhere is called the *neutral line*. Every magnet, whether natural or artificial, has two poles and a neutral line. The shortest line joining the two poles is termed the *axis* of the magnet.

187. **The Magnetic Equator or *acclinic line*** is the line which joins all those places of the earth where the needle remains quite horizontal, or where there is no dip. This line does not coincide with the geographical equator, nor is it a great circle, but a somewhat irregular curve crossing the geographical equator at two points almost exactly opposite each other, one near the west coast of Africa, in the Atlantic, and the other in the middle of the Pacific Ocean, and never receding from it further than  $12^{\circ}$ ; the position of the two being nearly coincident in that part of the Pacific where there are few islands, and most divergent when traversing the African and American continents.

188. **Magnetic Poles.**—At two points, or rather small linear spaces on the earth's surface, the needle assumes a position perpendicular to the horizon, or the dip is  $90^{\circ}$ . These two spots are called *Magnetic Poles*. At the north magnetic pole, the north pole of the needle dips; at the south magnetic

pole, the south pole of the needle dips. The terrestrial magnetic poles do not coincide with the geographical ones, nor are these points diametrically opposite. The position of these poles are latitude  $70^{\circ}$  N., long.  $97^{\circ}$  W., and lat.  $73\frac{1}{2}^{\circ}$  S., longitude  $147^{\circ}$  E.

The line of no variation passes through these poles, and the lines of equal variation converge towards them.

189. **Magnetic Needle.**—Any magnet freely suspended near its centre is usually called a *magnetic* needle, or more properly a *magnetised* needle. When a magnetised needle is so suspended or mounted that it can vibrate in the horizontal plane, it will take a definite direction, to which it always comes back after displacement. In this position of stable equilibrium, one of its ends points to the direction called magnetic north, and the other magnetic south, which differ, in general, by several degrees from geographical (or true) north and south. This is the principle on which compasses are constructed. The angle between the magnetic meridian and the geographical meridian is called the variation.

190. **Dip, or Inclination.**—When a needle is prepared in the unmagnetised state for mounting in a compass, with its centre of gravity very little below its point of support, and is adjusted to horizontality, on being magnetised it will place itself in a particular vertical plane called the magnetic meridian, and will take a particular direction in that plane. This direction is not horizontal except at the equatorial regions of the earth, but inclined generally at a considerable angle to the horizon; and this angle is called *dip*, or *inclination*. Its value at Greenwich, at present, is about  $67^{\circ}$ , the end which points to the north, pointing at the same time downwards.

In the northern hemisphere generally, it is the north end of the needle which dips, and in the southern hemisphere it is the end which points south.\*

191. **Mutual action of Poles.**—On presenting one end of a magnet to one end of a needle thus balanced, we obtain either repulsion or attraction, according as the pole which is presented is similar or dissimilar to that to which it is presented. *Poles of contrary names attract one another; poles of the same name repel one another.*

This property furnishes the means of distinguishing a body which is merely magnetic (that is, capable of temporary magnetization) from a permanent magnet. The former, a piece of soft iron, for example, is always attracted by either pole of a permanent magnet; while a body which has received permanent magnetization has, in ordinary cases, two poles, of which one is attracted where the other is repelled. Magnetic attractions and repulsions are exerted without modification through any body which may be interposed, provided it be not magnetic.

To help the seaman to understand the above remarks, let him proceed as follows:—Having provided a little unspun silk, by means of a bit of wax, or otherwise, attach the silk fibre to the magnetic needle by a single point at its middle. Place a magnet on the table, and hold the needle over the equator of the magnet. The needle sets horizontal. Move it towards the

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\* Dip first noticed by ROBERT NORMAN in 1576.

north end of the magnet, the south end of the needle dips, the dip augmenting as the north pole is approached, over which the needle, if free to move, will set itself exactly vertical. Move it back to the centre, it resumes horizontality; pass it towards the south pole, its north end now dips, and directly over the south pole the needle becomes vertical, its north end being now turned downwards. Thus we learn that on one side of the magnetic equator the north end of the needle dips; on the other side the south end dips, the dip varying from nothing to ninety degrees. If we go to the equatorial regions of the earth with a suitably suspended needle, we shall find the position of the needle horizontal. If we sail north, one end of the needle dips; if we sail south, the opposite end dips; and over the north or south terrestrial magnetic pole the needle sets vertical. In this manner we establish a complete parallelism between the action of the earth and that of an ordinary magnet.

The value of the dip, like that of the variation, differs in different localities. It is greatest in the polar regions, and decreases with the latitude to the equator, where it is approximately zero.

Dip, like the variation, varies greatly, not only from place to place, but also from time to time. In 1843 the dip at Greenwich was about  $69^{\circ} 1'$ , it has diminished, with a rate continually accelerating, till in 1868 it was  $67^{\circ} 56'$ . It is also subject to a slight annual and diurnal variations, being about  $15'$  greater in summer than in winter.

Intermediate to the poles and equator lines are drawn through all points where the needle makes the same angle with the horizon. These are called *Lines of Equal Inclination or Dip*.

192. The horizontal position of the needle and card is preserved by a sliding brass weight fitted for the purpose, or by dropping sealing wax on one end of the needle. This adjustment will often require to be repeated after a considerable change of place.

193. **Names of Poles.**—The phenomena of variation and dip above described evidently require us to regard the earth, in a broad sense, as a magnet, having one pole in the northern and the other in the southern hemisphere. Now, since poles which attract one another are dissimilar, it follows that the magnetic pole of the earth which is situated in the northern hemisphere is *dissimilar* to that end of a magnetised needle which points to the north. Hence, great confusion of nomenclature has arisen, the usage of the best writers being opposite to that which generally prevails. Popular usage in this country, however, calls that end or pole of a needle which points to the north the *north pole*, and that which points to the south the *south pole*.\*

\* Sir Wm. Thomson calls the north-seeking pole the *south pole*, and the other the *north pole*, because the former is similar to the south and the latter to the north pole of the earth. In like manner most French writers call the north-seeking pole of a needle the *austral*, and the other the *boreal* pole. Faraday, to avoid the ambiguity which has attached itself to the names north and south pole, calls the north-seeking end the *marked*, and the other the *unmarked* pole. Airy, for a similar reason, employs in his recent *Treatise on Magnetism*, the distinctive names *red* and *blue* to denote respectively the north-seeking and south-seeking ends, these names, as well those employed by Faraday, being purely conventional and founded on the custom of marking the north-seeking end of a magnet with a transverse notch or a spot of red paint. Maxwell and Jenkin in a report to the British Association call the south-seeking pole of a needle *positive*, and the north-seeking pole *negative*.

194. **Magnetic Induction.**—When a piece of iron is in contact with a magnet, or even when a magnet is simply brought near it, it becomes itself, for the time, a magnet with two poles and a neutral portion between them. If we scatter filings over the iron they will adhere to its ends, as shown (186). If we take away the influencing magnet the filings will fall off, and the iron will retain either no traces at all, or only very faint ones of its magnetization. If we apply similar treatment to a piece of steel, we obtain a result similar in some respects, but with very important differences in degree. The steel, while under the influence of the magnet, exhibits much weaker effects than the iron; it is much more difficult to magnetise than iron, and does not admit of being so powerfully magnetised; but, on the other hand, it retains its magnetization after the influencing magnet has been withdrawn. This property of retaining magnetism, when once imparted, has been named *coercive force*. Steel, especially, when very hard, possesses great coercive force; iron, especially, when very pure and soft, scarcely any.

In magnetization by influence, which is also called *magnetic induction*, it will be found on examination that the pole which is next the inducing pole is of contrary name to it; and it is on account of the mutual attraction of dissimilar poles that the iron is attracted by the magnet. The iron can in its turn support a second piece of iron, this again can support a third, and so on through many steps. A magnetic chain can thus be formed, having two poles. An action of this kind takes place in the clusters of filings which attach themselves to one end of a magnetised bar, these clusters being composed of numerous chains of filings.

195. **Magnetization by the action of the Earth.**—The action of the earth on magnetic substances resembles that of a huge permanent magnet, and hence the terrestrial magnetism will induce magnetism precisely as explained in 194. All soft or cast iron rods or bars, or other elongated forms of soft or cast iron, unless the position of their length is at a right-angle to the line of the direction of the earth's magnetic force, are immediately rendered magnetic by induction from the earth, and the nearer the iron is in direction to the line of force or dip the greater will be the amount of induction. When a bar of soft iron is held on the magnetic meridian and parallel to the dip, it becomes immediately endowed with feeble magnetic polarity. The lower extremity is a north pole, and if the north pole of a small magnetic needle be approached, it will be repelled. If the bar is held vertically the lower end will still be a north pole, but of less intensity; the upper end a south pole, also of less intensity. If the bar is held horizontally north and south, the north end will be a north pole, but of still lesser intensity; the south end a south pole, also of lesser intensity. If we now turn the bar in the same horizontal plane its magnetism will diminish, and if placed in an east and west direction, it will lose its polarity, and if we turn it still further until its position is reversed, the magnetic poles of the bar will be reversed.

While the bar is held with its length in the direction of the dip, if it be struck repeatedly with an iron hammer, it will be found, on removing it, to be a true magnet, the end which was lowest being charged with north magnetism, and this magnetism is not transient like the induced magnetism

of soft iron, changing its place in the bar with every change in the position of the bar, but is constant like that of a steel bar, retaining the same magnetism whatever be the position of the bar. By reversing the position of the bar and striking it a few blows with the hammer, its magnetism is reversed. The magnetism of the bar so struck resembles that of a steel magnet in all respects but this, that while, perhaps, no change can be remarked in hours or days, it infallibly diminishes in a long time. To express this partially permanent character, the term *Subpermanent Magnetism* has been adopted.

196. A sphere of soft iron will be magnetised in the same way, however held. The diameter in the line of dip will be the axis of magnetism, and the lower and north half of the surface will be north, the upper and south half south.

In bodies of any other shape the effects will be similar.

197. In the northern hemisphere all vertical or upright bars, such as stanchions and angle irons composing the frames of ships, are magnetised by induction, their lower ends being north poles, the upper ends south poles, the upper ends attracting the north pole of the needle held near them. On the other hand, in the southern hemisphere, these conditions are reversed; the upper ends of vertical iron are north poles, repelling the north pole of a compass needle and attracting the south pole. On the magnetic equator, where there is no dip, vertical soft iron has no polarity, because its position is at right angles to the earth's line of force or dip. It is different with horizontal pieces of soft iron; they exert the same influence on a compass needle in both hemispheres, and in all latitudes.

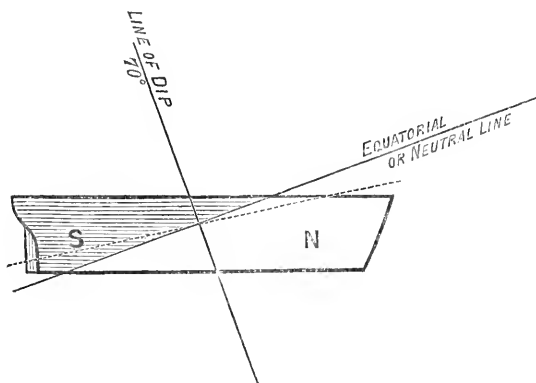
198. The hull of an iron ship acts as a permanent magnet on compasses placed outside the vessel as well as those placed inside; an iron ship must therefore be viewed in its effect on a properly placed magnet rather as one great magnet, than as an aggregation of smaller magnets.

Keeping in view that the inductive effect from the earth's magnetism is greatest in the line of the dip, and the existence of a neutral equatorial plane at right-angles to the line of dip in spherical bodies, we are prepared to see that each iron ship must have a distinct distribution of magnetism depending on the place of building, and the direction of the head and keel while building; the ship's polar axis and equatorial plane conforming more or less to the line of dip of the earth at the place where built, and a plane at right-angles to that line; abundant observation and experiment have proved this important general principle.

199. To illustrate this principle: let us suppose, as in the following figures 3, 4, 5, and 6, that four iron ships, or four composite built ships, with ribs, beams, stanchions, and deck girders of iron, are building on the cardinal points of the compass, in a port in England where the dip of the needle is  $70^\circ$ .

Fig. 3 shows the magnetic state of a ship built head North magnetic. The line marked Dip passes through the centre of the ship; it shows the direction of the line of the earth's magnetic force. The line marked Equatorial or Neutral line is the line of no deviation, and runs at right-angles to the Dip. The after body of the ship, or the portion which is shaded, has

Fig. 3. Head North while building.



S. (*blue*) polarity, and the fore body, or white portion in the figure, N. (*red*) polarity; the upper part of the stern would have the S. (*blue*) polarity developed in a high degree; the lower part of the bows would have the N. (*red*) polarity equally developed. At the stern the north end of a compass needle would be strongly attracted; at the bow the south end of the needle would be strongly attracted; while a compass placed outside of the ship's topsides, above the line of no deviation, the north end of the needle will be attracted; if it be placed below that line the north end of the needle will be repelled and the south end attracted, in accordance with the law of magnetism. (No. 191).

Fig. 4. Head South while building.

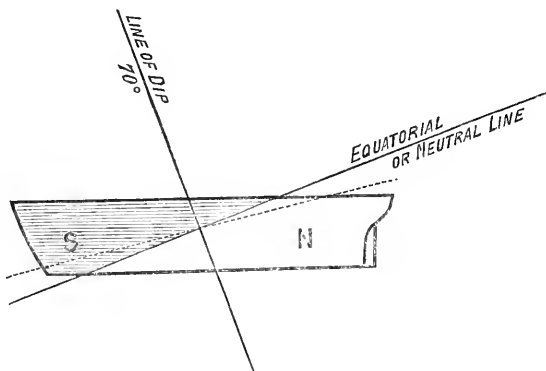


Fig. 4 represents the magnetic condition of a ship built head South. It will be seen by comparing fig. 4 with fig. 3 that the conditions are reversed; in fig. 3 the magnetism of the after body of the ship is south (*blue*), while in fig. 4 the after part of the ship possesses north (*red*) polarity; now the fore body of the ship has S. (*blue*) polarity, while in fig. 3 it has N. (*red*) polarity; the upper part of the bow has S. (*blue*) polarity developed in a high degree, and the lower part of the stern N. (*red*) polarity equalled developed. At the

stern the N. end of a needle would be repelled, and also attracted to the strong S. (*blue*) pole at the bow. The dotted line crossing the equatorial line in figs. 3 and 4 shows the probable position of the neutral line after the ship has been some time afloat, with her head in an opposite direction to that in which she was built, or after she has made a voyage.

Fig. 5. Head East while building.

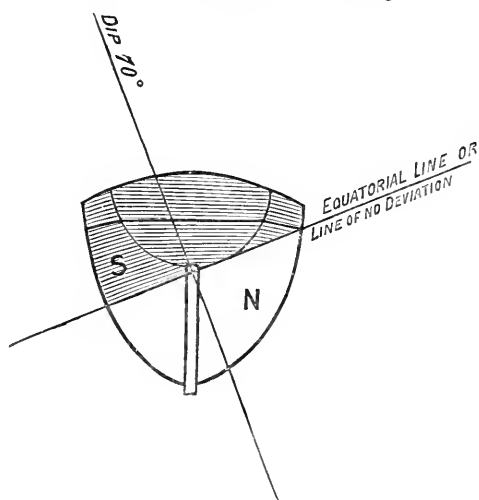
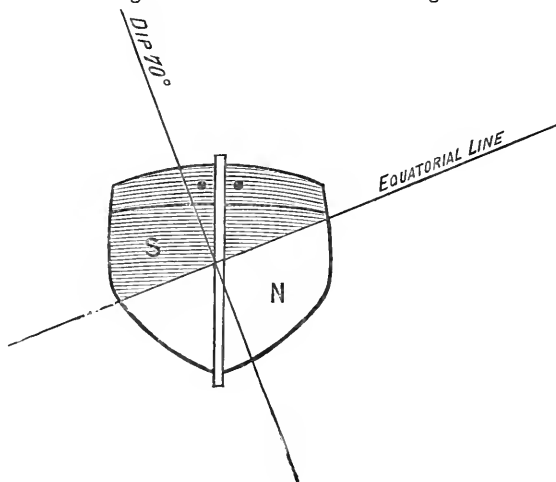


Fig. 5 is intended to show the magnetic state of a ship whose head has been east on the building slip. The whole of the upper part of the ship would have S. (*blue*) polarity; the whole of the lower part would have N. (*red*) polarity; but the magnetism of the starboard side of the upper works would be developed in higher degree than the port side, and the N. end of a compass needle, if carried at the usual height of a compass along the amidship line of the upper deck from end to end, would be attracted to the starboard side.

Fig. 6. Head West while building.





In fig. 6, ship built head west, the magnetic conditions of fig. 5, head east, are reversed; the whole of the upper part of the ship has still S. polarity, and the lower N. polarity; but the magnetism of the port side of the upper works is developed in a higher degree than the starboard side, and the N. end of a compass needle, if carried along the upper deck from end to end, would be attracted to the port side.\*

Fig. 7. Head North at Australia.

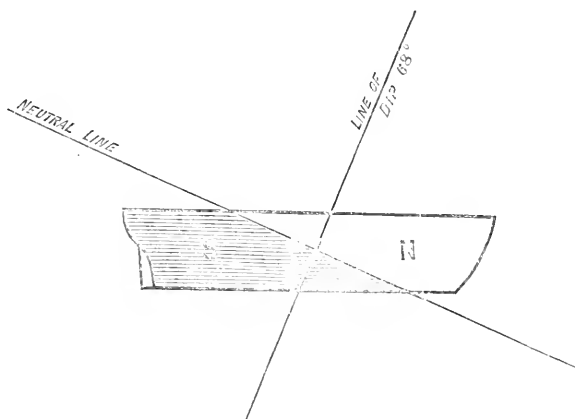


Fig. 7 represents an iron ship built head North in Australia, with a dip of about  $68^\circ$  South. In this ship the shaded part showing S. polarity lies below the equatorial line. It will be useful to compare this figure with figure 3, and mark the difference in the magnetic state of the two ships.

200. A little attention to the above diagrams will give the seaman a rough idea of the distribution of magnetism in iron ships; but it must be borne in mind that all large *detached* pieces of iron in a ship, such as iron masts, funnels, cylinders, and other masses of vertical iron are independent magnets; in north magnetic latitude, their lower ends being north poles, their upper ends south poles.

201. The compasses of composite ships with iron frames and iron deck beams, are affected in the same way as those of ships built wholly of iron.

\* From the special magnetic properties developed in a ship according to her position when building, it follows that a compass *ast*, in the usual place of the steering binnacle, the character of the deviation—though not the amount—may be approximately represented in a tabular form, as follows:—

| Approximate magnetic direction<br>of ship's head while building. | Approximate easterly deviation occurs<br>when ship's head by compass is near | Maximum westerly deviation<br>when ship's head by compass is near |
|--|--|---|
| N.   | W.   | E.  |
| N.E.   | N.W.   | S.E.  |
| E.   | N.   | S.  |
| S.E.   | N.E.   | S.W.  |
| S.   | E.   | W.  |
| S.W.   | S.E.   | N.W.  |
| W.   | S.   | N.  |
| N.W.   | S.W.   | N.E.  |

## DEVIATION OF THE COMPASS.

202. The deviation of the compass is the angle through which the magnetic needle is deflected from its natural position by the disturbing force of iron near it, that is, the angle included between the magnetic meridian and a plane passing through the poles of a compass needle.

The deviation is named East or West according as the north point of the compass so disturbed is to the east or west of its natural position.

Deviation consists of two principal parts, the Semicircular and the Quadrantal, following different laws, and requiring two different kinds of compensation; there is sometimes a third part of small amount called the Constant.

203. In the case of iron ships, as in that of iron bars (195), percussion and vibration by hammering in rivetting render the iron of which the vessel is constructed more susceptible to the inductive force of the earth, and causes the magnetism which the iron of the ship thus acquires to partake more of the character of permanent magnetism. Still this sub-permanent magnetism undergoes a considerable diminution by being submitted to percussion, with the ship's head in a different position to that in which it was when she was being built, and especially if in a contrary direction. But the iron of which a ship is constructed always retains a large amount of this sub-permanent magnetism as long as it remains in the form of a ship. The deviation arising from sub-permanent magnetism is greater than that which is the result of transient induced magnetism. The polarity of the ship's magnetism, while she remains on the stocks, takes the direction of the earth's line of force or dip, and its effects on compasses will evidently depend on the direction of the ship's head was whilst being built. Taking the case of a ship built head north (fig. 3, page 119), the fore part of the ship has acquired north magnetism, and its action will be precisely the same as that of the north pole of a magnet; hence, on northerly courses, the north end of the compass needle will be repelled, and the directive power of the needle will be diminished. On southerly courses the north end of the needle points towards the stern, which has acquired sub-permanent south magnetism, then the directive power of the needle is increased. On easterly and westerly courses the effects on the compass are greatest, since the force acts at right-angles to the needle; and on all intermediate positions of the ship's head the disturbances due to such positions are intermediate. As the ship's head is brought east of north, repulsion of the north end of the needle takes place, and westerly deviation is the result, and it reaches its maximum value when the fore-and-aft line of the ship is at right-angles to the needle; beyond that position the fore part of the ship attracts the south end of the needle, and westerly deviation is still the result. This attraction continues until the ship's head reaches south, when the line of action of the ship lies in the same direction as the needle, and no disturbance occurs, but the directive power of the needle is greater. On bringing the ship's head round west of south, the south pole of the needle still continues to be attracted, which causes easterly deviation, and it again attains its maximum when the fore-

and-aft line of the ship is at right-angles to the disturbed needle; this must occur to the north of west. After that point has been reached by the ship's head, the fore part of the ship repels the north end of the needle, easterly deviation still being the result until the ship's head is again at north. Thus we find that in an iron ship the disturbance of the compass is little or nothing when her head is on or near the points to which her head or stern were directed while building, and is greatest when the ship's head is directed to the points of the compass that were abeam while on the building slip; and, moreover, that easterly deviation is caused when the ship's head is in one half of the compass, and westerly deviation in the other. The deviation caused by sub-permanent magnetism, and the effects of magnetism induced in vertical iron, has received the name of *Semicircular Deviation*.

**Semicircular Deviation** is so called because it is easterly in one semicircle or half of the compass, and westerly in the other half, as the ship's head moves round a complete circle of azimuth. This error is caused by the sub-permanent magnetism acquired in building, and the magnetism induced in vertical iron. The part due to sub-permanent magnetism remains the same in kind, though different in amount, in all latitudes, unless the ship be subjected to strains or other mechanical violence. The part caused by the magnetism induced in vertical iron changes with a change of geographical position, or more correctly, as the dip changes, and is of contrary names on opposite sides of the magnetic equator, that is, if westerly deviation be produced on one side, easterly will be produced on the other. At the magnetic equator the earth's magnetism acts horizontally, and vertical soft iron will have no magnetism, and the semicircular deviation arising therefrom will disappear.

As a general rule the magnetism producing semicircular deviation, in a ship built in north magnetic latitude, attracts the north end of a compass needle to that part of a ship which was south from the compass while building; hence, the semicircular deviation in iron ships is generally represented by the effect of a magnet at the part of the ship which was south in building, with its south end towards the compass. Thus, in a ship built head north, the north end of the needle is drawn towards the stern. The following table will show the part of a ship towards which the north end of a needle is generally drawn, that is, the position of the permanent south pole developed in the process of construction.

| Ship's head while building | The north end of a compass needle on the<br>poop or quarter deck is usually drawn |  |
|----------------------------|---|--|
| North. . . . .             | towards the stern.  |  |
| N.E. . . . .               | „ starboard quarter.  |  |
| East . . . . .             | „ starboard side.   |  |
| S.E. . . . .               | „ starboard bow.  |  |
| South . . . . .            | „ bows or right ahead.  |  |
| S.W. . . . .               | „ port bow.   |  |
| West . . . . .             | „ port side.  |  |
| N.W. . . . .               | „ port quarter.   |  |

Fig. 8.  
Magnetic

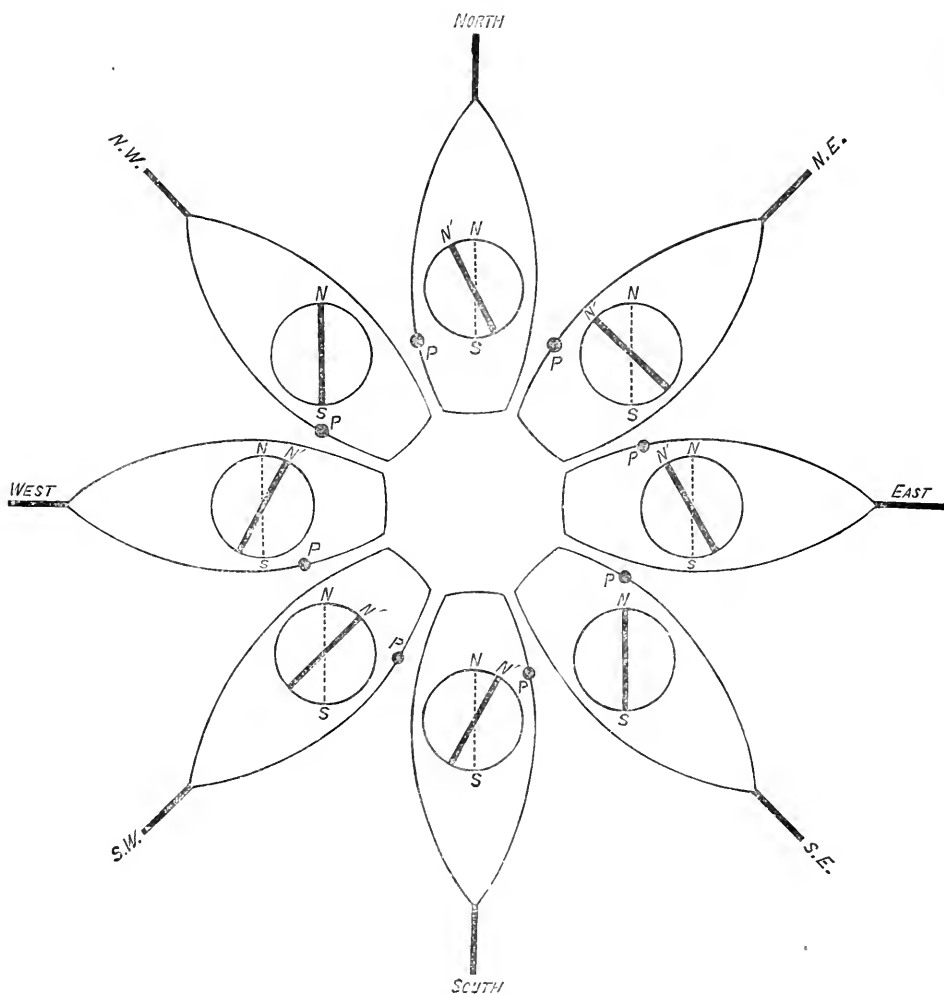


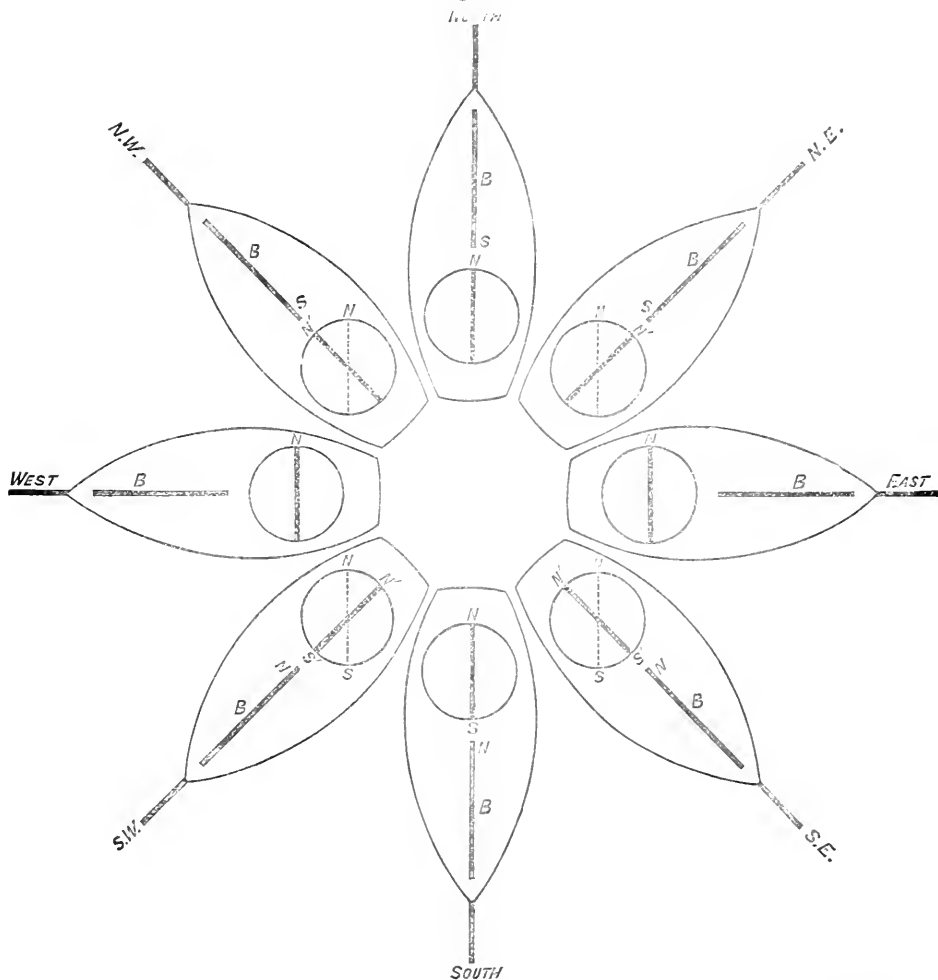
Figure 8 will further illustrate the way in which the permanent magnetism and the inductive magnetism of vertical iron acts upon the compass to produce semicircular deviation. Let it be supposed that the whole of the south polarity or attractive power of the above magnetism is concentrated in the point P on the port quarter of a ship built with her head near N.W. The ship is supposed to be swung round the compass, beginning at the N.W. point. The small circles represent the compass, the thick lines N'S the compass needle, the dotted lines the magnetic meridian or the direction of the needle when free from deviation. Beginning at N.W., and noting the position of the point P, it will be observed that there can be no semicircular deviation with ship's head in that direction, because the attractive force of the ship's

magnetism at the point P is in a line with a compass needle N S. As the ship's head swings round towards the west, the relative positions of the point P and the compass needle will alter, and P will exert a pulling force upon the north end of the needle, causing it to deviate to the right from N to N', shown in the figure at West. The easterly deviation will increase until the ship's head swings to S.W., where it attains its maximum or greatest amount. After passing S.W. it gradually decreases past South until the ship's head reaches S.E., the opposite direction to that in which her head was built, where it is again zero or nothing. The point P is now on the opposite side of the compass to what it was when her head was at N.W., but it will be observed that it is in a line with the needle, and can exert no deviating influence over it.

As the ship swings with her head towards the East, the needle will gradually be drawn to the left hand until the westerly deviation attains its maximum at N.E. After passing N.E. the westerly deviation will decrease past North until the ship's head again reaches N.W., at which point there is no deviation. A very slight inspection of the figure will show that in the semicircle from N.W. round by the West to S.E., the deviation is easterly; while in the semicircle, or half the compass, from S.E. round by the East, the deviation is westerly. The above is merely given for the sake of illustration, but it must be remembered that no two ships are alike in their influence on the compass, nor will the ship's magnetism have the same effect on two compasses placed on different parts of the deck.

204. **Quadrantal Deviation** is so named from its being easterly and westerly, alternately, in the four quadrants as the ship moves round a complete circle of azimuth. It is caused by the transient or inductive magnetism of horizontal soft iron, such as iron deck beams, the iron spindle of the wheel, &c. It is zero or nothing when a ship's head is near the North, South, East, or West points, and greatest on the quadrantal points. It is generally easterly in the N.E. and S.W. quadrants, and westerly in the N.W. and S.E. quadrants of the compass. Quadrantal deviation remains unchanged in all magnetic latitudes, and provided that the iron in the ship be of good quality, the quadrantal deviation will be little, if at all altered by lapse of time.

To illustrate the way in which horizontal soft iron produces Quadrantal deviation, let us suppose the whole of the induced magnetism in a ship to be represented by the soft iron bar B in figure 9. This cannot be so in actual practice, because the athwartship horizontal iron produces quadrantal deviation as well as the fore-and-aft iron, but we may suppose it may for the sake of clearness. The small circles represent the compass, the thick lines within the small circles the compass needle, the dotted lines within the compass the magnetic meridian. Beginning at north, it will be observed that the bar B is parallel with the magnetic meridian, and will therefore be an inductive magnet while it is in or near that position (195), its after end marked S being a south pole; but as the bar B is in a line with the compass needle N, it cannot exert any deviating power upon the needle, either to the right or left. As the ship's head swings towards the N.W., the relative positions of

Fig. 9.  
Magnetic.

the bar *B* and the needle *N* are altered, and the south end of the bar draws the north end of the needle to the left from *N* to *N'*. As the ship's head approaches the west, the bar *B* loses its polarity, and at west it is at right-angles to the magnetic meridian, and ceases to exert any influence on the compass. The ship's head now swings towards the S.W., and the bar *B*, as it turns towards the south pole, again becomes an inductive magnet; its after end being a *north pole*, and drawing the south end of the compass needle from *S* to *S'*. When the ship's head reaches south there is no quadrantal deviation, because the bar *B* is in a line with the compass needle. As her head swings towards the S.E., the needle is drawn from *S* to *S'*, causing westerly deviation. At east there is no deviation, for the same reason that there was none at west. After passing east, the after end of the bar *B* becomes a *south*

*pole*, and draws the north end of the needle to the right-hand in the N.E. quadrant. As the ship's head approaches the north, the quadrantal deviation gradually decreases until it becomes nothing at north. The reader will observe that the bar B in this case produces easterly deviation in the N.E. and S.W. quadrants, and westerly deviation in the N.W. and S.E. quadrants. Cases may arise where the deviation is westerly in the N.E. and S.W. quadrants, but they are very rare.

205. The constant part of the deviation is generally very small, and is the same for every point of the compass, it often arises from defects in the compass itself. An error in the correct magnetic bearing of a distant object used to ascertain the deviation, will give an *apparent* constant deviation: for example, if the correct magnetic bearing of a lighthouse be S.  $46^{\circ}$  E., and the observer assumes it to be S.  $44^{\circ}$  E., and finds the deviation by it, there will be an error of  $2^{\circ}$  in the deviation thus found on every point of the compass; or, in other words, the westerly deviation will be  $2^{\circ}$  less, and the easterly deviation will be  $2^{\circ}$  more than it ought to be. When a ship is swung hurriedly, and her head is not allowed to remain for a minute or two on any point before observations are made, there is a temporary constant deviation produced; and this temporary deviation is easterly when the ship is swung to the left, as from East to North, and is westerly when the ship is swung to the right, as from North to East.

**Mechanical Compensation or Correction of the Compass by means of Magnets and Soft iron.**—These adjustments were first proposed by Mr. Airy, the Astronomer Royal, and are now universal in the merchant service.

**Correction of the Semicircular Deviation.**—As this error is caused by sub-permanent magnetism and by magnetism induced in vertical iron, the same agents must be used to correct it properly, to hold good in all latitudes; but as it is impracticable to ascertain how much of it is due to the one, and how much to the other, it is customary to correct the whole of it by means of permanent magnets fixed on the deck, one before or abaft, and another at the side of the foot of the binnacle; but it must be remembered that this correction will only hold good for a small range of latitude, and while the ship's magnetism continues in the same state as when the correction was made.

The ship must be upright, or on an even beam, with all her *iron* stores on board, in the positions which they are intended to occupy while at sea.

The position of the binnacle being decided on, draw a line upon the deck, fore-and-aft, through the centre of the place where the binnacle is to stand.

Draw another line across the deck, at right-angles to the former, through the same centre.

Provide two or more powerful magnets from 18 inches to 2 feet in length.

Let the ship's head be swung to the north or south, *correct* magnetic—either of these points will do. When the ship's head is steady at one of these points, observe whether there is any deviation; if there is any, lay one of the magnets on or below the deck athwartship, with its centre exactly on the fore-and-aft line drawn on the deck at some distance from the binnacle; move it gradually (not hurriedly) to or from the foot of the binnacle until

the compass points correctly. The magnet may be placed either before or abaft the binnacle, whichever is most convenient, but its centre must always be over the fore-and-aft line drawn on the deck, and it must be kept at right angles to the ship's keel. If the compass needle deviate to the left, the north end of the magnet must be placed to the left, and conversely.

After the compass has been made to point correctly at either the north or south points, swing her head round to the east or west correct magnetic (either will do), and steady her head on one of these points.

If there be any deviation, place the other magnet fore-and-aft, either on the port or starboard side of the binnacle, with its centre on the athwartship line drawn on the deck; move it to or from the foot of the binnacle until the compass points correctly.

The adjuster should be careful to see that the centre of the magnet is kept on the fore-and-aft line, so that one of the poles of the magnet be no nearer the binnacle than the other.

**Correction of the Quadrantal Deviation.**—The semicircular deviation being corrected, and the binnacle being properly fitted with two small brass boxes, one on each side of and on a level with the compass; steady the ship's head on one of the quadrantal points N.E., S.E., S.W., or N.W.; if there is any deviation, fill one of the chain boxes with a quantity of small chain until the compass points correctly; if one chain box be not sufficient, fill the other. For greater certainty, swing the ship's head to each of the other quadrantal points. When this adjustment is once properly made, it ought to remain perfect at all times and in all latitudes.

Instead of the soft iron chain, the Liverpool Compass Committee prefer cast iron cylinders with hemispherical ends as correctors for the quadrantal deviation. These cylinders are of two sizes, one 9 inches long by 3 inches in diameter, the other 12 inches long by  $3\frac{1}{4}$  inches in diameter. The ship's head is to be steadied on one of the quadrantal points, and the correctors, one on each side of the compass, and on the same level as the needle, are to be moved to or from the compass until the quadrantal deviation is corrected. It is only in very *rare* instances that the correctors or chain-boxes are required to be placed on the fore-and-aft ends of the binnacle. The adjustment for the quadrantal deviation should always be made, as it tends to reduce the heeling error.\*

In some cases there is a small amount of quadrantal deviation produced by horizontal soft iron running from the quarters to the opposite bows, iron in this position produces a quadrantal deviation, which is greatest when the ship's head is at N., S., E., and W., and least with the ship's head at N.E., S.E., S.W., and N.W.; it is, however, generally of so small amount that it may, in ordinary cases, be disregarded.

**Heeling Error.**—Although a ship's compasses may be corrected by the above methods, they can only be depended upon so long as she remains

\* These correctors are too frequently absent; and it should be remembered that they very essentially improve the action of the compass—not only diminishing the deviation, but increasing the directive force.



upright. Besides the ordinary deviation of the compass there is a deviation caused by the heeling of iron ships, which may increase or decrease the deviation observed when the ship is upright. Cases have been observed in which the deviation from heeling has amounted to as much as two degrees for each degree of heel of the ship—that is, without altering the real direction of the ship's head, the apparent alteration in direction has amounted to  $40^\circ$  by heeling the ship from  $10^\circ$  to starboard to  $10^\circ$  to port. The effect is very serious in those parts where the wind is steady, and the ship inclined in the same direction for many days or weeks in succession.\*

210. **To ascertain the amount of heel.**—The instrument specially adapted to indicate the amount of heel is the *clinometer*. It consists of a brass semi-circle graduated, at the edge, to degrees, beginning at the middle of the arc and continued both ways; and to the centre a plumb line is attached. The instrument is fixed at right angles to a fore-and-aft section of the ship, as a beam, or athwartship bulkhead, with the diameter placed upwards and parallel to the deck. When the index points to O, the vessel is upright, but when she heels either way, the plumb line being free to move on its centre is always vertical, and the point at which it cuts the graduated edge shows the number of degrees that the vessel deviates from the perpendicular, that is, the heel of the ship. A compass card with the needle detached will answer the purpose, and an index may be made with a thread and plummet depending from the end.

211. **How the Deviation from Heeling is caused.**—The heeling error depends partly on vertical induction in transverse iron, and partly on vertical force arising from subpermanent magnetism in the ship, combined with that from vertical induction in vertical soft iron. The fore-and-aft iron is not disturbed from its horizontal position by heeling, consequently the athwartship beams then produce their full influence in disturbing the compass. When an iron ship heels over, forces, which before acted vertically, and did not disturb the horizontal compass needle, now act to one side and produce deviation; while transverse iron which was previously horizontal, becoming inclined, acquires magnetism by induction (195). In north magnetic latitude the upper or weather ends of athwartship beams, for example, become south poles, and the lower ends north poles; hence, from both these causes, the north end of the needle is drawn to windward. But, if the iron does not extend entirely across, as when a sky-light or hatchway is fitted, the opposite effects are produced; for then the end of the iron nearest the compass on the weather side is a north pole, and that nearest it on the lee side a south pole; and under these conditions the north end of needle is drawn to leeward.

In vertical iron the force acting on the needle is no longer directly under it, but is shifted to the weather side of the ship, and thus in north magnetic latitude, as a general rule, the tendency of both horizontal and

\* "Usually, in an iron ship, when her head is placed north or south, the ship's inclination through an angle of  $n$  degrees disturbs the compass through an angle of  $n$  degrees; but in some particular instances it has been known to disturb the compass as much as  $2n$  degrees. —*A Treatise on Navigation*, by G. B. Airy, M.A., LL.D., D.L., page 182.

vertical iron is to draw the north end of the needle to windward. The vertical action of subpermanent magnetism modifies the result of these causes, and may either cause an increase or a diminution of the error so produced. If a ship has acquired subpermanent magnetism by having been built with her head north, there is a strong vertical force acting *downwards* (see fig. 3, page 119) from the whole after body of the ship having south magnetism or polarity; this would conspire with the vertical induction in transverse iron, in attracting the north end of the needle to the weather side, as the ship heels over, and thereby increasing the change of deviation from other causes. On the other hand, if a ship be built with her head south, the vertical force acts *upwards* (see fig. 4, page 119), the after part of the ship has acquired north magnetism, or polarity, and the north end of the needle, as the ship heels over, is repelled by it to the lee side, the vertical force acting in antagonism, in this case, to the transverse force, thus decreasing the error caused by soft iron. Thus is shown why in England the deviation of ships built there, with their heads northerly, are most affected by heeling.

In the ordinary position of the compass on the quarter-deck, we may, in most cases, if we know the direction in which the ship's head was built, anticipate the direction of the heeling error, and form an approximate estimate of its amount. Ships built with their heads from about S.W. to S.E. by way of north, the upper parts have south polarity; and in those of this group built with their heads from N.W. to N.E., this south polarity is strongly developed near the position of the compass. In all these ships the north end of the compass needle will be drawn to windward, and forcibly so in the last named group. In the ships built with their heads from about S.W. to S.E. by way of south, their upper parts near the position of the compass have N. polarity, and hence the heeling error may be to leeward or to windward—and in either case small in amount—according as the vertical force, or force from transverse iron predominates.

**212. Position of ship's head for greatest and least change of deviation from heeling.**—There appears to be no deviation from heeling when the ship's head by compass is east or west, but it increases as the ship's head is moved from these points, and is greatest when the ship's head by compass is north or south. When the ship's head by compass is either east or west, the disturbing force, from the ship's heeling, acting at right angles to the fore-and-aft midship line, tends to bring the needle into the magnetic meridian, and consequently no change in deviation can be produced from heeling. On the other hand, when the ship's head by compass is either north or south, the disturbing force acts at right angles to the needle; hence the greatest change of deviation resulting from a vessel's heeling takes place when her fore-and-aft line is in the magnetic meridian.

**213.** In north latitude, in ships built with their heads to the north, with their compasses in the usual position, the deviation from heeling is much larger than in ships built with head to the south. In north latitude the north end of the needle is generally drawn towards the weather side of a ship, yet a small deviation to leeward has also been observed in north latitude, in some ships which were built in a southerly direction. In high south latitudes,

where the dip is south, the north end of the needle has been observed to deviate to leeward. Compasses which are least affected by heeling in the northern hemisphere have generally the greatest amount when south of the equator, and *vice versâ*.\*

214. **Effects of Heeling.**—The effect of the heeling error, when the north end of the needle is drawn to windward, is to throw a ship to windward of her supposed position when steering on northerly courses; and to throw her to leeward when steering on southerly courses. Therefore, to make a *straight* course, when heeling, a ship should be kept away by compass on either tack on northerly courses; and she should be luffed up on either tack on southerly courses. The effect in the few cases in which the compass needle is drawn to leeward is the reverse, and in the southern hemisphere, also, the reverse of these rules holds good; but this is a point which can only be ascertained for each ship.

The heeling error may be expressed in terms of the deviation when upright, and the following are the results:—

*On Northerly courses:—*

Starboard tack—E. dev. is increased, W. dev. is decreased.

Port tack—W. dev. is increased, E. dev. is decreased.

*On Southerly courses:—*

Starboard tack—West dev. is increased, E. dev. is decreased.

Port tack—W. dev. is decreased, E. dev. is increased.

And when the deviation when the ship is upright is small in amount and decreases by heeling, it may become reversed in name.

In the few cases in which the *North end of the compass needle is drawn to leeward*, the rule above is of course reversed.

215. **Correction of the Heeling Error.**—This correction is made by a vertical magnet placed in the binnacle immediately below the centre of the compass card. The ship's head is to be placed north and south, correct magnetic; she is then heeled over to port and to starboard, and the magnet raised or lowered until the compass points correctly. In most cases the north end of the vertical magnet should be uppermost.

The deviation arising from a ship heeling being semicircular, this correction holds good only while a ship continues near the magnetic latitude where the adjustment was made; hence, arrangements must be made for sliding the magnet along as different latitudes are reached, and for removing it, and even reversing it in high latitudes of opposite name.

216. After all the compensations have been accurately made, there will still remain small residual errors; for these the ship must be swung, and a table of deviations made for use. When an arrangement of magnets is employed to neutralise those large deviations occasionally found, and caused by the iron ship's magnetism, the compass so corrected can never be considered as entirely compensated, and the deviation must be expected to change on change of latitude, and from other causes. It will thus be seen that the seaman can have no absolutely safe guide, except in the system of actual and unceasing observation.

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\* This should be particularly considered by masters of iron ships about to proceed to a port south of the equator.

## METHODS OF FINDING THE AMOUNT OF THE DEVIATION.

217. When in port, there are two principal methods in general use for finding the deviation, viz:—Method I, by the known correct magnetic bearing of a distant object, and Method II, by reciprocal simultaneous bearings, *i.e.*, with a compass on board and a compass on shore.

218. METHOD I.—By the known bearing of a distant object.—The requisite warps being prepared, the ship is to be gradually swung round so as to bring her head successively upon each of the 32 points of the Standard Compass; and when the ship and the compass card are perfectly steady, and her head exactly on any one point, the direct bearing of some well-defined object is to be observed with the Standard Compass, and registered. The ship's head is to be gently warped round in the same manner to the next point, and when duly stopped and steadied there, the bearing of the same object is to be again set, and again recorded; and so on, point after point, till the exact bearing of the one object has been ascertained with the ship's head on every separate point of the compass.

219. The object selected for this purpose should be at such a distance that the diameter of the space through which the ship revolves shall make no sensible difference in its real bearing, and should not exceed the one-hundredth part of the distance of the object. The distance must depend on the range the ship takes when swinging; if she be at anchor, in a tide way, from 6 to 8 miles is not too much; brought up by the middle (in a dock) 2 miles will suffice.

220. The next step is to determine the *correct magnetic* bearing of the selected object from the ship; or in other words, the compass bearing it would have from on board if it were not disturbed by the attraction of the iron in the ship. This is effected by taking the compass to some place on shore (avoiding local influences) from which the part of the ship where the compass stood and the object of which the bearings had been observed shall be in one with the observer's eye, or else in the exactly opposite direction. The bearing of the object from that spot will evidently be the *correct magnetic* bearing from the ship by the compass. The difference between the *correct magnetic* bearing of the object and the successive bearings which were observed with the compass on board, when the ship's head was on the several points, will show the error of each of these points which was caused by the ship's iron; or, in other words, the Deviation of the Standard Compass according to the direction in which the ship's head was placed.

(b) The *correct magnetic* bearing of the distant object will be the mean value of all the observed bearings, if observed on equi-distant points; or of four or more compass bearings, if taken also, on equi-distant compass points.

221. II.—By reciprocal bearings.—Should there be no suitable object visible from the ship, and at the requisite distance as stated above, the deviations must be ascertained by the process of reciprocal bearings. A second compass is placed on shore where it will be entirely beyond the influence of iron of any description and where it can be distinctly

seen from the Standard Compass on board. Then take, simultaneously (known by pre-concerted signal), the bearing from each other of the compass on shore and the compass in the binnacle, as the ship is warped round so as to bring her head successively upon each of the thirty-two points of the Standard Compass on board, or on each alternate point.

To ensure the success of this operation, the compass on shore should not be more distant from the ship than is consistent with the most distinct visibility with the naked eye, of both compasses from each other. The observations should be made as strictly simultaneous as possible, the time at which each bearing is taken being noted both on shore and on board. It will be found convenient in practice, for the shore observer to chalk each observation on a black board, to be read at once from the ship, in order that the observation may be repeated if any apparent inconsistency presents itself.

Before this process is complete, the Standard Compass should be carried on shore, in order to be compared with the compass used there, by means of the bearing of some distant object, and the difference, if any, is to be recorded; and in all cases, when compasses are compared, the caps, pivots, &c., should be first carefully examined. The shore compass gives correct magnetic bearings.

The difference between the correct magnetic bearing of the standard compass as observed from the shore, and the bearing of the shore compass as observed from the ship, with her head in any particular point, reversed, *i.e.*, with  $180^\circ$  added or subtracted, will show the error on that point which was caused by the ship's iron; in other words the deviation of the standard compass according to the direction in which the ship's head was placed.

222. **III.—By Marks on the Dock Wall.**—This is a very convenient method where it can be practised. At Liverpool the correct magnetic bearings of the Vauxhall chimney, from various points of the dock walls, are painted in large figures on the walls, so that the bearing of the same chimney may be observed as the ship swings with the wind and tide; and at the same time that bearing marked on the wall, which is on a line between the Standard Compass and the chimney, is noted.

The difference between those bearings is the deviation for the point on which the ship's head is at the time.

In a similar manner, at Cronstadt, the correct magnetic bearings of a conspicuous point on a public building are painted on the mole.

223. If during the operation of swinging, a haze obscures the shore compass, while the sun at the time is shining brightly, a number of points may be secured by time-azimuths, which otherwise might be lost. Time-azimuths are also advantageous where the second of the above methods cannot be used for want of an assistant observer for the shore compass; and when the first of the above methods are not available owing to the length of the ship and the scope of the moorings, combined with the most distant objects in sight, not being sufficiently far off to render the difference of their bearings insensible as the ship swings round to the tide. In such cases *Godfray's*

*Azimuth Diagram*, as also Azimuth or Sun's True Bearing Tables, computed for intervals of four minutes, by Staff-Commander J. Burdwood, R.N., published by the Admiralty, will be found useful as superseding the calculation for the determination of the True Azimuth.

224. Commander Walker, R.N., has shown\* that the deviation may be ascertained with sufficient accuracy by selecting a distant object, as before, "and as the ship swings by wind or tide from one point to another, write down the compass bearings of the distant object opposite the direction of the ship's head. As the ship swings round there will be two nearly opposite points of the compass on which the bearings of the distant object agree, and this should be the correct magnetic bearing of the object." The deviation is then found as in the first method.

225. **The Dumb Card.**—The difficulty of finding the correct magnetic bearing of the ship's head may be obviated, however, by using the *dumb-card*, i.e., a compass-card without the needle, slung in gimbals, with its centre over a fore-and-aft line of the vessel, and as near to its middle as possible. The card is fitted with sight vanes, similar to an azimuth compass. Having obtained the correct magnetic bearing of a distant object, place the card so that it shall point out that direction, and screw the sight vanes to the card, so as to cut the object with the thread. Then, as the ship is swung, the card must still be kept pointing out the correct magnetic bearing of the object by means of the sight vanes, and where the fore-and-aft line meets the edge of the card, must then be the correct magnetic bearing of the ship's head.

226. **To name the Deviation.**—Rule.—*When the reading by the shore compass (reversed), or the correct magnetic bearing of the distant object, is to the right of the reading by the compass on board, the deviation is easterly; when to the left, westerly.*

Thus suppose the *correct* magnetic bearing from the shore compass, with ship's head at N.W., is N. 15° E., and the bearing of shore compass from the ship is S. 11° W.; to find deviation proceed thus:—

|   |             |
|---|-------------|
| Reverse of the bearing by shore compass | } S. 15° W. |
| or correct magnetic bearing .....       |             |
| Bearing from ship                       | S. 11° W.   |
| Deviation                               | 4 E.        |

When the ship's head lies N.N.E., let the binnacle compass bearing of the shore object or compass be N. 19° 30' E., and the bearing of the binnacle compass from the shore compass be S. 27° 0' W.: required the *deviation*.

The opposite point to S. 27° 0' W. is N. 27° 0' E., which is 7° 30' to the right of N. 19° 30' E. Hence the *deviation* is 7° 30' E.

227. The directions of the ship's head having been taken by the compass in the ship, are therefore affected by the local attraction, and the apparent compass bearing of the ship's head differs from the correct magnetic bearing by the amount of the local deviation due to the position of the ship. For

\* Magnetism of Ships and the Mariner's Compass.

instance, when the ship is apparently lying with her head east, it is not the true magnetic east, but supposing the local deviation to be one point easterly, the east point of the compass-card will be drawn to E. by S., and the true magnetic direction of the ship's head will be E. by S.

The observations and tabulated results are incomplete until the *correct magnetic bearing* of the ship's head at each observation is found.

228. The following shows the arrangement of tabular forms for finding the deviation by the several processes described.

### I. By bearing of a distant object.

Correct magnetic bearing of distant object from ship N.  $63^{\circ} 0' W.$ , distant 11 miles.

| Ship's Head<br>by the<br>Standard Compass. | Bearing of Distant<br>Object by the<br>Standard Compass. | Deviation<br>of<br>Standard Compass. |
|--|--|--------------------------------------|
| East .....                                 | N. $83^{\circ} 20' W.$                                   | $20^{\circ} 20' E.$                  |
| E. by S. ....                              | N. $82^{\circ} 15' W.$                                   | $19^{\circ} 15' E.$                  |
| E.S.E. ....                                | N. $81^{\circ} 5' W.$                                    | $18^{\circ} 5' E.$                   |
| S.E. by E. ....                            | N. $72^{\circ} 30' W.$                                   | $16^{\circ} 30' E.$                  |
| S.E. ....                                  | N. $77^{\circ} 40' W.$                                   | $14^{\circ} 40' E.$                  |

And similarly at all points of the compass.

### II. By reciprocal bearings.

| Time.*                              | Ship's Head<br>by the<br>Standard<br>Compass. | SIMULTANEOUS BEARINGS                 |                            | Deviation<br>of<br>Standard<br>Compass. |
|-------------------------------------|---|---------------------------------------|----------------------------|---|
|                                     |   | From Standard<br>Compass<br>on board. | From the shore<br>Compass. |   |
| 9 <sup>h</sup> 10 <sup>m</sup> A.M. | North ....                                    | S. $37^{\circ} 50' E.$                | N. $41^{\circ} 0' W.$      | $3^{\circ} 10' W.$                      |
| 9 14 "                              | N. by E. ...                                  | S. $45^{\circ} 0' E.$                 | N. $42^{\circ} 25' W.$     | $2^{\circ} 35' E.$                      |
| 9 17 "                              | N.N.E. ....                                   | S. $51^{\circ} 40' E.$                | N. $43^{\circ} 30' W.$     | $8^{\circ} 10' E.$                      |
| 9 21 "                              | N.E. by N..                                   | S. $57^{\circ} 20' E.$                | N. $44^{\circ} 10' W.$     | $13^{\circ} 10' E.$                     |
| 9 26 "                              | N.E. ....                                     | S. $61^{\circ} 50' E.$                | N. $45^{\circ} 0' W.$      | $16^{\circ} 50' E.$                     |
| 9 32 "                              | N.E. by E..                                   | S. $65^{\circ} 30' E.$                | N. $46^{\circ} 0' W.$      | $19^{\circ} 30' E.$                     |

And so on through all the points of the compass.

229. The seaman must remember that the corrections thus obtained belong to the compass by which the observations are made, and to that compass while it is in its proper place, and that these corrections will furnish no guide whatever to the effects of the iron on a compass placed in any other part of the ship; but if, while swinging, the direction of the ship's head by the other compasses is noted and tabulated, the deviation of all the compasses can be found.

\* The time—as taken by compared watches—may be omitted if the shore observations can be clearly made out by being chalked on a black board.

The following is a Table of Deviations to which reference is to be made in working the following examples.

TABLE OF DEVIATIONS.

| SHIP'S HEAD.   | DEVIATION. | SHIP'S HEAD.   | DEVIATION. |
|----------------|------------|----------------|------------|
| North . . . .  | 0 22' W.   | South . . . .  | 0 16' E.   |
| N. by E. . . . | 1 46 E.    | S. by W. . . . | 1 50 W.    |
| N.N.E. . . .   | 3 20 E.    | S.S.W. . . .   | 3 16 W.    |
| N.E. by N. . . | 5 14 E.    | S.W. by S. . . | 4 48 W.    |
| N.E. . . . .   | 7 14 E.    | S.W. . . . .   | 6 16 W.    |
| N.E. by E. . . | 8 54 E.    | S.W. by W. . . | 7 40 W.    |
| E.N.E. . . .   | 10 44 E.   | W.S.W. . . .   | 9 18 W.    |
| E. by N. . . . | 11 40 E.   | W. by S. . . . | 10 34 W.   |
| East. . . . .  | 10 44 E.   | West . . . .   | 11 50 W.   |
| E. by S. . . . | 9 54 E.    | W. by N. . . . | 11 10 W.   |
| E.S.E. . . .   | 9 8 E.     | W.N.W. . . .   | 10 16 W.   |
| S.E. by E. . . | 7 20 E.    | N.W. by W. . . | 9 18 W.    |
| S.E. . . . .   | 6 18 E.    | N.W. . . . .   | 7 52 W.    |
| S.E. by S. . . | 5 0 E.     | N.W. by N. . . | 6 18 W.    |
| S.S.E. . . .   | 3 24 E.    | N.N.W. . . .   | 5 2 W.     |
| S. by E. . . . | 1 42 E.    | N. by W. . . . | 3 10 W.    |

230. The purposes for which a Table of Deviations so formed are :—

1st.—To correct the course steered by the compass, in order that the correct magnetic course actually made good may be used in the calculation of the ship's reckoning, or to lay it down on the chart.

2nd.—If one or more bearings of the land are taken, to correct these bearings by the amount of deviation due to the direction of the ship's head at the time.

3rd.—If we wish to shape a course for a port, and having, either by calculation, or as taken from the chart, the correct magnetic course to be made good, so to apply the deviation as to obtain the compass course to be steered.

## RULE LIX.

To find the correct magnetic course, having given the compass course and deviation.

Express the compass course in degrees, &c.; look in the Table of Deviations for the deviation opposite the given course—then,

Easterly deviation allow to the right.

Westerly                   ,,                   left.

## EXAMPLES.

Correct the following compass courses for deviation, as given in Table above :—

$$\begin{array}{rcl}
 1. \text{ E.S.E.} & = & 6 \text{ points L. of S.} \\
 6 \text{ points L. of S.} & = & 67^{\circ} 30' \text{ L. of S.} \\
 \text{Deviation (Table)} & & 9 \quad 8 \text{ R.} \\
 \hline
 \text{Cor. mag. course} & & 58 \quad 22 \text{ L. of S.} \\
 \hline
 & & \text{or S. } 58 \quad 22 \text{ E.}
 \end{array}$$

In this instance the deviation being Easterly, allow to the right.

$$\begin{array}{rcl}
 2. \text{ N.N.W.} & = & 2 \text{ points L. of N.} \\
 2 \text{ points L. of N.} & = & 22^{\circ} 30' \text{ L. of N.} \\
 \text{Deviation (Table)} & & 5 \quad 2 \text{ L.} \\
 \hline
 \text{Cor. mag. course} & & 27 \quad 32 \text{ L. of N.} \\
 \hline
 & & \text{or N. } 27 \quad 32 \text{ W.}
 \end{array}$$

The deviation in this instance being Westerly, allow to the left.



|   |  |
|---|--|
| 3. S.W. = 4 points R. of S.<br>4 points R. of S. = $45^{\circ} 0'$ R. of S.<br>Deviation (Table) $\underline{6 \ 16}$ L.<br>Cor. mag. course $\underline{38 \ 44}$ R. of S.<br>or S. $38 \ 44$ W. | 4. W. = 8 points R. of S.<br>8 points R. of S. = $90^{\circ} 0'$ R. of S.<br>Deviation (Table) $\underline{11 \ 50}$ L.<br>Cor. mag. course $\underline{78 \ 10}$ R. of S.<br>or S. $78 \ 10$ W. |
|---|--|

|   |   |
|---|---|
| 5. W. $\frac{1}{4}$ N. = $7\frac{3}{4}$ pts. L. of N. = $87^{\circ} 11'$ L. of N.<br>Deviation = $\underline{11 \ 40}$ L.<br>$\underline{98 \ 51}$ L. of N.<br>$\underline{180 \ 0}$<br>Cor. mag. course $\underline{81 \ 9}$ R. of S.<br>or S. $81 \ 9$ W. | West = $11^{\circ} 50'$ W.<br>W. by N. = $\underline{11 \ 10}$ W.<br>$\underline{40 \ 40}$<br>Dev. for $\frac{1}{4}$ pt. = $\underline{0 \ 10}$<br>Dev. W. = $\underline{11 \ 50}$<br>Dev. for W. $\frac{1}{4}$ N. = $\underline{11 \ 40}$ W. |
|---|---|

|  |   |
|--|---|
| 6. N.W. by W. $\frac{3}{4}$ W. = $5\frac{3}{4}$ L. of N. = $61^{\circ} 41'$ L. of N.<br>Deviation = $\underline{10 \ 2}$ L.<br>$\underline{N. \ 71 \ 43}$ W. | N.W. by W. = $9^{\circ} 18'$ W.<br>W.N.W. = $\underline{10 \ 16}$ W.<br>Change for 1 pt. = $\underline{58}$<br>$\underline{4)58}$ |
|--|---|

The deviation (see Table) for N.W. by W. and W.N.W. is found, and the difference of these quantities is the correction for 1 point, which divided by 4 gives the correction for  $\frac{1}{4}$  point =  $0^{\circ} 14'$ . Now compass course is  $\frac{1}{4}$  point from W.N.W., therefore, apply correction  $0^{\circ} 14'$  to the deviation for W.N.W., the result is the deviation for N.W. by W.  $\frac{3}{4}$  W., and it is to be subtracted, because the deviation for N.W. by W. is less than for W.N.W.

|  |
|--|
| Change of dev. for $\frac{1}{4}$ pt. = $\underline{14}$<br>Dev. for W.N.W. = $\underline{10 \ 16}$<br>Dev. for N.W. by W. $\frac{3}{4}$ W. = $\underline{10 \ 2}$ W. |
|--|

|  |   |
|--|---|
| 7. N. $\frac{1}{2}$ E. = $\frac{1}{2}$ pt. R. of N. = $5^{\circ} 38'$ R. of N.<br>Deviation = $\underline{0 \ 42}$ R.<br>Correct magnetic course $\underline{6 \ 20}$ R. of N.<br>or N. $6^{\circ} 20'$ E. | Deviation at N. = $0^{\circ} 22'$ W.<br>N. by E. = $\underline{1 \ 46}$ E.<br>$\underline{2)1 \ 24}$<br>$\underline{0 \ 42}$ E. |
|--|---|

One deviation being W., and the other E., half the difference of the two is taken for the deviation.

|   |  |
|---|--|
| 8. N. $\frac{1}{2}$ W. = $\frac{1}{2}$ pt. L. of N. = $5^{\circ} 38'$ L. of N.<br>Deviation = $\underline{1 \ 46}$ L.<br>Correct magnetic course N. $\underline{7 \ 24}$ W. | Deviation at N. = $0^{\circ} 22'$ W.<br>N. by W. = $\underline{3 \ 10}$ W.<br>$\underline{2)3 \ 32}$ |
|---|--|

Half the sum of the deviations for N. and N. by W. is taken for deviation on N.  $\frac{1}{2}$  W.; both deviations being of the same name. Or proceed thus—take the deviations from Table for North and for N. by W.; take the difference and half it, apply this to the deviation for North, adding because the deviation is greater for N. by W. than for North.

|   |
|---|
| Dev. on $\frac{1}{2}$ pt. = $\underline{1 \ 46}$ W. |
|---|

### EXAMPLES FOR PRACTICE.

Correct the following courses steered for deviation, as given in the Table, page 136.

|                              |                              |                             |                               |
|------------------------------|------------------------------|-----------------------------|-------------------------------|
| 1. N.E. by N.                | 8. S.E. by E.                | 15. S.W. by S.              | 22. West                      |
| 2. North                     | 9. N. by E. $\frac{1}{2}$ E. | 16. S. $\frac{1}{2}$ E.     | 23. N.W. $\frac{1}{4}$ W.     |
| 3. N. by W. $\frac{1}{2}$ W. | 10. South                    | 17. W. $\frac{1}{2}$ S.     | 24. S. $\frac{1}{2}$ W.       |
| 4. S.W. $\frac{1}{2}$ W.     | 11. W. $\frac{1}{2}$ N.      | 18. N.N.E. $\frac{1}{2}$ E. | 25. W. by S. $\frac{1}{2}$ S. |
| 5. W. $\frac{1}{2}$ N.       | 12. S.E. $\frac{1}{4}$ S.    | 19. N. $\frac{1}{4}$ E.     | 26. E. $\frac{1}{2}$ S.       |
| 6. S.S.W. $\frac{1}{2}$ W.   | 13. E. $\frac{3}{4}$ N.      | 20. W. by N.                | 27. East                      |
| 7. E. by N.                  | 14. N.W. $\frac{1}{2}$ W.    | 21. S. by E.                | 28. W.N.W.                    |

231. Proceeding to correct the courses for the deviations given in Table I, a second Table, arranged like the following, may be made for all the points of the compass.

TABLE II.

| Courses steered by Compass. |    |              | Deviation. | Correct Magnetic Courses.                 |
|-----------------------------|----|--------------|------------|---|
| North .....                 | or | 0°           | 0° 22' W.  | N. 0° 22' W. or North.                    |
| N. by E. ....               | "  | N. 11 15' E. | 1 46 E.    | N. 13 1 E. " N. by E. $\frac{1}{8}$ E.    |
| N.N.E. ....                 | "  | N. 22 30 E.  | 3 20 E.    | N. 25 50 E. " N.N.E. $\frac{1}{4}$ E.     |
| N.E. by N. ..               | "  | N. 33 45 E.  | 5 14 E.    | N. 38 59 E. " N.E. $\frac{1}{2}$ N.       |
| N.E. ....                   | "  | N. 45 0 E.   | 7 14 E.    | N. 52 14 E. " N.E. $\frac{1}{2}$ E.       |
| N.E. by E. ....             | "  | N. 56 15 E.  | 8 54 E.    | N. 65 9 E. " N.E. by E. $\frac{3}{4}$ E.  |
| E.N.E. ....                 | "  | N. 67 30 E.  | 10 44 E.   | N. 78 14 E. " E. by N. nearly.            |
| E. by N. ....               | "  | N. 78 45 E.  | 11 40 E.   | S. 89 35 E. " East.                       |
| East. ....                  | "  | 90           | 10 44 E.   | S. 79 16 E. " E. by S.                    |
| E. by S. ....               | "  | S. 78 45 E.  | 9 54 E.    | S. 68 51 E. " E.S.E. $\frac{1}{8}$ E.     |
| E.S.E. ....                 | "  | S. 67 30 E.  | 9 8 E.     | S. 58 22 E. " S.E. by E. $\frac{1}{4}$ E. |
| S.E. by E. ....             | "  | S. 56 15 E.  | 7 20 E.    | S. 48 55 E. " S.E. $\frac{3}{8}$ E.       |
| S.E. ....                   | "  | S. 45 0 E.   | 6 18 E.    | S. 38 44 E. " S.E. $\frac{1}{2}$ S.       |
| S.E. by S. ....             | "  | S. 33 45 E.  | 5 0 E.     | S. 28 45 E. " S.S.E. $\frac{1}{2}$ E.     |
| S.S.E. ....                 | "  | S. 22 30 E.  | 3 24 E.    | S. 19 6 E. " S. by E. $\frac{3}{4}$ E.    |
| S. by E. ....               | "  | S. 11 15 E.  | 1 42 E.    | S. 9 33 E. " S. $\frac{7}{8}$ E.          |
| South .....                 | "  | 0            | 0 16 E.    | S. 0 16 W. " South.                       |
| S. by W. ....               | "  | S. 11 15 W.  | 1 50 W.    | S. 9 25 W. " S. $\frac{7}{8}$ W.          |
| S.S.W. ....                 | "  | S. 22 30 W.  | 3 16 W.    | S. 19 14 W. " S. by W. $\frac{3}{4}$ W.   |
| S.W. by S. ....             | "  | S. 33 45 W.  | 4 48 W.    | S. 28 57 W. " S.S.W. $\frac{1}{4}$ W.     |
| S.W. ....                   | "  | S. 45 0 W.   | 6 16 W.    | S. 38 44 W. " S.W. $\frac{1}{2}$ S.       |
| S.W. by W. ....             | "  | S. 56 15 W.  | 7 40 W.    | S. 48 35 W. " S.W. $\frac{3}{8}$ W.       |
| W.S.W. ....                 | "  | S. 67 30 W.  | 9 18 W.    | S. 58 12 W. " S.W. by W. $\frac{1}{2}$ W. |
| W. by S. ....               | "  | S. 78 45 W.  | 10 34 W.   | S. 68 11 W. " W.S.W. $\frac{1}{2}$ W.     |
| West .....                  | "  | 90           | 11 50 W.   | S. 78 10 W. " W. by S.                    |
| W. by N. ....               | "  | N. 78 45 W.  | 11 10 W.   | N. 89 55 W. " West.                       |
| W.N.W. ....                 | "  | N. 67 30 W.  | 10 16 W.   | N. 77 46 W. " W.N.W. $\frac{7}{8}$ W.     |
| N.W. by W. ....             | "  | N. 56 15 W.  | 9 18 W.    | N. 65 33 W. " N.W. by W. $\frac{3}{4}$ W. |
| N.W. ....                   | "  | N. 45 0 W.   | 7 52 W.    | N. 52 52 W. " N.W. $\frac{3}{8}$ W.       |
| N.W. by N. ....             | "  | N. 33 45 W.  | 6 18 W.    | N. 40 3 W. " N.W. by N. $\frac{5}{8}$ W.  |
| N.N.W. ....                 | "  | N. 22 30 W.  | 5 2 W.     | N. 27 32 W. " N.N.W. $\frac{1}{2}$ W.     |
| N. by W. ....               | "  | N. 11 15 W.  | 3 10 W.    | N. 14 25 W. " N. by W. $\frac{1}{4}$ W.   |

To obtain from the Table above the correct magnetic course of the ship from the course shown by the Standard Compass, look in the 1st column of the Table for the latter; the 2nd column gives the deviation when her head is on that point; and in the 3rd column (the deviation having been applied as directed in Rule LIX) the seaman will find the correct magnetic course given there, by inspection.

This Table will be found more useful than the common table of deviations, as it shortens the calculation, when it is required to fractions of a point, as a half, a quarter, &c., and when steering upon a whole point, the *correct* magnetic course is known at sight.

The following examples will show the use of the Table.

#### EXAMPLES.

Ex. 1. The ship's head by Standard Compass is N.E.  $\frac{1}{4}$  E.: what is the correct magnetic course? (using the table above).

Corr. mag. course for N.E. = N. 52° 14' E.

" " N.E. by E. = N. 65 9 E.

$$2) 117 \ 23$$

Corr. mag. co. for N.E.  $\frac{1}{4}$  E. = N. 58 41 E.

Here the courses taken from the Table are of the same name, therefore, half the sum is evidently the correct magnetic course corresponding to N.E.  $\frac{1}{4}$  E.

Ex. 2. Find correct magnetic course when Standard Compass course is N.  $\frac{1}{2}$  E. (using the above Table).

Corr. mag. course for North = 0° 22' W.

" " N. by E. = 13 1 E.

$$2) 12 \ 39$$

Corr. mag. course for N.  $\frac{1}{2}$  E. = 6 19 E.

Here the courses corresponding to North and N. by E. are of *contrary* names; hence, for a Standard Compass course, midway between N. and N. by E., we use half the difference of the *correct* magnetic courses corresponding to these points.

Ex. 3. Ship's head by Standard Compass is  $N. \frac{1}{4} E.$ ; find, by means of the Table, the corresponding correct magnetic course.

$$\begin{array}{rcl} \text{Corr. mag. course for North} & = & 0^{\circ} 22' W. \\ \text{" " " } N. \frac{1}{4} E. & = & 13 \quad 1 E. \\ & & \hline & & 4) 13 \quad 23 \end{array}$$

$$\begin{array}{rcl} \text{Difference for } \frac{1}{4} \text{ point} & = & 3 \quad 21 \\ \text{Corr. mag. course for North} & = & 0 \quad 22 W. \end{array}$$

$$\text{Corr. mag. course for } N. \frac{1}{4} E. = 2 \quad 59 E.$$

Ex. 4. Required the correct magnetic course when ship's head by Standard Compass is  $W. \frac{3}{4} N.$

$$\begin{array}{rcl} \text{Corr. mag. course for West} & = & S. 78^{\circ} 10' W. \\ & & \text{W. by N. } \left. \begin{array}{l} \text{is } N. 89^{\circ} 55' W. \text{ or } S. 90^{\circ} 5' W. \end{array} \right\} S. 90 \quad 5 W. \\ & & \hline & & 11 \quad 55 \\ & & 3 \\ & & \hline & & 4) 35 \quad 45 \end{array}$$

$$\begin{array}{rcl} \text{Difference for } \frac{3}{4} \text{ point} & + & 8 \quad 56 \\ \text{Corr. mag. course for West} & = & S. 78 \quad 10 W. \end{array}$$

$$\text{Corr. mag. course for } W. \frac{3}{4} N. = S. 87 \quad 6 W.$$

**232. Correction of Compass Bearings.**—In order to correct the bearing of the object as taken by the Standard Compass, note the direction of the ship's head by that compass while taking the observation, then enter the first column of either Table I or II with that, and in the second column will be found the deviation to be applied to the bearing of the object. (See 144-146, page 90). Easterly deviation to be allowed to the right and westerly to the left, as in Rule LIX.

**CAUTION.**—Be careful to remember that the deviation to be applied is that due to the compass course, *not that on the point of bearing*; and the consequence of a misapplication of the deviation, by applying that for the point of bearing instead of the deviation for the compass course may lead into danger, if not loss.

#### EXAMPLES.

Ex. 1. The bearing by Standard Compass of the South Foreland is  $N.N.W.$ , the course by the same is  $E.N.E.$ : required the correct magnetic bearing.

Taking out the deviation from the Table for the direction the ship's head was on at the moment the bearing was taken, we have

$$\begin{array}{rcl} \text{Bearing by Standard Compass of South Foreland} & N. 22^{\circ} 30' W. \text{ or } 22^{\circ} 30' L. \text{ of } N. \\ \text{Deviation by Table for } E.N.E. \text{ (applied to } right) & 10 \quad 44 E. \quad \text{" } 10 \quad 44 R. \\ & \hline \text{Correct magnetic bearing} & 11 \quad 46 W. \quad \text{" } 11 \quad 46 L. \text{ of } N. \\ & \text{or } N. 46^{\circ} 11' W. \end{array}$$

Ex. 2. Ship's head  $E.S.E.$  by compass, the bearing by the same compass of the Start Point is  $N. 20^{\circ} W.$ : required the correct magnetic bearing.

$$\begin{array}{rcl} \text{Bearing of Start Point by Standard Compass} & N. 20^{\circ} W. \text{ or } 20^{\circ} L. \text{ of } N. \\ \text{Deviation by Table (applied to the } left) & 14 W. \quad \text{" } 14 L. \\ & \hline \text{Correct magnetic bearing} & N. 34 W. \quad \text{" } 34 L. \text{ of } N. \\ & \text{or } N. 34^{\circ} W. \end{array}$$

Ex. 3. Two islands bear  $S.E.$  and  $W.S.W.$ ; the ship's head is  $N.E.$ : required the correct magnetic bearing of each.

$$\begin{array}{rcl} \text{Bearing by Standard Compass } S.E. & = & S. 45^{\circ} E. \text{ or } 45^{\circ} L. \text{ of } S. \\ \text{Deviation by Table (applied to the } right) & = & 7 E. \quad \text{" } 7 R. \\ & \hline \text{Correct magnetic bearing} & = & S. 38 E. \quad \text{" } 38 L. \text{ of } S. \\ & & \text{or } S. 38^{\circ} E. \end{array}$$

$$\begin{array}{rcl} \text{Bearing by Standard Compass } W.S.W. & = & S. 67^{\circ} 30' W. \text{ or } 67^{\circ} 30' R. \text{ of } S. \\ \text{Deviation by Table (applied to the } right) & = & 7 \quad 14 E. \quad \text{" } 7 \quad 14 R. \\ & \hline \text{Correct magnetic bearing} & = & S. 77 \quad 44 W. \quad \text{" } 77 \quad 44 R. \text{ of } S. \\ & & \text{or } S. 75^{\circ} W. \end{array}$$

## EXAMPLES FOR PRACTICE.

In the following examples the ship's compass course and the bearing of the object by compass are both given, and it is required to find the magnetic bearings of the objects, using the same deviation table (Table of Deviations, page 136).

| No. | Ship's Head<br>by Compass.     | Compass Bearing.          | No. | Ship's Head<br>by Compass. | Compass Bearing.          |
|-----|--------------------------------|---------------------------|-----|----------------------------|---------------------------|
| 1   | West.....                      | East.                     | 7   | E. $\frac{3}{4}$ N. ....   | N. $\frac{1}{4}$ W.       |
| 2   | S.S.S. $\frac{1}{2}$ E. ....   | E. by S. $\frac{1}{4}$ S. | 8   | N.E. $\frac{1}{4}$ E. .... | W. $\frac{3}{4}$ S.       |
| 3   | N.E. by N. ....                | North.                    | 9   | E. $\frac{3}{4}$ S. ....   | W. by S. $\frac{1}{4}$ S. |
| 4   | W.N.W. ....                    | South.                    | 10  | N. $\frac{1}{4}$ E. ....   | S. $\frac{1}{4}$ E.       |
| 5   | W. by N. $\frac{1}{2}$ N. .... | E. $\frac{1}{2}$ S.       | 11  | S. $\frac{1}{4}$ E. ....   | W. by N. $\frac{1}{2}$ N. |
| 6   | S. by W. $\frac{1}{4}$ W. .... | S. by W. $\frac{1}{4}$ W. | 12  | E. $\frac{1}{4}$ N. ....   | N. by W. $\frac{1}{4}$ W. |

233. Given a correct magnetic course by the chart between two points of land, to find the course that must be steered by compass.

## RULE LX.

Easterly deviation is allowed to the left.

Westerly                    „                    „                    right

taking care that the deviation applied is that of the *correct* magnetic course.

NOTE.—In this case it is important to remember, not only is the general rule of applying the deviation *reversed*, but the correction to be applied is the deviation due to the given magnetic course, not that due to a compass course, as in Rule LIX; that is, to the correct magnetic course as found from the chart, or by calculation; the deviation, as due to that course, must be applied as directed above, in order to find the course to be *steered* by compass approximately. It will be observed that on those courses near which the deviation is considerable, and rapidly changing, the deviation on a given magnetic course is considerably different from that on the compass course of the same name. In such cases it will be necessary to again enter the table with the *approximate* course and get the corresponding deviation and *apply it* to the correct magnetic course; the result will be the compass course to be steered to make good the given correct magnetic course.

## EXAMPLE.

Ex. 1. Required the Compass Course that shall make correct magnetic W. by S.

Entering the first column of Table I, or II, with W. by S. the deviation on that point is found to be  $10\frac{1}{2}^{\circ}$  W., which allowed to the *right* would be about West; and since the deviation for this last does not differ from the deviation used, it may be considered that to make correct magnetic W. by S. the course to be steered is about West.

234. By comparing the first and third columns of this Table II, the seaman may also by inspection, or a single interpolation, determine what course he will have to steer by the Standard Compass, in order to take up any given correct magnetic course. For example, let the given correct magnetic course be N.E., or N.  $45^{\circ}$  E.; on referring to column 3, it will be found that N.  $45^{\circ}$  E. lies nearly midway between N.  $38^{\circ} 59'$  E. and N.  $52^{\circ} 14'$  E., the

Standard Compass courses corresponding to which are N.E. by N. and N.E.; the course to be steered is consequently N.E.  $\frac{1}{2}$  N. If great accuracy be required, it will be necessary to find the exact proportion between the actual changes of the ship's head with reference to the horizon; referring to the same example he will find that the ship's head by Standard Compass between N.E. by N. and N.E., the actual angular change is  $13^{\circ} 15'$  represented by  $11^{\circ} 15'$  of the compass; in shaping a course therefore, between these points, the value of the half point is about  $6^{\circ} 37'$ , the quarter is  $3^{\circ} 18'$  and similarly for smaller divisions of the rhumb.

To prevent, however, the possibility of error in such an important operation as that of shaping a course, a separate Table, may be advantageously constructed expressly for that object. See Table III, where the desired course being sought in the first column is immediately followed by the course to be steered by the Standard Compass, and given in degrees and minutes, as well as points and fractional parts.

TABLE III.

| Correct Magnetic Course<br>proposed to be steered. | Course that must be steered by the<br>Standard Compass in order to make the<br>Correct Magnetic Course. |                               |
|--|---|-------------------------------|
| North .....  | North   | or nearly North.              |
| N. by E. ....                                      | N. $10^{\circ}$ E.  | " N. $\frac{1}{8}$ E.         |
| N.N.E. ....  | N. $19^{\circ}$ E.  | " N. by E. $\frac{3}{4}$ E.   |
| N.E. by N. ....                                    | N. $29^{\circ}$ E.  | " N.N.E. $\frac{5}{8}$ E.     |
| N.E. ....  | N. $38\frac{1}{2}^{\circ}$ E.   | " N.E. $\frac{1}{2}$ N.       |
| N.E. by E. ....                                    | N. $48\frac{1}{2}^{\circ}$ E.   | " N.E. $\frac{1}{4}$ E.       |
| E.N.E. ....  | N. $59^{\circ}$ E.  | " N.E. by E. $\frac{1}{4}$ E. |
| E. by N. ....                                      | N. $68^{\circ}$ E.  | " E.N.E.                      |
| East .....   | N. $79^{\circ}$ E.  | " E. by N.                    |
| E. by S. ....                                      | East  | " East.                       |
| E.S.E. ....  | S. $78^{\circ}$ E.  | " E. by S.                    |
| S.E. by E. ....                                    | S. $65^{\circ}$ E.  | " S.E. by E. $\frac{3}{4}$ E. |
| S.E. ....  | S. $52\frac{1}{2}^{\circ}$ E.   | " S.E. $\frac{3}{4}$ E.       |
| S.E. by S. ....                                    | S. $39\frac{1}{2}^{\circ}$ E.   | " S.E. $\frac{1}{2}$ S.       |
| S.S.E. ....  | S. $26\frac{1}{2}^{\circ}$ E.   | " S.S.E. $\frac{3}{8}$ E.     |
| S. by E. ....                                      | S. $13^{\circ}$ E.  | " S. by E. $\frac{1}{8}$ E.   |
| South .....  | South   | " South.                      |
| S. by W. ....                                      | S. $12\frac{1}{2}^{\circ}$ W.   | " S. by W. $\frac{1}{8}$ W.   |
| S.S.W. ....  | S. $25\frac{1}{2}^{\circ}$ W.   | " S.S.W. $\frac{1}{4}$ W.     |
| S.W. by S. ....                                    | S. $39^{\circ}$ W.  | " S.W. $\frac{1}{2}$ S.       |
| S.W. ....  | S. $52\frac{1}{2}^{\circ}$ W.   | " S.W. $\frac{1}{2}$ W.       |
| S.W. by W. ....                                    | S. $65\frac{1}{2}^{\circ}$ W.   | " S.W. by W. $\frac{3}{4}$ W. |
| W.S.W. ....  | S. $78^{\circ}$ W.  | " W. by S. $\frac{1}{4}$ S.   |
| W. by S. ....                                      | N. $89^{\circ}$ W.  | " West.                       |
| West .....   | N. $78\frac{1}{2}^{\circ}$ W.   | " W. by N.                    |
| W. by N. ....                                      | N. $68^{\circ}$ W.  | " W. by N. $\frac{3}{8}$ N.   |
| W.N.W. ....  | N. $58^{\circ}$ W.  | " N.W. by W. $\frac{1}{4}$ W. |
| N.W. by W. ....                                    | N. $48^{\circ}$ W.  | " N.W. $\frac{3}{8}$ W.       |
| N.W. ....  | N. $38^{\circ}$ W.  | " N.W. $\frac{1}{2}$ N.       |
| N.W. by N. ....                                    | N. $28^{\circ}$ W.  | " N.N.W. $\frac{1}{2}$ W.     |
| N.N.W. ....  | N. $18^{\circ}$ W.  | " N. by W. $\frac{3}{4}$ W.   |
| N. by W. ....                                      | N. $8\frac{1}{2}^{\circ}$ W.  | " N. $\frac{3}{4}$ W.         |
| North .....  | North   | " North.                      |

235. The following Examples are designed to show the method of correcting courses for leeway, variation, and deviation.

# EXAMPLES.

Ex. 1. Course steered E.N.E., wind S.E.; leeway  $2\frac{1}{2}$  points; variation  $1\frac{1}{4}$  W.; and the deviation  $2\frac{3}{4}$  points E.; required the true course.

Here the course by compass is E.N.E. or ..... 6 points right of North.  
The variation and deviation are of *contrary* names,  
their difference, viz. ( $2\frac{3}{4}$  E. —  $1\frac{1}{4}$  W. =  $1\frac{1}{2}$  E.)  
is  $1\frac{1}{2}$  E. and ..... +  $1\frac{1}{2}$  points right of North.

Therefore the sum is the course corrected for  
variation and deviation and is .....  $7\frac{1}{2}$  points right of North.

The ship being on the starboard tack the leeway is  
applied to the left, and hence is ..... —  $2\frac{1}{2}$  left.

Difference 5 points right of North.

True course N.E. by E.

Ex. 2. Course by compass N.N.W.; wind N.E.; leeway  $2\frac{1}{2}$  points; variation  $45^\circ$  W.; deviation  $16^\circ 52'$  E.: find the true course.

Here the ship's course is N.N.W. .... 2 points left of North.  
The ship being on the starboard tack the leeway is  
applied to the left, and hence is .....  $2\frac{1}{2}$  „ left.

Therefore the sum is the course corrected for leeway  
.....  $4\frac{1}{2}$  „ left.

Which expressed in degrees, &c., is .....  $50^\circ 38'$  left of North.

The variation and deviation are of *contrary* names,  
their difference, viz., ( $45^\circ$  W. —  $16^\circ 52'$  E.)  
 $28^\circ 8'$  W., is ..... 28 8 left.

Sum 78 46 left of North.

True Course N.  $78^\circ 46'$  W., or W. by N.

In this example the compass course and leeway are given in points, we therefore take the course and allow the leeway from the wind, which gives the course corrected for leeway, viz.,  $4\frac{1}{2}$  points left of North, which expressed in degrees, &c., is  $50^\circ 38'$  L. of N.; then the difference of the variation and deviation is taken as they are of *contrary* names, the remainder—which takes the name of the *greater*—is then applied, the result is the true course. We may, however, if we prefer so to do, express all the quantities in degrees, and the work will then stand as in the following example.

Ex. 3. Course by compass W. by S.; variation  $3\frac{1}{4}$  E.; deviation  $13^\circ 50'$  W.; wind S. by W.; leeway  $1\frac{3}{4}$  points: required the true course.

Compass course W. by S. .... =  $78^\circ 45'$  right of South.  
Variation  $3\frac{1}{4}$  points = 36 34 right.

Deviation ..... 115 19 right of South.  
..... 13 50 left.

Course corrected for variation and deviation ..... 101 29 right of South.  
Leeway, port tack  $1\frac{3}{4}$  points ..... = 19 41 right.

Sum exceeds  $90^\circ$  .... 121 10 right of South.  
Subtract from ..... 180

58 50 left of North.

∴ True Course is N.  $58^\circ 50'$  W.

Since no course can exceed  $90^\circ$  from *either* N. or S., when the course as in this example exceeds  $90^\circ$ , the result must be taken from  $180^\circ$ , and its name changed. (See Rule LV (a), page 111.)

## EXAMPLES FOR PRACTICE.

From the following Compass Courses find the True Courses:—

| No. | Compass Courses.                             | Winds.                    | Leeway.             | Variation.             | Deviation.             |
|-----|--|---------------------------|---------------------|------------------------|------------------------|
| 1.  | N.E. by E.                                   | N. by W.                  | $2\frac{1}{2}$ pts. | 2 pts. W.              | $3\frac{1}{2}$ pts. E. |
| 2.  | North  | E.N.E.                    | 2 "                 | 2 " W.                 | 1 " E.                 |
| 3.  | N.N.W.                                       | N.E.                      | $3\frac{1}{4}$ "    | $2\frac{3}{4}$ " E.    | $1\frac{1}{2}$ " E.    |
| 4.  | West   | S.S.W.                    | $2\frac{1}{2}$ "    | $2\frac{3}{4}$ " E.    | $\frac{3}{4}$ " E.     |
| 5.  | S.S.E. $\frac{1}{2}$ E.                      | S.W. $\frac{1}{2}$ S.     | $3\frac{1}{2}$ "    | $2\frac{1}{2}$ " E.    | $1\frac{1}{4}$ " W.    |
| 6.  | E. $\frac{3}{4}$ S.                          | N.E. by N.                | $3\frac{1}{4}$ "    | $1\frac{1}{2}$ " W.    | $1\frac{1}{2}$ " E.    |
| 7.  | N. by W.                                     | W. by N.                  | 1 "                 | $2\frac{1}{4}$ " W.    | $1\frac{1}{4}$ " W.    |
| 8.  | South  | W.S.W.                    | $2\frac{3}{4}$ "    | $1\frac{1}{2}$ " E.    | $1\frac{1}{4}$ " E.    |
| 9.  | W. by S. $\frac{1}{4}$ S.                    | N.W.                      | $2\frac{1}{4}$ "    | 2 " W.                 | $1\frac{1}{4}$ " W.    |
| 10. | N.E. by E. $\frac{1}{4}$ E.                  | N. by W.                  | $1\frac{1}{4}$ "    | $2\frac{1}{2}$ " E.    | $1\frac{1}{4}$ " E.    |
| 11. | S.W. by W.                                   | S. by E.                  | 2 "                 | 3 " E.                 | $1\frac{1}{2}$ " W.    |
| 12. | E. $\frac{3}{4}$ S.                          | S. by E.                  | $1\frac{3}{4}$ "    | $42^{\circ}$ o' E.     | $15^{\circ}$ o' E.     |
| 13. | N.E.   | N.N.W.                    | $1\frac{1}{4}$ "    | 12 o W.                | 16 30 E.               |
| 14. | W.N.W.                                       | North                     | 3 "                 | $42^{\circ}$ o E.      | 18 30 W.               |
| 15. | N.E. by E.                                   | N. by W.                  | $\frac{1}{2}$ "     | 14 o E.                | 19 o E.                |
| 16. | W. by S.                                     | S. by W.                  | $\frac{3}{4}$ "     | 10 30 E.               | 19 o W.                |
| 17. | South  | E.S.E.                    | $\frac{1}{4}$ "     | 17 o W.                | 3 o E.                 |
| 18. | West   | N.N.W.                    | $1\frac{1}{4}$ "    | 18 30 E.               | 21 o W.                |
| 19. | S.S.W. $\frac{3}{4}$ W.                      | S.E. by S.                | $2\frac{1}{2}$ "    | 17 o W.                | 5 o W.                 |
| 20. | N.W. by W.                                   | N. by E.                  | 3 "                 | 25 o W.                | $7\frac{1}{2}$ W.      |
| 21. | E. by N.                                     | S.E. by S.                | $1\frac{3}{4}$ "    | 32 o E.                | 12 o E.                |
| 22. | W. by S. $\frac{1}{2}$ S.                    | S. by W.                  | 2 "                 | 15 o E.                | 15 o W.                |
| 23. | E. $\frac{1}{2}$ S.                          | N.N.E. $\frac{1}{2}$ E.   | $2\frac{1}{2}$ "    | 21 o W.                | 4 o W.                 |
| 24. | S.W. by S.                                   | W. by N.                  | $1\frac{1}{2}$ "    | 25 o E.                | 10 o W.                |
| 25. | South  | E.S.E.                    | $1\frac{1}{4}$ "    | 52 o W.                | 2 o E.                 |
| 26. | S.W. $\frac{1}{2}$ S.                        | S.S.E. $\frac{1}{2}$ E.   | $1\frac{1}{2}$ "    | 52 o W.                | 13 o W.                |
| 27. | E. $\frac{1}{2}$ S.                          | S. by E. $\frac{1}{2}$ E. | $\frac{3}{4}$ "     | 52 o W.                | 24 o E.                |
| 28. | East   | S.S.E.                    | $2\frac{1}{4}$ "    | 8 30 E.                | 15 35 E.               |
| 29. | W. $\frac{1}{4}$ N.                          | N.N.W.                    | $1\frac{3}{4}$ "    | 8 30 E.                | 21 30 W.               |
| 30. | N. $\frac{1}{2}$ W.                          | W. by N.                  | $\frac{1}{2}$ "     | 15 45 E.               | 6 o W.                 |
| 31. | E. $\frac{1}{4}$ N.                          | N.N.E.                    | $2\frac{1}{4}$ "    | 13 o W.                | 20 o E.                |
| 32. | S.E. by E.                                   | S. by W.                  | $1\frac{3}{4}$ "    | 18 o W.                | 16 30' E.              |
| 33. | N. by W. $\frac{1}{2}$ W.                    | N.E. $\frac{1}{2}$ E.     | $2\frac{1}{4}$ "    | 53 o W.                | $8\frac{1}{2}$ W.      |
| 34. | up S.E.<br>off E. by N. }                    | South.                    | $4\frac{1}{2}$ "    | $1\frac{1}{4}$ pts. E. | 2 pts. W.              |
| 35. | up S.W. $\frac{1}{2}$ W. }<br>off W. by N. } | S. $\frac{1}{2}$ E.       | $5\frac{1}{4}$ "    | $1\frac{1}{4}$ " E.    | $2\frac{1}{2}$ " E.    |
| 36. | up N.W. $\frac{1}{2}$ N. }<br>off W. by N. } | N. by E.                  | $4\frac{1}{2}$ "    | $1\frac{1}{4}$ " E.    | $1\frac{1}{4}$ " E.    |

## NAPIER'S DIAGRAM.

236. It is often of the utmost importance in various branches of physical science to represent tables of *related numbers* by means of curve lines, or other figures that show *to the eye* the nature of the relations or laws expressed, or rather concealed, within the mass of figures constituting the tables. Not only does such a mode of representation at once manifest these laws—almost rendering them palpable—but it further points out in what cases natural laws are not represented, and therefore what the cases are that require a greater amount of observation. These modes of representation are commonly known as *Graphic Methods*.

Various "graphic methods" of delineating the deviation have been devised;\* but the method introduced here is due to J. R. Napier, Esq., F.R.S., and is one peculiarly adapted for this purpose, as it is equally applicable whether the points on which the observations have been made are or are not precisely equidistant. It requires no calculation, and only a moderate degree of neat-handedness.

The method consists of two parts, the diagram and the curve. The diagram is the same for all vessels.

**Construction of the Diagram**—In this method the diagram consists of a central or vertical line of convenient length—say 18 inches—which may be considered as representing the margin of the compass card cut at the north point, and straightened and extended in the following way:—

N                      E                      S                      W                      N

This line is divided into 32 equal parts, representing the 32 points of the compass, commencing at the top with north, and ranging in the order of N. by E., N.N.E., &c. The vertical line is then intersected at each of the 32 points by two straight lines inclined to it at an angle of  $60^\circ$ : one of these is a *plain* line inclined to the right; the other a *dotted* line inclined to the left; that is, on the right side of the vertical line, the dotted lines incline downwards, and the plain lines upwards. The reverse is the case on the left.

The central line is further divided in 360 equal parts, representing degrees, and these divisions are numbered from  $0^\circ$  at the top to  $360^\circ$  at the bottom. They are also numbered, according to the usual mode of dividing the circumference of the compass-card, from  $0^\circ$  at North and South, up to  $90^\circ$  at East and West.

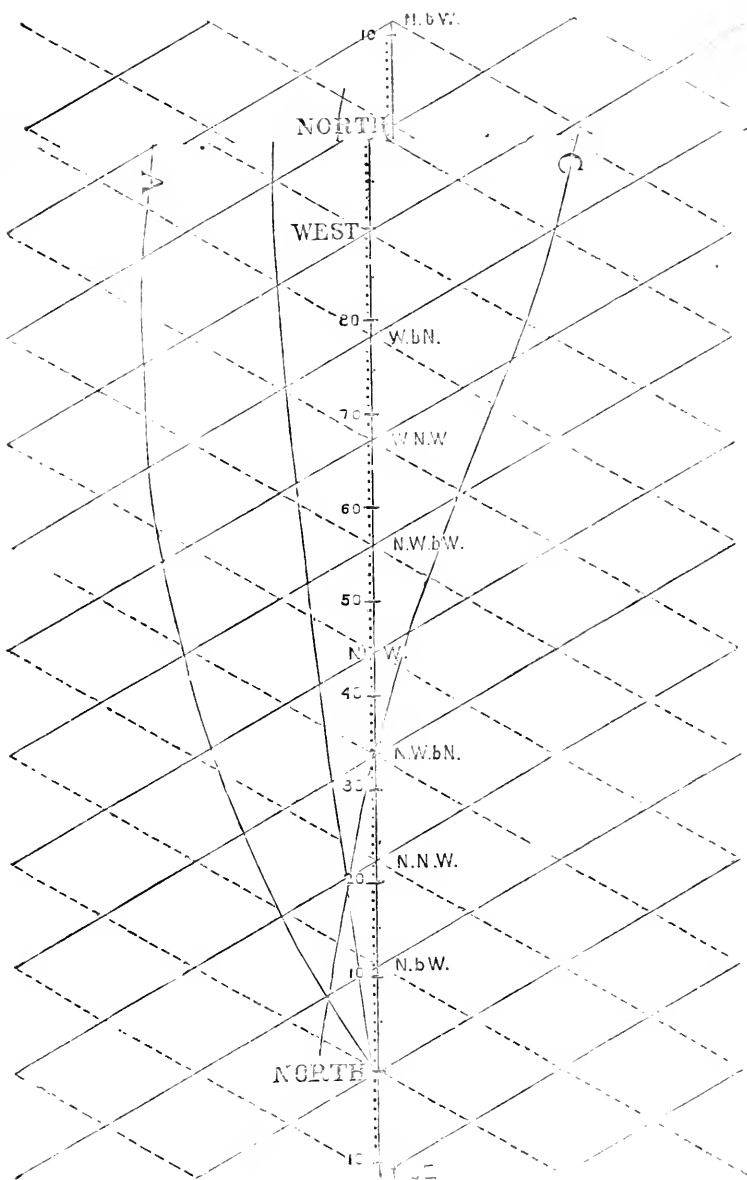
237. **Requisite Observations to be made.**—The least number of observed deviations available for obtaining a complete curve are the deviations on 4 points distributed equally, or nearly so, round the compass; but, if possible, the deviations should be observed on 8 or more points. If the observations are observed on 4 points only, these should be at or near N.E., S.E., S.W., and N.W., and from these it is possible to form a fairly approximate curve. The points next in importance are North, East, South, and West. If the deviations have been observed at or near the eight principal points, a curve can be drawn which will give the deviation on every point of the compass within very small limits of error.

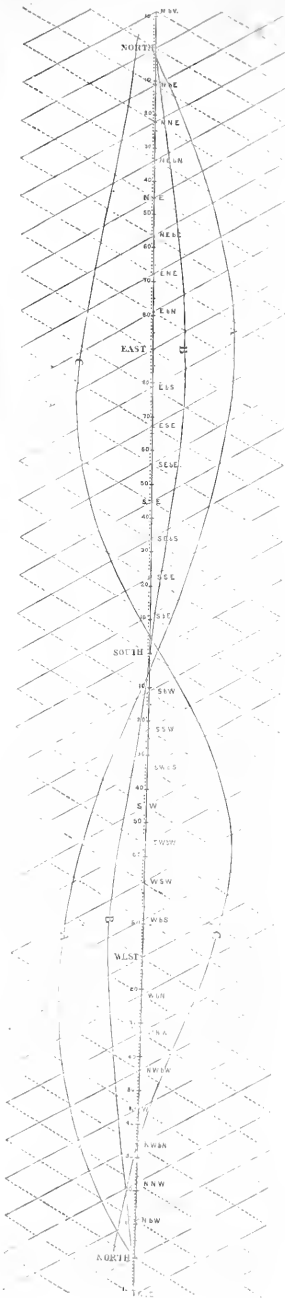
238. Cases may also occur in which by the ship swinging round at her anchors in a tide-way or to the wind, or by the aid of a steam-tug, the deviation may be observed on various directions of the ship's head, not being necessarily exact points of the compass; or similarly whilst under steam or sail at sea, a number of azimuths of the sun may be observed, and hence the deviation obtained.

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\* Graphic methods for correcting the ship's course for the Deviation of the Compass have also been designed by Rear Admiral Ryder, Mr. Archibald Smith, F.R.S., and Mr. W. W. Rundell. Admiral Ryder's, which is an extension of Napier's diagram, is published by the Admiralty. Mr. Smith's, known as the straight line method, is published by the Board of Trade, and also furnished to H.M. ships for fleet tactics, for which it is well adapted. Mr. Rundell's is known as the circular method. They are all useful in practice.







In these cases the Graphic method here described furnishes a ready and effectual mode of obtaining a result on which the error of individual observations are as far as possible compensated and any egregious errors eliminated.

239. **Construction of the Curve of Deviation.**—Easterly deviations are laid down to the right of the central line, Westerly deviations to the left. The plain and dotted lines make an angle of  $60^\circ$  with the central line and with each other, and so forming a set of equilateral triangles with the central line;\* the scale on each is the same, and the amount of the deviation may therefore be taken from the scale of degrees on the central line; then, if the deviation has been determined with the ship's head on an exact compass point, lay off the amount of the deviation on the dotted† line which passes through that point; but if not observed on the exact point, then on a line parallel to the dotted line, the compass course or direction of the ship's head being still taken from the central line, and mark the point so determined with a cross, or dot encircled in ink. Perform the same operation for each observed deviation. Then with a pencil and a light hand draw a flowing curve, passing as nearly as possible through all the crosses, or dots encircled; and when satisfied that the curve is good, draw it in ink. This is the curve of deviations.

If any of the pencil marks be out of the fair curve, it may be assumed that an error has been made in the observation for that point.

The process will be best understood by explaining the projection corresponding to the observations as given in the following table:—

| Ship's Head by<br>Standard Compass. | Deviation.  | Ship's Head by<br>Standard Compass. | Deviation. |
|-------------------------------------|-------------|-------------------------------------|------------|
| North .....                         | 6° 30' W.   | South .....                         | 5° 30' E.  |
| N.E. ....                           | 13   0   W. | S.W. ....                           | 28 35 E.   |
| East .....                          | 22 15 W.    | West .....                          | 19 15 E.   |
| S.E. ....                           | 23 30 W.    | N.W. ....                           | 3   0 E.   |

Deviation Curve C in Diagram.

1. The first compass course on which an observation has been made is North, and the observed deviation is  $6^\circ 30'$  W. With a pair of dividers take from the central line a distance equal to deviation  $6\frac{1}{2}^\circ$ , and from North on the vertical line lay off the deviation on the dotted line which passes through that point towards the left—the deviation being West; at the extremity of the distance make a dot or cross.

\* In Rear Admiral Ryder's plan, the central line is the diagonal of a square and the other lines make angles of  $45^\circ$  with it, and at right angles to each other and to the sides of the square, which sides are divided into  $360^\circ$ ; the top and bottom representing correct magnetic courses, the sides compass courses. By this method the correct magnetic course corresponding to a given compass course, or the compass course corresponding to a given correct magnetic course, is found as by a table of double entry. The two methods, it will be seen, are the same in principle. Mr. Napier's will perhaps be found more convenient in construction by the expert; Admiral Ryder's more simple in use by the inexperienced.

† If the table of deviations are given for the *correct magnetic* courses and not the *compass* courses or direction of the ship's head, the same process is gone through, except that the deviations are in that case laid off on the plain lines. It is, however, now generally understood that this procedure is contrary to practice and may lead to error.

2. The second compass course on which an observation has been made is N.E., and the observed deviation is  $13^{\circ} 0' W.$  With dividers take from the vertical line a distance equal to deviation  $13^{\circ}$ , and from N.E. on the vertical line lay it off on the dotted to the left—deviation being W.; and the point so determined mark with a cross or dot.

3. The third compass course on which an observation has been made is East, and the observed deviation is  $22^{\circ} 15' W.$  Take from vertical line  $22\frac{1}{4}^{\circ}$ , and from East on vertical line and on the dotted line passing through it, lay off the observed deviation to the left—deviation being W.; and mark the point so determined with a dot or cross.

4. Compass course S.E., observed deviation  $23^{\circ} 30' W.$  Take from the vertical line a distance equal to deviation  $23\frac{1}{2}^{\circ}$ , and from S.E. on the vertical line lay off on the dotted line passing through the same point the amount of deviation to the left—the deviation being W.; make a dot.

5. Compass course South, deviation  $5^{\circ} 30' E.$  Measure on the vertical line a distance equal to deviation  $5\frac{1}{2}^{\circ}$ , and having found compass course South on the vertical line, lay off the amount of deviation on the dotted line which passes through it towards the right—deviation being E.; and make a dot or cross.

6. Compass course S.W., deviation  $28^{\circ} 35' E.$  From the vertical line take a distance equal to observed deviation  $28\frac{1}{2}^{\circ}$ , and having found S.W. on the vertical line, lay off on the dotted line passing through that point the amount of deviation to the right—deviation being E.; make a dot or cross.

7. Compass course West, observed deviation  $19^{\circ} 15' E.$  Measure on vertical line a distance equal to deviation  $19\frac{1}{4}^{\circ}$ , and having found compass course West on the vertical line, lay off on the dotted line passing through that course the amount of deviation towards the right—deviation E.; and make a dot or cross.

8. Compass course N.W., deviation  $3^{\circ} 0' E.$  Take from vertical line a distance equal to  $3^{\circ}$ , and having found compass course, N.W., on the vertical line, place one foot of compass on that point and lay off on the dotted line passing through it the amount of deviation ( $3^{\circ}$ ) towards the right—deviation E.; and make a dot.

9. Then, with a pencil and a light hand, draw a flowing curve, passing as nearly as possible through all the crosses or dots, and if satisfied with the curve in pencil, draw it in ink.

NOTE.—The learner should take a pair of dividers, and go through the above process on the diagrams here given (see Plate I). He should then take the blank diagram (see Plate II), and make the curve on it.

Ex. 2. Construct a curve of deviations, using for the purpose the following observations:— (See Deviation Curve A in Diagram.)

| Ship's Head<br>by<br>Standard Compass. | Deviation.          | Ship's Head<br>by<br>Standard Compass. | Deviation.         |
|--|---------------------|--|--------------------|
| North .....                            | $1^{\circ} 15' W.$  | South .....                            | $1^{\circ} 50' E.$ |
| N.E. ....                              | $22^{\circ} 30' E.$ | S.W. ....                              | $15^{\circ} 0' W.$ |
| East .....                             | $26^{\circ} 50' E.$ | West .....                             | $26^{\circ} 0' W.$ |
| S.E. ....                              | $17^{\circ} 0' E.$  | N.W. ....                              | $27^{\circ} 0' W.$ |

The following describes the process of construction:—

1. With a pair of dividers take from the central line a distance equal to deviation  $1^{\circ} 15'$ , or  $1\frac{1}{4}^{\circ}$ , and from North on the vertical line, lay the distance off on the dotted line passing through that point and towards the left—being W.; at the extremity of the distance make a dot or cross.

2. Take from the vertical line a distance equal to  $22\frac{1}{2}^{\circ}$  ( $22^{\circ} 30'$ ), and lay it off on the dotted line, from N.E. towards the right—being E.; make a dot or cross.

3. Take from the vertical line a distance equal to  $26\frac{3}{4}^{\circ}$  ( $26^{\circ} 50'$ ), and lay it off on the dotted line, from East towards the right—being E.; make a dot or cross.
4. Take from the vertical line a distance equal to  $17^{\circ}$  ( $17^{\circ} 0'$ ), and lay it off on the dotted line, from S.E. towards the right—being E.; make a dot or cross.
5. From the vertical line take a distance equal to  $1\frac{1}{4}^{\circ}$  ( $1^{\circ} 50'$ ), and lay it off on the dotted line, from South towards the right—the deviation being E.; make a dot or cross.
6. From the vertical line take a distance equal to  $15^{\circ}$ , and lay it off on the dotted line, from S.W. towards the left—the deviation being W.; make a dot or cross.
7. From the vertical line take a distance equal to  $26^{\circ}$  and lay it off on the dotted line, from N.W. towards the left—deviation being W.; make a dot.
8. From the vertical line take a distance equal to  $27^{\circ}$ , and lay it off on the dotted line, from W. towards the left—deviation being W.; make a dot.
9. Repeat the admeasurement first made, from North, at the lower end of the vertical line.
10. Then, with a pencil and a light hand, draw a flowing curve, passing as nearly as possible through all the dots or crosses; when satisfied that the curve is good, draw it in ink. This is the curve of deviation.

Ex. 3. Construct a curve of deviations, using for the purpose the following observations:— (See Deviation Curve B in Diagram.)

| Ship's Head<br>by<br>Standard Compass. | Deviation.                 | Ship's Head<br>by<br>Standard Compass. | Deviation.                 |
|--|----------------------------|--|----------------------------|
| North .....                            | $0^{\circ} 22' \text{ W.}$ | South .....                            | $0^{\circ} 16' \text{ W.}$ |
| N.E. ....                              | $7 \ 14 \text{ E.}$        | S.W. ....                              | $6 \ 16 \text{ W.}$        |
| East .....                             | $10 \ 44 \text{ E.}$       | West .....                             | $11 \ 50 \text{ W.}$       |
| S.E. ....                              | $6 \ 18 \text{ E.}$        | N.W. ....                              | $7 \ 52 \text{ W.}$        |

Selecting those dotted lines which pass through the points representing the different directions of the ship's head, the deviations are laid off: thus, at North, we mark off  $0\frac{1}{2}^{\circ}$  ( $0^{\circ} 22'$ ) to the left on the dotted line passing through North—because deviation is West; at N.E., we take  $7\frac{1}{4}^{\circ}$  from the vertical line, and lay it off to the *right* (deviation being E.) on the dotted line passing through N.E.; at East,  $10\frac{1}{2}^{\circ}$  is taken from the vertical line and laid off to the right on the dotted line passing through East; and so with the others, being careful to remember that the known deviations must be laid down on the dotted lines, *easterly* to the *right* and *westerly* to the *left* of the vertical line. The curve is then drawn neatly through all the points so laid down, and it will be found that the deviation for any other point taken from the curve corresponds with that taken from the Table of Deviations given at page 136; and the curve thus drawn can be used instead of the Table.

240. **How the Curve is used.**—The curve of deviations having been completed, the diagram affords a ready and convenient method of applying the deviation to the ship's course. This correction may be required as follows:—1st, from the compass course which has been steered, it may be required to find the correct magnetic course to be laid down on the chart; or, 2nd, from the correct magnetic course given by the chart, it may be required to find the compass course on which the ship's head ought to be kept; or, 3rdly, if one or more bearings of the land are taken, to correct these bearings by the amount of the deviation due to the direction of the ship's head at the time. The corrections are given by the following rules.

241. To find the Deviation on any Compass Course.

### RULE LXI.

*On the central line find the given course; then, with a pair of dividers, measure the distance from that point to where the curve cuts the dotted line passing through the course; but if no dotted line proceeds from the course, then measure from the course on the central line to the curve in a direction exactly parallel to the nearest dotted lines: that distance measured on any part of the central line will give the deviation in degrees.*

### EXAMPLES.

Ex. 1. What is the deviation on Compass Course N.E. by N. (a) for the deviation curve B; (b) using the deviation A?

(a) Having found the given course on the central line, with a pair of dividers measure the distance from N.E. by N. to where the curve cuts the dotted line proceeding from that point; this distance taken to the central line gives  $6^{\circ}$  E.

(b) Measuring with a pair of dividers the distance from N.E. by N. to where the curve cuts the dotted line proceeding from that point, the deviation measured on the vertical line is found to be  $19^{\circ}$  E.

Ex. 2. Required deviation in compass course W.S.W., using deviation A.

Find W.S.W. on the vertical line, measure the distance from that point to where the curve cuts the dotted line proceeding from it; this distance taken to the vertical line gives deviation  $21\frac{1}{2}^{\circ}$  W.

Ex. 3. What is the deviation on compass course E.S.E., using deviation curve C?

Measure from E.S.E. on the vertical line to the point where the curve cuts the dotted lines proceeding from it; this distance taken to the central line gives deviation  $25^{\circ}$  W.

Ex. 4. What is the deviation for compass course N.E.  $\frac{1}{2}$  N., using the curve C?

Take N.E.  $\frac{1}{2}$  N. on the vertical line, and draw a faint pencil line parallel to the dotted lines until it meets the curve. The length of this line in degrees taken from the vertical line gives  $12\frac{1}{4}^{\circ}$  W., the deviation for N.E.  $\frac{1}{2}$  N.

Or thus:—Place one leg of a pair of dividers at N.E.  $\frac{1}{2}$  N. on the central line, and from thence measure the distance to the curve in a direction exactly parallel to the nearest dotted lines; this distance taken to the central line gives the deviation  $12\frac{1}{4}^{\circ}$  W., the deviation for N.E.  $\frac{1}{2}$  N.

Ex. 5. Find the deviation for Standard Compass Course N.  $84^{\circ}$  W., using deviation curve A.

Through N.  $84^{\circ}$  W. on the vertical line draw a pencil line parallel to the nearest dotted line, so that it may cross the curve.

Or thus:—Find N.  $84^{\circ}$  W. on the central line, and placing one foot of a pair of dividers on that point, from thence measure the distance in the direction of an imaginary line drawn parallel to the nearest dotted lines; apply this distance to the central line, which shows the deviation for the ship's course is  $26\frac{1}{2}^{\circ}$  W.

### EXAMPLES FOR PRACTICE.

Required the deviation for each of the following compass courses, using (a) the curve A, (b) the curve B, and (c) the curve C:—

S.S.E.; N.E. by N.; N.W.; N.W. by N.; S.W. by W.; W.N.W.; South; N.  $48^{\circ}$  E.; S.  $52^{\circ}$  W.; E. by S.  $\frac{1}{4}$  S.; N.  $41^{\circ}$  W.; and S.  $38^{\circ}$  E.

For further exercises in this matter the learner may take the Table of Deviations given on page 136, and using the curve B, find the deviations for each of the 32 points of the compass; the results ought to agree pretty nearly with those given in the Table.

NOTE.—Persons may differ one or two degrees in their estimate of what constitutes a fair curve; it is therefore quite likely that students may find their answers differ a degree or two from those given in this work.

We have now the following easily applied solution of the two following problems:—

**Problem I.**—From a Compass Course, to find the corresponding Correct Magnetic Course.

### RULE LXII.

*On the central line find the given Standard Compass Course, and move on the dotted line drawn from it, or in a direction parallel to the dotted lines till you reach the curve, and then move on a plain line, or in a direction parallel to the plain lines, till you get back to the central line. The point on the central line at which you arrive is the correct magnetic course required.*

NOTE.—The directions in the above rule are easiest done by means of a pair of dividers. To move on the *dotted* line, or in a direction parallel to it, place one leg of a pair of dividers on the course, and the other leg at that point on the curve which is intersected by the *dotted* line proceeding from the course, or a point on the curve where a line included between the leg of the dividers on the central line and the leg on the curve shall be *exactly parallel* to the nearest dotted lines, then to return to the central line—keep the first leg of the dividers fixed and lift the other off the curve, move in a direction parallel to the plain lines until you reach the central line, the point where the dividers cut the central shows the correct magnetic course.

### EXAMPLES.

Ex. 1. The course steered by standard compass is N.N.E.: what is the correct magnetic course to lay down on the chart (using the curve C in the diagram, Plate I.)

Find the given compass course N.N.E. on the central line, then take a pair of dividers, put one leg of the dividers on N.N.E., from which extend the other leg along the *dotted* line passing through the point till the curve is reached, then keeping the leg on the central fixed, move the one off the curve, and then return to the central line in a direction parallel to the *plain* line; it will be found to intersect it at N.  $13\frac{1}{2}^{\circ}$  E., or N. by E.  $\frac{1}{4}$  E., nearly, the required correct magnetic course.

Ex. 2. The course steered by compass is N.E. by N.: required the correct magnetic course (using curve A, Plate I.)

Follow the *dotted* line extending from N.E. by N. to where the curve cuts it, by placing one leg of a pair of dividers on the course found on the central line and the other at the point where the *dotted* passing through N.E. by N. cuts the curve, then keeping the leg on the central line fixed, lift the other from the curve and move in the direction of the nearest *plain* lines till the central line is reached; then the correct magnetic course will be found to be N.  $52^{\circ}$  E., or N.E.  $\frac{3}{4}$  E., nearly.

Ex. 3. The course steered is S.S.W.: required the correct magnetic course (using curve C, Plate I.)

Having found the compass course S.S.W. on the vertical line, place one leg of the dividers on the course and the other on the place where the *dotted* proceeding from it is intersected by the curve, then keeping the leg on the central line fixed, return with the other leg to the central line in a direction parallel to the *plain* line, it will be seen that the *correct* magnetic course is S.W.  $\frac{1}{4}$  W.

Ex. 4. Compass course W.S.W.: what correct magnetic course does this give on the curve A of deviations, Plate I?

From W.S.W. on the central line follow the *dotted* extending from that point until it reaches the curve, then keeping the leg of the dividers on the central line fixed, move the other that is placed on the curve, in a direction parallel to the *plain* line, until it cuts the central line, which shows the correct magnetic course S.  $47^{\circ}$  W., or S.W.  $\frac{1}{4}$  W.

Ex. 5. The course steered by compass is S.E.  $\frac{1}{2}$  E.: required the corresponding correct magnetic course (using curve C, Plate I.)

Place one leg of the dividers on S.E.  $\frac{1}{2}$  E. on the central line, and the other leg on the curve, being careful to keep the two points of the dividers exactly parallel to the nearest dotted lines, then lift the leg off the curve and return to the central line, the place where this last line intersects the central line, shows the correct magnetic course to be S.  $75\frac{1}{2}^{\circ}$  E., or E. by S.  $\frac{1}{4}$  S.

Ex. 6. Given the standard compass courses N.  $38^{\circ}$  E. and S.  $49^{\circ}$  W.: required the correct magnetic courses (using the A deviation curve, Plate I.)

Having found the standard compass course N.  $38^{\circ}$  E. on the central line, place one leg of the dividers on that spot and move the other leg out in a direction parallel to the nearest dotted line until it meets the curve; then, keeping the leg which is on the central line fixed, move the other leg in the direction of the *plain* lines until it returns to the central line. The point arrived at shows the *correct* magnetic course is N.  $58^{\circ}$  E., nearly, or N.E. by E.  $\frac{1}{4}$  E.

In a similar manner the correct magnetic course is found to be S.  $33^{\circ}$  W.

#### EXAMPLES FOR PRACTICE.

In each of the following examples the compass course is given to find the corresponding *correct* magnetic course, using curve A, curve B, and curve C.

Curve A.—N.  $41^{\circ}$  W.; N.  $65^{\circ} 30'$  E.; S.  $38^{\circ}$  E.; S.  $79^{\circ}$  W.; West; N.E.; S.E.  $\frac{1}{2}$  E.; S.  $89^{\circ} 30'$  W.; N.N.W.; S.S.W.

Curve B.—N.  $47\frac{1}{2}^{\circ}$  W.; N.  $76^{\circ}$  E.; S.  $26\frac{1}{2}^{\circ}$  E.; S.  $68\frac{1}{2}^{\circ}$  W.; S.  $78^{\circ}$  W.; N.  $52\frac{1}{2}^{\circ}$  E.; S.  $43^{\circ}$  E.; S.  $78^{\circ}$  W.; N.  $27\frac{1}{2}^{\circ}$  E.; and S.  $20^{\circ}$  W.

Curve C.—N.  $39^{\circ}$  W.; N.  $48^{\circ}$  E.; S.  $50^{\circ}$  E.; N.  $78^{\circ}$  W.; N.  $70^{\circ}$  W.; N.  $31\frac{1}{2}^{\circ}$  E.; S.  $76^{\circ}$  E.; N.  $70\frac{1}{2}^{\circ}$  W.; N.  $26^{\circ}$  W.; and S.  $47^{\circ}$  W.

**Problem II.**—From a given Correct Magnetic Course to find the corresponding Compass Course.

#### RULE LXIII.

*On the vertical line take the given correct magnetic course, and move on the plain line drawn from that point or in a direction parallel to the plain lines till you arrive at the curve; and then move on a dotted line, or in a direction parallel to the dotted lines till you get back to the vertical line. The point on the central line at which you arrive is the compass course required.\**

#### EXAMPLES.

Ex. 1. Given correct magnetic course N.N.E. to find the corresponding compass course (using curve C.)

Find N.N.E. on the central line, and placing one leg of the dividers on the spot, extend the other leg to the spot where the *plain* line proceeding from N.N.E. meets the curve; then keeping the leg on the central fixed, lift the one on the curve and return to the central line in a direction parallel to the *dotted* line, it will be found to intersect at N.E. by N., the required course by standard compass.

\* The only difficulty in applying these rules is to remember in each case whether we ought to depart from the central line by a *dotted* line, and return to it by a *plain* line; or whether we ought to depart from the central line by a *plain* line and return to it by a *dotted* line. The doubt will be removed if the following lines, in which the two lines are versified, are committed to memory:—

#### I.

“From compass course magnetic course to gain,  
Depart by dotted and return by plain.”

#### II.

“But if you wish to steer a course allotted,  
‘Take plain from chart and keep her head on dotted.’”



Ex. 2. What compass course will make correct magnetic S.E. (using A curve).

Find S.E. on the central line, put one leg of the dividers on the spot and the other leg on the curve where the *plain* line that passes through S.E. cuts the curve; then keep the leg that is on the central line fixed, lift the other leg off the curve and move it in the direction of the nearest dotted till it again touches the central line; the compass course that makes correct magnetic S.E. is shown on the central line to be S.  $67\frac{1}{2}^{\circ}$  E., or E.S.E.

Ex. 3. It is found from the chart that the correct magnetic course from the ship's position at noon to the Start Point is N.  $86^{\circ}$  E. What course must be steered by Standard Compass (using C curve)?

Find the correct magnetic course N.  $86^{\circ}$  E. on the vertical line, place one foot of the dividers on the spot, then follow thence, with the other leg in a direction parallel to the nearest *plain* line until it meets the curve, and then return with the other leg to the central line in a direction parallel to the *dotted* line; the compass course required is S.  $69\frac{1}{2}^{\circ}$  E.

Ex. 4. Required the compass course to make correct magnetic W. by N. (using A curve).

Find compass course W. by N. on the central line, put one leg of the dividers on W. by N. and the other on the curve where the *plain* line that passes through W. by N. cuts the curve; then keep the leg that is on the central line fixed, but lift the other off the curve and move it in the direction of the *dotted* line till it again touches the central line; it will then be seen that the compass course that makes correct magnetic W. by N. is N.  $51^{\circ}$  W., or N.W.  $\frac{1}{2}$  W.

Ex. 5. If the magnetic course required is N.W. by N., required the compass course on the C curve.

Find N.W. by N. on the central line; place one foot of the dividers on the spot, and the other foot on the place where the *plain* line proceeding from N.W. by N. meets the curve; then keeping the foot that is on the central fixed, return to the central line with the other leg in a direction parallel to the *dotted* line; it will be found to intersect at N.  $32\frac{1}{2}^{\circ}$  W., the required course by Standard Compass.

Ex. 6. Given the correct magnetic courses N.  $64^{\circ}$  E. and N.  $85^{\circ}$  W. to find the Standard Compass course, using the C deviation curve. Plate I.

Find N.  $64^{\circ}$  E. on the central line; place one foot of the dividers on the point and the other on the curve, being careful to keep both legs of the dividers exactly parallel to the nearest *plain* line; keep the foot of dividers that is on the central line fixed and move the other in the direction of the nearest dotted line till it meets the central line; the point of intersection in this instance is N.  $85\frac{1}{2}^{\circ}$  E.

In a similar manner the Standard Compass course corresponding to correct magnetic course N.  $85^{\circ}$  W. is found to be S.  $70^{\circ}$  W.

#### EXAMPLES FOR PRACTICE.

In each of the following examples the correct magnetic course is given to find the compass course, using curve A, curve B, and curve C.

Curve A.—S.  $73^{\circ} 30'$  W.; N.  $42^{\circ} 15'$  E.; S.  $15^{\circ} 30'$  W.; N.  $14^{\circ} 15'$  E.; N.  $62^{\circ} 45'$  E.; E.  $15^{\circ}$  S.; W.  $45^{\circ}$  S.; N.E. by N.; W.S.W.

Curve B.—S.  $85^{\circ}$  W.; N.  $36\frac{1}{2}^{\circ}$  E.; S.  $18^{\circ}$  W.; N.  $12\frac{1}{2}^{\circ}$  E.; N.  $54\frac{1}{2}^{\circ}$  E.; S.  $85\frac{1}{2}^{\circ}$  E.; S.  $53^{\circ}$  W.; N.  $29^{\circ}$  E.; and W. by S.

Curve C.—S.  $44^{\circ}$  W.; N.  $58\frac{1}{2}^{\circ}$  E.; S.  $5^{\circ}$  W.; N.  $24^{\circ}$  E.; N.  $83^{\circ}$  E.; S.  $50^{\circ}$  E.; S.  $22^{\circ}$  W.; N.E.  $\frac{1}{4}$  E.; and S.W.  $\frac{1}{2}$  S.

We shall now proceed to show the application of the foregoing rules to Questions 7, 8, 9, and 10 of List B, which contains the questions on the Deviation of the Compass required of Candidates for Certificates as Master Ordinary.

## QUESTION 7. LIST B.

242. Given the bearings of a distant object by Standard Compass on eight *equi-distant*\* points to find the Correct Magnetic Bearing of the distant object and thence the Deviation.

## RULE LXIV.

1°. If the Compass bearings are all of the same name, i.e., if they are all reckoned from N. or S. towards E. or W. :

*Take the sum of the Bearings in each column then add these sums together, and divide by 8 ; the result is the Correct Magnetic Bearing of the distant object.*

2°. If the Compass Bearing be of different names :

(a) If some of the Bearings are reckoned from North and the others from South :

*Take either set from 180°, and they will all be reckoned from the same point North or South ; the name as to East or West remains unaltered.*

(b) If some of the Bearings are towards the East and others towards the West :

*Find the sum of these which are reckoned towards East ; and also the sum of those which are towards the West ; then take the less from the greater, and mark the difference of the same name as the greater ; the result divided by 8 gives the Correct Magnetic Bearing of the distant object, which is of the same name as the difference.*

NOTE.—On the form given at the Marine Board Examinations there is not sufficient space to perform the last mentioned addition and division : there is only room to find the first two sums ; the rest, however, can be finished in the margin.

3°. To find the Deviation for each of the given Courses.—(a) If the Correct Magnetic and Compass bearings are of like names :

*Take their difference.*

(b) If one is reckoned from North and the other from South, first take the Correct Magnetic bearing from 180° and the remainder will have the same name as the compass bearing, then take the difference between the Correct Magnetic and Compass Bearings.

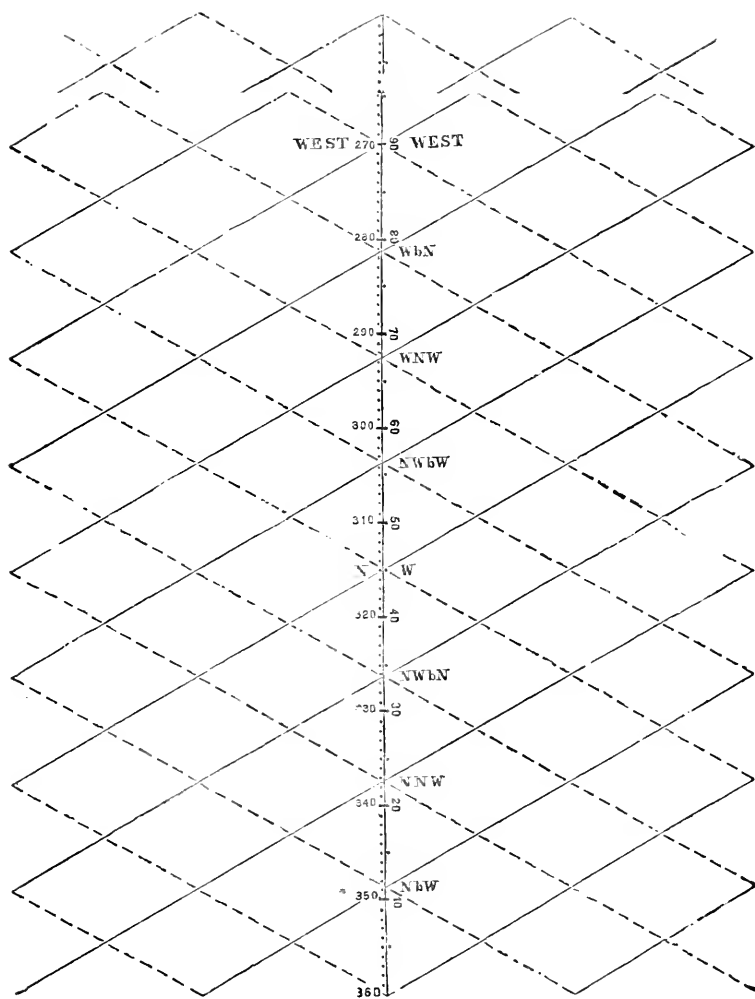
(c) If both bearings are from North or both from South, but one is towards East and the other towards West, take their sum :

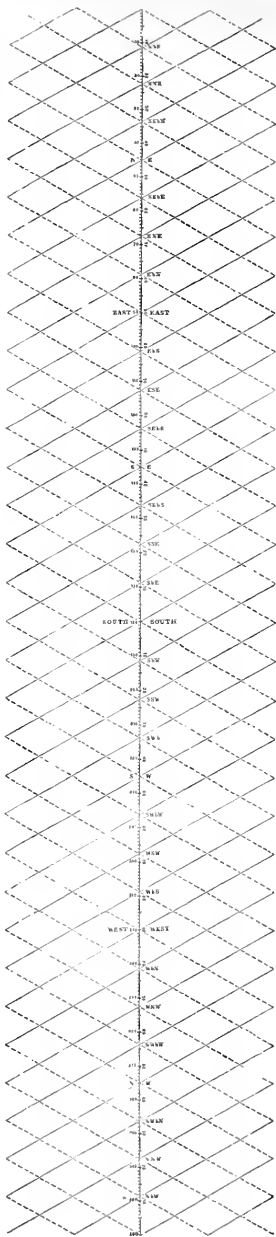
*The difference or sum will be the deviation.*

4°. To name the deviations.—If the Correct Magnetic bearing is to the right of the Compass Bearing the deviation is East, but if to the left it is West.

\* The 8 equi-distant points are the 4 cardinal points and the four quadrantal points, viz. : N.W., S.W., S.E., and N.E.

+ The Correct Magnetic Bearing thus found is not strictly accurate ; it will differ from the correct quantity by what is called the co-efficient A. The co-efficient A is found by adding the Deviations (algebraically),—that is, add together the Westerly deviations, also add the Easterly deviations together, and take the less from the greater, and mark the difference of the same name as the greater,—and divide by 8. This, however, is not required to be understood by Masters Ordinary, although it is required for Masters extra.





## EXAMPLE I.

In the following Table give the correct magnetic bearing of the distant object, and thence the Deviation.

| Ship's head<br>by<br>Standard<br>Compass. | Bearing of<br>Distant Object<br>by Standard<br>Compass. | Deviation<br>Required. | Ship's Head<br>by<br>Standard<br>Compass. | Bearing of<br>Distant Object<br>by Standard<br>Compass. | Deviation<br>Required. |
|---|---|------------------------|---|---|------------------------|
| North ....                                | S. 41° W.   |                        | South ....                                | S. 46° W.   |                        |
| N.E. ....                                 | S. 59 W.  |                        | S.W. ....                                 | S. 25 W.  |                        |
| East .....                                | S. 64 W.  |                        | West .....                                | S. 18 W.  |                        |
| S.E. ....                                 | S. 60 W.  |                        | N.W. ....                                 | S. 23 W.  |                        |

NOTE.—The above is the form in which the Table is given at the Local Marine Board Examinations. The Table is printed, excepting the columns of Bearings, which the Examiner fills up in writing. The following is the above example worked :—

| Ship's Head<br>by<br>Standard<br>Compass. | Bearing of<br>Distant Object<br>by Standard<br>Compass. | Deviation<br>Required. | Ship's Head<br>by<br>Standard<br>Compass. | Bearing of<br>Distant Object<br>by Standard<br>Compass. | Deviation<br>Required. |
|---|---|------------------------|---|---|------------------------|
| North ....                                | S. 41° W.   | 1° E.                  | South ....                                | S. 46° W.   | 3° W.                  |
| N.E. ....                                 | S. 59 W.  | 17 W.                  | S.W. ....                                 | S. 25 W.  | 17 E.                  |
| East .....                                | S. 64 W.  | 22 W.                  | West .....                                | S. 18 W.  | 24 E.                  |
| S.E. ....                                 | S. 60 W.  | 18 W.                  | N.W. ....                                 | S. 23 W.  | 19 E.                  |

S. 224° W.

S. 112 W.

8)336

S. 112° W.

S. 42° W. = Correct magnetic bearing of distant object.

Here we first add together the eight given bearings of the distant object, making 336°, and divide the sum by 8, giving as the result S. 42° W.—the correct magnetic bearing of the distant object.

We next take the difference between the correct magnetic bearing thus obtained and each bearing given in the table; thus, with the ship's head at North, the bearing by compass is S. 41° W. and the difference between this and the correct magnetic bearing S. 42° W. is 1°, and because the *correct magnetic* bearing is to the *right* hand of the standard compass bearing the deviation is East. Again, with the ship's head at N.E., the compass bearing is S. 59° W., and the difference between this and the *correct magnetic* bearing S. 42° W. is 17° but now the correct magnetic bearing is to the left of the compass bearing, hence the deviation is West, and so on with the remaining bearings, and the work will stand as follows:—

| Ship's Head.        | N.        | N.E.      | East.     | S.E.      |
|---------------------|-----------|-----------|-----------|-----------|
| Correct mag. bear.  | S. 42° W. | S. 42° W. | S. 42° W. | S. 42° W. |
| Standard com. bear. | S. 41 W.  | S. 59 W.  | S. 64 W.  | S. 60 W.  |
| Deviation           | 1 E.      | 17 W.     | 22 W.     | 18 W.     |
| Ship's head.        | S.        | S.W.      | West.     | N.W.      |
| Correct mag. bear.  | S. 42° W. | S. 42° W. | S. 42° W. | S. 42° W. |
| Standard com. bear. | S. 46 W.  | S. 25 W.  | S. 18 W.  | S. 23 W.  |
| Deviation           | 4 W.      | 17 E.     | 24 E.     | 19 E.     |

NOTE.—In the above work, the deviations are obtained by subtracting the less bearing from the greater, because they are all of the same name. (See Rule LXIV, 3° and 4°, page 162.)

## QUESTION 8. LIST C. (See Rule LXIII, Problem II, page 150.)

From the above table construct a Napier's Curve, and give the courses you would steer by standard compass to make the following courses correct magnetic:—

- (1.) S.E.      (2.) N.E.  $\frac{1}{4}$  E.      (3.) S.  $10^{\circ}$  W.      (4.) E.  $\frac{1}{4}$  N.

**To Construct the Curve from the Table.**—With a pair of dividers take from the central line  $1^{\circ}$ , the deviation for ship's head North; and lay it off from North, on the central line along the dotted line passing through the given point, and towards the right—being East; at the extremity of the distance make a dot or cross. Next take  $17^{\circ}$  from the vertical line, and with one foot of the dividers on N.E. on the vertical line, lay off this distance on the dotted line passing through the given point and to the left, because the deviation is West. Proceed in like manner with the deviation  $22^{\circ}$  W. at East; with  $18^{\circ}$  W. the deviation at S.E.; and with  $4^{\circ}$  W. the deviation at South. The deviation at S.W., West, and N.W. being easterly, must be applied to the right of the vertical line along the dotted lines proceeding from those point. Now draw with a pencil a curve passing as nearly possible through the points found, and when satisfied with its uniformity, draw it in ink.

**To find the Standard Compass Course.**—(1.) Place one leg of a pair of dividers on S.E. on the central line, and the other leg on the point where the *plain* line extending from S.E. is cut by the curve; then keep the first leg fixed and lift that on the curve, moving it in a direction parallel to the nearest *dotted* line, towards the central line; the compass course that makes *correct* magnetic S.E. is shown on the central line to be S.  $29^{\circ}$  E., or S.S.E.  $\frac{3}{4}$  E., (easterly.)

(2.) Take N.E.  $\frac{1}{4}$  E. on the central line, then placing one leg of the dividers on that spot, extend the other leg from this point and parallel to the nearest *plain* line until it cuts the curve; then keeping the first leg fixed, move the one on the curve parallel to the nearest *dotted* line and towards the central line; the compass course that makes *correct* magnetic N.E.  $\frac{1}{4}$  E. is shown on the central line to be E. by N.  $\frac{3}{4}$  N.

(3.) Place one leg of the dividers on S.  $10^{\circ}$  W. on the central line, and extend the other leg parallel to the nearest *plain* line, and to the *right* until it meets the curve; then keeping the leg on the central line fixed, move the leg on the curve thence parallel to the nearest *dotted* line until it arrives at the central line, which shows that the compass course to be steered is S.  $9^{\circ}$  W., nearly, in order to make S.  $10^{\circ}$  W. correct magnetic.

(4.) E.  $\frac{1}{4}$  N. is found on the central line, and one leg of the dividers being placed on the point, move the other leg to the left from that spot and parallel to the nearest *plain* line until it is cut by the curve; from thence, keeping the first leg fixed on the central line, move parallel to the nearest *dotted* line till the central line is reached; the compass course that makes *correct* magnetic E.  $\frac{1}{4}$  N. is shown on the central line to be S.  $72^{\circ}$  E.

## QUESTION 9. LIST B.

Suppose you steer the following courses by the Standard Compass, find the correct magnetic courses from the curve drawn:— (See Problem I, Rule LXII, page 149.)

- (1.) S.S.E.  $\frac{3}{4}$  E.      (2.) S.  $\frac{3}{4}$  W.      (3.) E. by N.  $\frac{3}{4}$  N.      (4.) N.  $\frac{1}{4}$  W.

(1.) With one leg of the dividers on S.S.E.  $\frac{3}{4}$  E. on the central line, move the other leg on a line to the *left* and parallel to the nearest *dotted* line until it cuts the curve; then keeping the first leg fixed, move the leg on the curve from thence parallel to the nearest *plain* one and towards the central line; the *correct* magnetic course is at once seen to be S.  $45\frac{1}{2}^{\circ}$  E.

(2.) Placing one leg of the dividers on S.  $\frac{3}{4}$  W. on the central line, move the other leg on a line to the *right*, parallel to the nearest *dotted* line and cutting the curve; from thence, keeping the first leg fixed on the central line, move in a direction parallel to the nearest *plain* line until the central line is reached; the *correct* magnetic course is thus shown to be S.  $10^{\circ}$  W.

(3.) Take the point on the central line representing E. by N.  $\frac{3}{4}$  N., place a leg of the dividers on that point and move the other leg in a direction parallel to the *dotted* lines, and after meeting the curve, return parallel to the *plain* lines, until the vertical line is again reached; the correct magnetic course is thus found to be N.  $48\frac{3}{4}^{\circ}$  E.

(4.) One leg of the dividers being fixed on N.  $\frac{1}{4}$  W. found on the central line, move the other leg in a direction parallel to the *dotted* lines till the curve is reached; and from thence returning to the central line in a direction parallel to the *plain* lines, we find *correct* magnetic course is North.

## QUESTION 10. LIST B.

Given the Bearings of two (or more) distant objects by the Standard Compass and also the Azimuth of the Ship's Head; required the correct magnetic bearing of these objects.

## RULE LXV.

1°. Find the Deviation corresponding to the direction of the ship's head, taking it from the Napier's Deviation Curve. (See Rule LXI, page 148).

2°. Apply the Deviation thus found to the Bearing of distant object by Standard Compass, according to Rule LIX, page 136, viz.: West Deviation to the left hand, East Deviation to the right hand.

The following bearings of distant objects have been taken by the Standard Compass as above; with the ship's head as given, find the correct magnetic bearing.

|    | Ship's Head. | Compass Bearing.          | Ship's Head. | Compass Bearing.                           |
|----|--------------|---------------------------|--------------|--|
| 1. | West .....   | East.                     | 3.           | E. $\frac{3}{4}$ N. ....                   |
| 2. | S.S.E. ....  | E. by S. $\frac{1}{4}$ S. | 4.           | N.E. $\frac{1}{4}$ E. ....                 |
|    |              |                           |              | N. $\frac{3}{4}$ W.<br>W. $\frac{1}{4}$ S. |

On the central line find the given course, West, and with a pair of dividers measure the distance from the point to where the curve cuts the *dotted* line proceeding from the course; this distance taken to the vertical line gives deviation  $24^{\circ}$  E. for ship's head at West.

We next apply the deviation to East—the bearing of distant object by standard compass—allowing it to the *right* hand; whence the correct magnetic bearing of distant object is S.  $66^{\circ}$  E.

Again, ship's course S.S.E. is found on the central line; with dividers measure from thence to where the *dotted* line proceeding from given course is cut by the deviation curve; this distance, taken from the central line, gives deviation  $13^{\circ}$  W.

The standard compass bearing of distant object taken when ship's head was at S.S.E. is E. by S.  $\frac{1}{4}$  S., or S.  $76^{\circ}$  E., to which apply deviation, found as above, to the *left* hand: the result is the correct magnetic bearing S.  $89^{\circ}$  E.

E.  $\frac{3}{4}$  N. is found on the central line; then from this spot measure the distance to the curve in a direction parallel to the nearest *dotted* line; and apply this to the central line which shows the deviation due to E.  $\frac{3}{4}$  N.—the direction of the ship's head—to be  $22\frac{1}{2}^{\circ}$  W.

Apply this deviation to compass bearing N.  $\frac{3}{4}$  W., or N.  $8^{\circ}$  W., to *left* hand, which gives correct magnetic bearing of distant object N.  $30\frac{1}{2}^{\circ}$  W.

N.E.  $\frac{1}{4}$  E. is the next given direction of the ship's head, which being found on the central line, place one leg of the dividers on the spot and move the other leg out in a direction parallel to the nearest *dotted* line until it meets the curve; this distance, taken by the dividers and applied to the central line, shows deviation for ship's head N.E.  $\frac{1}{4}$  E. to be  $18^{\circ}$  W.

The deviation thus found being applied to the *left* hand of W.  $\frac{1}{4}$  S., or S.  $87^{\circ}$  W., gives the correct magnetic bearing of distant object S.  $69^{\circ}$  W.

## EXAMPLE II.

I. In the following Table give the correct magnetic bearing of the distant object, and thence the Deviation :—

(Correct Magnetic Bearing of distant object = N.  $89^{\circ} 4' W.$ )

| Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North ....                       | S. $87^{\circ} W.$                             | $3^{\circ} E.$      | South ....                       | N. $87^{\circ} W.$                             | $2^{\circ} W.$      |
| N.E. ....                        | S. $70^{\circ} W.$                             | $21^{\circ} E.$     | S.W. ....                        | N. $75^{\circ} W.$                             | $14^{\circ} W.$     |
| East ....                        | S. $71^{\circ} W.$                             | $20^{\circ} E.$     | West ....                        | N. $68^{\circ} W.$                             | $21^{\circ} W.$     |
| S.E. ....                        | S. $81^{\circ} W.$                             | $10^{\circ} E.$     | N.W. ....                        | N. $72^{\circ} W.$                             | $17^{\circ} W.$     |

$$\begin{array}{r}
 \text{S. } 310^{\circ} \text{ W.} \\
 \text{S. } 418^{\circ} \text{ W.} \\
 \hline
 8)728 \\
 \hline
 \text{S. } 91^{\circ} \text{ W.} = \text{Correct Magnetic Bearing.} \\
 180
 \end{array}
 \qquad
 \begin{array}{r}
 \text{N. } 302^{\circ} \text{ W.} \\
 (180^{\circ} \times 4) = 720 \\
 \hline
 \text{S. } 418^{\circ} \text{ W.}
 \end{array}$$

or, N.  $89^{\circ} W.$

In this example the bearings given in the left hand column are reckoned from S. towards W., while the bearings in the right hand column are reckoned from N. towards W.; therefore, before adding up the latter column, each bearing must be subtracted from  $180^{\circ}$ , and the remainder, in each case, is the bearing reckoned from S. toward W. We may, however, proceed as above, viz. :—add up the Bearings reckoned from N. towards W.; and since there are four bearings so reckoned (from N. towards W.); take the sum from  $720$  ( $180 \times 4$ ); the remainder is the sum of the bearings to be reckoned from S. towards W. It is evident that to subtract the sum of the *four* bearings from  $720^{\circ}$  is the same thing as to subtract each bearing from  $180^{\circ}$  and to add the remainders.

| Ship's Head.             | N.                 | N.E.               | East.              | S.E.               |
|--------------------------|--------------------|--------------------|--------------------|--------------------|
| Correct magnetic bearing | S. $91^{\circ} W.$ | S. $91^{\circ} W.$ | S. $91^{\circ} W.$ | S. $91^{\circ} W.$ |
| Compass bearing          | S. $88^{\circ} W.$ | S. $70^{\circ} W.$ | S. $71^{\circ} W.$ | S. $81^{\circ} W.$ |
| Deviation                | $3^{\circ} E.$     | $21^{\circ} E.$    | $20^{\circ} E.$    | $10^{\circ} E.$    |
| Ship's Head.             | South              | S.W.               | West               | N.W.               |
| Correct magnetic bearing | N. $89^{\circ} W.$ | N. $89^{\circ} W.$ | N. $89^{\circ} W.$ | N. $89^{\circ} W.$ |
| Compass bearing          | N. $87^{\circ} W.$ | N. $75^{\circ} W.$ | N. $68^{\circ} W.$ | N. $72^{\circ} W.$ |
| Deviation                | $2^{\circ} W.$     | $14^{\circ} W.$    | $21^{\circ} W.$    | $17^{\circ} W.$    |

II. From the above Table construct a Napier's curve, and give the courses you would steer by standard compass to make the following courses correct magnetic :—

- (1.) W. by S.  $\frac{3}{4} S.$  (2.) N.  $\frac{1}{2} E.$  (3.) E. by S.  $\frac{3}{4} N.$  (4.) S.E.  $\frac{3}{4} S.$   
*Answers :—*(1.) West. (2.) N.  $1^{\circ} E.$  (3.) N.  $60^{\circ} E.$  (4.) S.  $49^{\circ} E.$

III. Suppose you steer the following courses by standard compass, find the correct magnetic courses from the curve drawn :—

- (1.) North. (2.) S.S.W.  $\frac{1}{4} W.$  (3.) E. by S.  $\frac{1}{4} S.$  (4.) N.E.  $\frac{1}{2} E.$   
*Answers :—*(1.) N.  $3^{\circ} E.$  (2.) S.  $15^{\circ} W.$  (3.) S.  $59^{\circ} E.$  (4.) N.  $71^{\circ} E.$





| Ship's Head.             | South.   | S.W.     | West.    | N.W.     |
|--------------------------|----------|----------|----------|----------|
| Correct magnetic bearing | N. 2° W. | N. 2° W. | N. 2° W. | N. 2° W. |
| Compass bearing          | N. 3 W.  | N. 1 E.  | N. 9 E.  | N. 12 E. |
| Deviation                | 1 E.     | 3 W.     | 11 W.    | 14 W.    |

## QUESTION 8. LIST B.

From the above Table construct a Napier's curve, and give the courses you will steer by standard compass to make the following courses, correct magnetic.

- |                          |                          |             |                            |
|--------------------------|--------------------------|-------------|----------------------------|
| 1. N.E. $\frac{1}{2}$ E. | 2. W.S.W.                | 3. N.N.W.   | 4. S.S.E.                  |
| 5. N.N.E.                | 6. S. $18\frac{1}{2}$ W. | 7. N. 4° E. | 8. S. $62\frac{1}{2}$ ° E. |

NOTE.—For the method of constructing the curve see No. 239, page 145, and for Rule for finding standard compass courses to steer, see Problem II, Rule LXIII, page 150.

- Answers.—1. N. 40° E.    2. S. 76° W.    3. N.  $14\frac{1}{2}$ ° W.    4. S. 26° E.  
 5. N. 18° E.    6. S. 19° W.    7. N. 5° E.    8. S. 73° E.

## QUESTION 9. LIST B.

Suppose you steer the following courses by the standard compass, find the correct magnetic courses from the curve drawn :—

- |                              |                        |              |             |
|------------------------------|------------------------|--------------|-------------|
| 1. E. by S. $\frac{1}{4}$ S. | 2. E. $\frac{3}{4}$ N. | 3. S. 85° W. | 4. N. 1° E. |
|------------------------------|------------------------|--------------|-------------|

For the Rule for working this Question, see Problem I, Rule LXII, page 149.

- Answer.—1. S.  $65\frac{1}{2}$ ° E.    2. N.  $84\frac{1}{2}$ ° E.    3. N.  $74\frac{1}{2}$ ° W.    4. N.  $1\frac{1}{2}$ ° W.

## QUESTION 10. LIST B.

You have taken the following bearings of distant objects by your standard compass as above, with the ship's head as given, find the correct magnetic bearings. (See Rule LXI, page 148).

| Ship's Head.             | Compass Bearing. | Ship's Head.                | Compass Bearing. |
|--------------------------|------------------|-----------------------------|------------------|
| S.E. by E. ....          | N. 68° E.        | S.S.W. $\frac{1}{2}$ W. ... | N. 4° E.         |
| W. $\frac{1}{4}$ N. .... | S. 54 W.         | N. $\frac{3}{4}$ E. ....    | South            |

|                                      |                        |                     |          |                         |                        |                     |         |
|--------------------------------------|------------------------|---------------------|----------|-------------------------|------------------------|---------------------|---------|
| Ship's head                          | { 7 $\frac{1}{2}$ ° E. | W. $\frac{1}{4}$ N. | { 11° W. | S.S.W. $\frac{1}{2}$ W. | { 1 $\frac{1}{2}$ ° W. | N. $\frac{3}{4}$ E. | { 0° E. |
| S.E. by E. gives                     |                        | gives ..            |          | gives .....             |                        | gives ..            |         |
| Comp. bear. N. 68 E.                 |                        | S. 54 W.            |          | N. 4 E.                 |                        | South 0             |         |
| Corr. mg. br. N. 75 $\frac{1}{2}$ E. |                        | S. 43 W.            |          | N. 2 $\frac{1}{2}$ E.   |                        | South               |         |

## EXAMPLES FOR EXERCISE.

## EXAMPLE I.

I. In the following Table give the correct magnetic bearing of the distant object, and thence the Deviation :—

| Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North ....                       | N. 60° W.                                      |                     | South ....                       | N. 66° W.                                      |                     |
| N.E. ....                        | N. 80 W.                                       |                     | S.W. ....                        | N. 53 W.                                       |                     |
| East ....                        | N. 84 W.                                       |                     | West ....                        | N. 42 W.                                       |                     |
| S.E. ....                        | N. 78 W.                                       |                     | N.W. ....                        | N. 41 W.                                       |                     |

Answer.—Correct Magnetic Bearing of Distant object is N. 63° W.

Deviations:—3° W.; 17° E.; 21° E.; 15° E.; 3° E.; 10° W.; 21° W.; 22° W.

II. From the Table construct a Napier's Curve (a); and give the courses you would steer by the standard compass to make the following courses correct magnetic:—

- (1.) N. by E. (2.) S.W.  $\frac{1}{2}$  W. (3.) E.  $\frac{1}{4}$  N. (4.) N.N.W. (5.) E.S.E. (6.) S.W.  $\frac{1}{2}$  S.  
(7.) N.  $\frac{1}{4}$  E. (8.) W.  $\frac{3}{4}$  S. (9.) N.  $\frac{1}{4}$  W. (10.) S.  $\frac{1}{4}$  W. (11.) E.  $\frac{1}{4}$  S. (12.) E.N.E.

For the method of constructing the Curve see No. 239, page 145; and for the Rule for finding the correct magnetic course see Problem II, Rule LXIII, page 150.

- Answer:—(1.) N.  $8\frac{3}{4}^{\circ}$  E. (2.) S.  $65\frac{3}{4}^{\circ}$  W. (3.) E.N.E. (4.) N.  $12^{\circ}$  W. (5.) S.  $88^{\circ}$  E.  
(6.) S.  $50^{\circ}$  W. (7.) N.  $3\frac{3}{4}^{\circ}$  E. (8.) N.  $75^{\circ}$  W. (9.) North. (10.) S.  $1^{\circ}$  E.  
(11.) N.  $72\frac{1}{2}^{\circ}$  E. (12.) N.  $49\frac{1}{2}^{\circ}$  E.

III. Suppose you have steered the following courses by standard compass, find the correct magnetic courses from the curve drawn:— See Problem I, page 149.

- (1.) N.E. by E. (2.) E.S.E. (3.) S.W. by S. (4.) South. (5.) S.E.  $\frac{1}{2}$  S.  
(6.) W. by N.  $\frac{3}{4}$  N. (7.) S.  $\frac{1}{4}$  W. (8.) E.  $\frac{3}{4}$  N. (9.) W.  $\frac{3}{4}$  S. (10.) N.E. by E.  $\frac{1}{2}$  E.  
(11.) N.W.  $\frac{1}{2}$  N. (12.) S.W.  $\frac{3}{4}$  W.

- Answer:—(1.) N.  $75\frac{3}{4}^{\circ}$  E. (2.) S.  $49\frac{1}{2}^{\circ}$  E. (3.) S.  $27\frac{1}{4}^{\circ}$  W. (4.) S.  $4^{\circ}$  W. (5.) S.  $26^{\circ}$  E.  
(6.) S.  $86^{\circ}$  W. (7.) S.  $5\frac{1}{4}^{\circ}$  W. (8.) S.  $77\frac{1}{2}^{\circ}$  E. (9.) S.  $62^{\circ}$  W. (10.) N.  $82^{\circ}$  E.  
(11.) N.  $60^{\circ}$  W. (12.) S.  $41\frac{3}{4}^{\circ}$  W.

IV. You have taken the following bearings by your standard compass as above; with the ship's head as given, find the correct magnetic bearings:—

| No. | Ship's Head                    | Bearing of Distant Object by Standard Compass. | No. | Ship's Head.                | Bearing of Distant Object by Standard Compass. |
|-----|--------------------------------|--|-----|-----------------------------|--|
| 1   | W.N.W. ....                    | South.   | 5   | N. $\frac{1}{4}$ E. ....    | S. $\frac{1}{4}$ E.                            |
| 2   | S.E. by E. ....                | N.W. by N.                                     | 6   | W. by N. $\frac{1}{2}$ N. . | E. $\frac{1}{2}$ S.                            |
| 3   | N.E. by N. ....                | North.   | 7   | E. $\frac{1}{4}$ N. ....    | E. $\frac{1}{4}$ N.                            |
| 4   | E. by S. $\frac{1}{2}$ S. .... | N.N.W.   | 8   | E. $\frac{3}{4}$ S. ....    | W. by S. $\frac{1}{4}$ S.                      |

- Answer:—(1.) Corr. mag. bear. S.  $24^{\circ}$  E. (2.) N.  $17^{\circ}$  W. (3.) N.  $14^{\circ}$  E. (4.) N.  $3^{\circ}$  W.  
(5.) S.  $3\frac{1}{2}^{\circ}$  E. (6.) N.  $72^{\circ}$  E. (7.) S.  $72^{\circ}$  E. (8.) N.  $84^{\circ}$  W.

### EXAMPLE II.

Ex. I. From the following table find the correct magnetic bearing of the distant object and thence the deviation:—

| Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North ....                       | N. $42^{\circ}$ W.                             |                     | South ....                       | N. $44^{\circ}$ W.                             |                     |
| N.E. ....                        | N. $17^{\circ}$ W.                             |                     | S.W. ....                        | N. $68^{\circ}$ W.                             |                     |
| East. ....                       | N. $9^{\circ}$ W.                              |                     | West ....                        | N. $76^{\circ}$ W.                             |                     |
| S.E. ....                        | N. $17^{\circ}$ W.                             |                     | N. W. ....                       | N. $64^{\circ}$ W.                             |                     |

Answer:—Correct magnetic bearing N.  $42^{\circ}$  W.

Deviation  $0^{\circ}$ ;  $25^{\circ}$  W.;  $33^{\circ}$  W.;  $25^{\circ}$  W.;  $2^{\circ}$  E.;  $26^{\circ}$  E.;  $34^{\circ}$  E.;  $22^{\circ}$  E.

II. From the above Table construct a Napier's curve and give the courses you would steer by standard compass to make the following courses correct magnetic:—

1. N.W.  $\frac{1}{2}$  W. 2. S.E.  $\frac{1}{2}$  S. 3. E.  $\frac{1}{4}$  S. 4. W.  $\frac{3}{4}$  S.

- Answer:—1. N.  $84^{\circ}$  W 2. S.  $24^{\circ}$  E. 3. S.  $58^{\circ}$  E. 4. S.  $53\frac{1}{2}^{\circ}$  W.

III. Suppose you steer the following courses by standard compass, find the correct magnetic course from the curve drawn :—

1. W. by N.  $\frac{3}{4}$  N.    2. South.    3. E. by N.  $\frac{1}{4}$  N.    4. N. by E.  $\frac{3}{4}$  E.  
*Answer* :—1. N.  $39^\circ$  W.    2. S.  $1\frac{3}{4}^\circ$  W.    3. N.  $43\frac{3}{4}^\circ$  E.    4. N.  $7^\circ$  E.

IV. You have taken the following bearings of distant objects by your standard compass as above; with the ship's head as given, find the correct magnetic bearing :—

| Ship's Head.  | Bearing of Distant Object by Standard Compass. | Ship's Head.                | Bearing of Distant Object by Standard Compass. |
|---------------|--|-----------------------------|--|
| S.E. ....     | N. by E. $\frac{1}{2}$ E.                      | W. by S. $\frac{3}{4}$ S... | E. $\frac{1}{2}$ N.                            |
| E. by S. .... | N. by W. $\frac{3}{4}$ W.                      | N.E. $\frac{1}{4}$ E.....   | S.W. $\frac{3}{4}$ S.                          |

*Answer* :—Deviations  $25^\circ$  W.  $32^\circ$  W.;  $32^\circ$  E.;  $26\frac{1}{2}^\circ$  W.

Correct magnetic bearings N.  $80^\circ$  W.; N.  $52^\circ$  W.; S.  $64^\circ$  E.; S.  $10^\circ$  W.

### EXAMPLE III.

I. From the following Table find the correct magnetic bearing of the distant object, and thence the deviation :—

| Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North ....                       | N. $13^\circ$ W.                               |                     | South ....                       | N. $23^\circ$ W.                               |                     |
| N.E. ....                        | N. $35^\circ$ W.                               |                     | S.W. ....                        | N. $2^\circ$ W.                                |                     |
| East .....                       | N. $41^\circ$ W.                               |                     | West ....                        | N. $5^\circ$ E.                                |                     |
| S.E. ....                        | N. $35^\circ$ W.                               |                     | N.W. ....                        | North. ....                                    |                     |

*Answer* :—Correct magnetic bearing, N.  $18^\circ 6'$  W.

Deviations :— $5^\circ$  W.;  $17^\circ$  E.;  $23^\circ$  E.;  $17^\circ$  E.;  $5^\circ$  E.;  $16^\circ$  W.;  $23^\circ$  W.;  $18^\circ$  W.

II. From the above Table construct a Napier's curve, and give the courses you would steer by standard compass to make the following courses correct magnetic :—

1. N.  $\frac{1}{2}$  W.    2. E.  $\frac{1}{2}$  S.    3. N.W. by W.  $\frac{1}{2}$  W.    4. W.  $\frac{1}{4}$  S.  
*Answer* :—1. North.    2. N.  $73^\circ$  E.    3. N.  $44^\circ$  W.    4. N.  $71^\circ$  W.

III. You have steered the following courses by standard compass; find the correct magnetic courses from the curve drawn :—

1. E.  $\frac{1}{2}$  N.    2. S.E.  $\frac{3}{4}$  E.    3. N.  $\frac{3}{4}$  W.    4. S.W.  $\frac{1}{4}$  S.  
*Answer* :—1. S.  $72\frac{1}{2}^\circ$  E.    2. S.  $35^\circ$  E.    3. N.  $16\frac{1}{2}^\circ$  W.    4. S.  $27^\circ$  W.

IV. You have taken the following bearings of distant objects by your standard compass; with the ship's head as given below, find the correct magnetic bearing :—

| Ship's Head.              | Bearing of Distant Object by Standard Compass. | Ship's Head.                 | Bearing of Distant Object by Standard Compass. |
|---------------------------|--|------------------------------|--|
| S.W. $\frac{1}{2}$ S..... | E. $\frac{1}{4}$ S.                            | N.E. $\frac{1}{4}$ N. ....   | W. $\frac{1}{4}$ S.                            |
| North .....               | S.E. $\frac{3}{4}$ S.                          | E. by S. $\frac{1}{2}$ S. .. | E. $\frac{1}{4}$ S.                            |

*Answer* :—Deviations :— $14^\circ$  W.;  $5^\circ$  W.;  $16^\circ$  E.;  $22^\circ$  E.

Correct magnetic bearings, N.  $84^\circ$  E.; S.  $42^\circ$  E.; N.  $77^\circ$  W.; S.  $65^\circ$  E.

## EXAMPLE IV.

I. From the following Table find the correct magnetic bearing of the distant object, and thence the deviation.

| Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North ....                       | N. $87^{\circ}$ E.                             |                     | South ....                       | S. $88^{\circ}$ E.                             |                     |
| N.E. ....                        | N. $71^{\circ}$ E.                             |                     | S.W. ....                        | S. $81^{\circ}$ E.                             |                     |
| East ....                        | N. $70^{\circ}$ E.                             |                     | West ....                        | S. $73^{\circ}$ E.                             |                     |
| S.E. ....                        | N. $82^{\circ}$ E.                             |                     | N.W. ....                        | S. $76^{\circ}$ E.                             |                     |

*Answer* :—Correct magnetic bearing, N.  $89^{\circ}$  E.

Deviations :— $2^{\circ}$  E.;  $18^{\circ}$  E.;  $19^{\circ}$  E.;  $7^{\circ}$  E.;  $3^{\circ}$  W.;  $10^{\circ}$  W.;  $18^{\circ}$  W.;  $15^{\circ}$  W.

II. From the above Table construct a Napier's curve, and give the course you would steer by standard compass to make the following courses correct magnetic :—

1. S.W.  $\frac{3}{4}$  W. 2. North. 3. S.  $45\frac{1}{2}^{\circ}$  E. 4. N.  $48\frac{3}{4}^{\circ}$  E.

*Answer* :—1. S.  $68^{\circ}$  W. 2. N.  $1^{\circ}$  W. 3. S.  $55^{\circ}$  E. 4. N.  $33\frac{1}{4}^{\circ}$  E.

III. You have steered the following courses by standard compass; find the correct magnetic courses from the curve drawn :—

1. E. by N.  $\frac{3}{4}$  N. 2. S.  $72^{\circ}$  E. 3. S.  $76^{\circ}$  W. 4. N.  $26\frac{1}{2}^{\circ}$  W.

*Answer* :—1. S.  $89^{\circ}$  E. 2. S.  $57\frac{1}{2}^{\circ}$  E. 3. S.  $60\frac{1}{2}^{\circ}$  W. 4. N.  $38\frac{1}{4}^{\circ}$  W.

IV. You have taken the following bearings of distant objects by your standard compass as above; with the ship's head as given, find the correct magnetic bearing.

| Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. |
|----------------------------------|--|----------------------------------|--|
| East .....                       | N. $87^{\circ}$ E.                             | W. $\frac{3}{4}$ N. ....         | N. $\frac{1}{4}$ W.                            |
| N.N.W. ....                      | N. $2^{\circ}$ E.                              | N.W. $\frac{1}{4}$ W. ....       | W. $\frac{1}{4}$ S.                            |

*Answer* :—S.  $74^{\circ}$  E.; N.  $9^{\circ}$  W.; N.  $21^{\circ}$  W.; S.  $71^{\circ}$  W.

## EXAMPLE V.

I. In the following Table give the correct magnetic bearing of the distant object, and thence the deviation :—

| Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North ....                       | S. $15^{\circ}$ E.                             |                     | South ....                       | S. $18^{\circ}$ E.                             | 2 $\frac{1}{2}$     |
| N.E. ....                        | S. $34^{\circ}$ E.                             |                     | S.W. ....                        | S. $11^{\circ}$ E.                             |                     |
| East ....                        | S. $31^{\circ}$ E.                             |                     | West ....                        | South  |                     |
| S.E. ....                        | S. $22^{\circ}$ E.                             |                     | N.W. ....                        | S. $3^{\circ}$ W.                              |                     |

*Answer* :—Correct magnetic bearing, S.  $16^{\circ}$  E.

Deviations :— $1^{\circ}$  W.;  $18^{\circ}$  E.;  $15^{\circ}$  E.;  $6^{\circ}$  E.;  $2^{\circ}$  W.;  $5^{\circ}$  W.;  $16^{\circ}$  W.;  $19^{\circ}$  W.

II. From the above Table construct a Napier's curve, and give the course you would steer by standard compass to make the following courses correct magnetic:—

1. N.  $73^\circ$  E.    2. N.  $68^\circ$  W.    3. S.  $87^\circ$  E.    4. S.  $2^\circ$  W.

*Answer*:—1. N.  $54^\circ$  E.    2. N.  $49^\circ$  W.    3. N.  $76^\circ$  E.    4. South.

III. Given the following courses by standard compass to find the correct magnetic courses from the curve drawn:—

1. S.  $84^\circ$  E.    2. N.  $77^\circ$  W.    3. N.  $64^\circ$  E.    4. S.  $5^\circ$  W.

*Answer*:—1. S.  $71^\circ$  E.    2. S.  $85^\circ$  W.    3. N.  $82^\circ$  E.    4. S.  $6^\circ$  W.

IV. You have taken the following bearings of two distant objects by your standard compass as above; with the ship's head N.  $39^\circ$  E.

St. Catherine's Point, N.  $82^\circ$  E.    Needles Light, N.  $8^\circ$  W.

*Answer*:—Deviation for ship's head, N.  $39^\circ$  E., is  $16^\circ$  E.

Correct magnetic bearing of St. Catherine's Point, S.  $82^\circ$  E.; and of the Needles Light, N.  $8^\circ$  E.

#### EXAMPLE VI.

I. From the following Table find the bearing of the distant object, and thence the deviation.

| Ship's Head<br>by<br>Standard<br>Compass. | Bearing of<br>Distant Object<br>by Standard<br>Compass. | Deviation<br>Required. | Ship's Head<br>by<br>Standard<br>Compass. | Bearing of<br>Distant Object<br>by Standard<br>Compass. | Deviation<br>Required. |
|---|---|------------------------|---|---|------------------------|
| North ....                                | North   |                        | South ....                                | N. $3^\circ$ E.   |                        |
| N.E. ....                                 | N. $16^\circ$ E.  |                        | S.W. ....                                 | N. $16^\circ$ W.  |                        |
| East .....                                | N. $24^\circ$ E.  |                        | West ....                                 | N. $23^\circ$ W.  |                        |
| S.E. ....                                 | N. $19^\circ$ E.  |                        | N.W. ....                                 | N. $15^\circ$ W.  |                        |

*Answer*:—Correct magnetic bearing, N.  $1^\circ$  E.

Deviations:— $1^\circ$  E.;  $15^\circ$  W.;  $23^\circ$  W.;  $18^\circ$  W.;  $2^\circ$  W.;  $17^\circ$  E.;  $24^\circ$  E.;  $16^\circ$  E.

II. From the above Table construct a Napier's curve, and give the courses you would steer by the standard compass to make the following courses correct magnetic:—

1. E. by S.    2. W. by S.  $\frac{1}{4}$  S.    3. North.    4. N.  $57\frac{1}{2}^\circ$  W.

*Answer*:—1. S.  $58^\circ$  E.    2. S.  $56^\circ$  W.    3. N.  $1^\circ$  W.    4. N.  $80^\circ$  W.

III. Suppose you steer the following courses by the standard compass, find the correct magnetic courses from the curve drawn:—

1. W.  $\frac{3}{4}$  N.    2. S.S.W.    3. E. by N.  $\frac{1}{2}$  N.    4. South.

*Answer*:—1. N.  $59\frac{1}{2}^\circ$  W.    2. S.  $31\frac{1}{4}^\circ$  W.    3. N.  $52\frac{1}{2}^\circ$  E.    4. S.  $2^\circ$  E.

IV. You have taken the following bearings of distant objects by your standard compass as above; with the ship's head as given, find the correct magnetic bearings:—

| Ship's Head<br>by Standard<br>Compass. | Bearing of Distant<br>Object by<br>Standard Compass. | Ship's Head<br>by Standard<br>Compass. | Bearing of Distant<br>Object by<br>Standard Compass. |
|--|--|--|--|
| S.E. ....                              | N.E. $\frac{1}{2}$ E.                                | S.W. $\frac{3}{4}$ S. ....             | W. $\frac{1}{4}$ N.                                  |
| South .....                            | North.   | E. $\frac{3}{4}$ N. ....               | S. $\frac{1}{4}$ E.                                  |

*Answers*:—Deviations,  $18^\circ$  W.;  $2^\circ$  W.;  $14^\circ$  E.;  $22^\circ$  W.; Correct magnetic bearings, N.  $33^\circ$  E.; N.  $2^\circ$  W.; N.  $73^\circ$  W.; S.  $25^\circ$  E.

## EXAMPLE VII.

I. From the following Table find the correct magnetic bearing of the distant object, and thence the deviation :—

| Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North ....                       | S. 87° W.                                      |                     | South ....                       | N. 84° W.                                      |                     |
| N.E. ....                        | S. 70° W.                                      |                     | S.W. ....                        | N. 77° W.                                      |                     |
| East ....                        | S. 72° W.                                      |                     | West ....                        | N. 68° W.                                      |                     |
| S.E. ....                        | S. 88° W.                                      |                     | N.W. ....                        | N. 72° W.                                      |                     |

*Answer* :—Correct magnetic bearing, N. 88° W.

*Answer* :—Deviations, 1. 5° E. 2. 22° E. 3. 20° E. 4. 4° E. 5. 4° W. 6. 11° W. 7. 20° W. 8. 16° W.

II. From the above Table construct a Napier's curve, and give the Courses you would steer by the standard compass to make the following courses correct magnetic :—

1. N. 79° E. 2. S. 48° E. 3. N. 84° W. 4. S. 42° W.

*Answer* :—1. N. 55° E. 2. S. 55° E. 3. N. 65° W. 4. S. 55° W.

III. Given the following courses steered by standard compass to find the correct magnetic courses from curve drawn :—

1. N. 72° W. 2. N. 84° E. 3. S. 20° W. 4. S. 78° E.

*Answer* :—1. S. 88° W. 2. S. 74° E. 3. S. 13° W. 4. S. 61° E.

IV. You have taken the following bearings of distant objects by your standard compass as above; with the ship's head as given, find the correct magnetic bearing :—

| Ship's Head.   | Bearing of Distant Object by Standard Compass. | Ship's Head.   | Bearing of Distant Object by Standard Compass. |
|----------------|--|----------------|--|
| S. 68° W. .... | N. 82° W.                                      | N. 78° W. .... | S. 3° E.                                       |
| N. 38° E. .... | S. 69° W.                                      | S. 9° E. ....  | N. 78° E.                                      |

*Answer* :—Deviations, 1. 15° W. 2. 21° E. 3. 20° W. 4. 3° W.

Correct magnetic bearings, 1. S. 83° W. 2. West. 3. S. 23° E. 4. N. 75° E.

## EXAMPLE VIII.

I. From the following Table find the correct magnetic bearing of the distant object, and thence the deviation :—

| Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North ....                       | S. 60° E.                                      |                     | South ....                       | S. 67° E.                                      |                     |
| N.E. ....                        | S. 44° E.                                      |                     | S.W. ....                        | East   |                     |
| East ....                        | S. 36° E.                                      |                     | West ....                        | N. 87° E.                                      |                     |
| S.E. ....                        | S. 40° E.                                      |                     | N.W. ....                        | S. 82° E.                                      |                     |

*Answer* :—Correct magnetic bearing, S. 64° E.

*Answer* :—Deviations :—1. 4° W. 2. 20° W. 3. 28° W. 4. 24° W. 5. 3° E. 6. 16° E. 7. 29° E. 8. 18° E.

II. From the above Table construct a Napier's curve, and give the courses you would steer by standard compass to make the following courses correct magnetic :—

1. N.N.W.  $\frac{3}{4}$  W.    2. E. by S.  $\frac{1}{4}$  S.    3. S.W.  $\frac{1}{4}$  W.    4. E.  $\frac{1}{4}$  N.  
*Answer* :—1. N.  $51^{\circ}$  W.    2. S.  $50\frac{1}{2}^{\circ}$  E.    3. S.  $27\frac{1}{2}^{\circ}$  W.    4. S.  $64\frac{1}{2}^{\circ}$  E.

III. Suppose you have steered the following courses by standard compass; find the correct magnetic courses from the curve drawn :—

1. W. by N.  $\frac{1}{2}$  N.    2. N.  $\frac{1}{4}$  E.    3. S.E.  $\frac{3}{4}$  S.    4. S.  $\frac{3}{4}$  W.  
*Answer* :—1. N.  $46\frac{1}{4}^{\circ}$  W.    2. N.  $2^{\circ}$  W.    3. S.  $57\frac{1}{2}^{\circ}$  E.    4. S.  $18\frac{1}{2}^{\circ}$  W.

IV. You have taken the following bearings of distant objects by your standard compass as above; with the ship's head as given, find the correct magnetic bearings :—

| Ship's Head. | Bearing of Distant Object by Standard Compass. | Ship's Head.               | Bearing of Distant Object by Standard Compass. |
|--------------|--|----------------------------|--|
| N.W. ....    | N.E.   | E. $\frac{1}{4}$ N. ....   | N. $\frac{3}{4}$ W.                            |
| S.S.W. ....  | East.  | W. by N. $\frac{1}{4}$ N.. | S. $\frac{1}{2}$ W.                            |

*Answer* :—Deviations :—1.  $18^{\circ}$  E.    2.  $18^{\circ}$  E.    3.  $28^{\circ}$  W.    4.  $27^{\circ}$  E.

Correct magnetic bearings :—1. N.  $63^{\circ}$  E.    2. S.  $72^{\circ}$  E.    3. N.  $36^{\circ}$  W.    4. S.  $33^{\circ}$  W.

### EXAMPLE IX.

I. From the following Table, find the correct magnetic bearing of the distant object, and thence the deviation :—

| Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North ....                       | S. $44^{\circ}$ E.                             |                     | South ....                       | S. $38^{\circ}$ E.                             |                     |
| N.E. ....                        | S. $50^{\circ}$ E.                             |                     | S.W. ....                        | S. $16^{\circ}$ E.                             |                     |
| East. ....                       | S. $58^{\circ}$ E.                             |                     | West ....                        | S. $21^{\circ}$ E.                             |                     |
| S.E. ....                        | S. $59^{\circ}$ E.                             |                     | N.W. ....                        | S. $34^{\circ}$ E.                             |                     |

*Answer* :—Correct magnetic bearing, S.  $40^{\circ}$  E.

*Answer*.—Deviations :—1.  $4^{\circ}$  E.    2.  $10^{\circ}$  E.    3.  $18^{\circ}$  E.    4.  $19^{\circ}$  E.    5.  $2^{\circ}$  W.  
 6.  $24^{\circ}$  W.    7.  $19^{\circ}$  W.    8.  $6^{\circ}$  W.

II. From the above table construct a Napier's curve, and give the courses you would steer by standard compass to make the following courses correct magnetic .—

1. E.  $\frac{3}{4}$  S.    2. S.  $\frac{1}{2}$  E.    3. W. by S.  $\frac{3}{4}$  S.    4. N.  $\frac{1}{4}$  W.  
*Answer* :—1. N.  $82^{\circ}$  E.    2. S.  $8\frac{1}{2}^{\circ}$  E.    3. West.    4. N.  $5^{\circ}$  W.

III. Suppose you steer the following courses by standard compass, find the correct magnetic courses from the curve drawn :—

1. S.W. by W.  $\frac{3}{4}$  W.    2. N.  $5^{\circ}$  W.    3. S.  $8^{\circ}$  E.    4. N.  $80\frac{1}{2}^{\circ}$  E.  
*Answer* :—1. S.  $40^{\circ}$  W.    2. N.  $\frac{1}{4}$  W.    3. S.  $5^{\circ}$  E.    4. S.  $83\frac{1}{2}^{\circ}$  E.

IV. You have taken the following bearings of distant objects by your standard compass as above; with the ship's head as given, find the correct magnetic bearings.

| Ship's Head.  | Compass Bearing.      | Ship's Head.              | Compass Bearing.          |
|---------------|-----------------------|---------------------------|---------------------------|
| E.N.E. ....   | E.S.E.                | E. $\frac{3}{4}$ S. ....  | W. $\frac{1}{4}$ N.       |
| S.W. by W. .. | S.E. $\frac{1}{2}$ S. | W. by N. $\frac{1}{4}$ N. | E. by N. $\frac{3}{4}$ N. |

*Answer*.—Deviations :—1.  $13\frac{1}{2}^{\circ}$  E.    2.  $25^{\circ}$  W.    3.  $19\frac{1}{2}^{\circ}$  E.    4.  $16^{\circ}$  W.

Correct magnetic bearings :—1. S.  $54^{\circ}$  E.    2. S.  $64^{\circ}$  E.    3. N.  $67\frac{1}{2}^{\circ}$  W.    4. N.  $54^{\circ}$  E.



## EXAMPLE X.

I. From the following table find the correct magnetic bearings of the distant object, and thence the deviation.

| Ship's head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North ....                       | West.  |                     | South ....                       | S. 86° W.                                      |                     |
| N.E. ....                        | S. 78° W.                                      |                     | S.W. ....                        | N. 89° W.                                      |                     |
| East ....                        | S. 77° W.                                      |                     | West ....                        | N. 81° W.                                      |                     |
| S.E. ....                        | S. 82° W.                                      |                     | N.W. ....                        | N. 79° W.                                      |                     |

*Answer* :—Correct magnetic bearing S. 88° W.

*Answer*.—Deviation:—1. 2° W. 2. 10° E. 3. 11° E. 4. 6° E. 5. 2° E. 6. 3° W. 7. 11° W. 8. 13° W.

II. Given the correct magnetic course, to find the courses to steer by standard compass:—

1. S. 87° E. 2. S. 83° W. 3. N. 8° W. 4. N. 57½° E.

*Answer*.—1. N. 81½° E. 2. N. 85½° W. 3. N. 4½° W. 4. N. 47° E.

III. Given courses by standard compass, to find correct magnetic:—

1. N. 85° E. 2. N. 86° W. 3. N. 63½° E. 4. S. 9° W.

*Answer*.—1. S. 83½° E. 2. S. 82° W. 3. N. 75½° E. 4. S. 9¾° W.

IV. You have taken the following bearings of distant objects by standard compass with ship's head as given below, find the correct magnetic bearing:—

| Ship's Head.   | Compass Bearing. | Ship's Head.   | Compass Bearing. |
|----------------|------------------|----------------|------------------|
| N. 12° E. .... | S. 75° E.        | S. 47° E. .... | S. 87° E.        |
| N. 86° W. .... | S. 3° W.         | S. 16° W. .... | S. 88° W.        |

*Answer*.—Deviations:—1. 2½° E. 2. 11½° W. 3. 5½° E. 4. 0°.

Correct magnetic bearings:—1. N. 77½° E. 2. S. 8½° E. 3. S. 81½° E. 4. S. 88° W.

## EXAMPLE XI.

I. From the following Table find the correct magnetic bearing of the distant object, and thence the deviation:—

| Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North ....                       | S. 17° W.                                      |                     | South ....                       | S. 12° W.                                      |                     |
| N.E. ....                        | South.   |                     | S.W. ....                        | S. 31° W.                                      |                     |
| East ....                        | S. 5° E.                                       |                     | West ....                        | S. 35° W.                                      |                     |
| S.E. ....                        | South.   |                     | N.W. ....                        | S. 30° W.                                      |                     |

*Answer*.—Correct magnetic, S. 15° W.

*Answer*.—Deviations:—1. 2° W. 2. 15° E. 3. 20° E. 4. 15° E. 5. 3° E. 6. 16° W. 7. 20° W. 8. 15° W.

II. From the above Table construct a Napier's curve and give the courses you would steer by standard compass to make the following courses correct magnetic :—

1. E.  $\frac{3}{4}$  S.      2. S.  $\frac{3}{4}$  W.      3. N.  $14\frac{3}{4}^\circ$  W.      4. S.  $44^\circ$  E.  
*Answer.*—1. N.  $78\frac{1}{2}^\circ$  E.      2. S.  $10^\circ$  W.      3. N.  $9\frac{1}{4}^\circ$  W.      4. S.  $62\frac{1}{2}^\circ$  E.

III. Suppose you steer the following courses by standard compass, find the correct magnetic courses from the curve drawn :—

1. W.  $\frac{3}{4}$  N.      2. N.E.  $\frac{1}{2}$  E.      3. N.  $78^\circ$  E.      4. S.  $11\frac{1}{4}^\circ$  W.  
*Answer.*—1. W. by S.      2. N.  $67^\circ$  E.      3. S.  $82^\circ$  E.      4. S.  $9^\circ$  W.

IV. You have taken the following bearings of distant objects by your standard compass as above; with the ship's head as given find the correct magnetic bearing :—

| Ship's Head.              | Compass Bearing. | Ship's Head.                   | Compass Bearing.          |
|---------------------------|------------------|--------------------------------|---------------------------|
| N. by W. $\frac{1}{2}$ W. | S. $3^\circ$ W.  | W. by S. $\frac{3}{4}$ S. ..   | N. $\frac{3}{4}$ E.       |
| S.W. by W. ....           | S. $86^\circ$ E. | E. by S. $\frac{1}{4}$ S. .... | E. by N. $\frac{1}{4}$ N. |

*Answer.*—Deviations :—1.  $8^\circ$  W.    2.  $18\frac{1}{2}^\circ$  W.    3.  $21^\circ$  W.    4.  $21^\circ$  E.

Correct magnetic bearings :—1. S.  $5^\circ$  E.    2. N.  $75\frac{1}{2}^\circ$  E.    3. N.  $12\frac{1}{2}^\circ$  W.    4. S.  $83^\circ$  E.

### EXAMPLE XII.

I. From the following Table find the correct magnetic bearing of the distant object, and thence the deviation :—

| Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North ....                       | S. $3^\circ$ W.                                |                     | South ....                       | S. $1^\circ$ E.                                |                     |
| N.E. ....                        | S. $1^\circ$ E.                                |                     | S.W. ....                        | S. $13^\circ$ W.                               |                     |
| East. ....                       | S. $9^\circ$ E.                                |                     | West ....                        | S. $15^\circ$ W.                               |                     |
| S.E. ....                        | S. $12^\circ$ E.                               |                     | N.W. ....                        | S. $8^\circ$ W.                                |                     |

*Answer.*—Correct magnetic bearing S.  $2^\circ$  W.

*Answer.*—Deviations :—1.  $1^\circ$  W.    2.  $3^\circ$  E.    3.  $11^\circ$  E.    4.  $14^\circ$  E.    5.  $3^\circ$  E.    6.  $11^\circ$  W.  
 7.  $13^\circ$  W.    8.  $6^\circ$  W.

II. Given the correct magnetic courses, to find the courses to steer by standard compass :—

1. N.  $41^\circ$  W.      2. N.  $66^\circ$  E.      3. S.  $39^\circ$  E.      4. S.  $79^\circ$  W.

*Answer.*—1. N.  $36\frac{1}{2}^\circ$  W.      2. N.  $60^\circ$  E.      3. S.  $54^\circ$  E.      4. N.  $88\frac{1}{4}^\circ$  W.

III. Suppose you steer the following courses by standard compass, find the correct magnetic bearings :—

1. N.  $32\frac{1}{2}^\circ$  W.      2. S.  $70^\circ$  W.      3. S.E. by E.  $\frac{1}{2}$  E.      4. N.  $31^\circ$  W.

*Answer.*—1. N.  $37^\circ$  W.      2. S.  $55\frac{1}{2}^\circ$  W.      3. S.  $47\frac{1}{2}^\circ$  E.      4. N.  $35^\circ$  W.

IV. You have taken the following bearing of distant objects by standard compass; with the ship's head as given below, find the correct magnetic bearings :—

| Ship's Head.             | Compass Bearing.                          | Ship's Head.          | Compass Bearing.                      |
|--------------------------|---|-----------------------|---------------------------------------|
| S. $\frac{3}{4}$ E. .... | Dungeness.<br>N.E. by E. $\frac{1}{2}$ E. | S. $65^\circ$ W. .... | Beachy Head.<br>N.W. $\frac{1}{2}$ W. |

*Answer.*—Deviations :—1.  $6^\circ$  E. ; 2.  $14^\circ$  W. ; and correct magnetic bearings, 1. N.  $68^\circ$  E. ;  
 2. N.  $64\frac{1}{2}^\circ$  W.

## THE TRAVERSE TABLE.

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243. In all collections of tables for the use of navigators there is inserted a table containing the *true difference of latitude and departure*, corresponding to certain *distances* (at intervals of one mile) up to 300 nautical miles, for every course, at intervals of a quarter point, and also of degrees, from  $0^\circ$  to a right angle ( $90^\circ$ ). Tables I and II (Raper or Norie).

In these Tables the *course* is found at the top of the Table, when under 4 points or  $45^\circ$ ; but at the bottom of the Table, when it exceeds 4 points or  $45^\circ$ . The first column contains the *distance* to 60 miles, the second column contains the *difference of latitude*, expressed in minutes and tenths, and the third column, similarly expressed, contains the *departure*; but if the course exceeds 4 points or  $45^\circ$ , the second column contains the *departure*, and the third column the *difference of latitude*. The other columns are a continuation of the former, exactly upon the same principle, and extending to 300 miles of distance.\* (See Tables I and II, Norie or Raper.)

### USE OF THE TABLE.

244. Given the course and distance, to find the difference of latitude and departure.

### RULE LXVI.

*With the Course open the Tables, and under or above the proper number of points (or degrees) and opposite the distance, will be found the difference of latitude and departure.*

*Obs.*—When the course is found at the bottom of the page, care must be taken to see that the diff. of lat. and the dep. are taken from the proper column *above* the words *departure* and *diff. lat.* It must be carefully remembered that when the course is *less* than 4 points or  $45^\circ$ , the *diff. lat. exceeds the dep.*; but when it is *more* than 4 points or  $45^\circ$  the *dep. exceeds the diff. lat.*

### EXAMPLES.

Ex. 1. A ship sails N.W.  $\frac{1}{2}$  N. a distance of 78 miles: required the difference of latitude and departure by inspection.

The given course is  $3\frac{1}{2}$  points; and referring to Table I we find the page assigned to this course to be page 14, Norie, or page 436, Raper's Navigation, in which against 78, in column headed *Dist.*, stands 60.3 under the head *Lat.*, and 49.5 under the head *Dep.* We conclude, therefore, that for the given course and distance, the difference of latitude is 60.3 miles, and the departure 49.5 miles.

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\* This table is constructed by solving a right-angled triangle, of which one angle represents the course, and the hypotenuse the distance; by giving these different and successive values, the corresponding values of the other two sides are found, which sides represent the true difference of latitude and departure. Inasmuch as the sine of an angle is the cosine of its complement, it is evident that the difference of latitude and departure for any course are the departure and difference of latitude for the complement of that course, and hence the table is compactly arranged by interchanging the headings of the columns containing these elements at the top and at the bottom of the page, and using the top reading for courses from  $0^\circ$  to  $45^\circ$ , and the bottom reading for courses from  $45^\circ$  to  $90^\circ$ . This table may be used for a great number of problems depending for their solution on the relation of the several parts of a right-angled triangle, and, since all the relations between any two quantities may be expressed as functions of some angle in terms of the sine, cosine, or tangent; it may be used, in fact, as a general proportional table.

Ex. 2. Suppose the course to be  $5\frac{1}{2}$  points, and the distance 98 miles.

Then, since the course here exceeds four points, we look for it at the foot of the page (page 10, Norie. or 432, Raper), and against 98 in the *distance* column we find in the adjacent column (marked at the bottom dep. and diff. lat.) *dep.* 86.4, and *diff. lat.* 46.2, so that the difference of latitude made is 46.2, and the departure 86.4.

Ex. 3. Course N.E. by N., distance 129 miles: find diff. lat. and dep.

Enter Table I, and find 3 points at the top, and in one of the columns marked *Dist.* find the distance 129, then in the columns opposite to this, marked *lat.* and *dep.* at top, stands the difference of latitude 107.3, and departure 71.7.

Ex. 4. Course E. by N.  $\frac{1}{2}$  N., distance 264 miles: find diff. of lat. and dep.

Open Table I at  $6\frac{1}{2}$  points, found at the bottom, and opposite the distance 264 stands departure 252.6, and difference of latitude 76.6.

Ex. 5. A ship sails N.  $40^\circ$  E., 50 miles: required the diff. of lat. and departure.

The course being less than  $45^\circ$ , is found at the top, and the distance being under 60 miles, is found in the left hand column; therefore, on the page (56 Norie) is  $40^\circ$  at the top, and opposite to 50 in the distance column (marked *Dist.*) is 38.3 *under Lat.*, and 32.1 *under Dep.*, the difference of latitude and departure required.

Ex. 6. A ship sails N.  $64^\circ$  W., 175 miles: required the diff. of lat. and departure.

The course being more than  $45^\circ$ , is found at the bottom, in page 42, and opposite to the distance 175 miles, is 76.7 *over Lat.*, and 157.3 *over Dep.*, which was required.

(a) To find diff. lat. and dep. when there are tenths in the distance.

*Take the distance as an entire number of miles, i.e., as a whole number, and find the corresponding diff. lat. and dep., from each of which cut off the right hand figure, or tenths, and remove the decimal point one place to the left hand, which will give the required diff. lat. and dep. in miles, and tenths of a mile.\* The tenths, however, must be increased by 1, if the figure cut off is 5, or upwards.*

#### EXAMPLES.

Ex 1. Course  $3\frac{1}{2}$  points, distance 20.3; required the diff. lat. and dep. corresponding thereto.

With course  $3\frac{1}{2}$  points, and dist. 20.3, taken as 203, we get the diff. of lat. 156.9, dep. 128.8; now cut off the right hand figure of each (the 9 and 8), and shifting the decimal point one place to the left, we have diff. lat. 15.7, and dep. 12.9. It will be observed that the tenths are increased by 1, in each case, as the figures cut off in both cases exceeds 5.

Ex. 2. Required the diff. lat. and dep. corresponding to course  $4\frac{1}{2}$  points, and dist. 24.3 miles.

With course  $4\frac{1}{2}$  points, and dist. 24.3 (as 243 miles), we find diff. lat. 154.2, and dep. 187.8: hence we obtain, after dropping the tenths, and removing the decimal point in each one place to the left, 15.4, and 18.8, for the required quantities. The tenths in the dep., it will be observed, are increased by 1, since the figure dropped exceeds 5.

Ex. 3. A ship sails E.N.E., distance 29.5; find diff. of lat. and dep. corresponding.

In this case take out for distance 295. Thus, for 6 points and distance—

$$295 = 112.9 \text{ diff. lat., } 272.5 \text{ dep.}$$

$$\therefore 29.5 = 11.3 \text{ diff. lat., } 27.3 \text{ dep.}$$

After dropping the tenths, and removing the decimal point one place to the left, we have diff. lat. 11.3 and dep. 27.3.

\* The reason of this rule is that the Traverse Table is entered with a distance *ten times* as great as the given distance, and the resulting diff. lat. and dep. is divided by ten. This is done by merely imagining the decimal point to be removed one place to the *right* before entering the table, and then one place to the *left* after taking out the results (see p. 26, (10).

Ex. 4. N. 3 pts. W., and dist. 20·6 miles (as 206), give diff. lat. 171·3, and dep. 114·4; dropping the tenths in each case (the 3 and the 4), and shifting the decimal point one place to the left, we get diff. lat. 17·1 N., and dep. 11·4 W.

Ex. 5. N. 65° E., and dist. 21·5 (as 215), give diff. lat. 90·9, and dep. 194·9, which is diff. lat. 9·1 N., and 19·5 E. It will be observed that the tenths are increased by 1, in each case, as the figure dropped exceeds 5.

(b) If the distance exceeds the limits of the Traverse Table.

Take the half, the third, &c., so as to bring it within the limits, taking care to multiply the corresponding quantities by 2, 3, &c.

Ex. 6. Let the course be  $3\frac{1}{4}$  points, and distance 435: required the corresponding diff. lat. and dep.

435 divided by 3 gives 145.

Course  $3\frac{1}{4}$  points, and dist. 145 give diff. lat. 116·5 and dep. 86·4

$\times 3$                        $\times 3$

Diff. lat. 349·5    Dep. 259·2

If the distance had been 43·5, the diff. lat. would have been 35·0, and the dep. 25·9.

(c) But when the distance is between 300 and 600 we may proceed as follows:—

Take out diff. of lat. and dep. for 300, and for the excess of 300; take the sum of the quantities thus found, cut off the last figure, and remove the decimal point as before.

Ex. 7. Course  $5\frac{3}{4}$  points, and distance 526: required the corresponding diff. of lat. and departure.

Course  $5\frac{3}{4}$  points, and dist. 300, give diff. lat. 128·3, and dep. 271·2

|     |       |       |
|-----|-------|-------|
| 226 | 96·6  | 204·3 |
| 526 | 224·9 | 475·5 |

If the distance were 52·6 we should proceed as above, and then cutting off the last figure of each, and removing the decimal point one place to the left, the diff. of lat. is 22·5, and dep. 47·6. The tenths are increased by 1, in each case, as the figure cut off in one exceeds 5, and in the other amounts to 5.

Ex. 8. Find from the Table the diff. lat. and dep. for 485·7 on a N. 37° W. course.

Course N. 37° W.

| Dist. | Diff. lat. | Dep.  |
|-------|------------|-------|
| 300   | 239·6      | 180·5 |
| 185   | 147·7      | 111·3 |
| 7     | 6          | 4     |
| 485·7 | 387·9      | 292·2 |

The decimal 7 we take out as 7, which gives diff. lat. 5·6 and dep. 4·2, and shifting the decimal point in each one place to the left we have for diff. lat. 0·6, and for the dep. 0·4.

### EXAMPLES FOR PRACTICE.

In each of the following examples find the difference of latitude and departure corresponding to the given course and distance.

| Given |                             |       | Given |           |       |
|-------|-----------------------------|-------|-------|-----------|-------|
| No.   | Course.                     | Dist. | No.   | Course.   | Dist. |
| 1.    | S.S.E.                      | 30    | 8.    | S. 72° W. | 35    |
| 2.    | E. by S.                    | 48    | 9.    | N. 21 W.  | 24·5  |
| 3.    | S.W. $\frac{1}{4}$ S.       | 136   | 10.   | S. 65 W.  | 25·7  |
| 4.    | W. $\frac{3}{4}$ N.         | 84    | 11.   | S. 80 W.  | 14·7  |
| 5.    | S.E. by E. $\frac{1}{4}$ E. | 56    | 12.   | N. 27 W.  | 30·6  |
| 6.    | S.W. $\frac{1}{4}$ W.       | 225   | 13.   | W. 10 S.  | 42·8  |
| 7.    | E. by N. $\frac{1}{4}$ N.   | 183   | 14.   | N. 18 W.  | 34·9  |

245. Given the difference of latitude and departure, to find the course and distance.

### RULE LXVII.

*Seek in the traverse Table (Table II) till the diff. lat. and dep., or the quantities agreeing most nearly with them, are found opposite each other in the proper columns; to the left or abreast of the quantities thus found, and under "Dist." will be the distance made good; and the Course (in degrees) must be taken from the top of the page when diff. lat. is greater than the dep.; but from the bottom of the page when the dep. is greater than the diff. lat.*

*The Course will have the same name (from N. or S. towards E. or W.) as the diff. lat. and dep. made good.*

NOTE.—Always seek for the larger of the two given numbers in the column next the distance, viz., the column marked "Diff. Lat." at the top, and examine page after page, until the smaller number is found by its side in the column marked "Dep." at the top; being careful to remember that when diff. lat. is greater than the dep. the course will be at the top; otherwise it is to be found at the bottom.

(a) When the diff. lat. and dep. on two successive pages of the Traverse Table, appear to be equally near the given diff. lat. and dep., neither page giving values actually corresponding to them, take a course midway between those on the two successive pages as the course actually made good.

(b) If the difference of latitude and departure, or any of the sides of the proposed triangle, should exceed the limits of the Traverse Table, they may be divided by any number that will bring them within these limits, and then the results from the Table multiplied by the same number will give the required parts of the proposed triangle; observing that the *angle or course must in no case be multiplied or divided*, because the course will be the same, whether determined to the whole difference of latitude or departure, or by using an aliquot part of the same.

### EXAMPLES.

Ex 1. A ship having sailed between the N. and E., until her difference of latitude is 199 miles, and the departure 144.6; required her course and distance.

In page 52, Norie, or page 474, Raper, these quantities will be found to correspond with 246 in the distance column, and with the angle  $36^\circ$  found at the top of the Table (the diff. lat. being greater than dep.); the course is therefore N.  $36^\circ$  E., and distance 246 miles.

Ex. 2. A ship has made upon one course 36 miles diff. lat. to the northward, and 58 miles dep. to the westward; required the course and distance run.

Look for 58 and 36 in two adjoining columns marked "diff. lat." and "dep." at the top. In the table will be found 57.7 and 36.0 abreast of each other. In the same line at the dist. column will be found 68, the distance sought. As 58, the dep., is greater than diff. lat. 36, the course is taken from the bottom of the page. It is  $58^\circ$ . As the ship has gone to the N. and W., the course she has made is N.  $58^\circ$  W.

Ex. 3. A ship having sailed between S. and W. until her difference of latitude is 40 miles, and her departure 139.4 miles; required the course and distance.

In page 32, Norie, or page 454, Raper, the course answering to diff. latitude 40 miles, and departure 139.4 miles, corresponds with the angle  $74^\circ$ , at the bottom of the Table, and opposite the distance 145 miles; the course is therefore S.  $74^\circ$  W., and distance 145 miles, which were required.

Ex. 4. Given the diff. lat. 240°0 S. and dep. 208°6 E.: required the corresponding course and distance. (See Rule LXVII (b), page 170).

As both diff. lat. and dep. exceed the limits of the table divide them by 2, so as to bring them within these limits, thus:—

| D. Lat. | Dep.    |
|---------|---------|
| 2)240°2 | 2)208°8 |
| 120°1   | 104°4   |

Then seeking for 120°1 and 104°4 in two adjoining columns marked "diff. lat." and "dep." at the top. In the table are found 120°0 and 104°3 abreast of each other. In the same line in the distance column will be found 159, which must be multiplied by 2 (the number the diff. lat. and dep. were divided by), the product 318 is the distance sought. As 120°1, the diff. lat., is greater than the dep., the course is taken from the top of the page. It is 41°. As the ship has gone to the S. and E., the course she has made is S. 41° E.

### EXAMPLES FOR PRACTICE.

In each of the following examples the difference of latitude and departure are given to find the corresponding course and distance.

| No. | Given      |          | No. | Given      |          |
|-----|------------|----------|-----|------------|----------|
|     | Diff. Lat. | Dep.     |     | Diff. Lat. | Dep.     |
| 1.  | 72°7 S.    | 25°0 E.  | 6.  | 37°9 N.    | 36°4 E.  |
| 2.  | 72°3 N.    | 171°7 E. | 7.  | 53°3 S.    | 76°0 W.  |
| 3.  | 64°0 N.    | 146°9 W. | 8.  | 160°7 S.   | 16°5 W.  |
| 4.  | 98°6 S.    | 37°5 E.  | 9.  | 172°6 S.   | 7°9 W.   |
| 5.  | 415°6 N.   | 240°0 W. | 10. | 164°2 N.   | 262°8 E. |

## TRAVERSE SAILING.

246. TRAVERSE SAILING is the case in plane sailing when the ship makes several courses in succession, the track being zigzag, and the direction of its several parts "traversing," or lying more or less athwart of each other. For all these actual courses and distances run on each, a single equivalent imaginary course and distance may be found, which the ship would have described had she sailed direct for the place of destination. Finding this course is called "Working a Traverse."

In order to do this, the difference of latitude and departure for each distinct course must be found, and the aggregate of the several differences of latitude and departure taken for the single difference of latitude and departure which would be made by sailing from the place left to that reached on a single course. The determination of this course, and the corresponding distance, is then to be effected.\*

\* The plane sailing formula—

$$\text{Dep.} = \text{Dist.} \times \text{Sine course (1).}$$

$$\text{D. Lat.} = \text{Dist.} \times \text{Cos. course (2).}$$

give for each course and distance the corresponding departure and difference of latitude; and taking the algebraic sum of all the diff. lats. and dep., we get the course from formula

$$\text{Tang. course} = \frac{\text{Dep.}}{\text{D. Lat.}}$$

and then the distance from formulæ (1) and (2). The *Traverse Table* is used to obviate the necessity of computations.

247. In resolving a traverse, it is usual to take the diff. lat. and the dep. due to each of the component courses from the traverse table; hence we proceed by the following

### RULE LXVIII.

1°. Draw out a form similar to that given in the example following.

2°. In the column headed Courses, enter each course in succession; and in column Dist., enter the distance run on each course.

In entering the Courses in the appropriate column, reckon, in each case, the points, and fractional parts of a point, from the North or South, whichever is nearest, and write them down as in the following example.

3°. Take out of the Traverse Tables (Table I or II, Raper or Norie), the difference of latitude and departure to each course and distance, and enter the latitude in column N. or S., and the departure in column E. or W., according to the name of the course.

Thus, if the course is S.E. by S., the difference of latitude must be entered in the column S., and the departure in the column E.; if the course is W.  $\frac{1}{4}$  N., the difference of latitude must be entered in the column N., and the departure in the column W.

3a. When the course is exactly North or South, the distance and diff. lat. are the same, there is no departure, and the whole distance is entered as difference of latitude in the corresponding column N. or S., as the case may be: so also when the course is due East or West, the departure is indential with the distance, there is no difference of latitude, and the whole distance run is entered as departure in the E. or W. column. (See pages 173—174, Exs. 2 and 3).

4°. Add the diff. of lats. in each column, and write the sum at the bottom of each, write the less of the two sums under the greater, and take their difference. Do the same with the departure.

5°. These differences are the diff. lat. and dep. made good on the whole and each takes the name of the column it stands in.

6°. The course and distance are then found by Rule LXVII, page 170.

NOTE.—(a). When there is no resulting departure the Traverse Table need not be referred to, as the ship has returned to the same meridian, and the course made good is North (N.) or South (S.), according as the diff. lat. is North or South, and the distance is equal to the diff. lat. (See example 5, page 175).

(b) Similarly, when there is no resulting difference of latitude, the course made good will be either East (E.) or West (W.) as the departure made good is East or West, and the distance will be of equal value with the difference of departures. See Ex. 4, page 174.

(c). Should the difference of latitudes and also the departures balance each other, in which case the ship will have made good neither difference of latitude nor departure, the vessel must be considered to have returned to the place from which she set out.

It may be advisable for a beginner, before he proceeds to take out the quantities from the Traverse Tables, to write a *dash* in all the places *not* to be occupied by a difference of latitude or departure, in order to avoid writing a quantity in the wrong column. Such helps, however, are useless to an expert computer.



Ex. 1. A ship from the Dudgeon Light, in lat.  $53^{\circ} 19' N.$ , sails S.S.E.  $\frac{1}{4} E.$ , 8 miles; E.N.E., 23 miles; N.W. by W.  $\frac{1}{2} W.$ , 36 miles; E.  $\frac{3}{4} N.$ , 48 miles; and N.W.  $\frac{1}{2} W.$ , 46 miles: required the latitude arrived at, also the course and distance made good.

| COURSES.   | DIST. | DIFF. LAT. |     | DEPARTURE. |      |
|--|-------|------------|-----|------------|------|
|  |       | N.         | S.  | E.         | W.   |
| S.S.E. $\frac{1}{4}$ E. . . = S. $2\frac{1}{4}$ E.*  | 8     | —          | 7'2 | 3'4        | —    |
| E.N.E. . . = N. 6 E.   | 23    | 8'8        | —   | 21'3       | —    |
| N.W. by W. $\frac{1}{2}$ W. = N. $5\frac{1}{2}$ W.   | 36    | 17'0       | —   | —          | 31'8 |
| E. $\frac{3}{4}$ N. . . = N. $7\frac{1}{2}$ E.   | 48    | 7'0        | —   | 47'5       | —    |
| N.W. $\frac{1}{2}$ W. . . = N. $4\frac{1}{2}$ W.   | 46    | 29'2       | —   | —          | 35'6 |
| * The courses are given in this double form merely as an illustration of the method of using them. |       | 62'0       | 7'2 | 72'2       | 67'4 |
|  |       | 7'2        | —   | 67'4       | —    |
|  |       | 54'8       | —   | 4'8        | —    |

*Explanation.*—The courses and distances are entered in their proper columns, in the same order as they stand in the question; then in Traverse Table I, Norie or Raper, turn to the page with 2½ points—which is found at the top, the course being less than 4 points—run the finger down the Dist. column till you come to 8, by the side of which stands 7°2 in Diff. lat. column, and 3°4 in Dep. column. Diff. lat. 7°2 is entered in the S. column, and Dep. 3°4 in the E. column, because the course is S. and E. (South and East). Next turn to the page of the Traverse Table with 6 points—found at the bottom, because more than 4 points—look for the distance 23, from the side of which take out Dep. 21°2, and Diff. lat. 8°8, which are entered under N. and E., because the course is N. and E. Proceed in a similar manner with the remaining courses.

The sum of the respective columns, N., S., E., and W., is next found, and set down at the bottom of each column, and the difference between the Northing, viz., 62°0, and the Southing, viz., 7°2, is taken, which leaves 54°8 N., which is the Diff. lat. made; the difference between the Easting 72°2, and Westing 67°4, leaves 4°8 E., departure.

We proceed in the next place to find the course and distance made good, thus :—

In Traverse Table II.  $\left\{ \begin{array}{l} \text{Diff. lat. } 54^{\circ} 8' \text{ N.} \\ \text{and Dep. } 4^{\circ} 8' \text{ E.} \end{array} \right\}$  give  $\left\{ \begin{array}{l} \text{Course N. } 5^{\circ} \text{ E.} \\ \text{Dist. } 55 \text{ miles.} \end{array} \right\}$  made good.

This is an illustration of the remark, that when the diff. lat. is more than the dep., the course is less than 4 points, or  $45^\circ$ , (see No. 141, page 89) and it is named from the N. towards the E., since the diff. lat. is N. and the dep. E.

|  |            |  |
|--|------------|--|
| Lat. left (or sailed from) Dudgeon Light | 53° 19' N. | } Lat. in is found according to<br>Rule XLVI, page 93. |
| Diff. lat. 54·8 . . . . .                | = 55 N.    |  |
| Lat. in (or arrived at) . . . . .        | 54 14 N.   |  |

Ex. 2. A ship from Cape Espichel, in lat.  $38^{\circ} 25' N.$ , sails as follows: S.W. by W., 28 miles; W. by N., 55 miles; West, 47 miles; S.E.  $\frac{3}{4}$  S., 25 miles; South, 101 miles; W.  $\frac{3}{4}$  S., 72 miles: required the latitude in, also the course and distance made good.

| COURSES.                                    | DIST. | DIFF. LAT.      |                                     | DEPARTURE.      |                                     |
|---|-------|-----------------|-------------------------------------|-----------------|-------------------------------------|
|   |       | N.              | S.                                  | E.              | W.                                  |
| S. 5 W. . . . .                             | 28    | —               | 15 <sup>6</sup>                     | —               | 23 <sup>3</sup>                     |
| N. 7 W. . . . .                             | 55    | 10 <sup>7</sup> | —                                   | —               | 53 <sup>9</sup>                     |
| W.* . . . .                                 | 47    | —               | —                                   | —               | 47 <sup>0</sup>                     |
| S. 3 <sup>1</sup> / <sub>4</sub> E. . . . . | 25    | —               | 20 <sup>1</sup>                     | 14 <sup>9</sup> | —                                   |
| S.* . . . .                                 | 101   | —               | 101 <sup>0</sup>                    | —               | —                                   |
| S. 7 <sup>1</sup> / <sub>4</sub> W. . . . . | 72    | —               | 10 <sup>6</sup>                     | —               | 71 <sup>2</sup>                     |
| * See Rule LXVIII, 3a,<br>page 172.         |       | 10 <sup>7</sup> | 147 <sup>3</sup><br>10 <sup>7</sup> | 14 <sup>9</sup> | 195 <sup>4</sup><br>14 <sup>9</sup> |
|   |       |                 | 136 <sup>6</sup>                    |                 | 180 <sup>5</sup>                    |
|   |       |                 |                                     |                 |                                     |

We seek in the Traverse Table till the diff. of lat. 136'6, and dep. 180'5, are found opposite each other, in their respective columns; the nearest to these are 180'5 and 136'0, which give the course (at the bottom of page, dep. being the most) S. 53° W., and distance 226'. This is an illustration of the remark, No. 141, page 89, that when the departure exceeds the difference of latitude, the course is more than 45°.

|                         |            |  |
|-------------------------|------------|--|
| Lat. left               | 38° 25' N. | } The lat. in is found according to<br>Rule XLVI, page 93. |
| D. Lat. 136'6           | = 2 17 S.  |  |
| Lat. in (or arrived at) | 36 8 N.    |  |

Ex. 3. A ship from lat. 37° 24' S., sails the following true courses:—S.W. by S., 20 miles; West, 16 miles; N.W. by W., 28 miles; S.S.E., 32 miles; E.N.E., 14 miles; S.W., 36 miles: required the lat. in, also the course and distance made good.

| COURSES.                            | DIST. | DIFF. LAT. |      | DEPARTURE. |      |
|-------------------------------------|-------|------------|------|------------|------|
|                                     |       | N.         | S.   | E.         | W.   |
| S. 3 W. . . . .                     | 20    | —          | 16'6 | —          | 11'1 |
| W. * . . . .                        | 16    | —          | —    | —          | 16 0 |
| N. 5 W. . . . .                     | 28    | 15'6       | —    | —          | 23'3 |
| S. 2 E. . . . .                     | 32    | —          | 29'6 | 12'3       | —    |
| N. 6 E. . . . .                     | 14    | 5'4        | —    | 12'9       | —    |
| S. 4 W. . . . .                     | 36    | —          | 25'5 | —          | 25'5 |
| * See Rule LXVIII, 3a,<br>page 172. |       | 21'0       | 71'7 | 25'2       | 75'9 |
|                                     |       | —          | 21'0 | —          | 25'2 |
|                                     |       | —          | 50'7 | —          | 50'7 |

We seek in the several pages of the Traverse Table II, for the diff. lat. 50'7; and dep. 50'7; the nearest found to these are diff. lat. 50'9, dep. 50'9, give course S. 45° W., distance 72 miles.

The diff. lat. and dep. being of equal amount, the course is 45°, or 4 points, which illustrates the remark, No. 141, page 89.

|                   |            |   |
|-------------------|------------|---|
| Lat. left.        | 37° 24' S. | } The lat. sailed from being South, and the ship having sailed South, the ship has evidently increased her South lat., whence the sum of lat. from and diff. lat. is taken to obtain lat. in.—(See Rule XLVI, 1 <sup>st</sup> , page 93). |
| Diff. lat. 50'7 = | 51 S.      |   |
| Lat. arrived at   | 38 15 S.   |   |

Ex. 4. A ship from lat. 20° 56' N. sails (all true courses) N.W. by N., 20 miles; S.W., 40 miles; N.E. by E., 60 miles; S.E., 55 miles; W. by S., 41 miles; E.N.E., 66 miles: required the latitude in, also the course and distance made good.

| COURSES.        | DIST. | DIFF. LAT. |      | DEPARTURE. |      |
|-----------------|-------|------------|------|------------|------|
|                 |       | N.         | S.   | E.         | W.   |
| N. 3 W. . . . . | 20    | 16'6       | —    | —          | 11'1 |
| S. 4 W. . . . . | 40    | —          | 28'3 | —          | 28'3 |
| N. 5 E. . . . . | 60    | 33'3       | —    | 49'9       | —    |
| S. 4 E. . . . . | 55    | —          | 38'9 | 38'9       | —    |
| S. 7 W. . . . . | 41    | —          | 8'0  | —          | 40'2 |
| N. 6 E. . . . . | 66    | 25'3       | —    | 61'0       | —    |
|                 |       | 75'2       | 75'2 | 149'8      | 79'6 |
|                 |       | —          | 75'2 | —          | 79'6 |
|                 |       | —          | —    | 70'2       | —    |

Course due East, and dist. 70'2, the same as the departure. (See No. 141, page 89).

The Traverse Table being filled up, the sums of the Northings and Southings are both 75'2, and being of contrary directions, show that the ship has returned to the same parallel of latitude which she sailed from. The sum of the Eastings is 149'8, and that of the Westings 79'6; their difference, 70'2, shows that the ship has gained so much to the Eastward, that being the greater. Consequently the *Course* is due *East*, and the *Distance* 70'2, the same as the departure.

Ex. 5. A ship sails from a place in lat.  $1^{\circ} 15' N.$ , the following true courses :—S.W. by W., 45 miles; E.S.E., 50 miles; S.W., 30 miles; S.E. by E., 60 miles; S.W.  $\frac{3}{4}$  S., 63 miles: required the latitude in, also the course and distance made good.

| COURSES.                     | DIST. | DIFF. LAT. |       | DEPARTURE.   |      |
|------------------------------|-------|------------|-------|--------------|------|
|                              |       | N.         | S.    | E.           | W.   |
| S. 5 W. . . . .              | 45    | —          | 25°0  | —            | 37.4 |
| S. 6 E. . . . .              | 50    | —          | 19.1  | 46.2         | —    |
| S. 4 W. . . . .              | 30    | —          | 21.2  | —            | 21.2 |
| S. 5 E. . . . .              | 60    | —          | 33.3  | 49.9         | —    |
| S. $3\frac{1}{4}$ W. . . . . | 63    | —          | 50.6  | —            | 37.5 |
|                              |       |            | 149.2 | 96.1<br>96.1 | 96.1 |

The Traverse Table being completed, the sum of the Southings is 149.2 miles, and to that amount the ship has altered her latitude. The miles of departure in the East column are 96.1, and those in the West column are also 96.1; but as the East and West departures destroy one another, there is no resulting departure; and therefore, it is not necessary to refer to the Traverse Table. The ship is under the same meridian as she sailed from; consequently, the course is due South, and the distance sailed is equal to the diff. of lat., viz., 149.2. This is according to No. 141, page 89.

Latitude left  $1^{\circ} 15' N.$

Diff. lat. 6,0)14,9.2

2 29.2 = 2 29 S.

Latitude in

1 14 S.

The ship being  $1^{\circ} 15'$ , or 75 miles, N. of the equator, must evidently be in S. lat. after making 149 miles of Southing. Thus, in subtracting one of the quantities from the other, the difference takes the name of the greater. Rule XLVI, page 93.

The course is South, and dist. 149.2, the same as diff. lat.

Ex. 6. A ship from latitude  $46^{\circ} 10' N.$ , sails as follows: S.  $48^{\circ} E.$ , 25 miles; S.  $51^{\circ} E.$ , 18.9 miles; N.  $87^{\circ} E.$ , 12.4 miles; S.  $70^{\circ} E.$ , 14.5 miles; S.  $68^{\circ} E.$ , 21.6 miles; N.  $25^{\circ} W.$ , 16.4 miles; N.  $8^{\circ} E.$ , 7.8 miles; N.  $19^{\circ} E.$ , 13.7 miles; N.  $76^{\circ} E.$ , 39.6 miles; required the lat. in, also the course and distance made good.

| COURSES.                   | DIST. | DIFF. LAT.   |      | DEPARTURE.   |     |
|----------------------------|-------|--------------|------|--------------|-----|
|                            |       | N.           | S.   | E.           | W.  |
| S. $48^{\circ} E.$ . . . . | 25    | —            | 16.7 | 18.6         | —   |
| S. $51^{\circ} E.$ . . . . | 18.9  | —            | 11.9 | 14.7         | —   |
| N. $87^{\circ} E.$ . . . . | 12.4  | 0.7          | —    | 12.4         | —   |
| S. $70^{\circ} E.$ . . . . | 14.5  | —            | 5.0  | 13.6         | —   |
| S. $68^{\circ} E.$ . . . . | 21.6  | —            | 8.1  | 20.0         | —   |
| N. $25^{\circ} W.$ . . . . | 16.4  | 14.9         | —    | —            | 6.9 |
| N. $8^{\circ} E.$ . . . .  | 7.8   | 7.7          | —    | 1.1          | —   |
| N. $19^{\circ} E.$ . . . . | 13.7  | 13.0         | —    | 4.5          | —   |
| N. $76^{\circ} E.$ . . . . | 39.6  | 9.6          | —    | 38.4         | —   |
|                            |       | 45.9<br>41.7 | 41.7 | 123.3<br>6.9 | 6.9 |
|                            |       | 4.2          |      | 116.4        |     |

Course N.  $88^{\circ} E.$  Dist. 116 $\frac{1}{2}$  miles.

Explanation.—The course  $48^{\circ}$  (found at the bottom of one of the pages in Table I), and dist. 25 (in dist. column), opposite this last stands 16.7 diff. lat., and 18.6 dep., and as the ship is sailing on a S. and E. course, the diff. lat. is written in the diff. lat. column, and the dep. in the East column.

To take out the next course and distance we proceed thus:— $51^{\circ}$  and dist.  $18^{\circ}0$ , taken as  $189$ , give diff. lat.  $118^{\circ}9$ , and dep.  $146^{\circ}9$ , now removing the decimal point in each, one place to the left we have diff. lat.  $118^{\circ}9 = 11^{\circ}83$ , and dep.  $146^{\circ}9 = 14^{\circ}69$ ; we do not require to use both the decimal places, but if, as in the case with both diff. lat. and dep., the second decimal figure amounts to 5, we add 1 to the first, and the diff. lat. thus becomes  $11^{\circ}0$ , and the dep.  $14^{\circ}7$ .

The third course is  $N. 87^{\circ} E.$ , and distance  $12^{\circ}4$ ; then  $87^{\circ}$  and dist.  $124$  (omitting the decimal point), give diff. lat.  $06^{\circ}5$ , and dep.  $123^{\circ}8$ ; now dropping the tenths in each, viz., the 5 and the 8, and increasing the preceding figures by 1 in each case, as the tenths exceed 5, we have, after removing the decimal point one place to the left, diff. lat.  $0^{\circ}7$ , and dep.  $12^{\circ}4$ .

Proceed in this way with the remaining courses, except the last, in which case the distance being more than 300, we proceed as follows:—

|                                       |  |
|---------------------------------------|--|
| Course $76^{\circ}$ , and dist. 300   | give diff. lat. $72^{\circ}6$ and dep. $291^{\circ}1$                |
| "      " <u>06</u>                    | " <u><math>23^{\circ}2</math></u> " <u><math>93^{\circ}1</math></u>  |
| ∴ Course $76^{\circ}$ , and dist. 396 | " <u><math>95^{\circ}8</math></u> " <u><math>384^{\circ}2</math></u> |

Now, cutting off the last figure in each, the 8 and the 2, and removing the decimal point one place to the left, we have diff. lat.  $0^{\circ}6$  (not  $0^{\circ}5$ , as the figure 8 which is dropped exceeds 5, one is added to the tenths), and dep.  $38^{\circ}4$ .

In Traverse Table II { Diff. lat.  $4^{\circ}2 N.$  } give { Course  $N. 88^{\circ} E.$  } made good.  
                                  { and Dep.  $116^{\circ}4 E.$  }                   { Dist.  $116^{\circ}2$  }

Latitude left  $46^{\circ} 10' N.$  }  
Diff. lat.  $4 S.$  }                   The latitude in is found according  
Lat. in  $46 6 N.$  }                   Rule XLVI, 2<sup>d</sup>, page 93.

### EXAMPLES FOR PRACTICE.

1. A ship from the Texel in lat.  $52^{\circ} 58' N.$ , sails W. by N., 44 miles; S. by E., 45 miles; W. by S., 35 miles; S.S.E., 44 miles; W.S.W.  $\frac{1}{2} W.$ , 42 miles; find diff. lat. and dep., the course and dist. made good, also the lat. arrived at.

2. A ship from Heligoland. lat.  $54^{\circ} 12' N.$ , sails W.S.W., 12 miles; N.W., 24 miles; S. by W., 20 miles; N.W. by W., 32 miles; S. by E., 36 miles; W. by N.  $\frac{1}{2} N.$ , 42 miles; S.S.E.  $\frac{1}{2} E.$ , 16 miles; W.  $\frac{3}{4} N.$ , 45 miles: required diff. lat. and dep., course and dist. made good, also the lat. arrived at.

3. A ship sails from lat.  $3^{\circ} 50' N.$ , sails S.S.W., 112 miles; S. by E., 86 miles; S.S.E., 112 miles; S. by W., 86 miles: find diff. lat. and dep., the course and dist., made good, also the lat. arrived at.

4. Yesterday we were in lat.  $19^{\circ} S.$ , and since then have sailed S.E.  $\frac{1}{2} S.$ , 13 miles; S. by E., 19 miles; S.E. by E., 22 miles; E. by S.  $\frac{1}{4} S.$ , 32 miles; N.N.E., 20 miles; N. by W.  $\frac{1}{4} W.$ , 27 miles; N.E. by E.  $\frac{1}{2} E.$ , 24 miles; S.W.  $\frac{1}{4} S.$ , 10 miles.

5. A ship from lat.  $1^{\circ} N.$ , sails East, 8 miles; E.  $\frac{1}{4} N.$ , 20 miles; S.E. by E., 33 miles; S.  $\frac{3}{4} W.$ , 31 miles; N.E.  $\frac{1}{2} N.$ , 43 miles; South, 28 miles; S.  $\frac{3}{4} E.$ , 21 miles; S. by W.  $\frac{1}{4} W.$ , 12 miles: required diff. lat. and dep., course and dist. made good, and also the lat. in.

6. A ship from lat.  $1^{\circ} 10' S.$ , sails E. by N.  $\frac{1}{2} N.$ , 56 miles; N.  $\frac{1}{4} E.$ , 80 miles; S. by E.  $\frac{1}{2} E.$ , 96 miles; N.  $\frac{1}{4} E.$ , 68 miles; E.S.E., 40 miles; N.N.W.  $\frac{1}{2} W.$ , 86 miles; E. by S., 65 miles: find diff. lat. and dep., course and dist. made good, also the lat. in.

7. A ship from lat.  $47^{\circ} 12' N.$ , sails S.  $31^{\circ} W.$ , 16 miles; N.  $72^{\circ} E.$ ,  $13^{\circ} 1'$ ; S.  $52^{\circ} W.$ ,  $15'$ ; S.  $44^{\circ} E.$ ,  $15^{\circ} 1'$ ; N.  $44^{\circ} W.$ ,  $19^{\circ} 7'$ ; N.  $77^{\circ} E.$ ,  $11^{\circ} 4'$ ; S.  $40^{\circ} W.$ ,  $16'$ ; S.  $14^{\circ} E.$ ,  $6'$ ; required the course and dist. made, the lat. arrived at, and the dep. made.

8. Since leaving lat.  $34^{\circ} 11' N.$ , we have sailed the following courses:—N.  $36^{\circ} W.$ ,  $27'$ ; N.  $24^{\circ} E.$ ,  $30'$ ; S.  $75^{\circ} W.$ ,  $47'$ ; S.  $80^{\circ} W.$ ,  $29'$ ; N.  $72^{\circ} W.$ ,  $42'$ ; N.  $78^{\circ} W.$ ,  $34'$ ; S.  $12^{\circ} E.$ ,  $28'$ ; required the course and dist. made, the lat. arrived at, and the dep. made.

9. Since leaving lat.  $36^{\circ} 35' S.$ , the ship has sailed N.  $84^{\circ} W.$ ,  $18'$ ; N.  $89^{\circ} W.$ ,  $30^{\circ} 4'$ ; N.  $67^{\circ} W.$ ,  $29^{\circ} 9'$ ; N.  $39^{\circ} W.$ ,  $33^{\circ} 9'$ ; N.  $8^{\circ} W.$ ,  $25^{\circ} 9'$ ; N.  $73^{\circ} W.$ ,  $34^{\circ} 9'$ ; N.  $86^{\circ} W.$ ,  $44^{\circ} 7'$ ; S.  $65^{\circ} E.$ ,  $56'$ ; required the lat. arrived at, and the course and dist. made good.

10. A ship sails from lat.  $1^{\circ} 46' N.$ , on the following compass courses, viz., S.W.  $\frac{3}{4} W.$ , 62 miles; S. by W., 16 miles; W.  $\frac{3}{4} S.$ , 40 miles; S.W.  $\frac{3}{4} W.$ , 29 miles; S. by E., 30 miles; and S.  $\frac{3}{4} E.$ , 14 miles: required the lat. arrived at, and the course and dist. made good, the variation of the compass being  $21\frac{1}{2}^{\circ} W.$

## PARALLEL SAILING.

248. When two places lie on the same parallel of latitude, or due east or west of each other, the distance between them estimated along a parallel, or E. and W. (which is all departure) is converted into difference of longitude; or, on the other hand, the difference of longitude is converted into distance by **Parallel Sailing**.

Since the meridians are all parallel at the equator and meet at the poles, the distance between any two meridians, measured east and west, is less as the latter is greater—that is, the *absolute number of miles*, or of feet, in a degree of longitude, is less as the latitude in which they are measured is greater. Hence, also, a given number of miles between two meridians corresponds to a greater difference of longitude, as the latitude in which they are measured is greater. For example, two places in lat.  $10^{\circ}$  and distant 60 miles east and west from each other, have  $60^{\circ}9'$  diff. long. In lat.  $60^{\circ}$  N. or S., two places similarly situated have  $2^{\circ}0'$  diff. long., while at  $73^{\circ}$  the diff. long. is  $3^{\circ}25'$ . Questions of this kind are solved by **Parallel Sailing**.

249. Given the departure made good on a given parallel of latitude, to find the diff. of long. corresponding thereto.

### RULE LXIX.

1°. Take out of the Tables the log. secant of latitude (rejecting 10 from index), and the log. of departure made good.

2°. Add these logs. together, and find the nat. number corresponding thereto. The result is the difference of longitude required.

250. In parallel sailing the latitude being constant, the difference of longitude bears a constant ratio to the distance, and all problems may be completely solved by the solution of a right-angled plane triangle, and therefore by inspection of the Traverse Table by

### RULE LXX.

*With the latitude of the parallel as a course, and the distance sailed on it as difference of latitude, the corresponding distance, in the Traverse Table, is the difference of longitude.*

### EXAMPLES.

Ex. 1. In lat.  $29^{\circ}51'$  S., the dep. made good 161 miles: required the diff. of long.

|                      |                                  |
|----------------------|----------------------------------|
| Lat. $29^{\circ}51'$ | Secant 0.061815                  |
| Dep. 161             | Log. 2.206826                    |
|                      | Log. 2.268641                    |
|                      | Diff. of long. $185^{\circ}6'$ . |
|                      | <i>By Inspection.</i>            |

In Traverse Table II, lat.  $30^{\circ}$  as course, dep. 161.1 in lat column, give diff. long.  $186^{\circ}$  in dist. col.

Ex. 2. A ship sailed 94.6 miles on the parallel  $64^{\circ}38'$  N.: required the diff. long.

|                      |                                  |
|----------------------|----------------------------------|
| Lat. $64^{\circ}38'$ | Secant 0.368141                  |
| Dep. 94.6            | Log. 1.975891                    |
|                      | Log. 2.344032                    |
|                      | Diff. of long. $220^{\circ}8'$ . |
|                      | <i>By Inspection.</i>            |

In Traverse Table II, lat.  $64^{\circ}$  as course and dep. 94.7 give diff. lat. in dist. column 216 miles; and course  $65^{\circ}$ , and dep. 94.7, give diff. long. in dist. column 224 miles: therefore the diff. long. for  $64\frac{1}{2}^{\circ}$  will =  $216 + 224 \div 2 = 220$  miles.

Ex. 3. From long.  $0^{\circ} 59' W.$  the dep. made was 125 East, on the parallel of  $52^{\circ}$ : required the long. in.

Lat.  $52^{\circ}$  Secant  $0.210658$   
Dep. 125 Log.  $2.096910$

Log.  $2.307568$   
Diff. long.  $6,0)20,3$

$3 \ 23 = 3^{\circ} 23' E.$   
Long. left  $0 \ 59 W.$

Long. in  $2 \ 24 E.$

Ex. 5. In lat.  $71^{\circ} 25' N.$ , the dep. made good was  $71\frac{1}{4}$  miles: required the diff. of long.

Lat.  $71^{\circ} 25'$  Secant  $0.496640$   
Dep.  $71.25$  Log.  $1.852785$

Log.  $2.349425$   
Diff. of long.  $223.6$  nearly.

Ex. 4. A ship from long.  $179^{\circ} 20' W.$  sails 109 miles West, on the parallel of  $61^{\circ} 25'$ ; what is the long. in?

Lat.  $61^{\circ} 25'$  Secant  $0.320176$   
Dep. 109 Log.  $2.037236$

Log.  $2.357602$   
Diff. of long.  $227.8 W.$

$6,0)22,8$   $3^{\circ} 48' W.$   
 $179 \ 20 W.$

$3 \ 48$  Long. in.  $183 \ 8 W.$   
 $360 \ 0$

or  $176 \ 52 E.$

Ex. 6. In lat.  $80^{\circ}$ , the dep. made good was 80 miles: required the diff. of long.

Lat.  $80^{\circ}$  Secant  $0.760330$   
Dep. 80. Log.  $1.903090$

Log.  $2.663420$   
Diff. of long.  $460.7$ .

### EXAMPLES FOR PRACTICE.

In each of the following examples the difference of longitude is required:—

|    | Lat. in.          | Dep.       |     | Lat. in.            | Dep.       |
|----|-------------------|------------|-----|---------------------|------------|
| 1. | $6^{\circ} 7' N.$ | $249' W.$  | 7.  | $64^{\circ} 16' N.$ | $265.7 W.$ |
| 2. | $19 \ 48 S.$      | $324 E.$   | 8.  | $51 \ 28 S.$        | $70.9 E.$  |
| 3. | $39 \ 57 N.$      | $398 W.$   | 9.  | $37 \ 0 N.$         | $94 W.$    |
| 4. | $51 \ 17 N.$      | $294.8 W.$ | 10. | $60 \ 0 S.$         | $204 E.$   |
| 5. | $60 \ 0 N.$       | $74 W.$    | 11. | $11 \ 15 N.$        | $365 W.$   |
| 6. | $46 \ 37 S.$      | $352 E.$   | 12. | $54 \ 53 S.$        | $342 E.$   |

251. The method of parallel sailing will apply correctly enough for all practical purposes to cases where the course is nearly east and west (true). In latitudes not higher than  $5^{\circ}$ , when the distance does not exceed 300 miles, the departure may be used at once for the difference of longitude, the resulting error scarcely exceeding one mile.

252. Given the difference of longitude of two places on the same parallel, to find their distance as measured along the parallel.

### RULE LXXI.

*To the log. of the diff. of long. add the cosine of lat. ; the sum (neglecting 10) is log. of the distance required.*

### EXAMPLE.

Ex. 1. Required the distance between St. Abb's Head, in latitude  $55^{\circ} 55' N.$ , longitude  $2^{\circ} 10' W.$ , and Uraniberg in the same latitude, but in longitude  $12^{\circ} 52' E.$

Longitude of St. Abb's Head  $2^{\circ} 10' W.$   
Longitude of Uraniberg  $12 \ 52 E.$

$15 \ 2$   
 $60$

Difference of longitude  $902$  miles.

Log. distance = log. diff. long. + log. cosine lat. — 10.

Log. diff. long.  $902 = 2.955207$

Log. cos. lat.  $55^{\circ} 55' = 9.748497$

Log. distance  $505.5 = 2.703704$

253. Given the meridian distance and difference of longitude to find the latitude.

### RULE LXXII.

*From the log. of meridian distance (adding 10 to the index) subtract the log. of diff. long.; the remainder is the log. cosine of the latitude.*

#### EXAMPLE.

Ex. 1. From a place in longitude  $3^{\circ} 12' W.$ , a ship sails due East 246 miles, and by observation is found to be in longitude  $4^{\circ} 8' E.$ : required the latitude of the parallel on which she sailed.

#### By Calculation.

|                      |             |                       |                                   |
|----------------------|-------------|-----------------------|-----------------------------------|
| Cos. lat. =          | mer. dist.  | Long. left            | $3^{\circ} 12' W.$                |
|                      | diff. long. | Long. in              | $4 \quad 8 E.$                    |
|                      |             | D. long.              | $7 \quad 20 = 440 \text{ miles.}$ |
| Mer. dist. 246       | log. (+ 10) | $12^{\circ} 39' 0935$ |                                   |
| Diff. long. 440      | log.        | $2^{\circ} 643453$    |                                   |
| Lat. $56^{\circ} 0'$ | cos.        | $9^{\circ} 747482$    |                                   |

#### By Inspection.

Since the diff. long. given, 440, exceeds the distance given in the Traverse Table, its half is taken, and also the half of the meridian distance 246, these are 220 and 123 respectively. Entering the tables with 220 as distance, and 123 as diff. lat., we find, on searching the table, these quantities, in their respective columns, on the page with  $56^{\circ}$  at the bottom; hence the latitude sought is  $56^{\circ}$ .

### EXAMPLES FOR PRACTICE.

1. Required the compass course and distance from A to B.

Given lat. A  $52^{\circ} 15' S.$ ; var.  $1\frac{1}{2}$  points W.; long. A  $37^{\circ} 30' W.$   
 B  $52 \quad 15 S.$ ; dev.  $8^{\circ} 50' W.$ ; B  $48 \quad 18 W.$

2. A and B lie on the parallel of  $58^{\circ} 30' N.$

Given long. A  $15^{\circ} 12' E.$   
 B  $13 \quad 18 W.$

What is the distance between them in nautical miles.

3. Define a great circle and a small circle of a sphere, giving an example of each. What connection is there between the tropic of Cancer and the Arctic Circle?

4. Required the compass course and distance from A to B.

Lat. A  $28^{\circ} 40' N.$ ; var.  $1\frac{3}{4}$  points W.; long. A  $2^{\circ} 20' E.$   
 B  $28 \quad 40 N.$ ; dev.  $8^{\circ} 50' E.$ ; B  $4 \quad 10 E.$

5. In what latitudes are the lengths of a degree of longitude 30 and 20 miles respectively?
6. In travelling 35 nautical miles on the parallel of  $55^{\circ} 25' N.$ , how much do I change my longitude?
7. Find the true course and distance from A to B.

Lat. A  $54^{\circ} 25' S.$ ; long. A  $15^{\circ} 30' E.$   
 B  $54 \quad 25 S.$ ; B  $9 \quad 15 W.$

## MIDDLE LATITUDE SAILING.

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254. **Middle Latitude Sailing** is a method founded on the principle of parallel sailing, converting Departure into Difference of Longitude, and the Difference of Longitude into Departure, when the ship's course lies obliquely across the meridian, that is, when besides departure she makes difference of latitude.

Suppose a ship, in going on the same course, from latitude  $40^{\circ}$  to latitude  $44^{\circ}$ , makes 100 miles departure: this departure, if made good altogether in latitude  $40^{\circ}$ , would give  $130.5$  difference of longitude by Rule LXIX, page 177; and again, if made good in latitude  $44^{\circ}$ , it would give 139 difference of longitude. Now, since the ship has sailed between these two parallels, and not on either of them exclusively, her real difference of longitude must be between 130.5 and 139, and therefore we may conclude it to be not far from that which would result from a departure made good altogether in the *middle parallel*; hence the name *Middle Latitude Sailing*. Middle latitude sailing, then, is founded on the consideration that the arc of the parallel of middle latitude of two places intercepted between their meridians, is nearly equal to the departure. If we conceive the ship to sail along this middle parallel, we may apply the principle of *parallel sailing* to the cases in point. In parallel sailing the departure (or distance) and difference of longitude are connected by the relation,  $\text{dep.} = \text{diff. of long.} \times \cos. \text{lat.}$  When the ship's course lies obliquely across the meridian, making good a difference of latitude, a modification of this formula gives the formula for middle latitude sailing,  $\text{dep. (nearly)} = \text{diff. of long.} \times \cos. \text{mid. lat.}$ ; or, in logarithms,  $\log. \text{dep.} = \log. \text{diff. of long.} + \log. \cos. \text{mid. lat.} - 10$ . Middle latitude sailing has thus the same two cases as parallel sailing, and accordingly the rules for inspection and computation already given, Rule LXIX, page 177, apply equally to this sailing, observing merely to read *middle latitude* for *latitude*.

255. To find the latitude and longitude in, the course and distance from a known place being given, by Traverse Table and Middle Latitude.

### RULE LXXIII.

1°. *With the given course and distance enter the Traverse Table, and take out true difference of latitude and departure (see Rule LXVI, page 167).*

2°. *With difference of latitude and latitude from, find latitude in (see Rule XLVI, page 93).*

3°. *Get the middle latitude, as directed, Rule XLVII, page 93.*

4°. *With the middle latitude as course, look in the difference of latitude column for the departure, the corresponding distance at the top is the difference of longitude.*

5°. *With difference of longitude and longitude from get longitude in, as in Rule XLIX, page 95.*

NOTE.—When the departure to be looked for as *difference of latitude* at the middle latitude, is beyond the limits of the Table, one-half, one-third, &c., must be used, and the resulting *difference of longitude* multiplied by the divisor, in order to get the whole *difference of longitude*.



## EXAMPLES.

Ex. 1. A ship from lat.  $52^{\circ} 6' N.$ , long.  $35^{\circ} 6' W.$ , sailed S.W. by W., 256 miles: required her latitude and longitude in.

Course S. 5 pts. W. } give diff. lat.  $142' 2$ , and dep.  $212' 9$  (see Rule LXVI, page 167).  
Distance 256 miles.

|          |                               |                             |
|----------|-------------------------------|-----------------------------|
| 6,0)14,2 | Diff. lat. $2^{\circ} 22' S.$ | 2)212'9                     |
| 2 22     | Lat. from $52^{\circ} 6' N.$  |                             |
|          | Lat. in $49^{\circ} 44' N.$   | $\frac{1}{2}$ dep. $106' 4$ |
|          | 2)101 50                      |                             |
|          | Mid. lat. $50^{\circ} 55'$    |                             |
|          |                               | 6,0)33,8                    |
|          |                               | 5 38                        |

Mid. lat.  $51^{\circ}$  as course (Table II), and half dep.  $106' 4$ , in diff. lat. column, give in dist. column 169 miles, the half the diff. of long. Then  $169 \times 2 =$  diff. long. 338.

|  |                                |
|--|--------------------------------|
|  | Long. from $35^{\circ} 38' W.$ |
|  | 35 6 W.                        |
|  | Long. in $40^{\circ} 44' W.$   |

*Explanation.*—The difference of latitude and departure are found as described in Rule LXVI, page 167. The latitude in is found by Rule XLVI, page 93; and thence the middle latitude, by adding the latitude from and latitude in together, and divided by 2 (see Rule XLVII, page 93). The departure exceeding the limits of the Tables, the half is taken. Then with *middle latitude* as a *course*, and *half the departure*, in *difference of latitude* column, half the difference of longitude is found in the *distance* column. This being doubled (as half the departure was taken) and divided by 60, gives the difference of longitude expressed in degrees and minutes. The ship is in *West* longitude, *sailing West*, add difference of longitude to longitude left to obtain longitude in (Rule XLIX, page 95).

This is the usual case at sea of Working the Day's Work.

Ex. 2. A ship from lat.  $48^{\circ} 27' S.$ , and long.  $29^{\circ} 12' W.$ , sails S.E. by S., 22.5 miles: required the latitude in, also the longitude in.

Course S.E. by S. = 3 pts.; then 3 pts. and dist. 22.5 give diff. lat.  $18' 7$ ,  
and dep.  $12' 5$  (see Rule LXVI, page 167).

|                               |                                      |
|-------------------------------|--------------------------------------|
| Diff. lat. $0^{\circ} 19' S.$ | } (See Rules XLVI & XLVII, page 93). |
| Lat. from $48^{\circ} 27' S.$ |                                      |
| Lat. in $48^{\circ} 46' S.$   |                                      |
| 2)97 13                       |                                      |
| Mid. lat. $48^{\circ} 36'$    |                                      |

Mid. lat.  $48\frac{1}{2}^{\circ}$  as course, and dep. as diff. lat. give in dist. column 19 miles, which is the diff. of long.

|                                |
|--------------------------------|
| Diff. long. $0^{\circ} 19' E.$ |
| Long. left $29^{\circ} 12' W.$ |
| Long. in $28^{\circ} 53' W.$   |

(The long. in is found by Rule XLIX, page 95).

Ex. 3. A ship from the Lizard, in lat.  $49^{\circ} 57' N.$ , sails W.S.W., 163 miles, variation  $2\frac{1}{2}$  points W.: required the latitude come to, and difference of longitude.

W.S.W. by compass is (allowing  $2\frac{1}{2}$  points westerly variation) S.W.  $\frac{1}{2}$  S. true, which in Table II, and dist. 163, gives diff. lat. 126, and dep.  $103' 4$ .

|          |                               |
|----------|-------------------------------|
| 6,0)12,6 |                               |
| 2 6      | or $2^{\circ} 6' S.$          |
|          | Lat. left $49^{\circ} 57' N.$ |
|          | Lat. in $47^{\circ} 51' N.$   |
|          | 2)97 48                       |
|          | Mid. lat. $48^{\circ} 54'$    |

Then mid. lat.  $48^{\circ} 54'$ , say  $49^{\circ}$ , as a course, and and dep.  $103' 4$ , found in the lat. column, opposite to which, in the dist. column, is 158, nearest, the difference of longitude.

Ex. 4. Lat. from  $59^{\circ} 0' N.$ , long. from  $3^{\circ} 33' E.$ , course S.E. by E.  $\frac{3}{4} E.$ , distance 191 miles.  
Course  $5\frac{3}{4}$  points, distance 191 miles (in Table I) give diff. lat.  $81.7$  and dep.  $172.7$ .

*D. Lat.*

6,0)8,17

1 21.7 or  $1^{\circ} 22' S.$   
Lat. from  $59^{\circ} 0' N.$   
Lat. in  $57^{\circ} 38' N.$   
116 38  
Mid. lat.  $58^{\circ} 19'$

*By Calculation.*

Mid. lat.  $58^{\circ} 19'$  sec.  $0.279655$   
Dep.  $172.7$  log.  $2.237292$   
log.  $2.516947$   
D. long.  $328.8$   
6,0)32,8.8  
5^{\circ} 28'.8

*By Inspection.*

|  |   |
|--|---|
| <p><math>58^{\circ}</math><br/>Dep. <math>159.0</math> give D. long. <math>300</math><br/><u>13.8</u>     „     <u>26</u><br/><math>172.8</math>     „     <math>326</math></p> <p>D. long. for middle lat. <math>58^{\circ}</math> is <math>326</math><br/>   „     „     <math>59^{\circ}</math> „ <math>335</math><br/>Diff. for <math>1^{\circ}</math> of mid. lat.     <math>9</math></p> <p><math>60' (or 1^{\circ}) : 19' :: 9</math><br/><u>          </u><br/><math>6,0)17,1</math><br/><u>2.85</u></p> | <p><math>59^{\circ}</math><br/>Dep. <math>154.5</math> give D. long. <math>300</math><br/><u>18.0</u>     „     <u>35</u><br/><math>172.5</math>     „     <math>335</math></p> <p>D. long. for mid. lat. <math>58^{\circ}</math> is     <math>326</math><br/>Corr. for <math>19'</math> (over <math>58^{\circ}</math>)     <math>+ 2.8</math><br/>D. long. for mid. lat. <math>58^{\circ} 19'</math> is <math>328.8</math></p> |
|--|---|

*Remark.*—When the mid. lat. is high and between two whole degrees, and also the dep. great as in this example, the diff. long. is best found by mid. lat.

Ex. 5. Sailed from A, in lat.  $50^{\circ} 48' N.$ , long.  $1^{\circ} 10' W.$ , S.  $41^{\circ} E.$ , 275 miles.

Entering Traverse Table II with *dist.* 275 miles, and *course*  $41^{\circ}$ , the *true diff. lat.* is  $207.5$  or  $3^{\circ} 27.5' S.$ ; applying this to *lat. from*, the *lat. in* is  $47^{\circ} 20.5' N.$  The corresponding *dep.* is taken out at the same opening, which is  $180.4$ . The *mid. lat.*, or half sum of *lat. from* and *lat. in*, is  $49^{\circ}$  to the nearest degree. The *dist.* corresponding to  $49^{\circ}$  as a course, and  $180.4$  in *diff. lat.* column, is found to be 275, in degrees  $4^{\circ} 35' E.$ , which is the *diff. long.* Applying this to the *long. from*,  $1^{\circ} 10' W.$ , we have the *long. in*  $3^{\circ} 25' E.$

#### EXAMPLES FOR PRACTICE.

In each of the examples following, the latitude and longitude arrived at are required to be found, having given the latitude and longitude from, with the course and distance sailed.

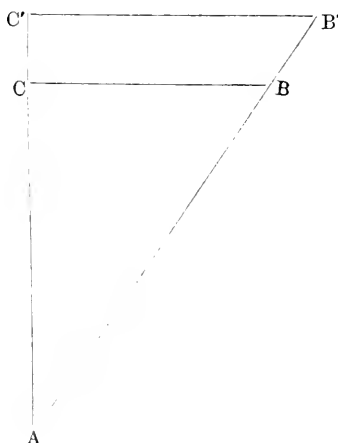
|    | Lat. from.          | Long. from.          | Course.                     | Dist. |
|----|---------------------|----------------------|-----------------------------|-------|
| 1. | $25^{\circ} 35' N.$ | $60^{\circ} 0' W.$   | E.N.E.                      | 296   |
| 2. | $32^{\circ} 30' N.$ | $25^{\circ} 24' W.$  | N.W. by W. $\frac{1}{2} W.$ | 212   |
| 3. | $39^{\circ} 30' S.$ | $74^{\circ} 20' E.$  | S.W. by W. $\frac{3}{4} W.$ | 210   |
| 4. | $46^{\circ} 24' S.$ | $178^{\circ} 28' E.$ | S.E. $\frac{3}{4} E.$       | 278   |
| 5. | $20^{\circ} 29' N.$ | $179^{\circ} 10' W.$ | W. by S. $\frac{1}{2} S.$   | 333   |
| 6. | $0^{\circ} 56' N.$  | $29^{\circ} 50' W.$  | S. $47^{\circ} E.$          | 168   |

## MERCATOR'S SAILING.

256. **Mercator's Sailing**, like middle latitude sailing, relates to finding the difference of longitude a ship makes when sailing on any oblique rhumb, and is a perfectly general and rigorously true method, which the other is not.

Mercator's sailing is characterised by the use of the *Table of Meridional parts*, and the chart constructed by means of it called *Mercator's chart*. With the assistance of this Table, the rules of plane trigonometry suffice for the solution of all the problems.

In the triangle ACB let A be the course, AB the distance, AC the true difference of latitude, CB the departure; then corresponding to AC, the Table of meridional parts gives AC', the meridional difference of latitude, and completing the right-angled triangle AC'B', C'B will be the difference of longitude. In addition, then, to the three canons of *plane sailing* which can be deduced from the triangle ACB, the triangle AC'B' gives the characteristic canon of *Mercator's sailing* (since  $C'B' = AC' \text{ tang. A}$ )  $\text{diff. long.} = \text{mer. diff. lat.} \times \text{tang. course.}$



257. Given the latitudes and longitudes of two places, to find the course and distance between them.

### RULE LXXIV.

- 1°. Find the true difference of latitude, according to Rule XLIV, page 91.
- 2°. Find the meridional difference of latitude, Rule XLV, page 92.
- 3°. Next find the difference of longitude, Rule XLVIII, page 94.
- 4°.\* To find the course.—From the log. of diff. of longitude (increasing its index by 10), subtract the log. of meridional diff. of lat.: the remainder is the tangent of course, which take out of the tables, and place before it the letter of diff. of lat., and after it the letter of diff. of long.
- 5°. To find the distance.—To the secant of course (rejecting 10 from the index), add the log. of diff. of lat.: the sum is the log. of distance, the natural number corresponding to which find in the Tables.

\* From the formula:—

$$\begin{aligned} \text{Tang. course} &= \frac{\text{Diff. long.}}{\text{Mer. diff. lat.}} \\ \text{Dist.} &= \frac{\text{True diff. lat.}}{\text{Cos. course}} \end{aligned}$$

$$\begin{aligned} \therefore \log. \text{ tang. course} - 10 &= \log. \text{ diff. long.} - \log. \text{ mer. diff. lat.} \\ \therefore \log. \text{ dist.} &= \log. \text{ true diff. lat.} + \log. \text{ sec. course} - 10. \end{aligned}$$

## EXAMPLES.

Ex. 1. Required the course and distance from Tynemouth Light to the Naze of Norway.

|                |             |                 |            |                 |             |
|----------------|-------------|-----------------|------------|-----------------|-------------|
| Lat. Tynemouth | 55° 1' N.   | Mer. parts      | 3970       | Long. Tynemouth | 1° 25' W.   |
| Lat. Naze      | 57 58 N.    | Mer. parts      | 4291       | Long. Naze      | 7 2 E.      |
|                | <u>2 57</u> | Mer. diff. lat. | <u>321</u> |                 | <u>8 27</u> |
|                | 60          |                 |            |                 | 60          |

Diff. of lat. 177 N.

Diff. of long. 507 E.

*To find the Course.*

|                      |             |           |
|----------------------|-------------|-----------|
| Diff. long. 507      | Log. (+ 10) | 12°705008 |
| Mer. diff. lat. 321  | Log.        | 2°56505   |
|                      | Tang.       | 10°198503 |
| Course N. 57° 40' E. |             |           |

*To find the Distance.*

|                   |        |          |
|-------------------|--------|----------|
| Course 57° 40'    | Secant | 0°271773 |
| Diff. of lat. 177 | Log.   | 2°247973 |
|                   | Log.   | 2°519746 |
| Distance 331.     |        |          |

Ex. 2. Required the course and distance from A to B.

|        |            |                 |            |         |            |
|--------|------------|-----------------|------------|---------|------------|
| Lat. A | 51° 23' N. | Mer. parts      | 3606       | Long. A | 9° 29' W.  |
| Lat. B | 48 23 N.   | Mer. parts      | 3326       | Long. B | 4 29 W.    |
|        | <u>3 0</u> | Mer. diff. lat. | <u>280</u> |         | <u>5 0</u> |
|        | 60         |                 |            |         | 60         |

Diff. of lat. 180 S.

Diff. of long. 300 E.

|                       |             |           |                 |        |          |
|-----------------------|-------------|-----------|-----------------|--------|----------|
| Diff. long. 300       | Log. (+ 10) | 12°477121 | Course 46° 58½' | Secant | 0°166014 |
| Mer. diff. lat. 280   | Log.        | 2°447158  | Diff. lat. 180  | Log.   | 2°255273 |
|                       | Tang.       | 10°029963 |                 | Log.   | 2°421287 |
| Course S. 46° 58½' E. |             |           | Distance 263.8. |        |          |

Ex. 3. Required the course and distance from Cape Bajoli to Cape Sicie.

|                  |            |                 |            |                   |            |
|------------------|------------|-----------------|------------|-------------------|------------|
| Lat. Cape Bajoli | 40° 1' N.  | Mer. parts      | 2624       | Long. Cape Bajoli | 3° 48' E   |
| Lat. Cape Sicie  | 43 3 N.    | Mer. parts      | 2867       | Long. Cape Sicie  | 5 51 E.    |
|                  | <u>3 2</u> | Mer. diff. lat. | <u>243</u> |                   | <u>2 3</u> |
|                  | 60         |                 |            |                   | 60         |

Diff. of lat. 182 N.

Diff. of long. 123 E.

|                      |             |           |                |        |          |
|----------------------|-------------|-----------|----------------|--------|----------|
| Diff. long. 123      | Log. (+ 10) | 12°089905 | Course 26° 51' | Secant | 0°049542 |
| Mer. diff. lat. 243  | Log.        | 2°385606  | Diff. lat. 182 | Log.   | 2°260071 |
|                      | Tang.       | 9°704299  |                | Log.   | 2°309613 |
| Course N. 26° 51' E. |             |           | Distance 204.  |        |          |

Ex. 4. Required the course and distance from Cape Formosa to St. Helena.

|                   |              |                 |             |                    |              |
|-------------------|--------------|-----------------|-------------|--------------------|--------------|
| Lat. Cape Formosa | 4° 15' N.    | Mer. parts      | 255         | Long. Cape Formosa | 6° 11' E.    |
| Lat. St. Helena   | 15 55 S.     | Mer. parts      | 968         | Long. St. Helena   | 5 45 W.      |
|                   | <u>20 10</u> | Mer. diff. lat. | <u>1223</u> |                    | <u>11 56</u> |
|                   | 60           |                 |             |                    | 60           |

Diff. of lat. 1210 S.

Diff. of long. 716 W.

|                      |             |           |                    |        |          |
|----------------------|-------------|-----------|--------------------|--------|----------|
| Diff. long. 716      | Log. (+ 10) | 12°854913 | Course 30° 21'     | Secant | 0°064012 |
| Mer. diff. lat. 1223 | Log.        | 3°087426  | Diff. of lat. 1210 | Log.   | 3°082785 |
|                      | Tang.       | 9°767487  |                    | Log.   | 3°146797 |
| Course S. 30° 21' W. |             |           | Distance 1402.     |        |          |

Ex. 5. Required the course and distance from Bahia to Fernando Po.

|                       |              |                 |                    |                        |              |
|-----------------------|--------------|-----------------|--------------------|------------------------|--------------|
| Lat. Bahia            | 13° 1' S.    | Mer. parts      | 788                | Long. Bahia            | 38° 32' W.   |
| Lat. Fernando Po      | 3 48 N.      | Mer. parts      | 228                | Long. Fernando Po      | 8 43 E.      |
|                       | <u>16 49</u> | Mer. diff. lat. | <u>1016</u>        |                        | <u>47 15</u> |
|                       | 60           |                 |                    |                        | 60           |
| Diff. of lat. 1009 N. |              |                 |                    | Diff. of long. 2835 E. |              |
| Diff. long. 2835      | Log. (+ 10)  | 13'452553       | Course 70° 17'     | Secant                 | 0'471895     |
| Mer. diff. lat. 1016  | Log.         | 3'006894        | Diff. of lat. 1009 | Log.                   | 3'003891     |
|                       | Tang.        | 10'445659       |                    | Log.                   | 3'475786     |
| Course N. 70° 17' E.  |              |                 | Distance 2991.     |                        |              |

Ex. 6. Required the course and distance from A to B.

|                          |               |                 |                        |                        |               |
|--------------------------|---------------|-----------------|------------------------|------------------------|---------------|
| Lat. A                   | 44° 44' S.    | Mer. parts      | 3007                   | Long. A                | 148° 39' W.   |
| Lat. B                   | 55 55 N.      | Mer. parts      | 4065                   | Long. B                | 44 44 E.      |
|                          | <u>100 39</u> | Mer. diff. lat. | <u>7072</u>            |                        | <u>193 23</u> |
|                          | 60            |                 |                        |                        | 360 0         |
| Diff. of lat. 6039 N.    |               |                 |                        |                        | <u>166 37</u> |
|                          |               |                 |                        |                        | 60            |
|                          |               |                 |                        | Diff. of long. 9997 W. |               |
| Diff. long. 9997         | Log. (+ 10)   | 13'999870       | Course 54° 43' 0"      | Secant                 | 0'238358      |
| Mer. diff. lat. 7072     | Log.          | 3'849542        | Parts for 26"          |                        | 77            |
|                          | Tang.         | 10'150328       | Diff. of lat. 6039     | Log.                   | 3'780965      |
| 54° 43'                  |               | <u>210</u>      |                        | 10457                  | Log. 4'019400 |
|                          |               | 446)11800(26    |                        |                        | <u>116</u>    |
|                          |               | 892             |                        |                        | 416)2840(7    |
|                          |               | <u>2880</u>     |                        |                        |               |
|                          |               | 2676            |                        |                        |               |
| Course N. 54° 43' 26" W. |               |                 | Distance 10457 nearly. |                        |               |

Ex. 7. Required the course and distance from Cape East, New Zealand, to Cape Horn.

|                          |              |                 |                        |                        |                 |
|--------------------------|--------------|-----------------|------------------------|------------------------|-----------------|
| Lat. Cape East           | 37° 42' S.   | Mer. parts      | 2445                   | Long. Cape East        | 178° 40' E.     |
| Lat. Cape Horn           | 55 59 S.     | Mer. parts      | 4072                   | Long. Cape Horn        | 67 16 W.        |
|                          | <u>18 17</u> | Mer. diff. lat. | <u>1627</u>            |                        | <u>245 56</u>   |
|                          | 60           |                 |                        |                        | 360 0           |
| Diff. of lat. 1097 S.    |              |                 |                        |                        | <u>114 4</u>    |
|                          |              |                 |                        |                        | 60              |
|                          |              |                 |                        | Diff. of long. 6844 E. |                 |
| Diff. long. 6844         | Log. (+ 10)  | 13'835310       | Course 76° 37' 0"      | Secant                 | 0'635515        |
| Mer. diff. lat. 1627     | Log.         | 3'211388        | Parts for 39"          |                        | 345             |
|                          | Tang.        | 10'623922       | Diff. of lat. 1097     | Log.                   | 3'040207        |
| 76° 37'                  |              | <u>558</u>      |                        |                        | <u>3'676067</u> |
|                          |              | 935)36400(39    |                        |                        | <u>53</u>       |
|                          |              | 2805            |                        |                        | 92)140(2        |
|                          |              | <u>8350</u>     |                        |                        |                 |
|                          |              | 8415            |                        |                        |                 |
| Course S. 76° 37' 39" E. |              |                 | Distance 4743'2 nearly |                        |                 |

## EXAMPLES FOR PRACTICE.

Required the course and distance from A to B in each of the following examples.

|       | LATITUDE.                  | LONGITUDE.               |       | LATITUDE.                  | LONGITUDE.                 |
|-------|----------------------------|--------------------------|-------|----------------------------|----------------------------|
| † 1.  | A 38° 14' N.<br>B 39 51 N. | A 2° 7' E.<br>B 4 18 E.  | † 11. | A 35° 14' S.<br>B 18 23 S. | A 75° 30' E.<br>B 12 2 E.  |
| ✓ 2.  | A 49 53 N.<br>B 48 28 N.   | A 6 19 W.<br>B 5 3 W.    | ✱ 12. | A 4 24 N.<br>B 8 48 S.     | A 7 46 W.<br>B 13 8 E.     |
| ✕ 3.  | A 53 18 N.<br>B 57 58 N.   | A 0 55 E.<br>B 7 3 E.    | ✱ 13. | A 57 43 S.<br>B 55 35 S.   | A 10 37 E.<br>B 1 28 W.    |
| ✱ 4.  | A 50 4 N.<br>B 51 25 N.    | A 5 42 W.<br>B 9 29 W.   | ✱ 14. | A 55 40 N.<br>B 50 25 N.   | A 2 25 W.<br>B 3 40 E.     |
| † 5.  | A 64 30 N.<br>B 60 40 N.   | A 4 20 W.<br>B 0 10 E.   | ✱ 15. | A 6 11 N.<br>B 6 0 S.      | A 80 15 W.<br>B 39 16 W.   |
| ✱ 6.  | A 22 55 S.<br>B 34 22 S.   | A 43 9 E.<br>B 18 29 W.  | † 16. | A 55 28 N.<br>B 57 58 N.   | A 1 9 E.<br>B 7 3 E.       |
| ✱ 7.  | A 54 54 S.<br>B 34 22 S.   | A 60 28 W.<br>B 18 24 E. | † 17. | A 35 51 S.<br>B 38 52 N.   | A 138 54 E.<br>B 165 53 W. |
| † 8.  | A 45 15 N.<br>B 47 10 N.   | A 35 26 W.<br>B 32 15 W. | ✕ 18. | A 15 30 N.<br>B 15 30 S.   | A 176 34 E.<br>B 176 34 W. |
| ✱ 9.  | A 34 22 S.<br>B 15 55 S.   | A 18 29 E.<br>B 5 43 W.  | ✕ 19. | A 22 22 S.<br>B 33 33 N.   | A 122 22 W.<br>B 111 11 E. |
| † 10. | A 49 57 N.<br>B 36 58 N.   | A 5 12 W.<br>B 25 12 W.  | ✱ 20. | A 17 0 N.<br>B 20 0 N.     | A 180 0 E.<br>B 161 0 E.   |

21. Required the compass course and distance from A to B.

Lat. A 33° 18' S.; long. A 72° 0' W.; var. 16° 0' E.  
B 42 3 S.; B 173 30 E.; dev. 9 25 E.

*170.09 W*  
*15-46*

258. To find the latitude and longitude in, having given the latitude from, the longitude from, and the course and distance between the two places by Traverse Table and meridional parts.\*

## RULE LXXV.

1°. *With given course and distance enter the Traverse Table and take out the corresponding true difference of latitude, Rule LXVI, page 167, from which and latitude from find latitude in, as in Rule XLVI, page 93, and then meridional difference of latitude, as in Rule XLV, page 92.*

2°. *At the given course look in the column of the true difference of latitude for the meridional difference latitude; the corresponding departure will be the difference of longitude, from which and the longitude from find the longitude in, as in Rule XLIX, page 95.*

\* The general method of solution by "meridional parts," is from the formula:—

True diff. lat. = dist.  $\times$  cos. course.

$\therefore$  log. true diff. lat. = log. dist. + log. cos. course — 10.

Diff. long. = mer. diff. lat.  $\times$  tang. course.

$\therefore$  log. diff. long. = log. mer. diff. lat. + log. tang. course — 10.

EXAMPLES.

Ex. 1. A ship from lat.  $55^{\circ} 1' N.$ , long.  $1^{\circ} 25' W.$ , sails S.S.E.  $\frac{1}{2}$  E., 246 miles : required the lat. in and long. in.

Entering Traverse Table II, with course S.  $2\frac{1}{2}$  points E., and distance 246, we obtain diff. lat.  $217^{\circ} 0$ , and dep.  $116^{\circ} 0$ .

|          |           |                     |                          |                               |       |                         |
|----------|-----------|---------------------|--------------------------|-------------------------------|-------|-------------------------|
| 6,0)21,7 | Lat. left | $55^{\circ} 1' N.$  | } Rule XLVI,<br>page 93. | Mer. parts                    | 3970  | } Rule XLV,<br>page 92. |
| 3° 37'   | D. lat.   | 3 37 S.             |                          | Mer. parts                    | 3607  |                         |
|          | Lat. in   | $51^{\circ} 24' N.$ |                          | Mer. diff. lat.               | 363   |                         |
|          |           |                     |                          | $\frac{1}{2}$ mer. diff. lat. | 181.5 |                         |

The course  $2\frac{1}{2}$  points, and half mer. diff. lat.  $181.5$  (in diff. lat. column), the nearest found in the Table is  $181.7$ , the corresponding departure is  $97.1$ , which multiplied by 2 (having divided mer. diff. lat. by 2) gives diff. long.  $194.2$  miles.

|            |            |                    |                          |  |  |
|------------|------------|--------------------|--------------------------|--|--|
| 6,0)19,4.2 | Long. left | $1^{\circ} 25' W.$ | } Rule XLVI,<br>page 93. | The ship being $1^{\circ} 25' W.$ , or $85'$ West of Greenwich, must evidently be in East longitude, after having sailed 194 miles to the Eastward (see Rule XLIX, page 95). |  |
| 3° 14'     | D. long.   | 3 14 E.            |                          |  |  |
|            | Long. in   | $1^{\circ} 49' E.$ |                          |  |  |

Ex. 2. A ship from lat.  $42^{\circ} 36' S.$ , long.  $178^{\circ} 43' E.$ , sails S.E.  $\frac{3}{4}$  E., 299 miles ; find lat. in and long. in.

Course  $4\frac{1}{4}$  points, and dist. 299, give diff. lat.  $178.1$ , dep.  $240.2$ .

|            |           |                     |                          |                 |       |                             |
|------------|-----------|---------------------|--------------------------|-----------------|-------|-----------------------------|
| 6,0)17,8.1 | Lat. left | $42^{\circ} 36' S.$ | } Rule XLVI,<br>page 93. | Mer. parts      | 2830  | } See Rule XLV,<br>page 92. |
| 2° 58'     | D. lat.   | 2 58 S.             |                          | Mer. parts      | 3078  |                             |
|            | Lat. in   | $45^{\circ} 34' S.$ |                          | Mer. diff. lat. | 2)248 |                             |
|            |           |                     |                          |                 | 124   |                             |

Course  $4\frac{1}{4}$  points, and half mer. diff. lat.  $124$  (in diff. lat. column), give in dep. column  $167.1$ , which doubled is  $334.9$ , the diff. long.

|            |            |                      |                          |
|------------|------------|----------------------|--------------------------|
| 6,0)33,4.2 | Long. left | $178^{\circ} 43' E.$ | } Rule XLIX,<br>page 95. |
| 5° 34'     | D. long.   | 5 34 E.              |                          |
|            |            | 184 17 E.            |                          |
|            |            | 360 0                |                          |
|            | Long. in   | $175^{\circ} 43' W.$ |                          |

Ex. 3. From lat.  $50^{\circ} 48' N.$ , and long.  $1^{\circ} 10' W.$ , sailed S.  $41^{\circ} E.$ , 275 miles : required the lat. in and long. in.

In the Traverse Table at the distance 275, and course  $41^{\circ}$ , the corresponding true diff. lat. is  $207.5$ , or  $3^{\circ} 27.5$ , which being subtracted from  $50^{\circ} 48' N.$ , the lat. in is  $47^{\circ} 20.5' N.$  ; taking out the mer. parts for  $50^{\circ} 48'$ , and  $47^{\circ} 20.5'$ , the mer. diff. lat. is found to be 317, to half which as a true diff. lat., and the course  $14^{\circ}$ , the dep. is  $137.8$ , twice which is  $275.6$ ,—that is, the diff. long. is  $4^{\circ} 36' E.$  : hence the long. in is  $3^{\circ} 26' E.$

Ex. 4. From lat.  $50^{\circ} 30' N.$ , and long.  $37^{\circ} 55' W.$ , sailed S.W.  $\frac{3}{4}$  S., until arrived at lat.  $52^{\circ} 15' N.$

|                               |                 |            |  |
|-------------------------------|-----------------|------------|--|
| Lat. from $50^{\circ} 30' N.$ | Mer. parts      | 3521       | } Course $3\frac{1}{4}$ points, and mer. diff. lat. in diff. lat. column, give in dep. column $125.4$ , which is the diff. long. |
| Lat. in $52^{\circ} 15' N.$   | Mer. parts      | 3690       |  |
|                               | Mer. diff. lat. | 169        |  |
|                               | 6,0)12,5.4      | Long. left | $37^{\circ} 55' W.$  |
|                               | 2° 5'           | D. long.   | 2 5 W.   |
|                               |                 | Long. in   | $40^{\circ} 0' W.$   |

EXAMPLES FOR PRACTICE.

For examples for practice in this problem take those given in middle latitude sailing at page 182.

## REMARKS ON MIDDLE LATITUDE AND MERCATOR'S SAILINGS.

259. "The difference of longitude found by middle latitude is true at the equator, and very nearly true for short distances in all latitudes, especially when the course is E. or W. In high latitudes, when the distance is great and the course oblique, the error becomes considerable; but the result may be made as accurate as we please by sub-dividing the distance run into small portions, and finding the difference of longitude for each portion separately. The difference of longitude deduced by middle latitude sailing is too small: an estimate of the error for places on the same side of the equator may be formed by the help of a few cases. Suppose the course 4 points or  $45^\circ$ , and the difference of latitude  $10^\circ$  or 600'; then if this difference of latitude is made good in any latitude below  $30^\circ$ , the error of the difference of longitude will not exceed 2'; if made good between the parallels of  $40^\circ$  and  $50^\circ$ , the error will be about 3'; and between  $60^\circ$  and  $70^\circ$  about 19', or  $\frac{1}{3}$  of a degree. For smaller distances the errors will be much less, and for greater distances much greater, as they vary in much more rapid proportion than the distances. It has been observed before that when the course is large, the difference of longitude should be found by middle latitude in preference to Mercator's sailing; because, although the latter is mathematically correct in principle, yet a small error in the course may, when the course is large, produce a considerable error in the difference of longitude. The reason of this is easily shown. In middle latitude sailing we convert the *departure* into difference of longitude. The process increases the departure in a proportion which is less than 2 to 1 in all latitudes below  $60^\circ$ ; and exceeds 3 to 1 in all latitudes beyond  $70^\circ$ . The error of the departure, increased in the same proportion, becomes thus the error of difference of longitude. Now when the course is nearly E. or W., the departure is nearly the same as the distance, and an error of some degrees in the course does not affect the departure sensibly; hence in this case the error of the difference of longitude depends on that of the distance alone. But in Mercator's sailing, on the other hand, we convert the *meridional difference of latitude* into difference of longitude, and the process, when the course is large, converts a given meridional difference of latitude into a difference of longitude much greater than itself; and thus increases the error of the meridional difference of latitude in the same proportion. Thus, for example, at the course  $80^\circ$ , the difference of longitude exceeds the meridional difference of latitude in the proportion of 6 to 1; at the course  $85^\circ$  this proportion is 11 to 1. Now, when the course is large, a slight change in it sensibly affects the difference of latitude, and also the meridional difference of latitude, which is deduced directly from it. In high latitudes the meridional parts vary rapidly, and the error of the difference of longitude is increased accordingly; hence the precept more especially demands attention in high latitudes."—*Raper's Practice of Navigation*, pp. 103, 104.



## THE DAY'S WORK.

260. THIS is the process of *finding the ship's place at noon*—that is, its latitude and longitude, having given the latitude and longitude at noon preceding, or a departure taken since, the compass courses and distances run in the interval, the leeway (if any), variation and deviation (if any), direction and rate of current (if any), &c., &c.

### RULE LXXVI.\*

1°. *Correct each course for leeway, variation and deviation (see Rules L to LV, pages 104 to 111), which arrange in the tabular form as in the example following. Add together the hourly distances sailed on each course, and insert the same in the Table, opposite the true course.*

**Departure Course.**—*When a departure has been taken, consider the opposite to the bearing as a course, which correct for variation, and the deviation due to the direction of the ship's head when the bearing was taken, and insert in the Table as an actual course, with the distance of the object as a distance. The departure course is generally put down in the Table as the first course. See No. 232, page 139.*

As the ship leaves the land, the bearing (by compass) of some prominent object or known headland is taken, and its distance is generally estimated by the eye; this process is called "taking a departure." The latitude and longitude of the landmark are known; and thence, by supposing the ship to have sailed on a course the *opposite* to the bearing of the object, through the distance that object is off, we thus obtain, on commencing a voyage, a determinate starting point, from whence to reckon the subsequent courses and distances. Thus, supposing for example a ship leaving the Tyne observes Tynemouth Light dipping, and setting it, finds its bearing to be W. by N., distant (by estimation) 20 miles. Now in sailing from Tynemouth light to the present position of the ship, she would have to sail in the *opposite* direction to the bearing of the lights, viz., E. by S., 20 miles. At the end of the day, the Day's Work gives us a change of the ship's place as referred to the landmark, and *not the supposed position*. For methods of determining the distance, see *Raper's Practice of Navigation*, on Taking Departures, ch. IV, pp. 114—122.

**Current Course.**—*The set of a current is to be corrected for variation only (being correct magnetic), and inserted in the Table as a course; the drift being taken as a distance. The current course is generally inserted in the Table as the last course.*

2°. *Take out of the Traverse Tables (Table I or II, Raper or Norie) the difference of latitude and departure to each course and distance (see Rule LXVI, page 167), and proceed to find the difference of latitude and departure made good as directed in Rule LXVIII, page 172, Traverse Sailing.*

3°. *Find the course and distance made good (see Rule LXVII, page 170).*

4°. *Find the latitude in by applying the difference of latitude to the latitude found (see Rule XLVI, page 93).*

If a departure has been taken, the difference of latitude is to be applied to latitude of the point of land; if otherwise, to yesterday's latitude.

\* Nearly the entire process of computing the Day's Work has already been given, and if the learner has thoroughly mastered the rules laid down in the preceding pages, he will find no difficulty in working the Day's Work without reference to them.

NOTE.—When the course is less than 5 points or  $56^\circ$ , the difference of longitude may be found by either or both *Middle Latitude* or *Mercator's* method, but if the course exceeds 5 points the method of *Middle Latitude* should be used in preference to *Mercator's* (see *Remarks* in page 188).

5°. To find the difference of longitude.—*By Middle Latitude Sailing.*

(a) Find the middle latitude as directed, Rule XLVII, page 93.

(b) Next at the page of *Traverse Table* on which the degrees (at top or bottom) correspond to middle latitude, find the departure in a difference of latitude column, then the corresponding distance is the difference of longitude (see Rule LXXIII, 4°, page 180).

When the latitude left and latitude in are of *contrary* names, that is, in low latitudes, no sensible error can arise from taking the departure itself as the difference of longitude.

6°. If the ship has made a due E. or due W. course good, the difference of longitude is found by *Parallel Sailing*, thus:—

With the latitude as a course and the departure in a difference of latitude column, then the corresponding distance is the difference of longitude (see Rule LXX, page 177).

7°. To find the difference of longitude.—*By Mercator's Sailing.*

(a) Find meridional difference of latitude (see Rule XLV, page 92.)

(b) Then with course and meridional difference of latitude (in a latitude column), find the corresponding departure, which is the difference of longitude (see Rule LXXV, page 186).

(c) With the longitude left and difference of longitude find the longitude in (see Rule XLIX, page 95).

When a departure has been taken the longitude left is that of the point of land; otherwise that of yesterday.

#### EXAMPLE I.

| H. | COURSES.                  | K. | $\frac{1}{10}$ | WINDS. | LEE-WAY.       | DEVIATION.              | REMARKS, &c.  |
|----|---------------------------|----|----------------|--------|----------------|-------------------------|---|
| 1  | S.S.E. $\frac{1}{2}$ E.   | 4  | 2              | East.  | pts.<br>2      | $7^\circ$ E.            | A point of land in lat. $42^\circ 12'$ S., long. $42^\circ 58'$ W., bearing by compass E. by N. $\frac{1}{4}$ N. dist. 21 miles. Ship's head S.S.E. $\frac{1}{2}$ E.; deviation as per log. |
| 2  |                           | 4  | 3              |        |                |                         |   |
| 3  |                           | 5  |                |        |                |                         |   |
| 4  |                           | 5  | 2              |        |                |                         |   |
| 5  |                           | 4  |                |        |                |                         |   |
| 6  | N.N.E.                    | 4  | 1              | East.  | $2\frac{1}{4}$ | $9^\circ$ E.            |   |
| 7  |                           | 3  | 8              |        |                |                         |   |
| 8  |                           | 3  | 5              |        |                |                         |   |
| 9  |                           | 3  | 2              |        |                |                         |   |
| 10 | S.W. $\frac{1}{3}$ W.     | 3  | 5              | W.N.W. | $1\frac{3}{4}$ | $7\frac{1}{2}^\circ$ W. |   |
| 11 |                           | 3  | 6              |        |                |                         | Variation $20^\circ$ W.   |
| 12 |                           | 4  |                |        |                |                         |   |
| 1  |                           | 4  | 2              |        |                |                         |   |
| 2  | N. $\frac{1}{4}$ E.       | 4  | 3              | W.N.W. | $2\frac{1}{2}$ | $1^\circ$ W.            |   |
| 3  |                           | 4  | 4              |        |                |                         |   |
| 4  |                           | 4  | 5              |        |                |                         |   |
| 5  | S.S.W.                    | 6  | 2              | West.  | $\frac{1}{2}$  | $2\frac{1}{2}^\circ$ W. |   |
| 6  |                           | 6  | 4              |        |                |                         |   |
| 7  |                           | 6  | 2              |        |                |                         |   |
| 8  |                           | 6  | 5              |        |                |                         |   |
| 9  | N. by W. $\frac{1}{2}$ W. | 6  | 2              | West.  | $\frac{3}{4}$  | $10^\circ$ W.           | A current set W.S.W. correct magnetic 26 miles from the time the departure was taken to the end of the day.   |
| 10 |                           | 5  | 7              |        |                |                         |   |
| 11 |                           | 5  | 3              |        |                |                         |   |
| 12 |                           | 5  | 4              |        |                |                         |   |

*The Departure Course.*

The opposite point to E. by N.  $\frac{1}{2}$  N. is W. by S.  $\frac{1}{2}$  S., and the ship's head being S.S.E.  $\frac{1}{2}$  E., the deviation is same as given in log. for S.S.E.  $\frac{1}{2}$  E., viz.,  $7^{\circ}$  E.

W. by S.  $\frac{1}{2}$  S. =  $6\frac{1}{2}$  pts. R. of S.

Deviation  $7^{\circ}$  R. }  
Variation  $20^{\circ}$  L. }  $13^{\circ}$  L.  
or  $73^{\circ} 8'$  R. of S.

True course  $60^{\circ} 8'$  R. of S.  
or S.  $60^{\circ}$  W., distance 21 miles.

This is inserted in the Traverse Table as 1st course.

*2nd Course, N.N.E.*

The deviation for N.N.E. is  $9^{\circ}$  E. H. K.

N.N.E. = 2 pts. R. of N. 6 4'1  
Leeway  $2\frac{1}{4}$  ,, L. 7 3'8  
8 3'5  
or  $0\frac{1}{4}$  ,, L. of N. 9 3'2

or N.  $2^{\circ} 49'$  E. of N., L. of N. 14'6  
Dev.  $9^{\circ}$  R. }  
Var.  $20^{\circ}$  L. } 11 L.

True course  $13^{\circ} 49'$  L. of N.  
or N.  $14^{\circ}$  W., distance 14'6 miles.

The distance, 14'6, is found by adding up the hourly distances from 6 o'clock until the course is changed at 10 o'clock.

*4th Course, N.  $\frac{1}{4}$  E.*

The deviation for N.  $\frac{1}{4}$  E. is  $1^{\circ}$  W.

N.  $\frac{1}{4}$  E. =  $\frac{1}{4}$  pt. R. of N. H. K.  
Leeway  $2\frac{3}{4}$  ,, R. 2 4'3  
3 4'4  
 $2\frac{3}{4}$  ,, R. of N. 4 4'5

or  $30^{\circ} 56'$  R. of N. 13'2  
Dev.  $1^{\circ}$  L. }  
Var.  $20^{\circ}$  L. } 21 0 L.

True Course  $9^{\circ} 56'$  R. of N.  
or N.  $10^{\circ}$  E., distance 13'2 miles.

*6th Course N. by W.  $\frac{1}{2}$  W.*

The dev. for N. by W.  $\frac{1}{2}$  W. is  $10^{\circ}$  W. H. K.

N. by W.  $\frac{1}{2}$  W. =  $1\frac{1}{2}$  L. of N. 9 6'2  
R. 10 5'7  
11 5'3  
 $\frac{3}{4}$  L. of N. 12 5'4

or  $8^{\circ} 26'$  L. of N. 22'6  
Dev.  $10^{\circ}$  L. }  
Var.  $20^{\circ}$  L. } 30 0 L.

True course  $38^{\circ} 26'$  L. of N.  
or, N.  $38^{\circ}$  W., distance 22'6.

*1st Course, S.S.E.  $\frac{1}{2}$  E.*

S.S.E.  $\frac{1}{2}$  E. =  $2\frac{1}{2}$  pts. L. of S. H. K. 1 4'2  
Leeway 2 ,, R. 2 4'3  
3 5'0  
 $0\frac{1}{2}$  ,, L. of S. 4 5'2  
5 4'0

or  $5^{\circ} 38'$  L. of S. 22'7  
Dev.  $7^{\circ}$  R. }  
Var.  $20^{\circ}$  L. } 13 L.

True Course  $18^{\circ} 38'$  L. of S.  
or S.  $19^{\circ}$  E., distance 22'7 miles.

The distance 22'7, is found by adding up the hourly distances sailed, until the course is altered at 6 o'clock. Insert this course and distance as 2nd course.

*3rd Course, S.W.  $\frac{1}{2}$  W.*

The deviation for S.W.  $\frac{1}{2}$  W. is  $7\frac{1}{2}^{\circ}$  W.

S.W.  $\frac{1}{2}$  S. =  $4\frac{1}{2}$  pts. R. of S. H. K.  
Leeway  $1\frac{3}{4}$  ,, L. 10 3'5  
11 3'6  
 $2\frac{3}{4}$  ,, R. of S. 12 4'0  
1 4'2

or  $30^{\circ} 56'$  R. of S.  
Dev.  $7^{\circ} 30'$  L. }  
Var.  $20^{\circ}$  0 L. } 27 30 L. 15'3

True Course  $3^{\circ} 26'$  R. of S.  
or S.  $3^{\circ}$  W., distance 15'3 miles.

Distance, 15'3, is found by adding up hourly distances from 10 o'clock until 2.

*5th Course, S.S.W.*

The deviation for S.S.W. is  $2\frac{1}{2}^{\circ}$  W.

S.S.W. = 2 pts. R. of S. H. K.  
Leeway  $\frac{1}{2}$  ,, L. 5 6'2  
6 6'4  
 $1\frac{1}{2}$  ,, R. of S. 7 6'2  
8 6'5

or  $16^{\circ} 53'$  R. of S.  
Dev.  $2^{\circ} 30'$  L. }  
Var.  $20^{\circ}$  0 L. } 22 30 L. 25'3

True Course  $5^{\circ} 37'$  L. of S.  
or S.  $6^{\circ}$  E., distance 25'3 miles.

*Current Course W.S.W.*

W.S.W. = 6 pts. R. of S.

or  $67^{\circ} 30'$  R. of S.

Deviation  $20^{\circ}$  0 L.

$47^{\circ} 30'$  R. of S.  
or, S.  $48^{\circ}$  W., distance 26'

The corrected courses are written down to the nearest degree, and the work will stand as follows:—

| COURSES.            | Dist. | N.    | S.             | E.    | W.             |
|---------------------|-------|-------|----------------|-------|----------------|
| S. 60° W. - - - - - | 21    |       | 10° 5          |       | 18° 2          |
| S. 19° E. - - - - - | 22° 7 |       | 21° 5          | 7° 4  |                |
| N. 14° W. - - - - - | 14° 6 | 14° 2 |                |       | 3° 5           |
| S. 3° W. - - - - -  | 15° 3 |       | 15° 3          |       | 0° 8           |
| N. 10° E. - - - - - | 13° 2 | 13° 0 |                | 2° 3  |                |
| S. 6° E. - - - - -  | 25° 3 |       | 25° 2          | 2° 6  |                |
| N. 38° W. - - - - - | 22° 6 | 17° 8 |                |       | 13° 9          |
| S. 48° W. - - - - - | 26    |       | 17° 4          |       | 19° 3          |
|                     |       | 45° 0 | 89° 9<br>45° 0 | 12° 3 | 55° 7<br>12° 3 |
|                     |       |       | 44° 9          |       | 43° 4          |

Difference latitude 44° 9 } give in Table II { Course S. 44° W. \*  
Departure ..... 43° 4 } { Distance 62½ miles.

Latitude left 42° 12' S. } Rule XLVI, p 93  
Diff. latitude 45 S. } Meridional parts 2798  
Latitude in 42 57 S. } Meridional parts 2859  
Sum 2) 85 9 } Mer. D. lat. 61 } Rule XLV, page 92.

Middle lat. 42 34

Course S. 44° W. } give in Table II { Difference of longitude 59° 0  
Mer. diff. lat. 61° 1 } { (in departure column).

Mid. latitude 42½° } give in Table II { Difference of longitude 59'  
Dep. 43° 4 (as d. lat.) } { (in distance column).

Longitude left 42° 58' W. }  
Diff. longitude 0 59 W. } Rule XLVI  
Longitude in 43 57 W. } page 93.

Previous to opening the Traverse Table to take out the difference of latitude and departure to each course and distance in the above table, fill up the columns not wanted: thus—in the first course, S. 60° W., the S. and W. will be wanted, and the N. and E. will not be wanted; fill up these last two columns by drawing a dash under N. and E. Proceed in the same manner with the other courses.

2. To find the difference of latitude and departure to each course and distance by the Traverse Table.

Enter Traverse Table, and take out the difference of latitude and departure corresponding to 60° and distance 21'. Insert them in the columns S. and W.

The second course is S. 19° E., and the distance 22° 7'. Then, 19 degrees and distance 227 (omitting the decimal point) give difference of latitude 21° 5, departure 7° 4, now dropping the tenths in each—namely, the 6 and the 9—and shifting the decimal point one place to the left, we have difference of latitude 21° 5, departure 7° 4 which insert in columns S. and E., the course being marked S. and E.

The third course is N. 14° W., and distance 14° 6'. Look for 14 degrees and distance 14° 6, which gives difference of latitude 14° 7, departure 3° 5; now dropping the tenths, the 7 and the 3, and increasing the preceding figure by 1, in the first case, as the tenths exceed 5, we have, by removing the decimal point one figure to the left, the difference of latitude 14° 2, and departure 3° 5.

Proceed in this way with the remaining courses.

Next we find the sum of the four columns, when it appears the ship has sailed 45° N., and 89·9 S.; therefore, upon the whole, the difference of latitude is 44·9 S. The sum of the eastings is 12·3, of the westings 55·7, and the departure made good is 43·4 W.

3. *To find the Course and Distance made good.*—The Difference of latitude is  $44^{\circ}9'$  and departure  $43.4$  found to correspond in their columns, give course S.  $44^{\circ}$  W., distance  $62\frac{1}{2}$  miles (see Rule LXVII, page 170).

4. We next apply the difference of latitude,  $45^{\circ}$  S. ( $44^{\circ}9'$ ), to the latitude left,  $42^{\circ} 12' \text{ S.}$ , (the latitude of point of land), taking the *sums*, as they are of same name, and the latitude  $42^{\circ} 57' \text{ S.}$ , takes the name of either (Rule XLVI, page 93).

5. *To find the Difference of Longitude.*—Take out the meridional parts for latitude left,  $42^{\circ} 12'$ , and also for latitude in,  $42^{\circ} 57'$ , and take the less from the greater, as the latitudes are of one name. The remainder is meridional difference of latitude (Rule XLV, page 92).

Or, find middle latitude by adding together latitude left and latitude in, and divide the sum by 2; the quotient is the middle latitude (Rule XLVII, page 93).

Then the course 44°, in Table II, and meridional difference of latitude 61', found in difference of latitude column, gives in departure column 59', or difference of longitude 59' (Rule LXXV, 2°, 186, page).

Or, the middle latitude  $42\frac{1}{2}^\circ$ , in Table II, and departure 43.4 in difference of latitude column, gives in distance column 59', the difference of longitude (Rule LXXIII ( $4^\circ$ ) page 180).

Thus:—Mid. lat.  $42^{\circ}$  and dep.  $43'4$  give in dist. column  $58\frac{1}{2}$   
and „ 43 „  $43'4$  „ „  $59\frac{1}{2}$   

2) 118

Diff. long. 59

The difference of longitude  $59'$  W. (that found by Mercator's sailing), added to longitude left  $42^{\circ} 58'$  W., gives longitude in  $43^{\circ} 57'$  W. (Rule XLIX, page 95).

EXAMPLE II.

| H. | COURSES.              | K. | $\frac{1}{10}$ | WINDS.   | LEE-WAY.               | DEVIATION.                 | REMARKS, &c.  |
|----|-----------------------|----|----------------|----------|------------------------|----------------------------|---|
| 1  | S. by W.              | 4  | 2              | W. by S. | pts.<br>$2\frac{1}{4}$ | $0^{\circ}$                | A point of land in lat. $62^{\circ} 18' N.$ , long. $85^{\circ} 17' E.$ , bearing by compass N. by E. $\frac{1}{4} E.$ , 16 miles. (Ship's head S. by W.) Deviation as per log. |
| 2  |                       | 3  | 9              |          |                        |                            |   |
| 3  |                       | 4  | 5              |          |                        |                            |   |
| 4  |                       | 4  | 0              |          |                        |                            |   |
| 5  | S.W. $\frac{3}{4}$ W. | 3  | 5              | S. by E. | $3\frac{1}{2}$         | $8^{\circ} W.$             |   |
| 6  |                       | 3  | 4              |          |                        |                            |   |
| 7  |                       | 3  | 2              |          |                        |                            |   |
| 8  |                       | 3  | 3              |          |                        |                            |   |
| 9  | E. $\frac{3}{4}$ S.   | 5  | 4              | S. by E. | $1\frac{3}{4}$         | $15^{\circ} E.$            |   |
| 10 |                       | 5  | 6              |          |                        |                            |   |
| 11 |                       | 5  | 5              |          |                        |                            |   |
| 12 |                       | 5  | 4              |          |                        |                            |   |
| 1  | W.N.W.                | 5  | 3              | North.   | 3                      | $18\frac{1}{2}^{\circ} W.$ | Variation $42^{\circ} E.$   |
| 2  |                       | 4  | 4              |          |                        |                            |   |
| 3  |                       | 4  | 2              |          |                        |                            |   |
| 4  |                       | 4  | 2              |          |                        |                            |   |
| 5  |                       | 5  | 0              |          |                        |                            |   |
| 6  | N.W. $\frac{1}{2}$ N. | 9  | 7              | S. by W. | 0                      | $16\frac{1}{2}^{\circ} W.$ | A current set the ship W.S.W. (correct magnetic, $22\frac{1}{2}$ miles.   |
| 7  |                       | 10 | 2              |          |                        |                            |   |
| 8  |                       | 11 | 4              |          |                        |                            |   |
| 9  |                       | 11 | 8              |          |                        |                            |   |
| 10 | E. $\frac{3}{4}$ N.   | 3  | 4              | N. by E. | $3\frac{1}{4}$         | $17\frac{1}{4}^{\circ} E.$ |   |
| 11 |                       | 3  | 2              |          |                        |                            |   |
| 12 |                       | 3  | 0              |          |                        |                            |   |
|    |                       | 2  | 8              |          |                        |                            |   |

## W. N. E. S. W. N.

*The Departure Course.*

The opposite point to N. by E.  $\frac{1}{4}$  E. is S. by W.  $\frac{1}{4}$  W., and the ship's head being S. by W., the deviation is the same as given in the log. for S. by W.

S. by W.  $\frac{1}{4}$  W. =  $1\frac{1}{4}$  pts. R. of S.

or  $14^{\circ} 4'$  R. of S.  
 Variation  $42^{\circ}$  R. }  
 Deviation 0 }  $42$  R.

True Course  $56$  R. of S.  
 or S.  $56^{\circ}$  W., distance 16 miles.

This is inserted in the Traverse Table as 1st course.

*2nd Course, S.W.  $\frac{3}{4}$  W.*

The deviation for S.W.  $\frac{3}{4}$  W. is  $8^{\circ}$  W.

S.W.  $\frac{3}{4}$  W. =  $4\frac{3}{4}$  pts. R. of S. H. K.  
 Leeway  $3\frac{1}{2}$  „ R. 5 3'5

Sum exc. 8 pts.  $8\frac{1}{4}$  „ R. of S. 7 3'2  
 Subtract from 16 8 3'3

$7\frac{3}{4}$  „ L. of N.  $13'4$

or  $87^{\circ} 11'$  L. of N.

Dev.  $8^{\circ}$  L. }  
 Var.  $42$  R. } 34 R.

True Course 53 L. of N.  
 or N.  $53^{\circ}$  W., distance  $13'4$ .

*4th Course, W.N.W.*

The deviation for W.N.W. is  $18\frac{1}{2}^{\circ}$  W.

W.N.W. = 6 pts. L. of N. H. K.  
 Leeway 3 „ L. 1 4'4

Sum exc. 8 pts. 9 „ L. of N. 2 4'2  
 Subtract from 16 4 5'0

7 „ R. of S.  $17'8$

or  $78^{\circ} 45'$  R. of S.

Dev.  $18^{\circ} 30'$  L. }  
 Var.  $42$  R. } 23 30 R.

Sum exc.  $90^{\circ}$  102 R. of S.  
 Subtract from 180

True Course 78 L. of N.  
 or N.  $78^{\circ}$  W., distance  $17'8$ .

*1st Course, S. by W.*

The deviation for S. by W. is  $0^{\circ}$ .

S. by W. = 1 pt. R. of S. H. K.  
 Leeway  $2\frac{1}{4}$  „ L. 1 4'2

$1\frac{1}{4}$  „ L. of S. 2 3'9  
 3 4'5  
 4 4'0

or  $14^{\circ} 4'$  L. of S.  
 Dev.  $0^{\circ}$  }  
 Var.  $42$  R. }  $42$  R.  $16'6$

True Course 28 R. of S.  
 or S.  $28^{\circ}$  W., distance  $16'6$ .

The distance  $16'6$  is found by adding up the hourly distances until the course is changed at 5 o'clock. Insert this course and distance in Traverse Table as the 2nd course.

*3rd Course, E.  $\frac{3}{4}$  S.*

The deviation for E.  $\frac{3}{4}$  S. is  $15^{\circ}$  E.

E.  $\frac{3}{4}$  S. =  $7\frac{1}{4}$  pts. L. of S. H. K.  
 Leeway  $1\frac{3}{4}$  „ L. 9 5'4

Sum exc. 8 pts. 9 „ L. of S. 10 5'6  
 Subtract from 16 11 5'4  
 12 5'3

7 „ R. of N.  $21'7$

or  $79^{\circ}$  R. of N.

Dev.  $15^{\circ}$  R. }  
 Var.  $42$  R. } 57 R. of N.

Sum exc.  $90^{\circ}$  136 R. of N.  
 Subtract from 180

True Course 44 L. of S.  
 or S.  $44^{\circ}$  E., distance  $21'7$ .

*5th Course, N.W.  $\frac{1}{2}$  N.*

The deviation for N.W.  $\frac{1}{2}$  N. is  $16\frac{1}{2}^{\circ}$  W.

N.W.  $\frac{1}{2}$  N. =  $3\frac{1}{2}$  pts. L. of N. H. K.  
 Leeway 0 5 9'7

Sum exc. 8 pts. 9 „ L. of N. 6 10'2  
 Subtract from 16 3 11'4  
 8 11'8

or  $39^{\circ} 22'$  L. of N.

Dev.  $16^{\circ} 30'$  L. }  
 Var.  $42$  R. }  $25 30$  R.  $43'1$

True Course 13 52 L. of N.  
 or N.  $14^{\circ}$  W., distance  $43'1$ .

6th Course, E.  $\frac{3}{4}$  N.

The deviation for E.  $\frac{3}{4}$  N. is  $17\frac{1}{4}^{\circ}$  E.

E.  $\frac{3}{4}$  N. =  $7\frac{1}{4}$  pts. R. of N. H. K.  
Leeway  $3\frac{1}{4}$  „ R. 9 3'4

Sum exc. 8 pts.  $10\frac{1}{2}$  „ R. of N. 10 3'2

Subtract from 16 11 3'0

$5\frac{1}{2}$  „ L. of S. 12'4

or  $61^{\circ}53'$  L. of S.

Dev.  $17^{\circ}15'$  R }  
Var. 42 R } 59 15 R.

True Course 2 38 L. of S.  
or S.  $3^{\circ}$  E., distance 12'4.

Current Course, W.S.W.

W.S.W. = 6 pts. R. of S.

or  $67^{\circ}30'$  R. of S.

Variation 42 R.

Sum exc.  $90^{\circ}$  109 30 R. of S.

Subtract from 180

True Course  $70^{\circ}30'$  L. of N.  
or N.  $71^{\circ}$  W., distance 22'5.

The corrected courses are written down to the nearest degree and the work will stand as follows:—

| COURSES.                   | DIST. | N.   | S.   | E.   | W.   |
|----------------------------|-------|------|------|------|------|
| S. $56^{\circ}$ W. . . . . | 16    |      | 8'9  |      | 13'3 |
| S. $28^{\circ}$ W. . . . . | 16'6  |      | 14'7 |      | 7'8  |
| N. $53^{\circ}$ W. . . . . | 13'4  | 8'1  |      |      | 10'7 |
| S. $44^{\circ}$ E. . . . . | 21'7  |      | 15'6 | 15'1 |      |
| N. $78^{\circ}$ W. . . . . | 17'8  | 3'7  |      |      | 17'4 |
| N. $14^{\circ}$ W. . . . . | 43'1* | 41'8 |      |      | 10'4 |
| S. $3^{\circ}$ E. . . . .  | 12'4  |      | 12'4 | 0'7  |      |
| N. $71^{\circ}$ W. . . . . | 22'5  | 7'3  |      |      | 21'3 |
|                            |       | 60'9 | 51'6 | 15'8 | 80'9 |
|                            |       | 51'6 |      |      | 15'8 |
|                            |       | 9'3  |      |      | 65'1 |

N.  $14^{\circ}$  W., distance 43'1.

|                     |           |               |           |
|---------------------|-----------|---------------|-----------|
| Course $14^{\circ}$ | Dist. 300 | D. lat. 291'1 | Dep. 72'6 |
| „ 14                | 131       | 127'1         | 31'7      |
| „ 14                | 431       | 418'2         | 104'3     |

Diff. lat.  $9'3$  and dep.  $65'1$  being found to correspond in their columns, give course N.  $82^{\circ}$  W., distance 66 miles.

Lat. left  $62^{\circ}18' N.$  }  
Diff. lat. 9 N. }  
Lat. in  $62^{\circ}27' N.$  }  
Sum 124 45 }  
Mid. lat. 62 22 }

See Rule XLIV p. 91,  
& Rule XLVII, p. 93.

The mid. lat. is high and between two whole degrees, therefore, we proceed thus:—

Mid. lat.  $62^{\circ}$  as course (in Table II), and dep.  $65'3$  (nearest to  $65'1$ ) as diff. lat., give in dist. column 139; and mid. lat.  $63^{\circ}$  and dep. 64 9 (nearest to  $65'1$ ) as diff. lat., give in dist. column 143: whence it is evident that for  $1^{\circ}$  (or 60') of mid. lat., the diff. long. increases 4': we next make the proportion

$$60' : 22' :: 4 : x$$

$$\frac{4}{1}$$

$$6,0)8,8$$

1'4 the correction for 22'

Mid. lat.  $62^{\circ}$  gives D. long. 139

Correction for 22' 1'4

∴ Mid. lat.  $62^{\circ}22'$  gives D. long. 140'4

Mid. lat.  $62^{\circ}22'$  sec. 0'333658

Dep.  $65'1$  log. 1'813581

Diff. long. 140'4 log. 2'147239

or  $2^{\circ}20'4$

Long. left  $85^{\circ}17' E.$

Diff. long. 2 20 W.

Long. in  $82^{\circ}57' E.$

Rule XLIX  
page 95.

\* To take out the diff. lat. and dep. for course N.  $14^{\circ}$  W., dist.  $41'3$ . (See Rule LXVI, (c) page 169.

## EXAMPLE III.

| H. | COURSES.            | K.                    | $\frac{1}{10}$ | WINDS.                    | LEE-<br>WAY.          | DEVI-<br>TION.  | REMARKS, &c.  |   |                         |               |                 |        |                |                |
|----|---------------------|-----------------------|----------------|---------------------------|-----------------------|-----------------|---|---|-------------------------|---------------|-----------------|--------|----------------|----------------|
| 1  | E. by S.            | 10                    | 6              | S. by E.                  | pts.<br>$\frac{1}{4}$ | $19^{\circ}$ E. | A point of land in<br>lat. $47^{\circ} 44'$ S., long.<br>$179^{\circ} 7'$ E., bearing by<br>compass N. by W. $\frac{1}{2}$ W.<br>dist. 11 miles. (Ship's<br>head E. by S.). Dev.<br>as per log.           |   |                         |               |                 |        |                |                |
| 2  |                     | 11                    | 4              |                           |                       |                 |   |   |                         |               |                 |        |                |                |
| 3  |                     | 11                    | 2              |                           |                       |                 |   |   |                         |               |                 |        |                |                |
| 4  |                     | 11                    | 4              |                           |                       |                 |   |   |                         |               |                 |        |                |                |
| 5  | E. $\frac{3}{4}$ S. | 12                    |                | S. by E. $\frac{1}{2}$ E. | $\frac{1}{2}$         | $20^{\circ}$ E. |   |   |                         |               |                 |        |                |                |
| 6  |                     | 12                    |                |                           |                       |                 |   |   |                         |               |                 |        |                |                |
| 7  |                     | 12                    | 3              |                           |                       |                 |   |   |                         |               |                 |        |                |                |
| 8  |                     | 12                    | 4              |                           |                       |                 |   |   |                         |               |                 |        |                |                |
| 9  | E.S.E.              | 12                    |                | South.                    | $\frac{3}{4}$         | $18^{\circ}$ E. |   |   |                         |               |                 |        |                |                |
| 10 |                     | 12                    | 4              |                           |                       |                 |   |   |                         |               |                 |        |                |                |
| 11 |                     | 13                    | 4              |                           |                       |                 |   |   |                         |               |                 |        |                |                |
| 12 |                     | 13                    | 4              |                           |                       |                 |   |   |                         |               |                 |        |                |                |
| 1  | N.E. by E.          | 13                    | 6              | N. by W.                  | $\frac{1}{2}$         | $19^{\circ}$ E. | Variation $14^{\circ}$ E.<br><br><br><br><br><br><br><br><br><br>A current set the ship<br>N.W. by N., correct<br>magnetic 13 miles from<br>the time the departure<br>was taken to the end<br>of the day. |   |                         |               |                 |        |                |                |
| 2  |                     | 14                    |                |                           |                       |                 |   |   |                         |               |                 |        |                |                |
| 3  |                     | 14                    | 3              |                           |                       |                 |   |   |                         |               |                 |        |                |                |
| 4  |                     | 13                    | 8              |                           |                       |                 |   |   |                         |               |                 |        |                |                |
| 5  |                     | 13                    | 8              |                           |                       |                 |   |   |                         |               |                 |        |                |                |
| 6  |                     | 13                    | 5              |                           |                       |                 |   |   |                         |               |                 |        |                |                |
| 7  |                     | 13                    | 5              |                           |                       |                 |   |   |                         |               |                 |        |                |                |
| 8  |                     | 13                    | 4              |                           |                       |                 |   |   |                         |               |                 |        |                |                |
| 9  |                     | S.E. $\frac{1}{4}$ E. | 12             |                           |                       |                 |   | 5 | S.S.W. $\frac{1}{2}$ W. | $\frac{3}{4}$ | $15^{\circ}$ E. |        |                |                |
| 10 |                     |                       | 12             |                           |                       |                 |   | 2 |                         |               |                 |        |                |                |
| 11 |                     |                       | 2              |                           |                       |                 |   | 4 |                         |               |                 | E.N.E. | $5\frac{3}{4}$ | $2^{\circ}$ E. |
| 12 |                     |                       | 2              |                           |                       |                 |   | 3 |                         |               |                 |        |                |                |

## W. N. E. S. W. N.

## Departure Course.

The point of land from which the departure is taken bears N. by W.  $\frac{1}{2}$  W., and the opposite point to this bearing is S. by E.  $\frac{1}{2}$  E. The ship's head when departure was taken is E. by S., the deviation for which is  $19^{\circ}$  E.

S. by E.  $\frac{1}{2}$  E. =  $1\frac{1}{2}$  pts. L. of S.

or  $16^{\circ} 53'$  L. of S.

Dev.  $19^{\circ}$  R. } 33 R.  
Var.  $14^{\circ}$  R. }

16 7 R. of S.

or S.  $16^{\circ}$  W., distance 11'.

## 2nd Course.

The dev. for E.  $\frac{3}{4}$  S. is  $20^{\circ}$  E. H. K.

E.  $\frac{3}{4}$  S. =  $7\frac{1}{4}$  pts. L. of S. 6 12

Leeway =  $\frac{1}{2}$  " L. 7 12'3

$7\frac{3}{4}$  " L. of S. 8 12'4

$7\frac{3}{4}$  " L. of S. 9 12

10 12'4

or  $87^{\circ} 11'$  L. of S.

Dev.  $20^{\circ}$  R. } 34 0 R.  
Var.  $14^{\circ}$  R. }

53 11 L. of S.

or S.  $53^{\circ}$  E., distance  $61'11$ .

## 1st Course.

The dev. for E. by S. is  $19^{\circ}$  E. H. K.

E. by S. = 7 pts. L. of S. 1 10'6

Leeway =  $\frac{1}{4}$  " L. 2 11'4

$7\frac{1}{4}$  " L. of S. 3 11'2

4 11'4

5 12

or  $81^{\circ} 34'$  L. of S.

Dev.  $19^{\circ}$  R. } 33 0 R. 56'6

Var.  $14^{\circ}$  R. }

True course 48 34 L. of S.

or S.  $49^{\circ}$  E., distance 56'6.

The distance 56'6 is found by adding up the hourly distances until the course is changed at 6 o'clock.

## 3rd Course.

The dev. for E.S.E. is  $18^{\circ}$  E. H. K.

E.S.E. = 6 pts. L. of S. 11 13'4

Leeway =  $\frac{3}{4}$  " L. 12 13'4

$6\frac{3}{4}$  " L. of S. 1 13'6

$6\frac{3}{4}$  " L. of S. 2 14

3 14'3

or  $75^{\circ} 56'$  L. of S.

Dev.  $18^{\circ}$  R. } 32 0 R. 68'7

Var.  $14^{\circ}$  R. }

43 56 L. of S.

or S.  $44^{\circ}$  E., distance 68'7



4th Course.

The dev. for N.E. by E. is  $19^{\circ}$  E. H. K.  
 N.E. by E. = 5 pts. R. of N. 4 13'8  
 Leeway =  $\frac{1}{2}$  „ R. 5 13'8  
                   6 13'5  
                    $5\frac{1}{2}$  „ R. of N. 7 13'5  
                                   8 13'4  
                   or  $61^{\circ} 53'$  R. of N.  
 Dev.  $19^{\circ}$  R. } 33 0 R. 68'0  
 Var. 14 R. }  
 Sum exc.  $90^{\circ}$  94 53 R. of N.  
 Subt. from 180 0  
 True course  $85^{\circ} 7'$  L. of S.  
                   or S.  $85^{\circ}$  E., distance 68'0.

6th Course.

The dev. for N. by E. is  $2^{\circ}$  E. H. K.  
 N. by E. = 1 pt. R. of N. 11 2'4  
 Leeway =  $5\frac{3}{4}$  „ L. 12 2'3  
                    $4\frac{3}{4}$  „ L. of N. 4'7  
                   or  $53^{\circ} 26'$  L. of N  
 Dev.  $2^{\circ}$  R. } 16 0 R.  
 Var. 14 R. }  
                   37 26 L. of N.  
 or N.  $37^{\circ}$  W., distance 4'7

5th Course.

The dev. for S.E.  $\frac{1}{4}$  E. is  $15^{\circ}$  E. H. K.  
 S.E.  $\frac{1}{4}$  E. =  $4\frac{1}{2}$  pts. L. of S. 9 12'5  
 Leeway =  $\frac{2}{4}$  „ L. 10 12'2  
                   5 „ L. of S. 24'7  
                   or  $56^{\circ} 15'$  L. of S.  
 Dev.  $15^{\circ}$  R. } 29 0 R.  
 Var. 14 R. }  
 True Course 27 15 L. of S.  
                   or S.  $27^{\circ}$  E., distance 24'7.

Current Course.

N.W. by N. = 3 pts. L. of N.  
                   or  $33^{\circ} 45'$  L. of N.  
 Var. 14 0 R.  
                   19 45 L. of N.  
 or N.  $20^{\circ}$  W., distance 13'.

The corrected courses are written down to the nearest degree, and the work will stand thus:—

| Courses.                        | Dist. | N.   | S.    | E.    | W.   |
|---------------------------------|-------|------|-------|-------|------|
| S. $16^{\circ}$ W. . . . .      | 11    |      | 10'6  |       | 3'0  |
| S. $49^{\circ}$ E. (a). . . . . | 56'6  |      | 37'1  | 42'7  |      |
| S. $53^{\circ}$ E. (b). . . . . | 61'1  |      | 36'8  | 48'8  |      |
| S. $44^{\circ}$ E. (c). . . . . | 68'7  |      | 49'4  | 47'7  |      |
| S. $85^{\circ}$ E. . . . .      | 68    |      | 5'9   | 67'7  |      |
| S. $27^{\circ}$ E. . . . .      | 24'5  |      | 21'8  | 11'1  |      |
| N. $37^{\circ}$ W. . . . .      | 4'7   | 3'8  | 2'2   |       | 2'8  |
| N. $20^{\circ}$ W. . . . .      | 13    | 12'2 |       |       | 4'4  |
|                                 |       | 16'0 | 161'6 | 218'0 | 10'2 |
|                                 |       |      | 16'0  | 10'2  |      |
|                                 |       |      | 145'6 | 207'8 |      |

To take out of the Traverse Table the courses marked (a), (b), and (c).

(a). Course S.  $49^{\circ}$  E., distance 56'6. Taking dist. 56'6 as 566 we have

| Course.      | Dist. | D. Lat. | Dep.  |
|--------------|-------|---------|-------|
| $49^{\circ}$ | 300   | 196'8   | 226'4 |
| 49           | 266   | 174'5   | 200'8 |
| 49           | 566   | 371'3   | 427'2 |

$\therefore$  S.  $49^{\circ}$  E. and dist. 56'6 gives diff. lat. 42'7 S., and dep. 37'1 E.

(b) Course S.  $53^{\circ}$  E., dist. 61.1. (Take dist. 61.1 as 611.)

| Course.      | Dist. | D. Lat.        | Dep.           |
|--------------|-------|----------------|----------------|
| $53^{\circ}$ | 300   | $180^{\circ}5$ | $239^{\circ}6$ |
| "            | 300   | $180^{\circ}5$ | $239^{\circ}6$ |
| "            | 11    | 6.6            | 8.8            |
| <hr/>        | <hr/> | <hr/>          | <hr/>          |
| 53           | 611   | $367^{\circ}6$ | $488^{\circ}0$ |

 $\therefore$  S.  $53^{\circ}$  E., dist. 61.1 gives diff. lat.  $36^{\circ}8$  S., and dep.  $48^{\circ}8$  E.(c) Course S.  $44^{\circ}$  E., dist.  $68^{\circ}7$ . (Take dist.  $68^{\circ}7$  as 687.)

| Course.      | Dist. | D. Lat.        | Dep.           |
|--------------|-------|----------------|----------------|
| $44^{\circ}$ | 300   | $215^{\circ}8$ | $208^{\circ}4$ |
| "            | 300   | $215^{\circ}8$ | $208^{\circ}4$ |
| "            | 87    | $62^{\circ}6$  | $60^{\circ}4$  |
| <hr/>        | <hr/> | <hr/>          | <hr/>          |
| 44           | 687   | $494^{\circ}2$ | $477^{\circ}2$ |

 $\therefore$  Course S.  $44^{\circ}$  E., dist.  $68^{\circ}7$ , gives diff. lat.  $49^{\circ}4$ , and dep.  $47^{\circ}7$ .Diff. lat.  $145^{\circ}6$  and dep.  $207^{\circ}8$ , found to correspond in the columns, give course S.  $55^{\circ}$  E., and distance 254 miles (see Rule LXVII, page 170).

|            |                    |
|------------|--------------------|
| Lat. left  | $47^{\circ}44'$ S. |
| Diff. lat. | $2^{\circ}26'$ S.  |
| <hr/>      | <hr/>              |
| Lat. in    | $50^{\circ}10'$ S. |

Sum  $2)97^{\circ}54'$ Mid. lat.  $48^{\circ}57'$ Mid. lat.  $48^{\circ}57'$  sec.  $0^{\circ}182621$ Dep.  $207^{\circ}8$  log.  $2^{\circ}317645$ D. long.  $316^{\circ}4$  log.  $2^{\circ}500266$ or  $5^{\circ}16'4$ 

Mid. lat.  $49^{\circ}$  as course in Table II, and half of the dep.  $103^{\circ}9$  (the whole dep. being too large a number to be found in the Table) gives in distance column 158, which multiplied by 2 (as only half the dep. was used in entering the Table) gives diff. long. 316 miles.

Long. left  $179^{\circ}7'$  E.  
D. long.  $326^{\circ}$   $5^{\circ}16'$  E.

Sum exc.  $180^{\circ}$   $184^{\circ}23'$  E.  
Subt. from  $360^{\circ}$   $0^{\circ}$

Long. in  $175^{\circ}37'$  W.

## EXAMPLE IV.

| H. | COURSES.                    | K. | $\frac{1}{10}$ | WINDS.                     | LEE-WAY.       | DEVIATION.                 | REMARKS, &c.   |
|----|-----------------------------|----|----------------|----------------------------|----------------|----------------------------|--|
| 1  | N.E. $\frac{1}{2}$ E.       | 6  |                | N.N.W.                     | $2\frac{1}{4}$ | $16\frac{1}{4}^{\circ}$ E. | A point of land in lat. $47^{\circ}35'$ S., long. $179^{\circ}26'$ E., bearing by compass S.E. $\frac{3}{4}$ E., dist. 15 miles. (Ship's head N.E. $\frac{1}{2}$ E.) Dev. as per log.      |
| 2  |                             | 6  | 2              |                            |                |                            |  |
| 3  |                             | 5  | 6              |                            |                |                            |  |
| 4  |                             | 6  | 4              |                            |                |                            |  |
| 5  | N.E. by E. $\frac{1}{2}$ E. | 5  | 7              | S.E. $\frac{1}{2}$ E.      | $2\frac{1}{4}$ | $17\frac{3}{4}^{\circ}$ E. |  |
| 6  |                             | 5  | 8              |                            |                |                            |  |
| 7  |                             | 5  | 9              |                            |                |                            |  |
| 8  |                             | 5  | 9              |                            |                |                            |  |
| 9  | S.E. $\frac{3}{4}$ E.       | 12 | 6              | N.E. by N.                 | 0              | $11^{\circ}$ E.            | Variation $25^{\circ}$ E.<br><br>A current set the ship N.E. by E. $\frac{3}{4}$ E., correct magnetic, $36\frac{1}{2}$ miles, from the time the departure was taken to the end of the day. |
| 10 |                             | 12 | 4              |                            |                |                            |  |
| 11 |                             | 12 | 3              |                            |                |                            |  |
| 12 |                             | 11 | 1              |                            |                |                            |  |
| 1  | South.                      | 4  | 7              | E.S.E.                     | 2              | $2\frac{1}{2}^{\circ}$ W.  |  |
| 2  |                             | 4  | 8              |                            |                |                            |  |
| 3  |                             | 4  | 9              |                            |                |                            |  |
| 4  |                             | 4  | 9              |                            |                |                            |  |
| 5  | N.W. b W. $\frac{1}{2}$ W.  | 4  | 2              | S.W. $\frac{1}{2}$ W.      | $1\frac{3}{4}$ | $18\frac{1}{2}^{\circ}$ W. |  |
| 6  |                             | 4  | 3              |                            |                |                            |  |
| 7  |                             | 4  | 5              |                            |                |                            |  |
| 8  |                             | 4  | 6              |                            |                |                            |  |
| 9  | N.W. $\frac{1}{2}$ W.       | 12 | 6              | S.W. b W. $\frac{1}{2}$ W. | $\frac{1}{4}$  | $18^{\circ}$ W.            |  |
| 10 |                             | 12 | 5              |                            |                |                            |  |
| 11 |                             | 12 | 4              |                            |                |                            |  |
| 12 |                             | 12 | 3              |                            |                |                            |  |

*Departure Course.*

The opposite point to S.E.  $\frac{3}{4}$  E. is  
N.W.  $\frac{3}{4}$  W.

$4\frac{3}{4}$  pts. L. of N.

or  $53^{\circ}26'$  L. of N.  
Dev.  $16^{\circ}15'$  R. }  $41$   $15$  R.  
Var. 25

True Course  $12$   $11$  L. of N.  
or N.  $12^{\circ}$  W., distance  $15'$ .

*2nd Course, N.E. by E.  $\frac{1}{2}$  E.*

Leeway  $5\frac{1}{2}$  pts. R. of N. H. K.  
 $2\frac{1}{4}$  ,, L. 5 5'7  
 $3\frac{1}{4}$  ,, R. of N. 7 5'9  
8 5'9

or  $36^{\circ}34'$  R. of N.  
Dev.  $17^{\circ}45'$  R. }  $42$   $45$  R. 23'3  
Var. 25 0 R. }

True Course  $79$   $19$  R. of N.  
or N.  $79^{\circ}$  E., distance  $23'3$ .

*4th Course, South.*

Leeway (port tack) 2 o pts. H. K.  
,, R. 1 4'7  
2 4'8  
2 ,, R. of S. 3 4'9  
4 4'9

or  $22^{\circ}30'$  R. of S.  
Dev.  $2^{\circ}15'$  L. }  $22$   $45$  R. 19'3  
Var. 25 0 R. }

True Course  $45$   $15$  R. of S.  
or S.  $45^{\circ}$  E., distance  $19'3$ .

*6th Course, N.W.  $\frac{1}{2}$  W.*

Leeway  $4\frac{1}{2}$  pts. L. of N. H. K.  
 $\frac{1}{4}$  ,, R. 9 12'6  
 $4\frac{1}{4}$  ,, L. of N. 10 12'5  
11 12'4  
12 12'3

or  $47^{\circ}49'$  L. of N.  
Dev.  $18^{\circ}$  L. }  $7$  0 R. 49'8  
Var. 25 R. }

True Course  $40$   $49$  L. of N.  
or N.  $41^{\circ}$  W., distance  $49'8$ .

*1st Course, N.E.  $\frac{1}{2}$  E.*

Leeway (port tack)  $4\frac{1}{2}$  pts. R. of N. H. K.  
 $2\frac{1}{4}$  ,, R. 1 6  
 $6\frac{1}{2}$  ,, R. of N. 3 5'6  
4 6'4

or  $75^{\circ}56'$  R. of N.  
Dev.  $16^{\circ}15'$  R. }  $41$   $15$  R. 24'2  
Var. 25 0 R. }

Exceeds  $90^{\circ}$   $117$   $11$  R. of N.  
Subtract from  $180$  0

True Course  $62$   $49$  L. of S.  
or S.  $63^{\circ}$  E., distance  $24'2$ .

*3rd Course, S.E.  $\frac{3}{4}$  E.*

$4\frac{3}{4}$  pts. L. of S. H. K.  
9 12'6  
(Leeway 0) or  $53^{\circ}26'$  L. of S. 10 12'4  
Dev.  $11^{\circ}$  R. } 36 0 R. 11 12'3  
Var. 25 R. } 12 11'1

True Course  $17$   $26$  L. of S. 48'4  
or S.  $17^{\circ}$  E., distance  $48'4$ .

*5th Course, N.W. by W.  $\frac{1}{2}$  W.*

Leeway  $5\frac{1}{2}$  pts. L. of N. H. K.  
 $1\frac{1}{4}$  ,, R. 5 4'2  
6 4'3  
 $3\frac{1}{4}$  ,, L. of N. 7 4'5  
8 4'6

or  $42^{\circ}11'$  L. of N.  
Dev.  $18^{\circ}30'$  L. }  $6$  30 R. 17'6  
Var. 25 0 R. }

True Course  $35$   $41$  L. of N.  
or N.  $36^{\circ}$  E., distance  $17'6$ .

*Current Course, N.E. by E.  $\frac{3}{4}$  E.*

$5\frac{3}{4}$  pts. R. of N.  
or  $64^{\circ}41'$  R. of N.  
Variation  $25$  0 R.

True Course  $89$   $41$  R. of N.  
or East, distance  $36'5$ .

| COURSES.                         | DIST. | N.   | S.   | E.   | W.   |
|----------------------------------|-------|------|------|------|------|
| N. $12^{\circ}$ W. . . . .       | 15    | 14'7 |      |      | 3'1  |
| S. $63^{\circ}$ E. . . . .       | 24'2  |      | 11'0 | 21'6 |      |
| N. $79^{\circ}$ E. . . . .       | 23'3  | 4'5  |      | 22'9 |      |
| S. $17^{\circ}$ E. (a) . . . . . | 48'4  |      | 46'3 | 14'2 |      |
| S. $45^{\circ}$ W. . . . .       | 19'3  |      | 13'7 |      | 13'7 |
| N. $36^{\circ}$ W. . . . .       | 17'6  | 14'2 |      |      | 10'4 |
| N. $41^{\circ}$ W. (b) . . . . . | 49'8  | 37'6 |      |      | 32'7 |
| East . . . . .                   | 36'5  |      |      | 36'5 |      |
|                                  |       | 71'0 | 71'0 | 95'2 | 59'9 |
|                                  |       | 71'0 |      | 59'9 |      |
|                                  |       | 0    |      | 35'3 |      |

For method of taking out the courses in the Traverse Table marked (a) and (b) respectively, see page 169 (b) and (c).

Having filled up the Traverse Table, the sum of the northings and southings are equal, consequently the latitude remains unaltered, or, the ship, after sailing the foregoing courses and distances, has returned to the same parallel. Altogether, the vessel has sailed  $95^{\circ}2'$  towards the east on four courses, while she has made  $59^{\circ}9'$  westing on the other four, leaving  $35^{\circ}3'$  of progress towards the east: hence

The Course is East, distance  $35^{\circ}3'$  (see No. 141, page 89).

*To find the Latitude and Longitude in.*

The ship not having altered her latitude, the latitude arrived at is the same as the latitude left, viz.,  $47^{\circ}35'$  S., and consequently the diff. of long. made good is to be found by Parallel Sailing, Rule LXX, page 177, thus:—

Lat.  $47^{\circ}35'$  } gives in Table II. { Diff. long.  $52^{\circ}1'$ .  
(as course) } { (in distance column.)

|               |                        |   |                        |
|---------------|------------------------|---|------------------------|
| Long. left    | $179^{\circ}26'$ E.    | } | Rule XLIX,<br>page 95. |
| Diff. long.   | $52^{\circ}5'$ E.      |   |                        |
| Long. in      | $180^{\circ}18'5''$ E. |   |                        |
| Subtract from | $360^{\circ}0'$        |   |                        |
| Long. in      | $179^{\circ}41'5''$ W. |   |                        |

#### EXAMPLE V.

| H. | COURSES.   | K. | $\frac{1}{10}$ | WINDS.     | LEE-WAY.       | DEVIATION.                 | REMARKS, &c.  |
|----|------------|----|----------------|------------|----------------|----------------------------|---|
| 1  | E. by N.   | 12 | 4              | S.E. by S. | $\frac{1}{4}$  | $17^{\circ}\frac{3}{4}$ E. | A point, Tynemouth in lat. $55^{\circ}1'$ N., long. $1^{\circ}25'$ W., bearing by compass W. by N. $\frac{1}{2}$ N. dist. 15 miles. (Ship's head E. by N.) Dev. as per log. |
| 2  |            | 12 | 2              |            |                |                            |   |
| 3  |            | 12 | 2              |            |                |                            |   |
| 4  |            | 12 | 2              |            |                |                            |   |
| 5  | E.S.E.     | 10 | 6              | South.     | $\frac{1}{2}$  | $13^{\circ}\frac{1}{2}$ E. |   |
| 6  |            | 10 | 5              |            |                |                            |   |
| 7  |            | 10 | 4              |            |                |                            |   |
| 8  |            | 10 | 5              |            |                |                            |   |
| 9  | N.E. by E. | 8  | 2              | S.E. by E. | 1              | $17^{\circ}\frac{1}{4}$ E. | Variation $21^{\circ}\frac{1}{4}$ W.  |
| 10 |            | 8  | 3              |            |                |                            |   |
| 11 |            | 8  | 3              |            |                |                            |   |
| 12 |            | 8  | 2              |            |                |                            |   |
| 1  | S.S.E.     | 7  | 4              | East.      | $1\frac{1}{4}$ | $5^{\circ}\frac{1}{2}$ E.  |   |
| 2  |            | 7  | 2              |            |                |                            |   |
| 3  |            | 7  | 2              |            |                |                            |   |
| 4  |            | 7  | 2              |            |                |                            |   |
| 5  | S.E. by S. | 5  | 8              | E. by N.   | 2              | $8^{\circ}\frac{1}{2}$ E.  | A current set the ship S.S.W. $\frac{1}{2}$ W. correct magnetic, 18 miles from the time the departure was taken to the end of the day.                                      |
| 6  |            | 5  | 6              |            |                |                            |   |
| 7  |            | 5  | 4              |            |                |                            |   |
| 8  |            | 5  | 2              |            |                |                            |   |
| 9  | E.S.E.     | 5  | 4              | N.E.       | $2\frac{1}{4}$ | $13^{\circ}\frac{1}{2}$ E. |   |
| 10 |            | 4  | 6              |            |                |                            |   |
| 11 |            | 4  | 5              |            |                |                            |   |
| 12 |            | 4  | 5              |            |                |                            |   |

W. N. E. S. W. N.

Departure Course.

Opposite to bearing E. by S.  $\frac{1}{2}$  S.  
 $6\frac{1}{2}$  pts. L. of S.  
 or  $73^{\circ} 8'$  L. of S.  
 Dev.  $17^{\circ} 45'$  R. }  
 Var.  $21^{\circ} 15'$  L. }  $3^{\circ} 30'$  L.  
 —————  
 $76^{\circ} 38'$  L. of S.  
 or S.  $77^{\circ}$  E., distance  $15'$ .

2nd Course, E.S.E.

Leeway  $6$  pts. L. of S.  
 $\frac{1}{2}$  „ L.  
 $6\frac{1}{2}$  „ L. of S.  
 or  $73^{\circ} 8'$  L. of S.  
 Dev.  $13^{\circ} 30'$  R. }  
 Var.  $21^{\circ} 15'$  L. }  $7^{\circ} 45'$  L.  
 —————  
 $80^{\circ} 53'$  L. of S.  
 or S.  $81^{\circ}$  E., distance  $42'$ .

4th Course, S.S.E.

Leeway  $2$  pts. L. of S.  
 $1\frac{1}{4}$  „ R.  
 $\frac{3}{4}$  „ L. of S.  
 or  $82^{\circ} 26'$  L. of S.  
 Dev.  $5^{\circ} 30'$  R. }  
 Var.  $21^{\circ} 15'$  L. }  $15^{\circ} 45'$  L.  
 —————  
 $24^{\circ} 11'$  L. of S.  
 or S.  $24^{\circ}$  E., distance  $29'$ .

6th Course, E.S.E.

Leeway  $6$  pts. L. of S.  
 $2\frac{1}{4}$  „ R.  
 $3\frac{3}{4}$  „ L. of S.  
 or  $42^{\circ} 11'$  L. of S.  
 Dev.  $13^{\circ} 30'$  R. }  
 Var.  $21^{\circ} 15'$  L. }  $7^{\circ} 45'$  L.  
 —————  
 $49^{\circ} 56'$  L. of S.  
 or S.  $50^{\circ}$  E., distance  $19'$ .

1st Course, E. by N.

Leeway  $7$  pts. R. of N.  
 $\frac{1}{4}$  „ L.  
 $6\frac{3}{4}$  „ R. of N.  
 or  $75^{\circ} 56'$  R. of N.  
 Dev.  $17^{\circ} 45'$  R. }  
 Var.  $21^{\circ} 15'$  L. }  $3^{\circ} 30'$  L.  
 —————  
 $72^{\circ} 26'$  R. of N.  
 or N.  $72^{\circ}$  E., distance  $49'$ .

3rd Course N.E. by E.

Leeway  $5$  pts. R. of N.  
 $1$  „ L.  
 $4$  „ R. of N.  
 or  $45^{\circ}$  R. of N.  
 Dev.  $17^{\circ} 15'$  R. }  
 Var.  $21^{\circ} 15'$  L. }  $4^{\circ}$  L.  
 —————  
 $41^{\circ}$  R. of N.  
 or N.  $41^{\circ}$  E., distance  $33'$ .

5th Course, S.E. by S.

Leeway  $3$  pts. L. of S.  
 $2$  „ R.  
 $1$  „ L. of S.  
 or  $11^{\circ} 15'$  L. of S.  
 Dev.  $8^{\circ} 30'$  R. }  
 Var.  $21^{\circ} 15'$  L. }  $12^{\circ} 45'$  L.  
 —————  
 $24^{\circ} 0'$  L. of S.  
 or S.  $24^{\circ}$  E., distance  $22'$ .

Current Course, S.S.W.  $\frac{1}{2}$  W.

$2\frac{1}{2}$  pts. R. of S.  
 or  $28^{\circ} 7'$  R. of S.  
 Var.  $21^{\circ} 15'$  L.  
 —————  
 $6^{\circ} 52'$  R. of S.  
 or S.  $7^{\circ}$  W., distance  $18'$ .

| COURSES.          | DIST. | N.   | S.                   | E.                    | W.  |
|-------------------|-------|------|----------------------|-----------------------|-----|
| S. 77° E. . . . . | 35    |      | 3'4                  | 14'6                  |     |
| N. 72° E. . . . . | 49    | 15'1 |                      | 46'6                  |     |
| S. 81° E. . . . . | 32    |      | 6'6                  | 41'5                  |     |
| N. 41° E. . . . . | 33    | 24'9 |                      | 21'6                  |     |
| S. 24° E. . . . . | 29    |      | 26'5                 | 11'8                  |     |
| S. 24° E. . . . . | 22    |      | 20'1                 | 8'9                   |     |
| S. 50° E. . . . . | 19    |      | 12'2                 | 14'6                  |     |
| S. 7° W. . . . .  | 18    |      | 17'9                 |                       | 2'2 |
|                   |       | 40'0 | 86'7<br>40'0<br>46'7 | 159'6<br>2'2<br>157'4 | 2'2 |

Diff. lat. 46'7 } give in Table II { Course S. 73½° E.  
Departure 157'4 } { Distance 164½'.

Lat. left 55° 1' N. }  
Diff. lat. 47 S. }  
Lat. in 54 14 N. }  
2)109 15 }  
Mid. lat. 54 37 }

See Rules XLVI, and  
XLVII, page 93.

To find Diff. long. (1) *By Calculation.*

Lat. 54° 37' sec. 0'237288  
Dep. 157'4 log. 2'197005  
Diff. long. 271'8 log. 2'434293

To find Diff. long. (2) *By Inspection.*

Mid. lat. 54° and dep. 157'5 in diff. lat. column (the nearest in Table to 157'4), gives in dist. column 268 for diff. long.; and mid. lat. 55° and dep. 157'7 in diff. lat. column give in dist. column diff. long. 275; whence it is evident that for 1° change of mid. lat. we have (275 — 268) = 7' change in diff. long., thus:—

$$\begin{array}{r} 60 : 37 :: 7 : x \\ \hline 7 \\ 6,0)25,9 \\ \hline 4'3 \end{array}$$

Mid. lat. 54° and dep. 157 give D. Long. 268  
Correction for 37' + 4'3  
∴ Mid. lat. 54° 37' and dep. 157'4 give 272'3

Long. left 1° 25' W.  
D. long. 272' or 4 32 E. }  
Long. in 3 7 E. } Rule XLIX  
page 95.

## Departure Course.

The opposite point to N.E. by N. is S.W. by S.

S.W. by S. = 3 pts. R. of S.  
or  $33^{\circ}45'$  R. of S.

Dev.  $11^{\circ}$  L.  $\left\{ \begin{array}{l} 36 \\ 25 \end{array} \right.$  o L.

True Course 2 15 L. of S.  
or S.  $2^{\circ}$  E., distance 17 miles.

## 1st Course.

W. by N. =  $78^{\circ}45'$  L. of N.

Leeway o  
Dev.  $11^{\circ}$  L.  $\left\{ \begin{array}{l} 36 \\ 25 \end{array} \right.$  o L.

Sum exc.  $90^{\circ}$  115 o  
Subtract from 180 o

True Course 65 o R. of S.  
or S.  $65^{\circ}$  W., distance 25 miles.

## 2nd Course, W.S.W.

W.S.W. = 6 pts. R. of S.  
Leeway (port tack)  $\frac{1}{2}$  " R.

$6\frac{1}{2}$  " R. of S.  
or  $73^{\circ}$  R. of S.

Dev.  $9^{\circ}$  L.  $\left\{ \begin{array}{l} 34 \\ 25 \end{array} \right.$  L.

True Course 39 R. of S.  
or S.  $39^{\circ}$  W., distance 22 miles.

## 3rd Course, W.N.W.

W.N.W. = o pts. L. of N.  
Leeway (port tack) 1 " R.

$\frac{5}{5}$  " L. of N.  
or  $50^{\circ}$  L. of N.

Dev.  $9^{\circ}$  L.  $\left\{ \begin{array}{l} 34 \\ 25 \end{array} \right.$  L.

True Course 90 L. of N.  
or West, distance 19 miles.

## 4th Course, S.W.

S.W. = 4 pts. R. of S.  
Leeway (starb. tack)  $1\frac{1}{2}$  " L.

$2\frac{1}{2}$  " R. of S.  
or  $31^{\circ}$  R. of S.

Dev.  $6^{\circ}$  L.  $\left\{ \begin{array}{l} 31 \\ 25 \end{array} \right.$  L.

or South, distance 16 miles.

## 5th Course, S.W. by W.

S.W. by W. = 5 pts. R. of S.  
Leeway (starb. tack)  $1\frac{1}{2}$  " L.

$3\frac{1}{2}$  " R. of S.  
or  $37^{\circ}$  R. of S.

Dev.  $8^{\circ}$  L.  $\left\{ \begin{array}{l} 33 \\ 25 \end{array} \right.$  L.

True Course 4 R. of S.  
or S.  $4^{\circ}$  W., distance 13 miles.

## 6th Course South.

South = o pts.  
Leeway (starb. tack)  $2\frac{1}{2}$  " L.

$2\frac{1}{2}$  " L. of S.  
or  $25^{\circ}$  L. of S.

Dev.  $0^{\circ}$  L.  $\left\{ \begin{array}{l} 25 \\ 25 \end{array} \right.$  L.

True Course 50 L. of S.  
or S.  $50^{\circ}$  E., distance 13 miles.

Current Course, N.W.  $\frac{3}{4}$  W.

N.W.  $\frac{3}{4}$  W. 53° L. of N.  
Variation 25 L.

True Course 78 L. of N.  
or N.  $78^{\circ}$  W., distance 6 miles.

## EXAMPLE VI.

| H  | COURSES.         | K | $\frac{1}{10}$ | WINDS.           | DEVIATION.     | REMARKS, &c. |
|----|------------------|---|----------------|------------------|----------------|--------------|
| 1  | W. by N.         | 6 | 3              | E.S.E.           | 0              | pts. 11° W.  |
| 2  |                  | 6 | 3              |                  |                |              |
| 3  |                  | 6 | 4              |                  |                |              |
| 4  |                  | 6 |                |                  |                |              |
| 5  | W.S.W.           | 5 | 6              | S.               | $\frac{1}{2}$  | 9° W.        |
| 6  |                  | 5 | 5              |                  |                |              |
| 7  |                  | 5 | 5              |                  |                |              |
| 8  |                  | 5 | 4              |                  |                |              |
| 9  | W.N.W.           | 5 | 5              | S.W.             | 1              | 9° W.        |
| 10 |                  | 4 | 8              |                  |                |              |
| 11 |                  | 4 | 6              |                  |                |              |
| 12 |                  | 4 | 6              |                  |                |              |
| 1  | S.W.             | 4 | 4              | W.N.W.           | $1\frac{1}{4}$ | 6° W.        |
| 2  |                  | 4 | 4              |                  |                |              |
| 3  |                  | 4 | 2              |                  |                |              |
| 4  |                  | 3 | 8              |                  |                |              |
| 5  | S.W. $\delta$ W. | 3 | 6              | N.W. $\delta$ W. | $1\frac{3}{4}$ | 8° W.        |
| 6  |                  | 3 | 4              |                  |                |              |
| 7  |                  | 3 | 3              |                  |                |              |
| 8  |                  | 3 | 3              |                  |                |              |
| 9  | S.               | 3 | 3              | W.S.W.           | $2\frac{1}{2}$ | 0°           |
| 10 |                  | 3 | 3              |                  |                |              |
| 11 |                  | 3 | 2              |                  |                |              |
| 12 |                  | 3 | 2              |                  |                |              |

A point, Lizard, in lat  $47^{\circ}58'$  N., long.  $5^{\circ}12'$  W., bearing by compass N.E. by N., distance 17 miles. (Ship's head W.  $\delta$  N) Dev. as per log.

Variation  $25^{\circ}$  W.

A current set (correct magnetic) N.W.  $\frac{3}{4}$  W., 6 miles, from the time the departure was taken to the end of the day.

| COURSES.               | DIST. | N.  | S.   | E.   | W.   |
|------------------------|-------|-----|------|------|------|
| S. $2^{\circ}$ E. . .  | 17    |     | 17°0 | 0°6  |      |
| S. $65^{\circ}$ W. . . | 25    |     | 10°6 |      | 22°7 |
| S. $39^{\circ}$ W. . . | 22    |     | 17°1 |      | 13°8 |
| West. . .              | 19    |     |      |      | 19°0 |
| South. . .             | 16    |     | 16°0 |      |      |
| S. $4^{\circ}$ W. . .  | 13    |     | 13°0 |      | 0°9  |
| S. $50^{\circ}$ E. . . | 13    |     | 8°4  | 10°0 |      |
| N. $78^{\circ}$ W. . . | 6     | 1°2 |      |      | 5°9  |
|                        |       | 1°2 | 82°1 | 10°6 | 62°3 |
|                        |       |     | 1°2  |      | 10°6 |
|                        |       |     | 80°9 |      | 51°7 |

Diff. lat.  $85^{\circ}9$  S. } gives in Table II } Course S.  $32\frac{1}{2}^{\circ}$  W.  
Departure  $51^{\circ}7$  W. } Distance 96 miles.

Lat. left  $49^{\circ}58'$  N. } Mer. parts 3471 }  
Diff. lat.  $1^{\circ}21'$  S. } Rules XLVI & XLVII, page 93. }  
Lat. in  $48^{\circ}37'$  N. } Mer. parts 3347 }  
Sum  $2^{\circ}08'35''$  } Mer. diff. lat. 124 } Rule XLIV, page 92.

Middle lat.  $49^{\circ}17'$  }  
Course S.  $32\frac{1}{2}^{\circ}$  W. } gives in Table II } Diff. long.  $79^{\circ}$ .  
Mer. diff. lat. 124 } (In departure column.)  
(D. lat. col.)

Mid. lat.  $49^{\circ}$  } Diff. long.  $79^{\circ}$  }  
Dep  $51^{\circ}8'$  (as diff. lat.) } gives in Table II } (In distance column.)

Longitude left  $5^{\circ}12'$  W. }  
Diff. longitude  $1^{\circ}19'$  W. } Rule XLIX, page 95.  
Longitude in  $6^{\circ}31'$  W.

## EXAMPLE VII.

| H. | COURSES.                  | K. | $\frac{1}{16}$ | WINDS.                      | LEE-WAY.            | DEVIATION.                 | REMARKS, &c.  |
|----|---------------------------|----|----------------|-----------------------------|---------------------|----------------------------|---|
| 1  | N.W. $\frac{1}{2}$ W.     | 3  | 4              | N. by E. $\frac{1}{2}$ E.   | pts. $1\frac{3}{4}$ | 18° W.                     | A point, Cape Swaine in lat. $52^{\circ} 15'$ N., long. $128^{\circ} 30'$ W., bearing by compass E. by N. $\frac{1}{2}$ N. dist. 16 miles. (Ship's head W.N.W.; deviation as per log. |
| 2  |                           | 3  | 6              |                             |                     |                            |   |
| 3  |                           | 3  |                |                             |                     |                            |   |
| 4  | E. $\frac{1}{4}$ S.       | 4  | 2              | N.N.E. $\frac{1}{2}$ E.     | 2                   | $15\frac{1}{2}^{\circ}$ E. |   |
| 5  |                           | 4  | 2              |                             |                     |                            |   |
| 6  |                           | 4  | 5              |                             |                     |                            |   |
| 7  |                           | 4  | 5              |                             |                     |                            |   |
| 8  |                           | 4  | 6              |                             |                     |                            |   |
| 9  | S. by E. $\frac{3}{4}$ E. | 5  | 2              | S.W.                        | $2\frac{1}{2}$      | 6° E.                      | Variation $25^{\circ}$ E.   |
| 10 |                           | 5  |                |                             |                     |                            |   |
| 11 |                           | 5  | 2              |                             |                     |                            |   |
| 12 |                           | 5  | 6              |                             |                     |                            |   |
| 1  | W. by N. $\frac{3}{4}$ N. | 3  | 6              | S.W.                        | $2\frac{3}{4}$      | $17\frac{1}{2}^{\circ}$ W. |   |
| 2  |                           | 3  | 4              |                             |                     |                            |   |
| 3  |                           | 3  | 6              |                             |                     |                            |   |
| 4  |                           | 3  | 4              |                             |                     |                            |   |
| 5  | S. $\frac{1}{4}$ E.       | 4  | 6              | S.W. by W. $\frac{1}{2}$ W. | $2\frac{1}{4}$      | 3° E.                      | A current set E. $b$ S. $\frac{3}{4}$ S correct magnetic 20 miles from the time the departure was taken to the end of the day.  |
| 6  |                           | 4  | 7              |                             |                     |                            |   |
| 7  |                           | 5  | 5              |                             |                     |                            |   |
| 8  |                           | 5  | 2              |                             |                     |                            |   |
| 9  | N.W.                      | 6  | 5              | W.S.W.                      | $1\frac{1}{4}$      | 17° W.                     |   |
| 10 |                           | 5  | 8              |                             |                     |                            |   |
| 11 |                           | 5  | 4              |                             |                     |                            |   |
| 12 |                           | 5  | 3              |                             |                     |                            |   |

| COURSES.                   | DIST. | N.   | S.           | E.   | W.           |
|----------------------------|-------|------|--------------|------|--------------|
| S. $80^{\circ}$ W. . . . . | 16    |      | 2'8          |      | 15'8         |
| N. $63^{\circ}$ W. . . . . | 10    | 4'5  |              |      | 8'9          |
| S. $24^{\circ}$ E. . . . . | 22    |      | 20'1         | 8'9  |              |
| S. $17^{\circ}$ E. . . . . | 21    |      | 20'1         | 6'1  |              |
| N. $32^{\circ}$ W. . . . . | 14    | 11'9 |              |      | 7'4          |
| South . . . . .            | 20    |      | 20'0         |      |              |
| N. $23^{\circ}$ W. . . . . | 23    | 2'2  |              |      | 9'0          |
| S. $45^{\circ}$ E. . . . . | 20    |      | 14'1         | 14'1 |              |
|                            |       | 37'6 | 77'1<br>37'6 | 29'1 | 41'1<br>29'1 |
|                            |       |      | 39'5         |      | 12'0         |

Diff. of lat.  $39'5$ , and dep.  $12'0$ , give course S.  $17^{\circ}$  W., and distance 41 miles.\* (Rule LXVII, page 170.)

|                                   |                       |                  |
|-----------------------------------|-----------------------|------------------|
| Lat. left $52^{\circ} 15' 0''$ N. | } Rule XLVI, page 93. | Mer. parts 3690  |
| Diff. lat. — $39' 5''$ S.         |                       |                  |
| Lat. in $51^{\circ} 35' 5''$ N.   |                       | Mer. parts 3626  |
| $2) 103^{\circ} 50' 5''$          |                       | M. diff. lat. 64 |
| Mid. lat. $51^{\circ} 55'$        |                       |                  |

\* The course being less than  $56^{\circ}$ , the diff. of long. may be found both by Middle Latitude and Mercator's sailing.

The course S.  $17^{\circ}$  W., and mer. diff. lat. 64 in lat. column, give dep.  $19' 6''$ , which is the required diff. of long., see Rule LXXV, page 186. Or mid. lat.  $52^{\circ}$  as course, and dep.  $12' 0''$ , give diff. of long.  $19\frac{1}{2}'$  in dist. column, Rule LXXIII ( $4^{\circ}$ ), page 180.

|  |                       |
|--|-----------------------|
| Long. Cape Swaine $128^{\circ} 30'$ W. | } Rule XLIX, page 95. |
| Diff. of long. + $20'$ W.              |                       |
| Long. in $128^{\circ} 50'$ W.          |                       |



EXAMPLE VIII.

| H. | COURSES.                | K. | $\frac{1}{10}$ | WINDS.                    | LEE-WAY.            | DEVIATION. | REMARKS, &c.   |
|----|-------------------------|----|----------------|---------------------------|---------------------|------------|--|
| 1  | N. $\frac{1}{2}$ W.     | 5  | 4              | W. by N.                  | pts. $1\frac{3}{4}$ | 2° W.      | A point of land in lat. $54^{\circ} 30'$ N., long. $60^{\circ} 0'$ W., bearing by compass W. by N. $\frac{1}{2}$ N. 14 miles. (Ship's head N.N.W.) Deviation 6° W. |
| 2  |                         | 5  | 4              |                           |                     |            |  |
| 3  |                         | 5  | 3              |                           |                     |            |  |
| 4  | S.W. $\frac{1}{2}$ S.   | 5  | 5              | W. by N.                  | $2\frac{3}{4}$      | 6° W.      |  |
| 5  |                         | 2  | 5              |                           |                     |            |  |
| 6  |                         | 2  | 5              |                           |                     |            |  |
| 7  |                         | 2  | 7              |                           |                     |            |  |
| 8  | N.N.E. $\frac{1}{2}$ E. | 3  | 6              | N.W. $\frac{1}{2}$ N.     | $2\frac{1}{2}$      | 4° E.      |  |
| 9  |                         | 3  | 5              |                           |                     |            |  |
| 10 |                         | 3  | 4              |                           |                     |            |  |
| 11 |                         | 3  | 7              |                           |                     |            |  |
| 12 |                         | 3  | 8              |                           |                     |            |  |
| 1  | W. $\frac{1}{2}$ N.     | 4  | 2              | N.N.W.                    | $2\frac{1}{4}$      | 11° W.     | Variation 42° West.  |
| 2  |                         | 4  | 4              |                           |                     |            |  |
| 3  |                         | 4  | 5              |                           |                     |            |  |
| 4  |                         | 4  | 6              |                           |                     |            |  |
| 5  | S.E. $\frac{1}{2}$ E.   | 6  | 5              | S. by W. $\frac{1}{2}$ W. | $\frac{1}{2}$       | 8° E.      | A current set the ship (correct magnetic) N.W. $\frac{1}{2}$ W., 23 miles, from the time the departure was taken to the end of the day.                            |
| 6  |                         | 6  | 4              |                           |                     |            |  |
| 7  |                         | 6  |                |                           |                     |            |  |
| 8  |                         | 5  | 8              |                           |                     |            |  |
| 9  | S. $\frac{1}{2}$ W.     | 2  | 4              | S.E. by E.                | 3                   | 1° W.      |  |
| 10 |                         | 2  | 3              |                           |                     |            |  |
| 11 |                         | 2  | 3              |                           |                     |            |  |
| 12 |                         | 2  |                |                           |                     |            |  |

| COURSES.           | DIST. | N.   | S.   | E.   | W.   |
|--------------------|-------|------|------|------|------|
| N. $59^{\circ}$ E. | 14    | 7'2  |      | 12'0 |      |
| N. $30^{\circ}$ W. | 21'1  | 18'3 |      |      | 10'6 |
| S. $40^{\circ}$ E. | 7'7   |      | 5'9  | 5'0  |      |
| N. $18^{\circ}$ E. | 18    | 17'1 |      | 5'6  |      |
| S. $17^{\circ}$ W. | 17'7  |      | 16'9 |      | 5'2  |
| East               | 24'7  |      |      | 24'7 |      |
| S. $4^{\circ}$ E.  | 9     |      | 9'0  | 0'6  |      |
| S. $87^{\circ}$ W. | 23    |      | 1'2  |      | 23'0 |
|                    |       | 42'6 | 33'0 | 47'9 | 38'8 |
|                    |       | 33'0 |      | 38'8 |      |
|                    |       | 9'6  |      | 9'1  |      |

Diff. lat. 9'6, dep. 9'1, give course N.  $43^{\circ}$  E., dist. 13 miles.\* (Rule LXVII, page 170).

Lat. left  $54^{\circ} 30'$  N.  
 Diff. lat.  $10$  N.  
 Lat. in  $54^{\circ} 40'$  N.  
 $2)109\ 10$   
 Mid. lat.  $54\ 35$

} See Rules XLVI & XLVII, page 93.

Mer. parts 3916  
 Mer. parts 3933  
 $\frac{17}{17}$

} Rule XLV, page 92.

Course  $43^{\circ}$ , and mer. diff. lat. 17, give in dep. column the diff. of long. 16 miles (Rule LXXV, page 186); or mid. lat.  $54\frac{1}{2}^{\circ}$  as course, and dep. 9'1 in diff. lat. column, give in dist. column 16, the diff. long. (Rule LXXIII, 4<sup>o</sup>, page 180).

\* The diff. of long. may be found both by Middle Latitude and Mercator's method—the course being less than  $56^{\circ}$ .

Long. left  $60^{\circ} 0'$  W.  
 Diff. long.  $16$  E.  
 Long. in  $59^{\circ} 44'$  W.

} Rule XLIX, page 95.

+

EXAMPLE IX.

| H. | COURSES.                  | K. | $\frac{1}{10}$ | WINDS.   | LEE-WAY. | DEVIATION. | REMARKS, &c.   |
|----|---------------------------|----|----------------|----------|----------|------------|--|
| 1  | N.N.W.                    | 8  |                | N.E.     | 1        | 12° W.     | A point of land in lat. 0° 15' S., long. 170° 44' E., bearing by compass N.E. $\frac{1}{2}$ E. dist. 17 miles. (Ship's head N.N.W.) Dev. as per log. |
| 2  |                           | 8  | 4              |          |          |            |  |
| 3  |                           | 7  | 6              |          |          |            |  |
| 4  | E.S.E.                    | 6  | 2              | N.E.     | 1½       | 13½° E.    |  |
| 5  |                           | 5  | 8              |          |          |            |  |
| 6  |                           | 5  | 4              |          |          |            |  |
| 7  | E. by N.                  | 5  | 2              | N. by E. | 2        | 18° E.     |  |
| 8  |                           | 5  | 4              |          |          |            |  |
| 9  |                           | 5  | 4              |          |          |            |  |
| 10 |                           | 3  | 4              |          |          |            |  |
| 11 | N. by W. $\frac{3}{4}$ W. | 4  | 4              | N.E.     | 1½       | 10¾° W.    |  |
| 12 |                           | 4  | 8              |          |          |            |  |
| 1  |                           | 5  | 4              |          |          |            |  |
| 2  |                           | 5  | 3              |          |          |            |  |
| 3  |                           | 5  | 7              |          |          |            |  |
| 4  |                           | 6  |                |          |          |            |  |
| 5  |                           | 7  |                |          |          |            |  |
| 6  | N.W. $\frac{1}{4}$ N.     | 7  | 6              | N.N.E.   | 1¾       | 17° W.     | A current set the ship N. by E., correct magnetic, 23 miles, from the time the departure was taken to the end of the day.                            |
| 7  |                           | 6  |                |          |          |            |  |
| 8  |                           | 5  | 4              |          |          |            |  |
| 9  |                           | 5  | 7              |          |          |            |  |
| 10 |                           | 5  | 3              |          |          |            |  |
| 11 |                           | 5  | 4              |          |          |            |  |
| 12 |                           | 5  | 4              |          |          |            |  |

| COURSES.          | DIST. | N.   | S.   | E.   | W.   |
|-------------------|-------|------|------|------|------|
| S. 47° W. . . . . | 17    |      | 11'6 |      | 12'4 |
| N. 38° W. . . . . | 24    | 18'9 |      |      | 14'8 |
| S. 29° E. . . . . | 28    |      | 24'5 | 13'6 |      |
| S. 53° E. . . . . | 23    |      | 13'8 | 18'4 |      |
| N. 39° W. . . . . | 30    | 23'3 |      |      | 18'9 |
| N. 71° W. . . . . | 27'4  | 8'9  |      |      | 25'9 |
| N. 19° E. . . . . | 23    | 21'7 |      | 7'5  |      |
|                   |       | 72'8 | 49'9 | 39'5 | 72'0 |
|                   |       | 49'9 |      |      | 39'5 |
|                   |       | 22'9 |      |      | 32'5 |

Diff. lat. 22'9 } give in Table II. { Course N. 55° W.  
Dep. 32'5 } distance 40'.

|            |           |             |             |
|------------|-----------|-------------|-------------|
| Lat. left  | 0° 15' S. | Long. left  | 170° 44' E. |
| Diff. lat. | 23 N.     | Diff. long. | 32'5 W.     |
| Lat. in    | 0 8 N.    | Long. in    | 170 11'5 E. |

Rule XLVI Page 63.      Rule XLIX Page 55.

Since the latitude left and latitude in are of contrary names, the ship has sailed near the equator, and the departure itself may be taken as the difference of longitude. (See No. 251, page 178, and 5° (b) note, page 190.)

## EXAMPLE X.

| H. | COURSES.      | K. | $\frac{1}{10}$ | WINDS.    | LEE-WAY.              | DEVIATION. | REMARKS, &c.  |
|----|---------------|----|----------------|-----------|-----------------------|------------|---|
| 1  | N.N.E.        | 9  | 5              | East.     | pts.<br>$\frac{1}{2}$ | 8° E.      | A point of land in lat. 43° 47' N., long. 7° 51' W., bearing by compass S.W. by S., dist. 13 miles. (Ship's head N.N.E.) Dev. as per log. |
| 2  |               | 9  | 5              |           |                       |            |   |
| 3  |               | 9  | 6              |           |                       |            |   |
| 4  |               | 9  | 4              |           |                       |            |   |
| 5  | E.N.E.        | 3  | 6              | S.E.      | $2\frac{3}{4}$        | 15½° E.    |   |
| 6  |               | 4  | 4              |           |                       |            |   |
| 7  |               | 5  |                |           |                       |            |   |
| 8  |               | 5  |                |           |                       |            |   |
| 9  | E.S.E.        | 6  |                | South.    | 2                     | 13½° E.    |   |
| 10 |               | 7  |                |           |                       |            |   |
| 11 |               | 6  | 4              |           |                       |            |   |
| 12 |               | 5  | 6              |           |                       |            |   |
| 1  | W. by N. ½ N. | 6  |                | S.W. ½ S. | $1\frac{1}{2}$        | 15¾° W.    | Variation 25° W.  |
| 2  |               | 5  | 6              |           |                       |            |   |
| 3  |               | 5  | 4              |           |                       |            |   |
| 4  |               | 6  |                |           |                       |            |   |
| 5  | S.S.E.        | 5  | 6              | S.W.      | $\frac{1}{2}$         | 5½° E.     | A current set the ship N. by W., correct magnetic, 21 miles, from the time the departure was taken to the end of the day.                 |
| 6  |               | 6  | 2              |           |                       |            |   |
| 7  |               | 6  | 4              |           |                       |            |   |
| 8  |               | 7  |                |           |                       |            |   |
| 9  | N.N.W.        | 6  | 5              | West.     | 1                     | 12° W.     |   |
| 10 |               | 6  | 4              |           |                       |            |   |
| 11 |               | 7  |                |           |                       |            |   |
| 12 |               | 7  | 2              |           |                       |            |   |

| COURSES.          | DIST. | N.    | S.   | E.   | W.   |
|-------------------|-------|-------|------|------|------|
| N. 17° E. . . . . | 13    | 12.4  |      | 3.8  |      |
| North . . . . .   | 38    | 38.0  |      |      |      |
| N. 27° E. . . . . | 18    | 16.0  |      | 8.2  |      |
| N. 79° E. . . . . | 25    | 4.8   |      | 24.5 |      |
| S. 83° W. . . . . | 23    |       | 2.8  |      | 22.8 |
| S. 48° E. . . . . | 25.2  |       | 16.9 | 18.7 |      |
| N. 48° W. . . . . | 27.1  | 18.1  |      |      | 20.1 |
| N. 36° W. . . . . | 21    | 17.0  |      |      | 12.3 |
|                   |       | 106.3 | 19.7 | 55.2 | 55.2 |
|                   |       | 19.7  |      | 55.2 |      |
|                   |       | 86.6  |      | 0    |      |

Course, North, distance 86'6.

The Traverse Table being completed, the sum of the northings is 106'3, while that of the southings is 19'7. The departure in the east column amounts to 55'2, and that in the west column, also, to 55'2; but as the east and west departures destroy one another, there is no resulting departure, and, therefore, it is not necessary to refer to the Traverse Table. The ship is under the same meridian as she sailed from, consequently the course is due North, and the distance sailed is equal to the diff. lat., viz., 86'6. This is according to No. 141, page 89.

To find the Latitude and Longitude in.

Latitude left 43° 47' N.  
Diff. latitude 1 27 N.

Latitude in 45 14 N.

Longitude left 7° 51' W.

Longitude in 7 51 W.

## EXAMPLES FOR PRACTICE.

## EXAMPLE I.

| II. | COURSES.   | K. | $\frac{1}{10}$ | WINDS.   | LEE-WAY.      | DEVIATION. | REMARKS, &c.  |
|-----|------------|----|----------------|----------|---------------|------------|---|
| 1   | S.E. by S. | 12 | 5              | E. by N. | $\frac{1}{4}$ | 3° E.      | A point, lat. 35° 15' N.<br>long. 75° 30' W., bearing<br>by compass W. by<br>N., dist. 19 miles.<br>(Ship's head S.E. by S.<br>Dev. as per log. |
| 2   |            | 12 | 5              |          |               |            |   |
| 3   |            | 12 | 6              |          |               |            |   |
| 4   |            | 12 | 6              |          |               |            |   |
| 5   | East.      | 9  | 8              | N.N.E.   | 1             | 23° E.     |   |
| 6   |            | 9  | 4              |          |               |            |   |
| 7   |            | 9  | 7              |          |               |            |   |
| 8   |            | 9  | 4              |          |               |            |   |
| 9   | N.E.       | 10 | 4              | N.N.W.   | $\frac{3}{4}$ | 17° E.     |   |
| 10  |            | 10 | 6              |          |               |            |   |
| 11  |            | 10 | 4              |          |               |            |   |
| 12  |            | 10 | 4              |          |               |            |   |
| 1   | North.     | 11 | 4              | W.N.W.   | $\frac{3}{4}$ | 4° E.      | Variation 15° W.  |
| 2   |            | 10 | 4              |          |               |            |   |
| 3   |            | 9  | 8              |          |               |            |   |
| 4   |            | 10 | 4              |          |               |            |   |
| 5   | N.N.E.     | 11 | 4              | East.    | $\frac{1}{2}$ | 13° E.     |   |
| 6   |            | 10 | 4              |          |               |            |   |
| 7   |            | 10 | 4              |          |               |            |   |
| 8   |            | 10 | 4              |          |               |            |   |
| 9   | E.N.E.     | 9  | 2              | North.   | 1             | 18½° E.    | A current set the ship<br>N.E. by E. correct<br>magnetic, 52 miles<br>from the time the de-<br>parture was taken to<br>the end of the day.      |
| 10  |            | 8  | 8              |          |               |            |   |
| 11  |            | 9  | 4              |          |               |            |   |
| 12  |            | 9  | 3              |          |               |            |   |

## EXAMPLE II.

| H. | COURSES.            | K. | $\frac{1}{10}$ | WINDS.                    | LEE-WAY.              | DEVIATION. | REMARKS, &c.  |
|----|---------------------|----|----------------|---------------------------|-----------------------|------------|---|
| 1  | East.               | 9  | 4              | S.S.E.                    | pts.<br>$\frac{3}{4}$ | 16° E.     | A point, Flambro' Head, lat. 54° 7' N., long. 0° 5' W., bearing by compass N.W. by W. dist. 17 miles. (Ship's head E.S.E.) Deviation 13° E. |
| 2  |                     | 9  | 6              |                           |                       |            |   |
| 3  |                     | 9  | 9              |                           |                       |            |   |
| 4  | S.E. by E.          | 10 | 4              | S. by W.                  | $\frac{1}{2}$         | 12° E.     |   |
| 5  |                     | 10 | 2              |                           |                       |            |   |
| 6  |                     | 10 | 4              |                           |                       |            |   |
| 7  | E. $\frac{1}{2}$ S. | 6  | 7              | S. by E. $\frac{1}{2}$ E. | 1 $\frac{1}{4}$       | 15° E.     |   |
| 8  |                     | 6  | 6              |                           |                       |            |   |
| 9  |                     | 6  | 7              |                           |                       |            |   |
| 10 | S. by W.            | 5  | 8              | S.E. by E.                | 2                     | 0°         |   |
| 11 |                     | 4  | 4              |                           |                       |            |   |
| 12 |                     | 4  | 6              |                           |                       |            |   |
| 1  | South.              | 4  | 6              | E.S.E.                    | 2 $\frac{1}{2}$       | 2° E.      | Variation 25° W.  |
| 2  |                     | 4  | 4              |                           |                       |            |   |
| 3  |                     | 4  | 4              |                           |                       |            |   |
| 4  | S.E. by S.          | 4  | 2              | E. by N.                  | 2 $\frac{3}{4}$       | 8° E.      |   |
| 5  |                     | 3  | 5              |                           |                       |            |   |
| 6  |                     | 3  | 5              |                           |                       |            |   |
| 7  | E.N.E.              | 3  | 3              | S.E.                      | 3 $\frac{1}{4}$       | 18° E.     | A current set (correct magnetic) N.N.E., 6 miles, from the time the departure was taken to the end of the day.                              |
| 8  |                     | 3  | 3              |                           |                       |            |   |
| 9  |                     | 3  | 3              |                           |                       |            |   |
| 10 |                     | 3  | 3              |                           |                       |            |   |
| 11 |                     | 3  | 3              |                           |                       |            |   |
| 12 |                     | 3  | 3              |                           |                       |            |   |

## EXAMPLE III.

| H. | COURSES. | K. | $\frac{1}{10}$ | WINDS.   | LEE-WAY.              | DEVIATION. | REMARKS, &c.  |
|----|----------|----|----------------|----------|-----------------------|------------|---|
| 1  | W.S.W.   | 10 | 6              | N.W.     | pts.<br>$\frac{3}{4}$ | 11° W.     | A point, lat. 37° 3' N. long. 9° W., bearing by compass E. b N. $\frac{1}{2}$ N. dist. 14 miles. (Ship's head W.S.W.) Deviation as per log. |
| 2  |          | 10 | 4              |          |                       |            |   |
| 3  |          | 10 | 5              |          |                       |            |   |
| 4  |          | 10 | 5              |          |                       |            |   |
| 5  | W. by N. | 8  |                | N. by W. | 1 $\frac{1}{4}$       | 17° W.     |   |
| 6  |          | 7  | 5              |          |                       |            |   |
| 7  |          | 7  | 5              |          |                       |            |   |
| 8  |          | 7  |                |          |                       |            |   |
| 9  | N.N.W.   | 12 | 4              | N.E.     | $\frac{1}{2}$         | 12° W.     |   |
| 10 |          | 12 | 6              |          |                       |            |   |
| 11 |          | 12 |                |          |                       |            |   |
| 12 |          | 12 |                |          |                       |            |   |
| 1  | North.   | 10 |                | W.N.W.   | $\frac{3}{4}$         | 2° W.      | Variation 22° W.  |
| 2  |          | 10 | 6              |          |                       |            |   |
| 3  |          | 10 | 4              |          |                       |            |   |
| 4  |          | 10 |                |          |                       |            |   |
| 5  | S.W.     | 6  | 2              | W.N.W.   | 1 $\frac{3}{4}$       | 6° W.      |   |
| 6  |          | 6  | 6              |          |                       |            |   |
| 7  |          | 6  | 2              |          |                       |            |   |
| 8  |          | 6  |                |          |                       |            |   |
| 9  | W. by S. | 7  | 4              | S. by W. | 1 $\frac{1}{4}$       | 14° W.     | A current set (correct magnetic W. b N. 30 miles from the time the departure was taken to the end of the day.                               |
| 10 |          | 7  | 4              |          |                       |            |   |
| 11 |          | 8  |                |          |                       |            |   |
| 12 |          | 8  | 2              |          |                       |            |   |

## EXAMPLE IV.

| H. | COURSES.                  | K. | $\frac{1}{10}$ | WINDS.                    | LEE-WAY.        | DEVIATION. | REMARKS, &c.   |
|----|---------------------------|----|----------------|---------------------------|-----------------|------------|--|
| 1  | S.W. $\frac{1}{2}$ W.     | 6  | 5              | S. by E. $\frac{1}{2}$ E. | pts.<br>2       | 6° W.      | A point of land in lat. 46° 12' S., long. 2° 10' W. bearing by compass E. by S. $\frac{1}{2}$ S., 20 miles. (Ship's head W. by compass.) Deviation 9° E. |
| 2  |                           | 6  | 2              |                           |                 |            |  |
| 3  |                           | 6  | 6              |                           |                 |            |  |
| 4  |                           | 6  | 7              |                           |                 |            |  |
| 5  | N. $\frac{3}{4}$ E.       | 8  |                | E.N.E.                    | $\frac{1}{4}$   | 6° E.      |  |
| 6  |                           | 8  | 2              |                           |                 |            |  |
| 7  |                           | 8  | 6              |                           |                 |            |  |
| 8  |                           | 9  |                |                           |                 |            |  |
| 9  | S. by E. $\frac{1}{2}$ E. | 6  | 2              | S.W. $\frac{1}{2}$ W.     | 2 $\frac{3}{4}$ | 0°         |  |
| 10 |                           | 5  | 5              |                           |                 |            |  |
| 11 |                           | 5  | 1              |                           |                 |            |  |
| 12 |                           | 4  | 6              |                           |                 |            |  |
| 1  | W. by S.                  | 6  | 2              | S. by W.                  | 2 $\frac{1}{4}$ | 8° W.      | Variation 14° E.   |
| 2  |                           | 6  |                |                           |                 |            |  |
| 3  |                           | 5  | 6              |                           |                 |            |  |
| 4  |                           | 6  | 5              |                           |                 |            |  |
| 5  | E.N.E.                    | 6  | 2              | S.E.                      | 2 $\frac{1}{2}$ | 11° E.     |  |
| 6  |                           | 6  | 5              |                           |                 |            |  |
| 7  |                           | 7  |                |                           |                 |            |  |
| 8  |                           | 6  | 6              |                           |                 |            |  |
| 9  | S.S.W. $\frac{1}{2}$ W.   | 6  | 7              | S.E.                      | 1 $\frac{3}{4}$ | 6° W.      | A current set the ship S.W. $\frac{1}{4}$ W. by compass 22 $\frac{1}{2}$ miles these last 5 hours.   |
| 10 |                           | 5  | 2              |                           |                 |            |  |
| 11 |                           | 5  | 6              |                           |                 |            |  |
| 12 |                           | 5  | 7              |                           |                 |            |  |

## EXAMPLE V.

| H. | COURSES.   | K. | $\frac{1}{10}$ | WINDS.   | LEE-<br>WAY.          | DEVI-<br>ATION. | REMARKS, &c.   |
|----|------------|----|----------------|----------|-----------------------|-----------------|--|
| 1  | W.S.W.     | 9  | 4              | N.W.     | pts.<br>$\frac{1}{2}$ | 10° W.          | A point, lat. 35° 10' N.<br>long. 5° 36' W., bear-<br>ing by compass E. by S.<br>(Ship's head N.N.E.)<br>dist. 9 miles. Devia-<br>tion 9° E. |
| 2  |            | 9  | 3              |          |                       |                 |  |
| 3  |            | 9  | 4              |          |                       |                 |  |
| 4  |            | 9  | 6              |          |                       |                 |  |
| 5  | North.     | 11 | 4              | W.N.W.   | $\frac{1}{4}$         | 3° W.           |  |
| 6  |            | 11 |                |          |                       |                 |  |
| 7  |            | 11 | 2              |          |                       |                 |  |
| 8  |            | 11 | 4              |          |                       |                 |  |
| 9  | N.W.       | 8  | 4              | W.S.W.   | $\frac{3}{4}$         | 17° W.          |  |
| 10 |            | 8  | 3              |          |                       |                 |  |
| 11 |            | 8  | 4              |          |                       |                 |  |
| 12 |            | 8  | 4              |          |                       |                 |  |
| 1  | S.W. by S. | 11 |                | W. by N. | $\frac{1}{2}$         | 5° W.           | Variation 23° W.   |
| 2  |            | 11 | 5              |          |                       |                 |  |
| 3  |            | 11 | 4              |          |                       |                 |  |
| 4  |            | 11 | 4              |          |                       |                 |  |
| 5  | W.S.W.     | 9  | 6              | N.W.     | $\frac{1}{2}$         | 10° W.          |  |
| 6  |            | 9  | 5              |          |                       |                 |  |
| 7  |            | 9  | 4              |          |                       |                 |  |
| 8  |            | 9  |                |          |                       |                 |  |
| 9  | East.      | 6  | 4              | S.S.E.   | 1                     | 15° E.          | A current set the ship<br>(correct magnetic)<br>S.E. by E., 15 miles.  |
| 10 |            | 6  | 4              |          |                       |                 |  |
| 11 |            | 6  |                |          |                       |                 |  |
| 12 |            | 6  |                |          |                       |                 |  |

## EXAMPLE VI.

| H. | COURSES.                | K. | $\frac{1}{10}$ | WINDS.                  | LEE-<br>WAY.           | DEVI-<br>ATION. | REMARKS, &c.  |
|----|-------------------------|----|----------------|-------------------------|------------------------|-----------------|---|
| 1  | N.N.W. $\frac{1}{2}$ W. | 3  | 5              | N.E.                    | pts.<br>$1\frac{3}{4}$ | $2^{\circ}$ W.  | A point, lat $29^{\circ} 59'$ N.<br>long. $32^{\circ} 54'$ E., bearing<br>by compass N.N.E. $\frac{1}{4}$ E.<br>dist. 15 miles. (Ship's<br>head N.W. by W.)<br>Deviation $6^{\circ}$ W. |
| 2  |                         | 4  | 2              |                         |                        |                 |   |
| 3  |                         | 4  | 3              |                         |                        |                 |   |
| 4  |                         | 2  | 7              |                         |                        |                 |   |
| 5  | E.S.E.                  | 3  |                | N.E.                    | 2                      | $7^{\circ}$ E.  |   |
| 6  |                         | 3  | 3              |                         |                        |                 |   |
| 7  |                         | 4  |                |                         |                        |                 |   |
| 8  |                         | 5  | 4              |                         |                        |                 |   |
| 9  | S. $\frac{3}{4}$ E.     | 5  |                | E.S.E.                  | $2\frac{1}{4}$         | $2^{\circ}$ W.  |   |
| 10 |                         | 5  | 5              |                         |                        |                 |   |
| 11 |                         | 4  | 5              |                         |                        |                 |   |
| 12 |                         | 4  | 6              |                         |                        |                 |   |
| 1  | N.E. $\frac{1}{4}$ N.   | 4  | 7              | E.S.E.                  | $1\frac{1}{2}$         | $8^{\circ}$ E.  | Variation $25^{\circ}$ W.   |
| 2  |                         | 4  | 2              |                         |                        |                 |   |
| 3  |                         | 4  | 4              |                         |                        |                 |   |
| 4  |                         | 3  | 7              |                         |                        |                 |   |
| 5  | W. $\frac{1}{2}$ N.     | 3  |                | S.S.W. $\frac{1}{2}$ W. | $1\frac{1}{4}$         | $9^{\circ}$ W.  |   |
| 6  |                         | 3  | 5              |                         |                        |                 |   |
| 7  |                         | 4  | 3              |                         |                        |                 |   |
| 8  |                         | 3  | 6              |                         |                        |                 |   |
| 9  | N. by E.                | 3  | 6              | E. by N.                | $\frac{1}{4}$          | $6^{\circ}$ E.  | A current set the ship<br>(correct magnetic)<br>N.E., 30 miles, from<br>the time the departure<br>was taken to the end<br>of the day.   |
| 10 |                         | 8  | 5              |                         |                        |                 |   |
| 11 |                         | 9  | 3              |                         |                        |                 |   |
| 12 |                         | 9  | 2              |                         |                        |                 |   |

EXAMPLE VII.

| H. | COURSES.                  | K. | $\frac{1}{10}$ | WINDS.     | LEE-WAY.              | DEVIATION. | REMARKS, &c.   |
|----|---------------------------|----|----------------|------------|-----------------------|------------|--|
| 1  | N.N.W.                    | 10 |                | West.      | pts.<br>$\frac{3}{4}$ | 1° E.      | A point, lat. 44° 20' S., long. 176° 49' W., bearing by compass E. by N. $\frac{1}{4}$ N., distance 18 miles. (Ship's head N.N.W.) Deviation as per log. |
| 2  |                           | 9  | 4              |            |                       |            |  |
| 3  |                           | 9  | 4              |            |                       |            |  |
| 4  |                           | 9  |                |            |                       |            |  |
| 5  | West.                     | 8  | 4              | N.N.W.     | 1                     | 8° W.      |  |
| 6  |                           | 8  | 4              |            |                       |            |  |
| 7  |                           | 8  | 4              |            |                       |            |  |
| 8  |                           | 8  | 4              |            |                       |            |  |
| 9  | W. by S.                  | 11 | 6              | N.W. by N. | $\frac{1}{2}$         | 9° W.      |  |
| 10 |                           | 12 | 2              |            |                       |            |  |
| 11 |                           | 11 | 8              |            |                       |            |  |
| 12 |                           | 12 |                |            |                       |            |  |
| 1  | S.S.W. $\frac{1}{4}$ W.   | 6  | 3              | West.      | $1\frac{1}{4}$        | 10° W.     | Variation 15° E.<br><br>A current set the ship (correct magnetic) N. by E., 18 miles, from the time the departure was taken to the end of the day.       |
| 2  |                           | 6  |                |            |                       |            |  |
| 3  |                           | 6  | 4              |            |                       |            |  |
| 4  |                           | 6  |                |            |                       |            |  |
| 5  | South.                    | 9  | 3              | E.S.E.     | $\frac{3}{4}$         | 8° W.      |  |
| 6  |                           | 9  | 4              |            |                       |            |  |
| 7  |                           | 9  | 5              |            |                       |            |  |
| 8  |                           | 9  | 4              |            |                       |            |  |
| 9  | E. by E. $\frac{1}{2}$ E. | 12 | 5              | E. by S.   | $\frac{1}{4}$         | 9° W.      |  |
| 10 |                           | 12 | 6              |            |                       |            |  |
| 11 |                           | 12 | 5              |            |                       |            |  |
| 12 |                           | 12 | 4              |            |                       |            |  |

EXAMPLE VIII.

| H. | COURSES.              | K. | $\frac{1}{10}$ | WINDS.   | LEE-WAY.              | DEVIATION. | REMARKS, &c.  |
|----|-----------------------|----|----------------|----------|-----------------------|------------|---|
| 1  | E.S.E.                | 12 | 4              | N.E.     | pts.<br>$\frac{1}{2}$ | 13° E.     | A point, lat. 62° 18' N. long. 63° 17' W., bearing by compass W.N.W. (Ship's head E.S.E.), dist. 21 miles. Deviation as per log.                                    |
| 2  |                       | 12 | 5              |          |                       |            |   |
| 3  |                       | 12 | 5              |          |                       |            |   |
| 4  |                       | 12 | 3              |          |                       |            |   |
| 5  | E. $\frac{3}{4}$ N.   | 4  | 4              | N.N.E.   | $3\frac{1}{4}$        | 17° E.     |   |
| 6  |                       | 4  | 3              |          |                       |            |   |
| 7  |                       | 4  | 3              |          |                       |            |   |
| 8  |                       | 4  | 3              |          |                       |            |   |
| 9  | E. $\frac{3}{4}$ S.   | 8  | 4              | S.S.E.   | $1\frac{1}{2}$        | 13° E.     |   |
| 10 |                       | 8  | 5              |          |                       |            |   |
| 11 |                       | 8  | 6              |          |                       |            |   |
| 12 |                       | 8  | 5              |          |                       |            |   |
| 1  | S.W. $\frac{3}{4}$ W. | 3  | 5              | S. by E. | $3\frac{3}{4}$        | 8° W.      | Variation 60° W.<br><br>A current set the ship (correct magnetic) E. by S. $\frac{1}{2}$ S., 49 miles, from the time the departure was taken to the end of the day. |
| 2  |                       | 3  | 5              |          |                       |            |   |
| 3  |                       | 3  | 3              |          |                       |            |   |
| 4  |                       | 3  | 2              |          |                       |            |   |
| 5  | S. by W.              | 5  | 3              | W. by S. | $2\frac{1}{4}$        | 0°         |   |
| 6  |                       | 5  | 3              |          |                       |            |   |
| 7  |                       | 5  | 3              |          |                       |            |   |
| 8  |                       | 5  | 2              |          |                       |            |   |
| 9  | W.N.W.                | 4  | 2              | North.   | 3                     | 17° W.     |   |
| 10 |                       | 4  | 2              |          |                       |            |   |
| 11 |                       | 4  | 2              |          |                       |            |   |
| 12 |                       | 4  | 2              |          |                       |            |   |

## EXAMPLE IX.

| H. | COURSES.                | K. | $\frac{1}{10}$ | WINDS.                    | LEE-WAY.               | DEVIATION. | REMARKS, &c.   |
|----|-------------------------|----|----------------|---------------------------|------------------------|------------|--|
| 1  | South.                  | 5  | 8              | E.S.E.                    | pts.<br>$1\frac{1}{4}$ | 2° E.      | A point, lat. $59^{\circ} 49' N.$ long. $43^{\circ} 54' W.$ , bearing by compass N.E. $\frac{1}{2}$ N., distance 14 miles. (Ship's head South. Deviation as per log. |
| 2  |                         | 4  | 5              |                           |                        |            |  |
| 3  |                         | 4  | 4              |                           |                        |            |  |
| 4  | N.E. $\frac{1}{2}$ N.   | 6  | 6              | E. by S. $\frac{1}{2}$ S. | 1                      | 14° E.     |  |
| 5  |                         | 6  | 4              |                           |                        |            |  |
| 6  |                         | 6  | 4              |                           |                        |            |  |
| 7  |                         | 6  | 2              |                           |                        |            |  |
| 8  | S.S.W. $\frac{1}{2}$ W. | 5  | 5              | S.E. $\frac{1}{2}$ S.     | $1\frac{1}{2}$         | 5° W.      |  |
| 9  |                         | 5  | 4              |                           |                        |            | Variation $53^{\circ} W.$  |
| 10 |                         | 5  | 4              |                           |                        |            |  |
| 11 |                         | 5  | 4              |                           |                        |            |  |
| 12 | E. $\frac{1}{2}$ S.     | 5  | 4              | S. by E. $\frac{1}{2}$ E. | $\frac{3}{4}$          | 17° E.     |  |
| 1  |                         | 8  | 3              |                           |                        |            |  |
| 2  |                         | 8  | 4              |                           |                        |            |  |
| 3  |                         | 8  | 4              |                           |                        |            |  |
| 4  | S.W. $\frac{1}{2}$ S.   | 4  | 6              | S.S.E. $\frac{1}{2}$ E.   | 2                      | 5° W.      |  |
| 5  |                         | 5  | 4              |                           |                        |            | A current set the ship (correct magnetic) S.E. $\frac{1}{4}$ E., 1.7 knots per hour during the whole of the day.   |
| 6  |                         | 4  | 4              |                           |                        |            |  |
| 7  |                         | 4  | 4              |                           |                        |            |  |
| 8  | S.E. $\frac{1}{2}$ S.   | 6  | 4              | E. by N. $\frac{1}{2}$ N. | 1                      | 10° E.     |  |
| 9  |                         | 6  | 2              |                           |                        |            |  |
| 10 |                         | 6  | 6              |                           |                        |            |  |
| 11 |                         | 6  | 6              |                           |                        |            |  |
| 12 |                         | 6  | 3              |                           |                        |            |  |

## EXAMPLE X.

| H. | COURSES.                  | K. | $\frac{1}{10}$ | WINDS.                    | LEE-WAY.               | DEVIATION.                | REMARKS, &c.   |
|----|---------------------------|----|----------------|---------------------------|------------------------|---------------------------|--|
| 1  | S.W. $\frac{1}{2}$ W.     | 4  | 8              | S. by E.                  | pts.<br>$2\frac{1}{4}$ | 6° W.                     | A point of land, lat. $36^{\circ} 10' S.$ , long. $110^{\circ} 10' W.$ , bearing by compass E. by N., dist 14 miles. (Ship's head S.W. $\frac{1}{2}$ W.) Deviation as per log. |
| 2  |                           | 5  | 2              |                           |                        |                           |  |
| 3  |                           | 5  | 2              |                           |                        |                           |  |
| 4  | W. by S. $\frac{1}{2}$ S. | 5  | 3              | S. by W.                  | $2\frac{1}{2}$         | 10° W.                    |  |
| 5  |                           | 4  | 3              |                           |                        |                           |  |
| 6  |                           | 4  | 3              |                           |                        |                           |  |
| 7  |                           | 4  | 3              |                           |                        |                           |  |
| 8  | W. by N. $\frac{3}{4}$ N. | 6  | 3              | S.W.                      | 2                      | $8\frac{1}{2}^{\circ} W.$ |  |
| 9  |                           | 5  | 4              |                           |                        |                           | Variation $20^{\circ} E.$  |
| 10 |                           | 6  | 2              |                           |                        |                           |  |
| 11 |                           | 6  | 4              |                           |                        |                           |  |
| 12 | N.W. $\frac{1}{2}$ W.     | 5  | 6              | W. by S. $\frac{3}{4}$ S. | $2\frac{1}{2}$         | $5\frac{1}{2}^{\circ} W.$ |  |
| 1  |                           | 5  | 4              |                           |                        |                           |  |
| 2  |                           | 5  | 5              |                           |                        |                           |  |
| 3  |                           | 5  | 8              |                           |                        |                           |  |
| 4  | W. by S.                  | 7  | 4              | S. $\frac{1}{2}$ W.       | $1\frac{1}{2}$         | 9° W.                     |  |
| 5  |                           | 7  | 4              |                           |                        |                           | A current set the ship the last 8 hours E. $\frac{1}{2}$ S. (correct magnetic) 2 miles an hour.  |
| 6  |                           | 8  | 2              |                           |                        |                           |  |
| 7  |                           | 8  | 2              |                           |                        |                           |  |
| 8  | S.W.                      | 5  | 2              | S. by E.                  | $2\frac{1}{2}$         | 5° W.                     |  |
| 9  |                           | 4  |                |                           |                        |                           |  |
| 10 |                           | 5  | 7              |                           |                        |                           |  |
| 11 |                           | 5  | 4              |                           |                        |                           |  |
| 12 |                           | 5  | 4              |                           |                        |                           |  |



## EXAMPLE XI.

| H. | COURSES.   | K. | $\frac{1}{10}$ | WINDS.     | LEE-WAY.      | DEVIATION. | REMARKS, &c.   |
|----|------------|----|----------------|------------|---------------|------------|--|
| 1  | N.W. by W. | 8  | 4              | N. by E.   | $\frac{3}{4}$ | 4° W.      | A point of land in lat. 55° 59' S., long. 67° 16' W., bearing by compass E.S.E., dist. 17 miles. (Ship's head W.) Dev. 8° W. |
| 2  |            | 8  | 4              |            |               |            |  |
| 3  |            | 8  | 4              |            |               |            |  |
| 4  |            | 8  | 4              |            |               |            |  |
| 5  | North.     | 6  | 6              | E.N.E.     | 1             | 3° E.      |  |
| 6  |            | 5  | 6              |            |               |            |  |
| 7  |            | 5  | 6              |            |               |            |  |
| 8  |            | 6  |                |            |               |            |  |
| 9  | N.W. by N. | 11 | 4              | N.E. by N. | $\frac{1}{4}$ | 1° W.      | Variation 23° W.   |
| 10 |            | 11 |                |            |               |            |  |
| 11 |            | 11 | 2              |            |               |            |  |
| 12 |            | 11 |                |            |               |            |  |
| 1  | West.      | 11 | 4              | S.S.W.     | $\frac{1}{4}$ | 9° W.      |  |
| 2  |            | 11 | 6              |            |               |            |  |
| 3  |            | 12 | 4              |            |               |            |  |
| 4  |            | 12 | 4              |            |               |            |  |
| 5  | N.N.E.     | 7  | 3              | East.      | 1             | 15° E.     | A current set the ship N. by W. correct magnetic, 27 miles, from the time the departure was taken to the end of the day.     |
| 6  |            | 7  | 4              |            |               |            |  |
| 7  |            | 7  | 4              |            |               |            |  |
| 8  |            | 7  | 4              |            |               |            |  |
| 9  | S.S.E.     | 9  | 5              | East.      | $\frac{1}{2}$ | 5° W.      |  |
| 10 |            | 9  | 5              |            |               |            |  |
| 11 |            | 9  | 4              |            |               |            |  |
| 12 |            | 9  | 4              |            |               |            |  |

## EXAMPLE XII.

| H. | COURSES.   | K. | $\frac{1}{10}$ | WINDS.     | LEE-WAY.       | DEVIATION. | REMARKS, &c.   |
|----|------------|----|----------------|------------|----------------|------------|--|
| 1  | W.N.W.     | 6  | 3              | S.W.       | pts.<br>1      | 18° W.     | A point, Butt of Lewis in lat. 58° 29' N., long. 6° 12' W., bearing by compass S.E. by S., dist. 15 miles. (Ship's head West) Deviation 16° W. |
| 2  |            | 6  | 3              |            |                |            |  |
| 3  |            | 6  | 2              |            |                |            |  |
| 4  |            | 6  | 2              |            |                |            |  |
| 5  | S.W. by W. | 6  | 2              | N.W. by W. | $1\frac{1}{4}$ | 9° W.      |  |
| 6  |            | 5  | 8              |            |                |            |  |
| 7  |            | 5  | 6              |            |                |            |  |
| 8  |            | 5  | 4              |            |                |            |  |
| 9  | W. by N.   | 5  | 2              | N. by W.   | $1\frac{1}{2}$ | 17° W.     | Variation 31° W.   |
| 10 |            | 4  | 8              |            |                |            |  |
| 11 |            | 4  | 6              |            |                |            |  |
| 12 |            | 4  | 4              |            |                |            |  |
| 1  | N. by W.   | 3  | 2              | W. by N.   | $2\frac{1}{2}$ | 7° W.      |  |
| 2  |            | 2  | 6              |            |                |            |  |
| 3  |            | 3  | 2              |            |                |            |  |
| 4  | W. by S.   | 5  | 6              | N.W. by N. | $1\frac{3}{4}$ | 14° W.     |  |
| 5  |            | 4  | 6              |            |                |            | A current set (correct magnetic) E.S.E., 9 miles, from the time the departure was taken to the end of the day.                                 |
| 6  |            | 4  | 4              |            |                |            |  |
| 7  |            | 5  |                |            |                |            |  |
| 8  | W.N.W.     | 5  | 3              | North.     | $1\frac{1}{4}$ | 18° W.     |  |
| 9  |            | 5  | 3              |            |                |            |  |
| 10 |            | 5  | 4              |            |                |            |  |
| 11 | North.     | 6  | 5              | W.N.W.     | $\frac{1}{2}$  | 2° W.      |  |
| 12 |            | 6  | 5              |            |                |            |  |

## EXAMPLE XIII.

| H. | COURSES.                | K. | $\frac{1}{10}$ | WINDS.   | LEE-WAY.               | DEVIATION. | REMARKS, &c.   |
|----|-------------------------|----|----------------|----------|------------------------|------------|--|
| 1  | S. E. by E.             | 3  | 2              | S. by W. | pts.<br>$2\frac{1}{2}$ | 8° E.      | A point of land in lat 62° 9' S., long. 140° 17' E., bearing by compass S.S.W. $\frac{1}{2}$ W. dist. 25 miles. (Ship's head S.E. $\frac{1}{2}$ E.) Dev. 7° E. |
| 2  |                         | 3  | 4              |          |                        |            |  |
| 3  |                         | 3  | 4              |          |                        |            |  |
| 4  | W. by S.                | 5  |                | S. by W. | $1\frac{3}{4}$         | 11° W.     |  |
| 5  |                         | 4  | 4              |          |                        |            |  |
| 6  | S.S.W.                  | 4  | 6              | West.    | 2                      | 3° W.      |  |
| 7  |                         | 4  | 5              |          |                        |            |  |
| 8  |                         | 4  | 3              |          |                        |            |  |
| 9  |                         | 4  | 2              |          |                        |            |  |
| 10 | N.N.W.                  | 3  | 6              | West.    | $2\frac{3}{4}$         | 5° W.      |  |
| 11 |                         | 3  | 4              |          |                        |            |  |
| 12 |                         | 3  | 2              |          |                        |            |  |
| 1  |                         | 2  | 8              |          |                        |            | Variation 31° E.   |
| 2  | N.N.E. $\frac{1}{4}$ E. | 2  | 4              | East.    | $3\frac{1}{4}$         | 5° E.      |  |
| 3  |                         | 2  | 2              |          |                        |            |  |
| 4  |                         | 1  | 8              |          |                        |            |  |
| 5  |                         | 1  | 6              |          |                        |            | A current set by compass S. $\frac{3}{4}$ W., 3 miles an hour for $7\frac{1}{2}$ hours.  |
| 6  | S.S.E.                  | 2  | 4              | East.    | 3                      | 5° E.      |  |
| 7  |                         | 2  | 2              |          |                        |            |  |
| 8  |                         | 2  | 4              |          |                        |            |  |
| 9  | East.                   | 1  | 6              | N.N.E.   | $3\frac{1}{2}$         | 11° E.     |  |
| 10 |                         | 1  | 4              |          |                        |            |  |
| 11 | N.W.                    | 1  | 5              | N.N.E.   | 4                      | 8° W.      |  |
| 12 |                         | 1  | 5              |          |                        |            |  |

## EXAMPLE XIV.

| H. | COURSES.                  | K. | $\frac{1}{10}$ | WINDS.              | LEE-WAY.               | DEVIATION. | REMARKS, &c.   |
|----|---------------------------|----|----------------|---------------------|------------------------|------------|--|
| 1  | S.S.W. $\frac{1}{4}$ W.   | 3  | 6              | West.               | pts.<br>$2\frac{3}{4}$ | 11° W.     | A point, lat. 50° 20' S. long. 20° 10' E., bearing by compass N.E. $\frac{1}{2}$ N. dist. 15 miles. Deviation 25° E. (Ship's head E. $\frac{1}{2}$ N.) |
| 2  |                           | 3  | 5              |                     |                        |            |  |
| 3  |                           | 4  |                |                     |                        |            |  |
| 4  |                           | 4  | 2              |                     |                        |            |  |
| 5  | S.S.W.                    | 6  | 4              | W. $\frac{1}{2}$ N. | $1\frac{3}{4}$         | 10° W.     |  |
| 6  |                           | 6  | 5              |                     |                        |            |  |
| 7  |                           | 6  | 4              |                     |                        |            |  |
| 8  |                           | 6  | 3              |                     |                        |            |  |
| 9  | N.N.W. $\frac{1}{2}$ W.   | 6  |                | W. $\frac{1}{2}$ S. | 2                      | 13° W.     | Variation $2\frac{1}{4}$ pts. W.<br><i>25° 19'</i>   |
| 10 |                           | 6  | 2              |                     |                        |            |  |
| 11 |                           | 6  |                |                     |                        |            |  |
| 12 |                           | 5  | 8              |                     |                        |            |  |
| 1  | E. by S. $\frac{3}{4}$ S. | 5  | 4              | S. $\frac{1}{2}$ E. | $2\frac{1}{4}$         | 21° E.     |  |
| 2  |                           | 5  | 6              |                     |                        |            |  |
| 3  |                           | 5  | 5              |                     |                        |            |  |
| 4  | S.W. by W.                | 5  | 5              | Ditto.              | $2\frac{1}{2}$         | 18° W.     |  |
| 5  |                           | 5  | 4              |                     |                        |            | A current set the ship by compass (correct magnetic) E.S.E., 2 miles an hour during the whole day.   |
| 6  |                           | 5  | 4              |                     |                        |            |  |
| 7  |                           | 5  | 3              |                     |                        |            |  |
| 8  |                           | 5  | 6              |                     |                        |            |  |
| 9  | S. $\frac{1}{2}$ E.       | 10 | 6              | West.               | 0                      | 1° W.      |  |
| 10 |                           | 11 | 4              |                     |                        |            |  |
| 11 |                           | 12 | 4              |                     |                        |            |  |
| 12 |                           | 12 | 6              |                     |                        |            |  |

## EXAMPLE XV.

| H. | COURSES.                  | K. | $\frac{1}{10}$ | WINDS.              | LEE-WAY.           | DEVIATION.            | REMARKS, &c.  |
|----|---------------------------|----|----------------|---------------------|--------------------|-----------------------|---|
| 1  | S. by E. $\frac{1}{2}$ E. | 12 |                | E. $\frac{1}{2}$ S. | pts. $\frac{1}{4}$ | 5° E.                 | A point of land in lat. 46° 20' S., long. 176° 44' W., bearing by compass E. by N. $\frac{1}{4}$ N. dist. 23 miles. (Ship's head S. by E. $\frac{1}{2}$ E.) Deviation as per log. |
| 2  |                           | 11 | 6              |                     |                    |                       |   |
| 3  |                           | 12 | 2              |                     |                    |                       |   |
| 4  |                           | 12 | 3              |                     |                    |                       |   |
| 5  | S. by W.                  | 9  | 2              | S.E. by E.          | $\frac{3}{4}$      | 26° E.                |   |
| 6  |                           | 9  | 6              |                     |                    |                       |   |
| 7  |                           | 9  | 4              |                     |                    |                       |   |
| 8  |                           | 7  | 5              | W.                  | $1\frac{1}{4}$     | 2 $\frac{1}{2}$ ° W.  |   |
| 9  | S.S.W. $\frac{1}{4}$ W.   | 7  | 5              |                     |                    |                       | Variation 15° E.  |
| 10 |                           | 7  | 4              |                     |                    |                       |   |
| 11 |                           | 7  | 6              |                     |                    |                       |   |
| 12 |                           | 7  | 6              |                     |                    |                       |   |
| 1  | W. by S.                  | 11 | 3              | N.W. by N.          | $\frac{1}{2}$      | 16 $\frac{1}{2}$ ° E. |   |
| 2  |                           | 10 | 8              |                     |                    |                       |   |
| 3  |                           | 10 | 8              |                     |                    |                       |   |
| 4  |                           | 10 | 6              |                     |                    |                       |   |
| 5  | W.                        | 9  | 8              | N.N.W.              | 1                  | 17° E.                | A current set the ship N.W. $\frac{1}{4}$ W. (correct magnetic) $1\frac{1}{2}$ knots per hour, from the time the departure was taken to the end of the day.                       |
| 6  |                           | 9  | 6              |                     |                    |                       |   |
| 7  |                           | 9  | 4              |                     |                    |                       |   |
| 8  |                           | 9  | 6              |                     |                    |                       |   |
| 9  | N.N.W.                    | 9  | 3              | W.                  | $\frac{3}{4}$      | 20 $\frac{1}{2}$ ° W. |   |
| 10 |                           | 9  | 4              |                     |                    |                       |   |
| 11 |                           | 9  | 6              |                     |                    |                       |   |
| 12 |                           | 9  | 5              |                     |                    |                       |   |

## EXAMPLE XVI.

| H. | COURSES.                    | K. | $\frac{1}{10}$ | WINDS.                      | LEE-WAY.            | DEVIATION. | REMARKS, &c.   |
|----|-----------------------------|----|----------------|-----------------------------|---------------------|------------|--|
| 1  | E. $\frac{1}{2}$ N.         | 4  | 8              | S.S.E. $\frac{1}{2}$ E.     | pts. $1\frac{1}{4}$ | 12° E.     | A point of land in lat. 46° 37' N., long. 53° 30' W., bearing by compass S.W. $\frac{3}{4}$ W. dist. 19 miles. (Ship's head E. $\frac{1}{2}$ N.) Deviation as per log. |
| 2  |                             | 5  | 2              |                             |                     |            |  |
| 3  |                             | 5  | 2              |                             |                     |            |  |
| 4  |                             | 4  | 8              |                             |                     |            |  |
| 5  | N. by E. $\frac{3}{4}$ E.   | 7  | 6              | E. $\frac{1}{2}$ N.         | $\frac{1}{2}$       | 20° E.     |  |
| 6  |                             | 7  | 8              |                             |                     |            |  |
| 7  |                             | 8  | 8              |                             |                     |            |  |
| 8  |                             | 9  | 6              |                             |                     |            |  |
| 9  | S.E. $\frac{1}{4}$ S.       | 10 | 6              | N.E. by E. $\frac{1}{2}$ E. | $\frac{1}{4}$       | 9° W.      | Variation 31° West.  |
| 10 |                             | 9  | 4              |                             |                     |            |  |
| 11 |                             | 9  | 4              |                             |                     |            |  |
| 12 |                             | 10 |                |                             |                     |            |  |
| 1  | W. by N. $\frac{1}{4}$ N.   | 9  | 6              | S.W. $\frac{1}{2}$ W.       | $\frac{1}{2}$       | 6° W.      |  |
| 2  |                             | 8  | 6              |                             |                     |            |  |
| 3  |                             | 9  | 8              |                             |                     |            |  |
| 4  |                             | 8  | 4              |                             |                     |            |  |
| 5  | N.E. $\frac{3}{4}$ E.       | 10 | 4              | N.N.W.                      | $\frac{1}{4}$       | 20° E.     | A current set the ship (correct magnetic) E. by N. $\frac{1}{2}$ N., 17 miles, from the time the departure was taken to the end of the day.                            |
| 6  |                             | 10 | 6              |                             |                     |            |  |
| 7  |                             | 9  | 8              |                             |                     |            |  |
| 8  |                             | 9  | 2              |                             |                     |            |  |
| 9  | S.E. by E. $\frac{3}{4}$ E. | 8  | 5              | N.E. $\frac{1}{2}$ E.       | $\frac{1}{2}$       | 2° W.      |  |
| 10 |                             | 8  | 5              |                             |                     |            |  |
| 11 |                             | 7  | 8              |                             |                     |            |  |
| 12 |                             | 7  | 2              |                             |                     |            |  |

## EXAMPLE XVII.

| H. | COURSES.              | K. | $\frac{1}{10}$ | WINDS.                    | LEE-WAY.        | DEVIATION.            | REMARKS, &c.   |
|----|-----------------------|----|----------------|---------------------------|-----------------|-----------------------|--|
| 1  | W.N.W.                | 13 | 4              | S.E.                      | pts.<br>0       | 23 $\frac{1}{2}$ ° W. | A point, lat. 51° 8 $\frac{1}{2}$ ' N. long. 1° 23' E., bearing by compass S.W. $\frac{3}{4}$ S., dist. 25 miles. (Ship's head W.N.W. Dev. as per log. |
| 2  |                       | 13 |                |                           |                 |                       |  |
| 3  |                       | 13 | 6              |                           |                 |                       |  |
| 4  | W. $\frac{1}{2}$ S.   | 10 |                | S.S.W.                    | $\frac{1}{2}$   | 23° W.                |  |
| 5  |                       | 9  | 6              |                           |                 |                       | Variation 25° W.   |
| 6  |                       | 9  | 4              |                           |                 |                       |  |
| 7  |                       | 9  | 5              |                           |                 |                       |  |
| 8  |                       | 9  | 5              |                           |                 |                       |  |
| 9  | West.                 | 8  | 4              | N.N.W.                    | $\frac{3}{4}$   | 23 $\frac{1}{2}$ ° W. |  |
| 10 |                       | 8  | 4              |                           |                 |                       |  |
| 11 |                       | 8  | 4              |                           |                 |                       |  |
| 12 |                       | 8  | 6              |                           |                 |                       |  |
| 1  | N. $\frac{3}{4}$ E.   | 9  | 5              | N.W. by W.                | $\frac{1}{2}$   | 5 $\frac{1}{4}$ ° E.  |  |
| 2  |                       | 9  | 4              |                           |                 |                       |  |
| 3  |                       | 9  | 6              |                           |                 |                       |  |
| 4  |                       | 9  | 4              |                           |                 |                       |  |
| 5  | North.                | 10 | 5              | W.N.W.                    | $\frac{1}{4}$   | 0 $\frac{3}{4}$ ° E.  | A current set the ship N.W. by W. $\frac{3}{4}$ W., correct magnetic, 32 miles from the time the departure was taken to the end of the day.            |
| 6  |                       | 10 | 6              |                           |                 |                       |  |
| 7  |                       | 11 |                |                           |                 |                       |  |
| 8  |                       | 10 | 4              |                           |                 |                       |  |
| 9  | N.W. $\frac{1}{4}$ W. | 7  | 4              | N. by E. $\frac{1}{2}$ E. | 1 $\frac{1}{4}$ | 20° W.                |  |
| 10 |                       | 7  |                |                           |                 |                       |  |
| 11 |                       | 7  | 4              |                           |                 |                       |  |
| 12 |                       | 7  | 4              |                           |                 |                       |  |

## EXAMPLE XVIII.

| H. | COURSES.            | K. | $\frac{1}{10}$ | WINDS.                  | LEE-WAY.        | DEVIATION. | REMARKS, &c.  |
|----|---------------------|----|----------------|-------------------------|-----------------|------------|---|
| 1  | E. $\frac{1}{4}$ S. | 12 | 4              | North.                  | pts.<br>0       | 20° E.     | A point, lat. 37° 45' N. long. 15° 0' E., bearing by compass W. $\frac{1}{2}$ N. dist. 42 miles. (Ship's head E. $\frac{1}{4}$ S. Deviation as per log. |
| 2  |                     | 13 |                |                         |                 |            |   |
| 3  |                     | 13 | 6              |                         |                 |            |   |
| 4  |                     | 14 |                |                         |                 |            |   |
| 5  | E. $\frac{1}{2}$ S. | 12 |                | N.N.E. $\frac{1}{2}$ E. | $\frac{1}{4}$   | 17° E.     | Variation 14° W.  |
| 6  |                     | 11 | 4              |                         |                 |            |   |
| 7  |                     | 11 | 6              |                         |                 |            |   |
| 8  |                     | 12 |                |                         |                 |            |   |
| 9  | S.S.E.              | 5  | 4              | East.                   | 2 $\frac{1}{4}$ | 2° E.      |   |
| 10 |                     | 5  | 5              |                         |                 |            |   |
| 11 |                     | 5  | 6              |                         |                 |            |   |
| 12 |                     | 5  | 5              |                         |                 |            |   |
| 1  | N.N.E.              | 2  | 4              | East.                   | 3 $\frac{1}{4}$ | 11° E.     |   |
| 2  |                     | 2  |                |                         |                 |            |   |
| 3  |                     | 1  | 6              |                         |                 |            |   |
| 4  |                     | 2  |                |                         |                 |            |   |
| 5  | E. $\frac{1}{2}$ S. | 9  | 5              | N.N.E. $\frac{1}{2}$ E. | $\frac{1}{2}$   | 17° E.     | A current set E.S.E. (correct magnetic) 2 $\frac{1}{2}$ miles per hour for the last 21 hours.   |
| 6  |                     | 9  | 5              |                         |                 |            |   |
| 7  |                     | 9  |                |                         |                 |            |   |
| 8  |                     | 9  |                |                         |                 |            |   |
| 9  | E.S.E.              | 8  | 4              | N.E.                    | $\frac{3}{4}$   | 14° E.     |   |
| 10 |                     | 8  | 6              |                         |                 |            |   |
| 11 |                     | 8  | 5              |                         |                 |            |   |
| 12 |                     | 9  |                |                         |                 |            |   |

| No. | COURSES.                  | DIST. | WINDS.                      | LEE-WAY.        | DEVIATION. | REMARKS, &c.  |
|-----|---------------------------|-------|-----------------------------|-----------------|------------|---|
| 19. | S. $\frac{1}{2}$ W.       | 9     | S.E. by E.                  | pts.            | 1° W.      | A point, in lat. 34° 50' S., long. 25° 1' E., bearing by compass N. $\frac{1}{2}$ W., distance 15 miles. (Ship's head S. by E. $\frac{1}{2}$ E. Dev. 5° E. Variation 28° West.<br>A current set by compass W. by S. $2\frac{1}{2}$ miles an hour from the time the departure was taken to the end of the day.     |
|     | E.N.E.                    | 11    | S E.                        | 1 $\frac{3}{4}$ | 18° E.     |   |
|     | S.S.E.                    | 19    | East.                       | 2 $\frac{1}{4}$ | 6° E.      |   |
|     | E.S.E.                    | 13    | N.E.                        | 1 $\frac{1}{2}$ | 13° E.     |   |
|     | S.E.                      | 26    | E.N.E.                      | 1 $\frac{3}{4}$ | 10° E.     |   |
|     | E.N.E.                    | 7     | N.                          | 2 $\frac{1}{4}$ | 18° E.     |   |
|     | N.W. by N.                | 10    | N.E. by N.                  | 1               | 16° W.     |   |
|     | S.E. $\frac{1}{2}$ E.     | 22    | N.E. by E.                  | 1 $\frac{1}{2}$ | 10° E.     |   |
|     | N.E.                      | 13    | N.N.W.                      | 2 $\frac{1}{2}$ | 15° E.     |   |
|     |                           |       |                             |                 |            |   |
| 20. | S.W.                      | 10.7  | W.N.W.                      | 1               | 6° W.      | A point, in lat. 25° 30' S., long. 45° 7' E., bearing by compass N.E. by E. $\frac{1}{2}$ E., distance 17 miles. (Ship's head S.W.) Dev. as per log.<br>Variation 22° West.<br>A current set by compass S.W. $\frac{1}{2}$ W. 35 miles, from the time the departure was taken to the end of the day.              |
|     | W.N.W.                    | 8.7   | S.W.                        | 1 $\frac{1}{2}$ | 10° W.     |   |
|     | W. by S.                  | 27.9  | S. by W.                    | 1 $\frac{1}{2}$ | 11° W.     |   |
|     | S.E. by S.                | 28    | S.W. by S.                  | 1 $\frac{1}{2}$ | 5° E.      |   |
|     | S.W. by W.                | 8.7   | S. by E.                    | 1 $\frac{1}{2}$ | 8° W.      |   |
|     | E. by S.                  | 12.2  | S. by E.                    | 1 $\frac{1}{2}$ | 10° E.     |   |
|     | S.S.W. $\frac{1}{2}$ W.   | 11.4  | S.E. $\frac{1}{2}$ S.       | 2 $\frac{1}{2}$ | 4° W.      |   |
|     | S. by E.                  | 11.2  | S.W. by W.                  | 1 $\frac{1}{2}$ | 2° E.      |   |
|     | S.W. $\frac{1}{2}$ S.     | 6.7   | W. by N. $\frac{1}{2}$ N.   | 2               | 6° W.      |   |
|     |                           |       |                             |                 |            |   |
| 21. | East.                     | 52.9  | S.S.E.                      | 1 $\frac{1}{2}$ | 11° E.     | A point, Cape East, in lat. 37° 42' S., long. 178° 40' E., bearing by compass W. $\frac{1}{2}$ S. dist. 23 miles. (Ship's head East.) Dev. as per log.<br>Variation 14° East.<br>A current set by compass E. by N. $\frac{1}{2}$ N., 48 miles, from the time the departure was taken to the end of the day.       |
|     | South.                    | 10.5  | E.S.E.                      | 1 $\frac{1}{2}$ | 1° E.      |   |
|     | N.N.E.                    | 23.4  | East.                       | 1 $\frac{1}{2}$ | 4° E.      |   |
|     | S.E. $\frac{1}{2}$ E.     | 12    | N.E. by E. $\frac{1}{2}$ E. | 2               | 7° E.      |   |
|     | E.S.E.                    | 25.1  | N.E.                        | 1               | 8° E.      |   |
|     | E. by N. $\frac{1}{2}$ N. | 13    | N. by E.                    | 2 $\frac{1}{2}$ | 11° E.     |   |
|     | East.                     | 22.2  | N.N.E.                      | 1 $\frac{1}{2}$ | 11° E.     |   |
|     | E. $\frac{1}{2}$ N.       | 37.6  | S.E. by S.                  | 1 $\frac{1}{2}$ | 10° E.     |   |
|     |                           |       |                             |                 |            |   |
|     |                           |       |                             |                 |            |   |
| 22. | W.N.W.                    | 30    | North.                      | 1 $\frac{1}{2}$ | 10° W.     | A point, lat. 56° 27' S., long. 68° 37' W., bearing by compass E. $\frac{1}{2}$ S., distance 15 miles. (Ship's head W.N.W.) Dev. as per log.<br>Variation 22½° East.<br>A current set the ship S.S.W. $\frac{1}{2}$ W. (correct magnetic), 19 miles, from the time the departure was taken to the end of the day. |
|     | S.W. by W.                | 14.8  | N.W. by W.                  | 1 $\frac{1}{2}$ | 8° W.      |   |
|     | N. by E. $\frac{1}{2}$ E. | 16.2  | N.W. $\frac{1}{2}$ W.       | 1 $\frac{1}{2}$ | 3° E.      |   |
|     | N.W.                      | 16.6  | N.N.E.                      | 1 $\frac{1}{2}$ | 8° W.      |   |
|     | N. $\frac{1}{2}$ W.       | 8.3   | W.N.W.                      | 2 $\frac{1}{2}$ | 2° W.      |   |
|     | S.W. $\frac{1}{2}$ W.     | 11    | W.N.W.                      | 3               | 7° W.      |   |
|     | W.N.W.                    | 12.4  | S.W.                        | 2 $\frac{1}{2}$ | 10° W.     |   |
|     | S.W. by W.                | 30    | N.W. by W.                  | 1 $\frac{1}{2}$ | 8° W.      |   |
|     | N. by W. $\frac{1}{2}$ W. | 25.9  | N.E. $\frac{1}{2}$ E.       | 1 $\frac{1}{2}$ | 4° W.      |   |
|     |                           |       |                             |                 |            |   |
| 23. | W. $\frac{3}{4}$ N.       | 38    | N. by W. $\frac{1}{4}$ W.   | 1 $\frac{1}{2}$ | 12° W.     | A point, in lat. 16° 5' S., long. 179° 36' W., bearing by compass N.E., dist. 15 miles. (Ship's head S.W. by W.) Dev. 8° W. Variation 37° West.<br>A current set the ship during the day S.W. $\frac{1}{2}$ S. (correct magnetic) 24 miles.   |
|     | W.                        | 26    | N.N.W.                      | 1 $\frac{1}{2}$ | 13° W.     |   |
|     | N.N.W.                    | 34    | N.E.                        | 1 $\frac{1}{2}$ | 5° W.      |   |
|     | S.W. by W.                | 56    | N.E.                        | 0               | 8° W.      |   |
|     | S.S.W.                    | 45    | S.E.                        | 1 $\frac{1}{4}$ | 3° W.      |   |
|     | S. by E.                  | 26    | S.W. by W.                  | 1 $\frac{1}{4}$ | 2° E.      |   |
|     |                           |       |                             |                 |            |   |

## PRELIMINARY RULES IN NAUTICAL ASTRONOMY.

### CIVIL AND ASTRONOMICAL DAY.

261. The **Civil Day**, or common method of reckoning time, begins at midnight, and ends the following midnight, the interval being divided into two periods of 12 hours each; the first twelve hours, from midnight to noon, are denoted by A.M. (*ante meridian*); the latter, from noon to midnight are styled P.M. (*post meridian*); thus we say 10 A.M. when an event occurred at 10 o'clock in the morning, and 10 P.M. when it occurred at 10 o'clock in the evening.

262. The **Astronomical Day** begins at noon and ends at the following noon, and is later than the civil day by twelve hours. The hours are reckoned throughout, or continuously from  $0^h$  to  $24^h$ . The distinction of A.M. and P.M. is not recognised in astronomical time. Thus, 11 o'clock in the forenoon of the second of January in the civil reckoning of time corresponds to January 1 day 23 hours in the astronomical reckoning; and 1 o'clock in the afternoon of the former to January 2 days 1 hour of the latter reckoning.

263. Since the civil day commences at the midnight *preceding* the noon which commences the astronomical day, it is evident that the civil mode of reckoning is always twelve hours in advance of the civil reckoning, and hence we have the following Rule for converting civil into astronomical time.

Given civil time at ship, to reduce it to astronomical time.

#### RULE LXXVII.

1°. If the civil time at ship be P.M., it will also be astronomical time, P.M. being omitted.

2°. If the civil time be A.M., add twelve to the hours and subtract one from the days of the month; also omit A.M. The result in each case is the Astronomical Date.

#### EXAMPLES.

Ex. 1. May 10th, at  $5^h 30^m$  P.M., civil time is  $5^h 30^m$  astronomical time of the same date; because the 10th astronomical day begins at noon of the 10th civil day, and  $5^h 30^m$  have elapsed since that noon. But  $5^h 30^m$  A.M. civil time on May 10th is  $17^h 30^m$  astronomical time on the 9th of May, for the 9th day of the month, according to the astronomical reckoning, commences at noon of the 9th civil time, and ends at noon of the 10th civil day (the hours being reckoned up to 24) and  $5^h 30^m$  A.M. of the 10th is  $17^h 30^m$  from noon of the 9th.

Ex. 2. October 7th, at  $3^h 20^m$  P.M., civil time, is October 7th, at  $3^h 20^m$  astronomical time. (See 1° of Rule LXXVII.)

Ex. 3. October 7th, at  $3^h 20^m$  A.M., civil date, is October 6th  $15^h 20^m$  astronomical date; since 7th less 1st is 6th, and  $12^h$  added to  $3^h 20^m$  is  $15^h 20^m$ . (See 2° of Rule.)

Ex. 4. January 31st, at  $7^h 20^m$  P.M., civil time, is January 31st, at  $7^h 20^m$  astronomical time. (Rule LXXVII, 1°.)

Ex. 5. February 1<sup>st</sup>, at 6<sup>h</sup> 18<sup>m</sup> A.M., civil date, is January 31<sup>d</sup> 18<sup>h</sup> 18<sup>m</sup> astronomical date; since February 1<sup>d</sup>, diminished by 1<sup>d</sup>, gives January 31<sup>d</sup>, and 12<sup>h</sup> added to 6<sup>h</sup> 18<sup>m</sup> is 18<sup>h</sup> 18<sup>m</sup>. (Rule LXXVII, 2°.)

Ex. 6. What is the astronomical date corresponding to 1873, January 1<sup>st</sup>, 8<sup>h</sup> A.M. The corresponding astronomical date is 1872, December 31<sup>d</sup> 20<sup>h</sup>. In this case the year is diminished by 1, since in diminishing the day of the month by 1, the reckoning throws us back into the last month of the previous year, *i.e.*, the day before January 1<sup>st</sup>, 1873, also 12<sup>h</sup> added to 8<sup>h</sup> is 20<sup>h</sup>.

### EXAMPLES FOR PRACTICE.

Express the following dates in astronomical time.

|  |  |
|--|--|
| 1. Jan. 2 <sup>nd</sup> , 4 <sup>h</sup> 38 <sup>m</sup> 9 <sup>s</sup> A.M. | 7. Dec. 31 <sup>st</sup> , 6 <sup>h</sup> 18 <sup>m</sup> 34 <sup>s</sup> P.M. |
| 2. Feb. 27 <sup>th</sup> , 8 12 0 P.M.                                       | 8. July 1 <sup>st</sup> , 8 3 24 P.M.  |
| 3. Aug. 14 <sup>th</sup> , 6 28 40 P.M.                                      | 9. July 1 <sup>st</sup> , 11 30 10 A.M.  |
| 4. April 1 <sup>st</sup> , 7 54 19 A.M.                                      | 10. Oct. 1 <sup>st</sup> , 0 10 12 P.M.  |
| 5. June 4 <sup>th</sup> , 4 18 3 A.M.  | 11. 1872, Jan. 1 <sup>st</sup> , 8 9 50 A.M.                                   |
| 6. Sept. 1 <sup>st</sup> , 8 10 52 A.M.                                      | 12. 1873, Jan. 1 <sup>st</sup> , 0 44 12 A.M.                                  |

264. Given the astronomical date to find the corresponding civil date.

### RULE LXXVIII.

If the hours of astronomical time be less than 12<sup>h</sup> write P.M. after it, and it will be the required civil time; but if the astronomical time be greater than 12<sup>h</sup>, add 1 to the days, diminish the hours by 12 and write A.M. after it: the result will be the required civil time.

Express the following astronomical dates in civil time:—

|  |  |
|--|--|
| (1.) Jan. 10 <sup>th</sup> , 16 <sup>h</sup> 31 <sup>m</sup> 15 <sup>s</sup> | (2.) Oct. 14 <sup>th</sup> , 15 <sup>h</sup> 17 <sup>m</sup> 13 <sup>s</sup> |
| Feb. 3 <sup>rd</sup> , 11 28 56  | Dec. 3 <sup>rd</sup> , 5 16 12   |
| (3.) May 17 <sup>th</sup> , 7 15 11  | (4.) Mar. 31 <sup>st</sup> , 23 10 16  |
| Mar. 13 <sup>th</sup> , 23 15 7  | Mar. 21 <sup>st</sup> , 7 24 12  |
| (5.) Sep. 1 <sup>st</sup> , 8 10 54  | (6.) 1872, Jan. 1 <sup>st</sup> , 9 50 41                                    |
| Aug. 31 <sup>st</sup> , 20 10 54   | 1872, Dec. 31 <sup>st</sup> , 22 48 56                                       |

## LONGITUDE IN ARC AND LONGITUDE IN TIME.

265. The earth rotates uniformly on her axis once in twenty-four hours, and thus every spot on her surface describes a complete circle, or 360°, in that space of time; hence the longitude of any place is proportional to the time the earth takes to revolve through the angle between the first meridian and the meridian of the place, and thus the longitude of a place may be expressed either in *arc* or in *time*.\* Longitude in arc and longitude in time are easily convertible, for since 360° is equivalent to 24<sup>h</sup> ( $360 \div 24 = 15^\circ$ ), 15° is equivalent to 1<sup>h</sup>; 15' to 1<sup>m</sup>, and 15" to 1<sup>s</sup>; whence

|   |
|---|
| 1° is equivalent to 4 <sup>m</sup> ( <i>i.e.</i> , the 15 <sup>th</sup> part of 1 hour or 60 <sup>m</sup> ) |
| 1' " 4 <sup>s</sup> ( <i>i.e.</i> , the 15 <sup>th</sup> part of 1 minute or 60 <sup>s</sup> )              |
| 1" " 4 <sup>t</sup> ( <i>i.e.</i> , the 15 <sup>th</sup> part of 1 second or 60 <sup>t</sup> )†             |

and the following rules are sufficiently clear.

\* In reckoning by arc, each degree is divided into sixty minutes, and each minute into sixty seconds. In reckoning by time, each hour is also divided into sixty minutes, and the minutes into sixty seconds. But a distinct notation for each of these has been adopted, degrees, minutes, and seconds, being represented by ° ' ", and hours, minutes, and seconds, by <sup>h</sup> <sup>m</sup> <sup>s</sup>; and care should be observed not to use the same marks for both, great confusion arising from so doing.

† A third is the name given to the sixtieth part of a second.





# RULE LXXX.

Reduce the hours and minutes into minutes, after which place the seconds, &c., then divide all by 4, and the quotient will be the degrees, minutes, &c., of the corresponding arc; or, in other words, after dividing by 4, mark the resulting figures thus:—Those under minutes (<sup>m</sup>) degrees (°); those under seconds (") minutes (′), those under thirds (″) seconds (″).

## EXAMPLES.

Ex. 1. Turn 1<sup>h</sup> 5<sup>m</sup> 12<sup>s</sup> into arc.

$$\begin{array}{r} 1^h \ 5^m \ 12^s \\ 60 \\ \hline 4)65^m \ 12^s \ 0^t \\ \hline 16^\circ \ 18' \ 0'' \end{array}$$

Multiply 1<sup>h</sup> by 60 add the minutes (5) and divide by 4, the quotient is 16 with remainder 1. Multiply this remainder by 60, and to the product add the 12 seconds; the sum is 72: Again, the quotient of 72 divided by 4 is 18, which is minutes (′); whence the arc corresponding to the time 1<sup>h</sup> 5<sup>m</sup> 12<sup>s</sup> is 16° 18′.

Ex. 2. Reduce 6<sup>h</sup> 24<sup>m</sup> 43<sup>s</sup> into arc.

$$\begin{array}{r} 6^h \ 24^m \ 43^s \\ 60 \\ \hline 4)384^m \ 43^s \ 0^t \\ \hline 96^\circ \ 10' \ 45'' \end{array}$$

Multiplying 6<sup>h</sup> by 60, and adding the 24<sup>m</sup> to the product, gives 384 as the sum; the quotient of this divided by 4 is 96, with no remainder. 43<sup>s</sup> divided by 4 gives quotient 10 with remainder 3; remainder 3 multiplied by 60 gives 180 which divided by 4 gives quotient 45: therefore 96° 10′ 45″ is the arc which corresponds to 6<sup>h</sup> 24<sup>m</sup> 43<sup>s</sup>.

Ex. 3. What arc corresponding to 0<sup>h</sup> 47<sup>m</sup> 36<sup>s</sup>?

$$\begin{array}{r} 4)0^h \ 47^m \ 36^s \\ \hline 11^\circ \ 54' \end{array}$$

In this instance it is not necessary to multiply by 60, as there are no hours to reduce into minutes: we divide 47<sup>m</sup> at once by 4.

Ex. 4. What is the equivalent arc to 9<sup>h</sup> 25<sup>m</sup> 37<sup>s</sup>?

$$\begin{array}{r} 9^h \ 25^m \ 37^s \\ 60 \\ \hline 4)565^m \ 37^s \ 0^t \\ \hline 141^\circ \ 24' \ 15'' \end{array}$$

Ex. 5. Convert 8<sup>h</sup> 17<sup>m</sup> 35<sup>s</sup>·5 into arc.

$$\begin{array}{r} 8^h \ 17^m \ 35^s \cdot 5 \\ 60 \\ \hline 4)497^m \ 35^s \ 30^t \\ \hline 124^\circ \ 23' \ 52'' \cdot 5 \end{array}$$

Multiply the hours (8<sup>h</sup>) by 60, and adding the minutes (17<sup>m</sup>) to the product gives 497<sup>m</sup>; divide the result by 4; the quotient is 124, with remainder 1. Again, multiply the remainder just obtained (1<sup>s</sup>) by 60, and to the product add the seconds of time, viz., 35; the sum is 95, then divided by 4, the quotient is 23 (minutes of arc) with remainder 3. Next multiply this last remainder by 60, the product is 180, to which add the 30; and the sum 210 divided by 4 gives 52 of arc, and remainder 2, to which annex a cypher and divide by 4, the quotient is 5 of seconds of arc.

Ex. 6. Convert 11<sup>h</sup> 39<sup>m</sup> 50<sup>s</sup>·7 into arc.

$$\begin{array}{r} 11^h \ 39^m \ 50^s \cdot 7 \\ 60 \\ \hline 4)699^m \ 50^s \ 42^t \\ \hline 174^\circ \ 57' \ 40'' \cdot 5 \end{array}$$

Multiply 11<sup>h</sup> by 60 and to product 660 add 39<sup>m</sup>, dividing the sum, viz., 699 by 4 gives 174 with remainder 3; this remainder (3) multiplied by 60, and 50 added to product gives 230; this sum divided by 4 gives 57 with remainder 2; remainder 2 multiplied by 60 and 42 added, gives sum 162, which divided by 4 gives 40 and remainder 2; remainder 2 with a cypher annexed and divided by 4 gives quotient 5; whence the arc corresponding to 11<sup>h</sup> 39<sup>m</sup> 50<sup>s</sup>·7 is 174° 57′ 40″·5.

## EXAMPLES FOR PRACTICE.

Convert the following times into arc:

|   |   |   |  |
|---|---|---|--|
| 1. 1 <sup>h</sup> 13 <sup>m</sup> 52 <sup>s</sup> | 6. 9 <sup>h</sup> 49 <sup>m</sup> 38 <sup>s</sup> | 11. 0 <sup>h</sup> 21 <sup>m</sup> 30 <sup>s</sup> ·9 | 16. 0 <sup>h</sup> 20 <sup>m</sup> 41 <sup>s</sup> |
| 2. 3 52 4   | 7. 0 34 58·2                                      | 12. 11 41 6·66  | 17. 8 36 56  |
| 3. 0 42 12  | 8. 1 41 1·6                                       | 13. 0 3 52  | 18. 5 0 51   |
| 4. 11 15 21                                       | 9. 5 59 4   | 14. 0 9 56  | 19. 11 59 57                                       |
| 5. 4 29 5   | 10. 8 17 6  | 15. 0 0 52  | 20. 0 1 52   |

## GREENWICH DATE.

### REDUCTION OF GREENWICH DATE.

266. **Def.**—The Greenwich Date is the day and time (reckoned astronomically) at Greenwich corresponding to a given day and time elsewhere. It is necessary to find the Greenwich date before the information contained in the Nautical Almanac can be made available, because all the elements there tabulated are given for time at the meridian of Greenwich.

As in almost every computation of nautical astronomy we are dependent for some data upon the Nautical Almanac,—and these are commonly given for Greenwich,—it is generally the first step in such a computation to deduce an exact or, at least, an approximate value of the Greenwich astronomical time. It need hardly be added that the Greenwich time should never be otherwise expressed than astronomically.

The Greenwich Date is found at once from a chronometer, the error and the rate of which is known; but it can also be found by means of the approximate time at place and the approximate longitude.

To find the Greenwich date, the time at any other place and the longitude being given.

#### RULE LXXXI.

1°. *Express the ship time astronomically* (Rule LXXVII, page 218).

2°. *Convert the longitude into time* (Rule LXXIX, page 220).

3°. *In West longitude.*—ADD longitude in time to ship time; the sum, if less than 24 hours, is the corresponding Greenwich date on the same day with the ship date; if greater than 24 hours, reject the 24 hours, and put the day one forward.

4°. *In East longitude.*—From ship astronomical time SUBTRACT longitude in time, if less than the hours, minutes, &c., of ship date; the remainder is the corresponding Greenwich date of the same day as the ship date; if the longitude in time be greater than the hours, minutes, &c., of ship astronomical, ADD 24 hours to the latter, and put the day one back before the subtraction is made.

5°. *When it is noon at the place.*—The longitude in time, if west, is the Greenwich date (apparent time); but if east, SUBTRACT the longitude in time from 24 hours; the remainder is the Greenwich date (apparent time) after noon of the preceding day.

(a). From this last it is evident that when the sun is on a meridian in West longitude, the Greenwich apparent time is precisely equal to the longitude, that is, the Greenwich apparent time is *after* the noon of the same date with the ship date, by a number of hours, &c., equal to longitude. When the sun is on a meridian in East longitude, the Greenwich apparent time is *before* the noon of the same date as the ship date, by a number of hours equal to the longitude in time.

NOTE.—A bad habit prevails in writing dates, of separating the month and day from the hours, minutes, and seconds. *The day of the month should always precede the minor divisions of time which give the precise instant of the day intended.*

## EXAMPLES.

Ex. 1. November 9th, at 4<sup>h</sup> 10<sup>m</sup> P.M., apparent time at ship, longitude 32° 45' W.: required the corresponding time at Greenwich, or the Greenwich date.

|                      |  |           |   |
|----------------------|--|-----------|---|
| Ship date (A.T.)     | Nov. 9 <sup>d</sup> 4 <sup>h</sup> 10 <sup>m</sup> | Longitude | 32° 45'                                       |
| Long. in time        | + 2 11   |           | 4   |
| Greenwich date, Nov. | 9 6 21   | 6,0)13,1  | o   |
|                      |  |           | 2 <sup>h</sup> 11 <sup>m</sup> 0 <sup>s</sup> |

Ex. 2. June 5th, at 7<sup>h</sup> 15<sup>m</sup> A.M., app. time at ship, longitude 140° 30' E.: find corresponding Greenwich date.

|                    |   |
|--------------------|---|
| Ship date (A.T.)   | June 4 <sup>d</sup> 16 <sup>h</sup> 15 <sup>m</sup> |
| Longitude in time  | — 9 22  |
| Green. date (A.T.) | June 4 9 53   |

Ex. 4. April 27th, at 5<sup>h</sup> 35<sup>m</sup> 35<sup>s</sup> A.M., app. time at ship, long. 122° 13' W.: what is corresponding Greenwich date?

|                       |   |
|-----------------------|---|
| Ship date (A.T.)      | April 26 <sup>d</sup> 17 <sup>h</sup> 35 <sup>m</sup> 45 <sup>s</sup> |
| Longitude 122° 13' W. | + 8 8 52  |
|                       | 26 25 44 37   |
|                       | — 24  |

Green. date (A.T.) April 27 1 44 37

In example 4, the added longitude advances the day of the month. (This illustrates latter part of 3° of the Rule.) In example 5, a day (or 24 hours) is borrowed before the subtraction is made, since the longitude in time exceeds the astronomical ship date, thus making the days of the month at Greenwich one less than at the place. (This illustrates the latter part of 4° of the Rule.)

Ex. 6. 1873, January 1st, 3<sup>h</sup> 40<sup>m</sup> 20<sup>s</sup> P.M., mean time at ship, long. 95° 7' E.: find the Greenwich date.

|                        |  |
|------------------------|--|
| Ship date (M.T.) 1873, | Jan. 1 <sup>d</sup> 3 <sup>h</sup> 40 <sup>m</sup> 20 <sup>s</sup> |
| Longitude 95° 7' E.    | — 6 20 28  |

Green. date (M.T.) 1872, Dec. 31 21 19 52

Ex. 8. 1872, June 12th, 6<sup>h</sup> 40<sup>m</sup> A.M., app. time at ship, long. 42° 16' W.: find the Greenwich date.

|                      |   |
|----------------------|---|
| Ship date (A.T.)     | June 11 <sup>d</sup> 18 <sup>h</sup> 40 <sup>m</sup> 0 <sup>s</sup> |
| Longitude 42° 16' W. | + 2 49 4  |

Green. date (A.T.) June 11 21 29 4

Ex. 10. Required the Greenwich date when the sun is on the meridian of a place in long. 80° 44' E., on January 12th.

The sun being on the meridian, it is apparent noon: hence

|                      |  |
|----------------------|--|
| Ship date (A.T.)     | Jan 12 <sup>d</sup> 0 <sup>h</sup> 0 <sup>m</sup> 0 <sup>s</sup> |
| Longitude 80° 44' E. | — 5 22 56  |

Green. date (A.T.) Jan. 11 18 37 4

In example 10, the hours, &c., of longitude to be subtracted are to be taken from a borrowed day, or 24 hours, thus making the day of the month at Greenwich one less than at the place. (See 5° of Rule.)

Ex. 3. January 3rd, at 8<sup>h</sup> 12<sup>m</sup> P.M., mean time at ship, long. 50° 45' E.: find Greenwich date.

|                    |   |
|--------------------|---|
| Ship date (M.T.)   | January 3 <sup>d</sup> 8 <sup>h</sup> 12 <sup>m</sup> |
| Longitude in time  | — 3 23  |
| Green. date (M.T.) | Jan. 3 4 49   |

Ex. 5. July 20th, at 3<sup>h</sup> 35<sup>m</sup> 7<sup>s</sup> P.M., mean time at ship, long 85° 24' E.: find corresponding Greenwich date.

|                      |  |
|----------------------|--|
| Ship date (M.T.)     | July 20 <sup>d</sup> 3 <sup>h</sup> 35 <sup>m</sup> 7 <sup>s</sup> |
|                      | + 24   |
|                      | or 19 27 35 7  |
| Longitude 85° 24' E. | — 5 41 36  |

Green. date (M.T.) 19 21 53 31

Ex. 7. 1872, January 1st, 9<sup>h</sup> 1<sup>m</sup> A.M., mean time at ship, long. 107° 4' W.: find the Greenwich date.

|                        |  |
|------------------------|--|
| Ship date (M.T.) 1871, | Dec. 31 <sup>d</sup> 21 <sup>h</sup> 1 <sup>m</sup> 0 <sup>s</sup> |
| Longitude 107° 4' W.   | + 7 8 16   |

Green. date (M.T.) 1872, Jan. 1 4 9 16

Ex. 9. 1872, October 1st, long. 2° W., the sun on meridian: required Greenwich date (app. time).

|                  |  |
|------------------|--|
| Ship date (A.T.) | October 1 <sup>d</sup> 0 <sup>h</sup> 0 <sup>m</sup> |
| Longitude 2° W.  | + 8  |

Green. date (A.T.) October 1 0 8

Ex. 11. What is the Greenwich date when the sun is on the meridian of a place in long. 155° 19' W., on March 31st?

|                       |  |
|-----------------------|--|
| Ship date (A.T.)      | March 31 <sup>d</sup> 0 <sup>h</sup> 0 <sup>m</sup> 0 <sup>s</sup> |
| Longitude 155° 19' W. | + 10 21 16   |

Green. date (A.T.) March 31 10 21 16

Ex. 12. 1872, February 1st, long.  $135^{\circ}$  E.: find the Greenwich date when the sun is on the meridian.

Ship date (A.T.) February 1<sup>d</sup> 0<sup>h</sup> 0<sup>m</sup>  
Longitude  $135^{\circ}$  E. — 9 0

Green. date (A.T.) January 31 15 0

Ex. 13. 1873, January 1st, the ship in long.  $160^{\circ} 30'$  E.: required the Greenwich date when the sun is on the meridian.

Ship date (A.T.) 1873, Jan. 1<sup>d</sup> 0<sup>h</sup> 0<sup>m</sup>  
Longitude  $160^{\circ} 30'$  E. — 10 42

Green. date (A.T.) 1872, Dec. 31 13 18

### EXAMPLES FOR PRACTICE.

Required the Greenwich date in each of the following examples:—

|     |                   |  |                |                               |
|-----|-------------------|--|----------------|-------------------------------|
| 1.  | 1876, January 6th | at $3^{\text{h}} 40^{\text{m}} 16^{\text{s}}$ P.M. | apparent time  | long. $66^{\circ} 56' 0''$ W. |
| 2.  | February 13th     | at 8 40 3 A.M.                                     | apparent time, | long. 21 4 0 W.               |
| 3.  | February 1st      | at 5 10 50 A.M.                                    | mean time,     | long. 145 20 30 E.            |
| 4.  | March 15th        | at 9 16 22 P.M.                                    | apparent time, | long. 17 4 0 E.               |
| 5.  | May 15th          | at 8 38 35 A.M.                                    | apparent time, | long. 141 51 15 W.            |
| 6.  | November 1st      | at 5 0 10 P.M.                                     | mean time,     | long. 114 30 0 E.             |
| 7.  | December 1st      | at 8 0 5 A.M.                                      | mean time,     | long. 158 10 0 W.             |
| 8.  | July 1st          | at 4 0 33 P.M.                                     | apparent time, | long. 170 55 15 E.            |
| 9.  | August 4th        | at 6 31 32 P.M.                                    | apparent time, | long. 100 17 30 E.            |
| 10. | September 1st     | at 8 29 1 A.M.                                     | mean time,     | long. 148 47 30 W.            |
| 11. | December 28th     | at 2 42 10 P.M.                                    | mean time,     | long. 50 40 0 E.              |
| 12. | July 8th          | at 0 4 36 A.M.                                     | apparent time, | long. 178 51 0 W.             |
| 13. | February 1st      | at noon,   | apparent time, | long. 153 40 0 E.             |
| 14. | June 1st          | at noon,   | apparent time, | long. 83 50 0 E.              |
| 15. | March 2nd         | at noon,   | apparent time, | long. 1 25 0 W.               |
| 16. | 1877, January 1st | at noon,   | apparent time, | long. 149 10 0 E.             |

## REDUCTION OF ELEMENTS FROM NAUTICAL ALMANAC.

The *Nautical Almanac*\* or *Astronomical Ephemeris* contains the right ascension, declination, &c., of the principal heavenly bodies for given equidistant instants of Greenwich time; the right ascension and declination of the sun and planets, for example, being given for every day at noon ( $0^{\text{h}} 0^{\text{m}} 0^{\text{s}}$ ), at Greenwich while for the moon these elements are given for every hour. Before we can find from the *Almanac* the value of any of these quantities for a given local or ship time, we must find the corresponding Greenwich date (Rule LXXXI, page 222). Where this time is exactly one of the instants for which the required quantity is put down in the *Ephemeris*, nothing more is necessary than to transcribe the quantity as there put down. But when, as is mostly the case, the time falls between two of the times in the *Ephemeris* we must obtain the required quantity by interpolation, it being requisite to apply a correction to that taken from the *Almanac*, in order to reduce it to its value at the given instant. To facilitate this interpolation the *Almanac* contains the rate of change, or difference of each of the quantities in some unit of time, or, which is in general the simplest method, we may make use of certain tables computed for the purpose, called tables of *proportional* logarithms.

\* The French *Ephemeris*, *La Connaissance des Temps*, is computed for the meridian of Paris, the German *Berliner Astronomisches Jahrbuch* for the meridian of Berlin. All these works are published annually several years in advance.

To use the difference columns with advantage, the Greenwich time should be expressed in that unit of time for which the difference is given: thus, when the difference is for one hour, the time must be expressed in hours and decimals of an hour; when the difference is for one minute of time, the time should be expressed in minutes and decimals of a minute.

267. **Simple Interpolation.**—In the greater number of cases in practice, it is sufficiently exact to obtain the requisite quantities by *simple* interpolation; that is, by assuming that the difference of the quantities are proportional to the differences of the times, which is equivalent to assuming that the differences in the Ephemeris are constant. This, however, is never the case; but the error arising from the assumption will be smaller the less the interval between the times in the Ephemeris; hence, those quantities which vary most irregularly, as the Moon's Right Ascension and Declination, are given for every hour of Greenwich time; others, as the Moon's Parallax and Semidiameters, for every twelfth hour, or for noon and midnight; others, as the Sun's Right Ascension, &c., for each noon; others, as the right ascensions and declinations of the fixed stars, for every tenth day of the year.

#### TO REDUCE SUN'S DECLINATION.

268. The declination of the sun is given in the "Nautical Almanac," pages I and II of each month, for every day both for apparent and mean noon at Greenwich. The *difference of declination* for one hour ("*Var. in 1 hour*") is always annexed, and is intended to facilitate the reduction of the quantities from noon to any other time. In general it is necessary to take out the required quantities for the nearest Greenwich time to the given time, and interpolate in either direction to the given instant of Greenwich time.

#### Method I.—By hourly difference.\*

##### RULE LXXXII.

1°. *Get a Greenwich date by means of ship time, expressed astronomically, and longitude (see Rule LXXXI, page 222), or by means of chronometer.*

To express the Greenwich time in hours and decimals of an hour. Annex a cipher to the minutes and divide by 60, or divide the minutes by 6, and consider the quotient as tenths of an hour, and to this prefix the hours. For example, let it be required to express 7<sup>h</sup> 18<sup>m</sup> in hours and decimals of an hour. Then 6 is contained in 18 three times; to this prefix the hours (7) and we have 7.3 hours.—(See Ex. 3, page 44.)

2°. *Take out of Nautical Almanac the declination for the nearest noon to the given Greenwich date, noting whether the declination is increasing or decreasing; and a little to the right place the "difference for 1 hour," found in page I, N.A.*

(a). When Greenwich date is given in *apparent* time, use page I of the month, but call them 1<sup>st</sup> when they amount to five, or above—thus 42<sup>nd</sup> 7 would be 43<sup>rd</sup>.

(b). The tenths of seconds (") of declination may be rejected when less than five, but for *mean* time, use page II of the month.

(c). When the seconds of time (in Greenwich date) are less than 30<sup>s</sup>, they may be rejected; but if above 30<sup>s</sup>, increase the minutes of time by 1<sup>m</sup>; thus Greenwich time 2<sup>h</sup> 35<sup>m</sup> 40<sup>s</sup> would be called 2<sup>h</sup> 36<sup>m</sup>.

\* This method of reducing the sun's declination is required to be used by the Board of Trade at the Local Marine Board Examinations.

3°. Multiply the “Hourly Diff.” by the hours and fractional parts of an hour that have elapsed since, or must elapse before that noon, as the case may be; the product reduced to minutes and seconds is the change of declination in the time from noon.

4°. Apply this correction to the declination for the nearest noon to the given time i.e., the declination of the same noon as that for which the “Var. in 1 hour” has been taken as follows:—

(a) When the Decl. is increasing, the correction for the time elapsed since noon is additive, but the correction for the time that must elapse is subtractive.

(b) When the Decl. is decreasing, the correction for the time elapsed since noon is subtractive, but the correction for the time that must elapse before noon is additive.

The result is declination sought.

#### EXAMPLES.

Ex. 1. Greenwich Date, Jan. 10<sup>d</sup> 6<sup>h</sup>; in this case take 22° 08 the Diff. for 1 hour on the 10th, which multiplied by 6 gives the correction of the Decl. for the 10th day—to be *subtracted* because the Declination is decreasing and we have multiplied by the number of hours that have elapsed since noon.

Ex. 2. Greenwich Date, Jan. 10<sup>d</sup> 19<sup>h</sup>; in this case take 23° 14 the “Var. in 1 hour” on the 11th, which multiplied by the difference between 24<sup>h</sup> and 19<sup>h</sup> gives the correction of the Decl. for the 11th day—to be *added* because the Decl. is *decreasing* and we have multiplied by the number of hours that must elapse before noon the 11th day.

Ex. 3. Greenwich Date, April 2<sup>d</sup> 6<sup>h</sup> $\frac{1}{2}$ ; in this case take 57° 49, the “Var. in 1 hour” on the 2nd, which multiplied by 6 $\frac{1}{2}$ , gives the correction of the declination for the 2nd April—to be *added* because the Decl. is *increasing* and we have multiplied by 6 $\frac{1}{2}$  hours the time that has elapsed since noon, April 2nd.

Ex. 4. Greenwich Date, April 2<sup>d</sup> 17<sup>h</sup> $\frac{1}{2}$ ; in this case take 57° 25, the “Var. in 1 hour” on the 3rd; which multiplied by 6 $\frac{1}{2}$  (the difference between 24<sup>h</sup> and 17<sup>h</sup> $\frac{1}{2}$ ) gives the correction of the Decl. for the 3rd day—to be *subtracted* because the Decl. is *increasing* and we have multiplied by the number of hours that must elapse before noon, 3rd.

(5°). If the correction when subtractive exceeds the declination itself, subtract the declination from the proportional part; the remainder is the declination of the contrary name.

In March when the declination changes from South to North, and in September when it changes from North to South, if the correction, by being subtractive, exceed the declination, subtract the declination from the correction, and call the remainder *N.* in March, but *S.* in September.—(See example 3.)

METHOD II.—By proportional logarithms.

#### RULE LXXXIII.

1°. Find a Greenwich date.

2°. Take out of the Nautical Almanac the declination for the noon at Greenwich, and that following it.

3°. When the declinations are of like names, take their difference; but when of different names, take the sum: this is the daily variation of declination.

(a) When the declination is increasing, place the sign of addition (+) before the daily variation; but when the declination is decreasing, place the sign of subtraction (—) before it.

4°. Under the daily variation place the hours and minutes of Greenwich time, and take from the table (Table XXI A, Raper, or XXXIII, Norie,) log. of change of declination in 24 hours and log. of hours and minutes of Greenwich time; the sum of these logs. found in the table will give the proportional part of daily change of declination.

In using Table XXI A, Raper, or Norie XXXIII, minutes (') of declination, and hours of time (h), are found at the top of the columns; seconds (") of declination, and minutes (m) of time, at the side columns.

5°. Apply the proportional part to the declination at the first noon, adding when the declination is increasing; but subtracting when the declination is decreasing; the result is the declination at the time required.

## EXAMPLES.

Ex. 1. 1876, January 13th, at 3<sup>h</sup> 54<sup>m</sup> 16<sup>s</sup> P.M., app. time at ship, long. 30° 4' E.: find the sun's declination.

|                               |  |                                   |   |
|-------------------------------|--|-----------------------------------|---|
| Ship date (A.T.) January      | 13 <sup>d</sup> 3 <sup>h</sup> 54 <sup>m</sup> 16 <sup>s</sup> | Longitude                         | 30° 4'  |
| Longitude (30° 4' E.) in time | — 2 0 16   |                                   | 4   |
| Green. date (A.T.) January    | 13 <sup>d</sup> 1 <sup>h</sup> 54 <sup>m</sup> 0 <sup>s</sup>  | 54 <sup>m</sup> = $\frac{54}{60}$ | —   |
|                               |  | 60)54 <sup>0</sup>                | 6,0)12,0 16                                   |
|                               | or, 1 <sup>h</sup> 9   | 9                                 | 2 <sup>h</sup> 0 <sup>m</sup> 16 <sup>s</sup> |

## Method I.

Decl., page I, N.A., for January 13th, app. noon, is 21° 32' 34" S., decreasing, and Hourly diff. is 25"·24.

H. diff., 13th, noon 25"·24  
Green. time 1<sup>h</sup> 54<sup>m</sup> = 1<sup>h</sup> 9 × 19

22716  
2524

Correction — 47'956

Decl., noon, 13th, 21° 32' 24" S., decr.

Correction — 48

Red. decl. 21 31 46 S.

## Method II.

Decl. app. noon, page I, N.A.

Jan. 13th, 21° 32' 33"·6 S.  
14th, 21 22 15"·2 S.

Daily var. — 10 18 log. 3674  
Green. time 1<sup>h</sup> 54<sup>m</sup> log. 1'1015

Correction — 0 49 log. 1'4689  
13th, at noon 21 32 34 S.

Red. decl. 21 31 45 S.

The correction 49" is subtracted from declination at noon, because the declination is decreasing.

Having found the Greenwich date, the sun's declination is taken from the Nautical Almanac, where it is found in page I of the month (the Greenwich date being in app. time), and on the same page and in column headed "Var. in 1 hour" is found the change of declination for 1 hour past noon; next observe that the declination is decreasing, and make a note of it. Now, since the declination changes 25"·24 in 1 hour past noon, how much does it change in the Greenwich time past noon, viz., 1<sup>h</sup> 54<sup>m</sup>? First annex a cypher to the minutes (54<sup>m</sup>) and divide by 60; thus 60 is contained in 540 nine times and nothing over. To this we prefix the hour, and we then have the Greenwich time 1<sup>h</sup> 54<sup>m</sup> = 1<sup>h</sup>·9 expressed in hours and decimals of an hour. (See Rule XVIII, page 43). Set this under the hourly diff. and then proceed as in multiplication of decimals, the resulting figures are 47956, but as we have two decimals in the multiplicand and one place in the multiplier, in all three places, three figures are to be marked off from the right hand, leaving 47' (see Rule XV, page 37), but as the first figure to the right of the decimal point exceeds 5, we increase the seconds by 1' whence the correction of decl. is — 48.

Ex. 2. 1876, May 21st, at 7<sup>h</sup> 50<sup>m</sup> A.M., mean time at ship, long. 149° 30' E.: required the sun's declination.

|  |   |                                      |  |
|--|---|--------------------------------------|--|
| Ship date (M.T.) May   | 20 <sup>d</sup> 19 <sup>h</sup> 50 <sup>m</sup> | By Hourly Diff.                      |  |
| Longitude 149° 30' E.  | — 9 58  | 52 <sup>m</sup> = $\frac{3}{80}$ 520 |  |
| Green. date (M.T.) May   | 20 9 52   |                                      | 866 or .87 nearly.                       |
| Decl., page II, N.A., May 20th, at noon,   |   | Decl. mean noon, page II, N.A.       |  |
| is 20° 6' 52" N. ( <i>increasing</i> ), Hourly diff. at noon, May 20th, 30" .80. |   | May 20th,                            | 20° 6' 52" N.                            |
| Hourly diff.   | + 30" .80                                       | 21st,                                | 20 19 1 N.                               |
| 9 <sup>h</sup> 52 <sup>m</sup> = 9 <sup>h</sup> .87 nearly                       | × 9 87  | Daily variation                      | + 12 9 log. 2956                         |
|  | 21560   | Green. time                          | 9 <sup>h</sup> 52 <sup>m</sup> log. 3860 |
|  | 24640   | Correction                           | + 5' 0" log. 6816                        |
|  | 27720   | Decl. 20th, noon                     | 20 6 19 N.                               |
|  | 6,030,39960                                     | Red. decl.                           | 20 11 19 N.                              |
| Correction + 5' 4" nearly.   |   |                                      |  |

Decl. 20th, noon 20° 6' 52" N., *incr.*  
 Corr. for 9<sup>h</sup> 52<sup>m</sup> = + 5 4

The correction 5' 0" is *added* to the declination at noon, because the declination is *increasing*.

(See next page for Explanation).

Red. decl. 20 11 56 N.

*Explanation.*—Having found the Greenwich date; with this date the sun's declination must be taken out of the Nautical Almanac, page II for May (the Greenwich date being mean time), and in page I of the month, in the column headed "diff. for 1 hour" is found the change for one hour past noon; next observe whether the declination is increasing or decreasing. In this instance it is increasing, and we note this. Now the next question that presents itself for consideration is, since the declination increases 30" .80 in one hour, what will be the change in the Greenwich time past noon, viz., 9<sup>h</sup> 52<sup>m</sup>? We have now to express this in hours and decimal parts of an hour. Then 52<sup>m</sup> =  $\frac{2}{3}$  of an hour, and annexing cyphers to 52 and dividing 60, we have 60 in 520, or 6 in 52 goes eight times and four over; 6 is contained in 40 (the remainder and a cypher annexed) six times and four over, or seven times nearly—two places of decimals only being used. Set the .87 under the hourly difference to which prefix the 9<sup>h</sup>, and then proceed as in common multiplication. The resulting figures are 3039960, but as we have two decimal places in the multiplicand, and two decimal places in the multiplier, in all four, *four* figures are to be marked off from the right hand, leaving 303"; but since the first decimal figure (9) exceeds 5 we increase the seconds by 1" in consequence, and the correction is 304", which divided by 60 gives + 5' 4" the correction of declination.

Ex. 3. 1876, March 19th, 22<sup>h</sup> 39<sup>m</sup>, app. time at Greenwich: required the sun's declination.

|                                   |                                 |                                      |            |
|-----------------------------------|---------------------------------|--------------------------------------|------------|
| March 19th                        | 22 <sup>h</sup> 39 <sup>m</sup> | 21 <sup>m</sup> = $\frac{3}{80}$ 210 |            |
|                                   | 24 0                            |                                      | 35         |
| Time from noon, Mar. 20th         | 1 21                            |                                      |            |
|                                   | or, 1 <sup>h</sup> .35          |                                      |            |
| Decl. page I, N.A.                |                                 |                                      |            |
| March 20th, at noon               | 0° 5' 53" N. ( <i>incr.</i> )   | Hourly diff.                         | 59" .24    |
| Correction for 1 <sup>h</sup> .35 | 1 20                            |                                      | 1' 35      |
| Red. decl.                        | 0 4 33 N.                       |                                      | 29620      |
|                                   |                                 |                                      | 17772      |
|                                   |                                 |                                      | 5924       |
|                                   |                                 |                                      | 6,079,9740 |
|                                   |                                 |                                      | 1' 19" 97  |

In this case the Greenwich noon of the 20th is nearer to the given Greenwich time than Greenwich noon 19th, therefore, take out the declination from page I, *Nautical Almanac* (because apparent time), for noon 20th; also, the variation in 1 hour corresponding to this declination, viz., 59 .24. Next subtract the hours, minutes, &c., of Greenwich time from 24 hours, the remainder 1<sup>h</sup> 21<sup>m</sup> is the time that *must elapse before noon* 20th. We divide the minutes of this last by 60 to get decimals of an hour, thus, 6 is contained in 21 three times and three over; a cypher being annexed to the remainder 3 makes 30, then 6 is contained in 30 five times, hence we have .65 (see Rule XVIII, page 43), to this we prefix the hours (1) and we then have 1<sup>h</sup> .35. Next multiply the hourly difference by this, and the resulting figures are 799740, then since we have two



decimal figures in the multiplicand ( $\cdot 24$ ), and two in the multiplier, ( $\cdot 35$ ) in all four, *four* figures must be marked off from the right hand, leaving 79, which being increased by 1 in consequence of the first figure on the right of the decimal point exceeding 5, gives for the correction  $80''$ , which divided by 60 gives  $1' 20''$ . And since the declination at noon, 20th, is *increasing*, it is evident that the declination at  $1^h 21^m$  before that noon will be less than at noon, and the correction  $1' 20''$  is therefore to be subtracted; whence the **Reduced Declination** is  $0^\circ 4' 33''$  N. (see No. 5° (a) of the Rule LXXXII).

Ex. 4. 1876, February 11th, at  $8^h 54^m 47^s$  P.M., app. time, long.  $11^\circ 4' W.$ : find the declination.

|   |                               |                            |                                   |
|---|-------------------------------|----------------------------|-----------------------------------|
| Ship date (A.T.) February 11 <sup>d</sup>   | $8^h 54^m 47^s$               | Longitude                  | $11^\circ 4'$                     |
| Longitude in time                           | $+ 44 \ 16$                   |                            | $\underline{\hspace{1cm}} 4$      |
| Green. date (A.T.) February 11 <sup>d</sup> | $9 \ 39 \ 3$                  |                            | $44^m 16^s$                       |
|   | $9^h 65$                      |                            |                                   |
| Decl. page I, N.A.                          |                               | Hourly diff., page I, N.A. |                                   |
| Feb. 11th at noon                           | $14^\circ 7' 52'' S. (decr.)$ | Feb. 11th at noon          | $49'' 14$                         |
| Corr. for $9^h 39^m$                        | $- 7 \ 45$                    |                            | $\underline{\hspace{1cm}} 9^h 65$ |
| Red. decl.                                  | $13 \ 59 \ 58 \ S.$           |                            | $6,0)47,4^m 2010$                 |
|   |                               | Correction                 | $\underline{\hspace{1cm}} 7' 54$  |

269. To find the declination of the sun at the time of its transit over a given meridian.

When the sun is on a meridian in **WEST** longitude, the Greenwich *apparent* time is precisely equal to the longitude; that is, the Greenwich apparent time is *after* the noon of the same date with the ship date by a number of hours, equal to the longitude in time. When the sun is on a meridian in **EAST** longitude, the Greenwich apparent time is *before* the noon of the same date as the ship date by a number of hours, equal to the longitude in time. Hence, to obtain the sun's declination for apparent noon at any meridian we have.

#### RULE LXXXIV.

Take the declination from the Nautical Almanac (page I of the month) for Greenwich apparent noon of the same date as the ship date, and apply a correction equal to the hourly difference multiplied by the longitude, observing to add or subtract this correction according as the numbers in the Nautical Almanac may indicate for a time before or after noon.

#### EXAMPLES.

Ex. 1. 1876, September 10th, the sun on the meridian, long.  $100^\circ 35' E.$ : required the sun's declination.

|           |   |
|-----------|---|
| Longitude | $100^\circ 35' E.$                        |
|           | $\underline{\hspace{1cm}} 4$              |
|           | $6,0)40,2 \ 20$                           |
|           | $\underline{\hspace{1cm}} 6^h 42^m 20^s.$ |

The longitude being  $6^h 42^m 20^s$  East, the Green. A.T. is  $6^h 42^m$  before the noon of September 10th—the same date as the ship date. The decl. is taken out of the *Nautical Almanac*, page I of the month; also take out at the same time the hourly diff.; the work will stand thus:—

|                           |                             |
|---------------------------|-----------------------------|
| Sun's decl., page I, N.A. | H.D., page I, N.A.          |
| Sept. 10th, noon          | $4^\circ 43' 8'' N., decr.$ |
| Corr. for $6^h 42^m$      | $+ 6 \ 22$                  |
| Red. decl.                | $6 \ 49 \ 30 \ N.$          |
|                           | $6,0)38,2 \ 168$            |

As the declination is *decreasing*, the declination at  $6^h 42^m$  before noon will be greater than that for noon.

Correction  $\underline{\hspace{1cm}} 5' 22$

Ex. 2. 1876, June 1st, long.  $75^{\circ}$  W.: required the declination when the sun is on the meridian.

|                          |   |
|--------------------------|---|
| Ship date (A.T.)         | June 1 <sup>d</sup> 0 <sup>h</sup> 0 <sup>m</sup> |
| Long. in time            | + 5 0   |
| Green. date (A.T.)       | June 1 5 0  |
| H. diff., noon, June 1st | 19° 81  |
| Time from noon           | X 5   |
|                          | 6,0)9,9°05  |
| Correction               | + 1 39  |
| Decl., June 1st, noon    | 22 8 51 N., <i>incr.</i>                          |
| Red. decl.               | 22 10 30 N.                                       |

Ex. 3. In the last question suppose the long.  $75^{\circ}$  E.

|                          |   |
|--------------------------|---|
| Ship date (A.T.)         | June 1 <sup>d</sup> 0 <sup>h</sup> 0 <sup>m</sup> |
| Long. in time            | — 5 0   |
| Green. date (A.T.)       | May 31 19 0                                       |
| H. diff., June 1st, noon | 19° 85  |
| Time from noon, June 1st | 5   |
|                          | 6,0)9,9°35  |
|                          | — 1 39  |
| Decl. June 1st, noon     | 22 8 51 N. <i>incr.</i>                           |
| Red. decl.               | 22 7 12 N.  |

270. **Interpolation by second differences.**—The differences between the successive values given in the Nautical Almanac as functions of time, are called the *first differences*; the differences between these successive differences are called the *second differences*; the differences of the second differences are called the *third differences*, &c. In simple interpolation we assume the function to vary uniformly; that is, we regard the first difference as constant, neglecting the second difference, which is, consequently, assumed to be zero. In interpolation by second differences we take into account the variation in the first difference, but we assume *its* variations to be constant; that is, we assume the second difference to be constant, and the third difference to be constant.

When the Nautical Almanac is employed we can take the second differences into account in a very simple manner. In this work, since the year 1863, the difference given for a unit of time is always the difference belonging to the instant of Greenwich time against which it stands, and it expresses, therefore, the rate at which the function is changing *at that instant*. This difference, which we may here call the first difference, varies with the Greenwich time, and (the second difference being constant) it varies uniformly, so that its value for any intermediate time may be found by simple interpolation, using the second differences as first differences. Now, in computing a correction for a given interval of Greenwich time, we should employ the *mean*, or *average* value, of the first difference for the interval, and this mean value, when we regard the second differences as constant, is that which belongs to the middle of the interval. Hence, to take into account the second differences, we have only to observe the very simple rule—*employ that (interpolated) value of the first difference which corresponds to the middle of the interval for which the correction is to be computed.*

271. **Degree of dependence.**—The sun's declination changes nearly  $1'$  an hour, or  $1''$  in  $1^m$ , in March and September; hence to insure it to  $1''$  in the extreme case, the Greenwich date must be true to  $1^m$ .

## EXAMPLES FOR PRACTICE.

Required the sun's declination in each of the following examples:—

[These are preparatory to working Amplitudes, Azimuths, &c.]

|     |                    |   |                   |                  |
|-----|--------------------|---|-------------------|------------------|
| 1.  | 1876, January 5th, | 6 <sup>h</sup> 23 <sup>m</sup> 32 <sup>s</sup> A.M. | app. time at ship | long. 108° 7' W. |
| 2.  | February 2nd,      | 3 9 0 P.M.  | app. time at ship | long. 52 45 W.   |
| 3.  | March 31st,        | 6 2 12 P.M.   | app. time at ship | long. 156 3 E.   |
| 4.  | March 26th,        | 7 8 22 A.M.   | mean time at ship | long. 72 47 E.   |
| 5.  | May 16th,          | 9 17 20 A.M.  | mean time at ship | long. 45 40 W.   |
| 6.  | April 29th,        | 2 26 52 P.M.  | mean time at ship | long. 110 57 W.  |
| 7.  | June 10th,         | 8 45 0 P.M.   | app. time at ship | long. 129 30 E.  |
| 8.  | November 1st,      | 10 20 16 A.M.                                       | mean time at ship | long. 11 17 E.   |
| 9.  | September 1st,     | 8 20 40 A.M.  | app. time at ship | long. 172 9 E.   |
| 10. | October 1st,       | 6 11 50 A.M.  | mean time at ship | long. 68 15 W.   |
| 11. | December 16th,     | 4 35 32 A.M.  | app. time at ship | long. 4 8 E.     |
| 12. | November 14th,     | 6 45 8 P.M.   | mean time at ship | long. 100 2 E.   |

In each of the following examples it is required to find the sun's declination when the sun is on the meridian (at apparent noon):—

|     |                  |                  |     |                   |                 |
|-----|------------------|------------------|-----|-------------------|-----------------|
| 13. | 1876, Jan. 19th, | long. 86° 57' W. | 19. | 1876, July 28th,  | long. 2° 0' W.  |
| 14. | Feb. 16th,       | long. 72 59 E.   | 20. | Sept. 22nd,       | long. 156 0 W.  |
| 15. | Mar. 21st,       | long. 168 3 E.   | 21. | Oct. 1st,         | long. 170 58 E. |
| 16. | May 8th,         | long. 10 35 W.   | 22. | Dec. 22nd,        | long. 179 52 E. |
| 17. | June 21st,       | long. 167 15 E.  | 23. | 1877, Jan. 1st,   | long. 156 48 E. |
| 18. | Mar. 20th,       | long. 129 0 W.   | 24. | 1876, Sept. 23rd, | long. 174 15 E. |

272. **The Polar Distance** of a heavenly body is its angular distance from the elevated pole of the heavens; it is measured by the intercepted arc of the hour circle passing through it, or by the corresponding angle at the centre of the sphere. According as the North or South pole is elevated, we have the *North Polar Distance*, or the *South Polar Distance*.

273. To find the polar distance of a celestial object, proceed according to the following rule:—

## RULE LXXXV.

When the latitude of the place, and declination of the object, are of the same name subtract the declination from 90°; but when the latitude and declination are of contrary names, add the declination to 90°; the result in either case is the polar distance.

When the latitude is 0, the declination, either added to or taken from 90°, is the polar distance.

## EXAMPLES.

| Lat.    | Declination.  | Polar Distance.           |
|---------|---------------|---------------------------|
| N. .... | 8° 12' 18" S. | 98° 12' 18"               |
| N. .... | 22 30 0 N.    | 67 30 0                   |
| S. .... | 2 31 15 S.    | 87 28 45                  |
| N. .... | 30 23 15 S.   | 120 23 15                 |
| S. .... | 7 22 32 N.    | 97 22 32                  |
| S. .... | 26 42 12 S.   | 63 17 48                  |
| 0 ....  | 12 48 2 N.    | { 102 48 2<br>or 77 11 58 |

## TO FIND THE EQUATION OF TIME.

274. **Apparent Solar Day** is the interval between two successive transits of the actual sun's centre over the same meridian; it begins when that point is on the meridian. The apparent solar day is variable in length from two causes; first, the sun does not move uniformly in the ecliptic—its apparent path sometimes describing an arc of  $57'$ , and at other times an arc of  $61'$  in a day; second, the ecliptic twice crosses the equinoctial—the great circle whose plane is perpendicular to the axis of rotation—and hence is inclined to it in its different parts; at the points of intersection the inclination is about  $23^{\circ} 27'$ , at two other limiting points they are parallel. A uniform measure of time is obtained by the invention of the *Mean Solar Day*.

275. **Mean Solar Day** is the interval between two successive transits of the *mean sun* over the same meridian; it begins when the mean sun is on the meridian. This fictitious body is conceived to move in the equinoctial with the mean motion of the actual sun in the ecliptic. The length of the mean solar day is the average length of the *apparent solar days* for the space of a solar year.

276. **Equation of Time** is the difference between apparent and mean time. It is measured by the angle at the pole of the heavens between two circles passing, the one through the apparent sun's centre, the other through the mean sun. The Equation of Time is so called because it enables us to reduce apparent to mean, or mean to apparent time. In consequence of the motion of the sun in the ecliptic being variable, and the ecliptic not being perpendicular to the axis of the earth's rotation, apparent time is variable, and this fluctuation is considerable, amounting to upwards of half an hour—apparent noon sometimes taking place as much as  $16^m$  before mean noon, and at others as much as  $14\frac{1}{2}^m$  after. These are the greatest values of the equation of time; it vanishes altogether four times a year—this occurring about April 15th, June 15th, September 1st, and December 24th. It is calculated and inserted in the Nautical Almanac for every day in the year. On page I of each month the equation of time given is that to be used in deducing mean from apparent time; that on page II is to be used in deducing apparent from mean time. The difference in the value of the two arises from the one being that at apparent noon, and the other that at mean noon. As these may be separated by an interval of more than a quarter of an hour, the equation of time given in pages I and II may differ by a quarter of the "Var. in 1 hour" given in the adjoining column. The equation of time is itself a portion of mean time.

277. **To reduce equation of time to Greenwich date.**—The method of correcting the equation of time for the Greenwich date is similar to that for correcting the sun's declination, and the "Variation in 1 hour" may be used for the purpose.

## RULE LXXXVI.

1°. *Get a Greenwich date, as before.*

NOTE.—The time by chronometer when error and rate are applied to it, gives Mean Time at Greenwich.

2°. Take out of Nautical Almanac (page II of the month) the equation of time for the noon of Greenwich date, and mark it additive or subtractive, according to the heading of equation of time at the top of the column in page I of the month; also take from the column in page I, the "Var. in 1 hour."\*

NOTE.—It sometimes happens that the precept for applying the Eq. of Time changes in the course of the month. Thus in April 1876, a black line is placed between the Eq. T. for the 14th and that for the 15th, indicating that a change of precept occurs between those days. The Equations above the line has to be added, those below have to be subtracted.

3°. Multiply the "Var. in 1 hour" by the hours, and when great precision is necessary, by the fractional parts of an hour also. The result is the correction to be applied to the equation of time taken from the Nautical Almanac, and is to be added when equation of time is increasing but subtracted when equation of time is decreasing; the result is the Equation of time sought.

NOTE.—When correcting backwards from the following noon, the rule will be Equation increasing, subtract, and decreasing, add.

(a) When the correction, being subtractive, exceeds the equation of time itself, subtract the equation of time from the correction; the remainder is the reduced equation of time sought—and it is to be subtracted from apparent time when equation of time at noon is directed to be added, but added to apparent time when equation of time at noon is directed to be subtracted; i.e. the Equation has to be applied to A.T. according to the precept for the day following the given day.

#### EXAMPLES.

Ex. 1. 1876, January 29th, 6<sup>h</sup> 53<sup>m</sup> 49<sup>s</sup> mean time at Greenwich; find Equation of time to be applied to apparent time (in working the chronometer.)

| Eq. of Time, page II, N.A.  |   | Hourly Diff. page I, N.A.                          |                                  |
|-----------------------------|---|--|----------------------------------|
| Jan. 29th, add              | 13 <sup>m</sup> 20 <sup>s</sup> 1 <sup>i</sup> <i>incr.</i> | Jan. 29th, at noon                                 | 0 <sup>s</sup> 44 <sup>t</sup> 7 |
| Corr. for 6 <sup>h</sup> 9  | + 3 <sup>i</sup>  | 6 <sup>h</sup> 54 <sup>m</sup> is 6 <sup>h</sup> 9 | 6 <sup>t</sup> 9                 |
| Red. Eq. Time               | 13 23 <sup>i</sup> 2  |  | 4023                             |
| (To be added to app. time.) |   |  | 2682                             |
|                             |   | Correction   | 3 <sup>i</sup> 0843              |
|                             |   | or,  | 3 <sup>s</sup> 1                 |

In working this example the "Diff. for 1 hour" is taken from the Nautical Almanac from the column in page I of the month, and against the given day. The Greenwich date being mean time, take the equation of time from page II of the month, and mark it *additive* to app. time as directed at the top of the column in page I; also note that the equation is increasing. The Green. time being 6<sup>h</sup> 54<sup>m</sup> or 6<sup>h</sup> 9; hourly difference is multiplied by 6<sup>h</sup> 9 giving the product 30843; and since there are three decimals figures in H. D. (.447) and one in Green. time (.0) in all four, four decimal places are marked off from the right hand of the product, the result 3<sup>i</sup> 0843 or 3<sup>s</sup> 1 is the correction to be applied to the Eq. of time at noon, and is to be *added* to it because it is that due to a time elapsed since noon while the Eq. T. is increasing.

\* As the equation of time is not a uniformly varying quantity, it is not quite accurate to compute its correction as above, by multiplying the given hourly difference by the number of hours in the Greenwich time; for that process assumes that this hourly difference in the same for each hour. The variations in the hourly difference are, however, so small that it is only when extreme precision is required that recourse must be had to the more exact method of interpolation for second differences.

Ex. 2. 1876, September 30th,  $10^h 15^m$  mean time at Greenwich: find the Equation of time to be applied to app. time in working the chronometer.

| Eq. of Time, page II, N.A.          |                            | Diff. for $1^h$ , page I, N.A. |                 |
|-------------------------------------|----------------------------|--------------------------------|-----------------|
| Sept. 30th, noon, <i>subt.</i>      | $10^m 11^s.5$ <i>incr.</i> | Sept. 30th, at noon,           | $0^s 80.5$      |
| Corr. for $10\frac{3}{4}^h$         | $+ 8.3$                    |                                | $10\frac{1}{4}$ |
| Red. Eq. T.                         | $10 19.8$                  | Diff. for 10 hours             | $80.50$         |
| (To be <i>subtracted</i> from A.T.) |                            | Diff. for $\frac{1}{4}$ hour   | $201$           |
|                                     |                            | Correction                     | $8^s 251$       |
|                                     |                            |                                | or, $8^s.3$     |

Ex. 3. 1876, December 23rd,  $22^h 56^m$ , mean time at Greenwich: find equation of time to be applied to apparent time.

| Green. date, Dec. 23rd,             |                         | $22^h 56^m$    |           |
|-------------------------------------|-------------------------|----------------|-----------|
| Subtract from                       |                         | $24$           | $0$       |
| Time from noon, Dec. 24th,          |                         | $1$            | $4$       |
| Eq. of time, page II, N.A.          |                         | Hourly diff.   |           |
| Dec. 24th, <i>subt.</i>             | $0 6^s.68$ <i>incr.</i> | Time from noon | $1^s 246$ |
| Corr. for $1^h$                     | $- 1.25$                |                | $1^h$     |
| Red. eq. of time                    | $0 5.43$                | Correction     | $1^s 246$ |
| (To be <i>subtracted</i> from A.T.) |                         |                |           |

In this example the equation of time is taken for the nearest noon to Greenwich date, viz., Dec. 24th. To obtain the correction we go back 1 hour, and since the equation of time is *increasing* at noon, Dec. 24th, it was *less* at one hour *earlier*, therefore the correction is *subtractive*.

Ex. 4. 1876, August 31st,  $5^h 42^m 15^s$ , mean time at Greenwich: find equation of time to be applied to apparent time.

| Eq. of time, page II, N.A.          |                            | Hourly diff., page I, N.A. |              |
|-------------------------------------|----------------------------|----------------------------|--------------|
| Aug. 31st, at noon, <i>add</i>      | $0^m 18^s.41$ <i>decr.</i> | Aug. 31st, noon,           | $0^s 78.0$   |
| Corr. for $5^h 42^m$                | $- 4.45$                   | $5^h 42^m$                 | $= 5.7$      |
| Red. eq. of time, <i>subt.</i>      | $0 3.04$                   |                            | $546$        |
| (To be <i>subtracted</i> from A.T.) |                            |                            | $390$        |
|                                     |                            | Correction                 | $4.446$      |
|                                     |                            |                            | or, $4^s.45$ |

In this case the correction is *subtractive*, and exceeds in amount the equation of time at noon, therefore the equation of time is taken from the correction, and the remainder is the reduced equation of time to be *subtracted* from A.T., according to the precept for the day following the given day—a change of precept occurring between Aug. 31st and Aug. 32nd (Sept. 1st.)—which change is shown by means of a black line drawn between the Equations for the two named days.

Ex. 5. 1876, June 13th,  $22^h 25^m 21^s$  mean time at Greenwich; find equation of time to be applied to apparent time, in working the chronometer.

| Greenwich date, June 13th,    |                            | Hourly Diff. page I, N.A. |           |
|-------------------------------|----------------------------|---------------------------|-----------|
| or,                           |                            | June 13th, noon,          | $0^s 520$ |
|                               |                            |                           | $22.4$    |
| Eq. T. page II, N.A.          |                            |                           | $2080$    |
| June 13th, noon, <i>subt.</i> | $0^m 10^s.57$ <i>decr.</i> |                           | $1040$    |
| Correction for $22^h.4$       | $- 11.65$                  |                           | $1040$    |
| Red. Eq. T. ( <i>add</i> )    | $0 1.08$                   | Correction                | $11.6480$ |
| (To be <i>added</i> to A.T.)  |                            | or,                       | $11^s.65$ |

In this case also, the correction is subtractive, and exceeds the Equation itself, therefore, the equation is subtracted from the correction and a change of precept is made *i.e.*, the equation of time at noon being *subtractive*, after it has been subtracted from the correction; to the remainder prefix the precept *add* to A.T.

By using the Eq. T. of time corresponding to the nearest Greenwich noon, *viz.*, that for June 14th the work will stand thus:

|                                 |   |                           |                    |
|---------------------------------|---|---------------------------|--------------------|
| Green. date, June 13th,         | 22 <sup>h</sup> 25 <sup>m</sup>               | Hourly Diff. page I, N.A. |                    |
| Subtract from                   | 24  | June 14th, at noon,       | 0 <sup>s</sup> 526 |
| Time from noon, June 14th       | 1 <sup>h</sup> 35                             | Time from noon 14th       | 1 <sup>h</sup> 6   |
|                                 | or, 1 <sup>h</sup> 6 nly.                     |                           | 3156               |
| Eq. T. page II, N.A.            |   |                           | 526                |
| June 14th, at noon, <i>add</i>  | 0 <sup>m</sup> 1 <sup>s</sup> 99 <i>incr.</i> | Correction                | 8416               |
| Correction for 1 <sup>h</sup> 6 | — 0 <sup>s</sup> 84                           | or,                       | 0 <sup>s</sup> 84  |
| Red. Eq. T. add                 | 0 1 <sup>h</sup> 15                           |                           |                    |

(To be added to A.T.)

The Eq. Time would be *less* at 1<sup>h</sup>6 *before* noon than what it is at noon, the correction is therefore subtracted from the noon Eq. of Time.

### EXAMPLES FOR PRACTICE.

In each of the following examples it is required to find the equation of time corresponding to the given Greenwich date:—

|                    |   |                      |  |
|--------------------|---|----------------------|--|
| 1. 1876, Jan. 5th, | at 4 <sup>h</sup> 33 <sup>m</sup> 0 <sup>s</sup> M.T. | 11. 1876, June 13th, | at 22 <sup>h</sup> 52 <sup>m</sup> 0 <sup>s</sup> M.T. |
| 2. " Feb. 18th,    | at 8 20 0 M.T.  | 12. " Aug. 31st,     | at 15 54 0 A.T.  |
| 3. " Mar. 24th,    | at 3 4 8 M.T.   | 13. " May 14th,      | at 9 36 0 A.T.   |
| 4. " April 14th,   | at 16 8 10 M.T.                                       | 14. " April 13th,    | at 21 36 53 M.T.                                       |
| 5. " May 19th,     | at 6 56 0 M.T.  | 15. " Nov. 14th,     | at 21 35 0 A.T.  |
| 6. " June 13th,    | at 22 49 50 M.T.                                      | 16. " July 20th,     | at 20 57 16 M.T.                                       |
| 7. " July 16th,    | at 1 14 0 A.T.  | 17. " Dec. 23rd,     | at 18 2 54 M.T.  |
| 8. " Aug. 31st,    | at 21 14 40 A.T.                                      | 18. " Oct. 26th,     | at 7 56 21 M.T.  |
| 9. " Sept. 18th    | at 0 53 10 M.T.                                       | 19. " Dec. 24th,     | at 1 30 0 A.T.   |
| 10. " Oct. 5th,    | at 19 19 2 A.T.                                       | 20. " Aug. 31st,     | at 1 48 0 M.T.   |

## CORRECTION OF THE OBSERVED ALTITUDE.

278. **The Altitude** of a celestial body is the angular distance of the body from the horizon. It is measured by the arc of a circle of Azimuth (which is hence generally called a circle of altitude) passing through the plane of the body, or by the corresponding angle at the centre of the sphere.

279. The corrections necessary to reduce an altitude observed from the sea-horizon with a quadrant or sextant, &c., to the *true* altitude, consist of the index correction, the dip, the correction of altitude, or the joint effect of refraction and parallax, and, in certain cases, of the semi-diameter.

The altitudes of heavenly bodies are observed from the deck of a ship at sea, with the sextant, for the purpose of finding latitude, longitude, &c. Such an altitude is called the "*observed altitude*." There are certain instrumental and circumstantial sources of error by which this is affected:—(a) The sextant (supposed otherwise to be in adjustment) may have an index error: (b) The eye of the observer being elevated above the surface of the sea, the horizon will appear to be depressed, and the consequent altitude in reality too great: and (c) One of the limbs of the body may be observed instead of its centre. When the correction

for these errors and method of observing are applied—"the index correction," "correction" for dip, and "semi-diameter,"—the observed is reduced to the *apparent altitude*. But, again, for the sake of comparison and computation, all observations must be transformed into what they would have been, had the bodies been viewed through a uniform medium, and from one common centre—the centre of the earth. The altitude supposed to be so taken is called the "*true altitude*;" it may be deduced from the apparent altitude by applying the corrections called "corrections for refraction" (Table V, Norie, or XXXI, Raper), and "correction for parallax" (Table VI, Norie, or XXXIV, Raper), which, however, are sometimes given in tables combined under the names "correction of altitude" (Table XVIII, Norie). (*a'*) "Correction for refraction;" when a body is viewed through the atmosphere, refraction will cause the apparent to be greater than the true altitude; hence the correction for refraction is subtractive in finding the true from the apparent altitude. (*b'*) "Correction for parallax;" the position of the observer on the surface, especially for near bodies, will cause the apparent to be less than the true altitude; hence the correction for parallax is additive in finding the true from the apparent altitude.

## TO CORRECT THE SUN'S ALTITUDE.

### RULE LXXXVII.

- 1°. *Correct the observed altitude of the sun for index error, if any.*
- 2°. *Subtract the dip answering to height of eye (Table V, Norie, and Table XXX, Raper); the remainder is the apparent altitude of the limb observed.*
- 3°. *Subtract the refraction (Table IV, Norie, and XXXI Raper), add the parallax (Table VI, Norie, XXXIV, Raper); or take out the "correction in altitude of sun" (Table XVIII, Norie), and subtract it; the remainder is the true altitude of the observed limb.*
- 4°. *Take from page II of the month in the Nautical Almanac the sun's semi-diameter, adding it when the sun's lower limb (L.L.) is observed; the result thus obtained is the true altitude of the sun's centre.*

Table 9, Norie, and Table 38, Raper, contain the gross correction of altitude, or the corrections for dip, refraction, sun's semi-diameter, and parallax—exclusive of index error, which are sometimes used in solving questions in nautical astronomy when great precision is not necessary.

### EXAMPLES.

Ex. 1. 1876, January 6th, the observed altitude sun's L.L.  $39^{\circ} 8' 30''$ , index correction  $+ 33''$ , height of eye 19 feet: required the true altitude.

| <i>Raper.</i>        |   | <i>Norie.</i>          |  |
|----------------------|---|------------------------|--|
| Obs. alt. sun's L.L. | $39^{\circ} 8' 30''$  | Obs. alt. sun's L.L.   | $39^{\circ} 8' 30''$                         |
| Index correction     | $+ 33$  | Index correction       | $+ 33$                                       |
|                      | <hr/>   |                        | <hr/>  |
| Dip (Table 30.)      | $39 \quad 9 \quad 3$<br>$- \quad 4 \quad 15$  | Dip (Table 5.)         | $39 \quad 9 \quad 3$<br>$- \quad 4 \quad 11$ |
|                      | <hr/>   |                        | <hr/>  |
| App. alt. sun's L.L. | $39 \quad 4 \quad 48$   | App. alt. sun's L.L.   | $39 \quad 4 \quad 52$                        |
| Ref. (Table 31.)     | $\left. \begin{array}{l} - \quad 1 \quad 5 \\ - \text{Par. (Table 34.)} \end{array} \right\}$ | Corr. alt. (Table 18.) | $- \quad 1 \quad 3$                          |
| —Par. (Table 34.)    |   |                        | <hr/>  |
| True alt. sun's L.L. | $39 \quad 3 \quad 43$   | True alt. sun's L.L.   | $39 \quad 3 \quad 49$                        |
| Semi-diameter        | $+ 16 \quad 18$   | Semi-diameter          | $+ 16 \quad 18$                              |
|                      | <hr/>   |                        | <hr/>  |
| True altitude        | $39 \quad 20 \quad 1$   | True altitude          | $39 \quad 20 \quad 7$                        |



Ex. 2. 1876, June 18th, the observed altitude sun's L.L.  $71^{\circ} 19' 20''$ , index correction  $+ 3' 46''$ , height of eye 18 feet: required the true altitude.

|                      |                       |                          |                       |
|----------------------|-----------------------|--------------------------|-----------------------|
| Obs. alt. sun's L.L. | $71^{\circ} 19' 20''$ | Obs. alt. sun's L.L.     | $71^{\circ} 19' 20''$ |
| Index correction     | $+ 3' 46''$           | Index correction         | $+ 3' 46''$           |
|                      | <hr/>                 |                          | <hr/>                 |
| Dip (Table 30.)      | $71^{\circ} 23' 6''$  | Dip (Table 5)            | $71^{\circ} 23' 6''$  |
|                      | $- 4' 10''$           |                          | $- 4' 4''$            |
|                      | <hr/>                 |                          | <hr/>                 |
| Ref. $- 0' 20''$ }   | $71^{\circ} 18' 56''$ | Corr. of alt. (Table 18) | $71^{\circ} 19' 2''$  |
| Par. $+ 3' 3''$ }    | $- 17''$              |                          | $- 17''$              |
|                      | <hr/>                 |                          | <hr/>                 |
| Semid., p. II, N.A.  | $71^{\circ} 18' 39''$ | Semi-diameter            | $71^{\circ} 18' 45''$ |
|                      | $+ 15' 46''$          |                          | $+ 15' 46''$          |
|                      | <hr/>                 |                          | <hr/>                 |
| True altitude        | $71^{\circ} 34' 25''$ | True altitude            | $71^{\circ} 34' 31''$ |

Ex. 3. 1876, October 8th, the observed altitude sun's L.L.  $19^{\circ} 50' 10''$ , index correction  $+ 50''$ , height of eye 16 feet.

|                      |                       |                        |                       |
|----------------------|-----------------------|------------------------|-----------------------|
| Obs. alt. sun's L.L. | $19^{\circ} 50' 10''$ | Obs. alt. sun's L.L.   | $19^{\circ} 50' 10''$ |
| Index correction     | $+ 50''$              | Index correction       | $+ 50''$              |
|                      | <hr/>                 |                        | <hr/>                 |
| Dip                  | $19^{\circ} 51' 0''$  | Dip                    | $19^{\circ} 51' 0''$  |
|                      | $- 4' 0''$            |                        | $- 3' 50''$           |
|                      | <hr/>                 |                        | <hr/>                 |
| Ref. $- 2' 41''$ }   | $19^{\circ} 47' 0''$  | Correction of altitude | $19^{\circ} 47' 10''$ |
| Par. $+ 8' 3''$ }    | $- 2' 33''$           |                        | $- 2' 29''$           |
|                      | <hr/>                 |                        | <hr/>                 |
| Semi-diameter        | $19^{\circ} 44' 27''$ | Semi-diameter          | $19^{\circ} 44' 41''$ |
|                      | $+ 16' 3''$           |                        | $+ 16' 3''$           |
|                      | <hr/>                 |                        | <hr/>                 |
| True altitude        | $20^{\circ} 0' 30''$  | True altitude          | $20^{\circ} 0' 44''$  |

Ex. 4. 1876, August 8th, observed altitude sun's U.L.  $12^{\circ} 52' 30''$ , index correction  $+ 3' 10''$ , height of eye 17 feet.

|                      |                       |                      |                       |
|----------------------|-----------------------|----------------------|-----------------------|
| Obs. alt. sun's U.L. | $12^{\circ} 52' 30''$ | Obs. alt. sun's U.L. | $12^{\circ} 52' 30''$ |
| Index correction     | $+ 3' 10''$           | Index correction     | $+ 3' 10''$           |
|                      | <hr/>                 |                      | <hr/>                 |
| Dip 17 feet          | $12^{\circ} 55' 40''$ | Dip                  | $12^{\circ} 55' 40''$ |
|                      | $- 4' 5''$            |                      | $- 3' 57''$           |
|                      | <hr/>                 |                      | <hr/>                 |
| Ref. $- 4' 11''$ }   | $12^{\circ} 51' 35''$ | Correction altitude  | $12^{\circ} 51' 43''$ |
| Par. $+ 8' 8''$ }    | $- 4' 3''$            |                      | $- 3' 56''$           |
|                      | <hr/>                 |                      | <hr/>                 |
| Semi-diameter        | $12^{\circ} 47' 32''$ | Semi-diameter        | $12^{\circ} 47' 47''$ |
|                      | $- 15' 49''$          |                      | $- 15' 49''$          |
|                      | <hr/>                 |                      | <hr/>                 |
| True altitude        | $12^{\circ} 31' 43''$ | True altitude        | $12^{\circ} 31' 58''$ |

## EXAMPLES FOR PRACTICE.

|     |                  |                      |                            |             |             |              |
|-----|------------------|----------------------|----------------------------|-------------|-------------|--------------|
| 1.  | 1876, Jan. 29th, | Obs. alt. sun's L.L. | $17^{\circ} 44' 30''$      | Index corr. | $- 1' 25''$ | Eye 16 feet. |
| 2.  | " Feb. 18th,     | "                    | $48^{\circ} 4' 10''$       | "           | $+ 0' 55''$ | " 12 "       |
| 3.  | " Mar. 24th,     | "                    | $29^{\circ} 50' 30''$      | "           | $+ 1' 3''$  | " 17 "       |
| 4.  | " April 20th     | "                    | $76^{\circ} 3' 0''$        | "           | $- 1' 27''$ | " 10 "       |
| 5.  | " May 8th,       | "                    | $58^{\circ} 38' 20''$      | "           | $- 1' 10''$ | " 18 "       |
| 6.  | " June 19th,     | "                    | $24^{\circ} 48' 30''$      | "           | $- 1' 14''$ | " 20 "       |
| 7.  | " July 16th,     | "                    | $65^{\circ} 1' 0''$        | "           | $+ 0' 17''$ | " 14 "       |
| 8.  | " Aug. 7th,      | "                    | $85^{\circ} 13' 20''$      | "           | $- 2' 10''$ | " 18 "       |
| 9.  | " Sept. 2nd,     | "                    | U.L. $28^{\circ} 16' 20''$ | "           | $- 4' 8''$  | " 10 "       |
| 10. | " Oct. 17th,     | "                    | U.L. $67^{\circ} 44' 0''$  | "           | $- 1' 38''$ | " 15 "       |
| 11. | " Nov. 15th,     | "                    | U.L. $14^{\circ} 3' 40''$  | "           | $+ 4' 1''$  | " 12 "       |
| 12. | " Dec. 14th,     | "                    | U.L. $12^{\circ} 10' 5''$  | "           | $- 0' 49''$ | " 12 "       |

# TO FIND THE LATITUDE BY A MERIDIAN ALTITUDE OF THE SUN.

## RULE LXXXVIII.

1°. *With the ship's date and longitude in time, find the Greenwich date in apparent time (Rule LXXXI, 5°, page 222).*

2°. *Take the sun's declination from Nautical Almanac (page I of the month), and correct it for the Greenwich date (Rule LXXXIII, page 225).*

Instead of proceeding according to 1° and 2° the declination may be found thus:—(1) Take the sun's declination from the *Nautical Almanac*, for apparent noon, page I; and also the corresponding hourly difference. (2) Multiply the hourly diff. by long. in time, expressed in hours and decimals of an hour. (3) When the declination is *increasing* the correction is to be *added* in *West*, but *subtracted* in *East* longitude; but when the declination is *decreasing* *subtract* in *West* but *add* in *East* longitude. See Rule LXXXIV, page 229.

3°. *Correct the observed altitude for index error, dip, semi-diameter, and refraction and parallax, and thus get the true altitude (Rule LXXXVII, page 236); subtract true altitude from 90°: the result will be the true zenith distance.\**

4°. *Call the zenith distance N., when the observer is North of sun, or when the sun bears South; call zenith distance S., when the observer is South of sun, or when it bears North.*

5°. *Add together the declination and zenith distance, when they have the same name (see examples 1 and 3); but take the difference if their names be unlike (see examples 2, 5, and 6); the latitude is N. or S., as the greater is.*

6°. *When the declination is 0°, the zenith distance is the latitude, and of the same name as the zenith distance (see example 7); and when the zenith distance is 0°, the declination is the latitude, which is of the same name as the declination (see example 4).*

## EXAMPLES.

Ex. 1. 1876, January 15th, in longitude 72° 42' W., the observed meridian altitude of the sun's L.L. (lower limb) was 59° 42' 10", bearing North; index error + 2' 10", height of eye 14 feet: required the latitude.

The observation was made when the sun was on the meridian, that is, at apparent noon; the date therefore at the place of observation is January 15th, 0<sup>h</sup> 0<sup>m</sup> 0<sup>s</sup>. But the meridian of the place of observation is 72° 42' W. of meridian of Greenwich, and therefore, the sun is 72° 42' W. of meridian of Greenwich; or, in time 4<sup>h</sup> 50<sup>m</sup> 48<sup>s</sup>, since 72° 42' is equivalent to 4<sup>h</sup> 50<sup>m</sup> 48<sup>s</sup> (see below). It is, therefore, 4<sup>h</sup> 50<sup>m</sup> 48<sup>s</sup> *past* apparent noon at Greenwich, and the Greenwich date is found by *adding* 4<sup>h</sup> 50<sup>m</sup> 48<sup>s</sup> to the time of apparent noon at ship, January 15th, thus:—

|                      |  |  |
|----------------------|--|--|
| Ship date, January   | 15 <sup>d</sup> 0 <sup>h</sup> 0 <sup>m</sup> 0 <sup>s</sup> | 72° 42'  |
| Longitude 72° 42' W. | + 4 50 48  | 4  |
| Greenwich date Jan.  | 15 4 50 48   | 4 <sup>h</sup> 50 <sup>m</sup> 48 <sup>s</sup> |

With this date the sun's declination must be taken out of *Nautical Almanac*, where it will be found in page I for January. It may be reduced to Greenwich date by means of the Tables, or by "hourly diff.," thus:—

\* When true altitude exceeds 90°, subtract 90° from it.

Decl., page I, N.A.  
 Jan. 15th at noon  $21^{\circ} 11' 32'' \cdot 2$  S. (*decr.*)  
 Corr. for  $4^h 51^m$   $2 \ 12' \cdot 4$   
 Red. decl.  $21 \ 9 \ 20$  S.

Hourly diff., page I, N.A.  
 Jan. 15th  $- 27'' \cdot 30$   
 $4^h 51^m = 4^h \cdot 85$   $\times 4^h \cdot 85$   
 $13650$   
 $21840$   
 $10920$   
 $6,0)132'4050$   
 Correction  $- 2 \ 12' \cdot 4$

In working this example the H. diff. for the noon of the day is taken without correcting it for the middle time as explained in No. 27<sup>o</sup> page 230. We divide the minutes of Greenwich time by 6; thus, 6 is contained in 51 eight times and three over, 6 is contained in 30 (the remainder 3 with a 0 added) five times; hence we have the decimal .85, to this we prefix the hours (4), and we then have  $4^h \cdot 85$  to multiply by. As the Green. date wants  $10^m$  of 5 hours, we might have multiplied the hourly diff. by 5, and deducted one-sixth of hourly diff. from the product.

*Raper.*  
 Obs. alt. sun's L.L.  $59^{\circ} 42' 10''$  N.  
 Index error  $+ 2 \ 10$   
 Dip (Table 30)  $59 \ 44 \ 20$   
 $- 3 \ 40$   
 App. alt. sun's L.L.  $59 \ 40 \ 40$   
 Refraction (Table 31)  $- 34$   
 Parallax (Table 34)  $59 \ 40 \ 6$   
 $+ 4$   
 True alt. sun's L.L.  $59 \ 40 \ 10$   
 Semi-diameter  $+ 16 \ 18$   
 True altitude  $59 \ 56 \ 28$   
 $90 \ 0 \ 0$   
 Zenith distance  $30 \ 3 \ 32$  S.  
 Declination  $21 \ 9 \ 20$  S.  
 Latitude  $51 \ 12 \ 52$  S.

*Norie.*  
 Obs. alt. sun's L.L.  $59^{\circ} 42' 10''$  N.  
 Index error  $+ 2 \ 10$   
 Dip (Table 5)  $59 \ 44 \ 20$   
 $- 3 \ 36$   
 Corr. alt. (Table 18)  $59 \ 40 \ 44$   
 $- 29$   
 Semi-diameter  $59 \ 40 \ 15$   
 $+ 16 \ 18$   
 True altitude  $59 \ 56 \ 33$   
 $90 \ 0 \ 0$   
 Zenith distance  $30 \ 3 \ 27$  S.  
 Declination  $21 \ 9 \ 20$  S.  
 Latitude  $51 \ 12 \ 47$  S.

The meridian zenith distance and declination are added, because they are of the same name. (This is according to No. 5<sup>o</sup> of the Rule).

Ex. 2. 1876, February 3rd, in longitude  $139^{\circ} 42' W.$ , the observed meridian altitude of the sun's L.L.  $56^{\circ} 56' 56''$ , bearing South; index correction  $- 3' 4''$ ; height of eye 14 feet.

Ship date, February  $3^d \ 0^h \ 0^m \ 0^s$   
 Long.  $139^{\circ} 42' W.$   $+ 9 \ 18 \ 48$   
 Greenwich date, Feb.  $3 \ 9 \ 18 \ 48$

Decl. page I, N.A., Feb. 3rd  $= 16^{\circ} 37' 7''$   
 S., *decr.* Hourly diff.  $43'' \cdot 95$ .

Hourly diff. Feb. 3rd noon  $43'' \cdot 95$   
 T. from noon,  $9^h 18^m$   $+ 9' 3$   
 $13185$   
 $39555$   
 $6,0)40,8'735$

Corr.  $- 6 \ 49$   
 Decl. noon, Feb. 3rd  $16 \ 37 \ 7$  S.  
 Red. decl.  $16 \ 30 \ 18$  S.

By Raper: index corr.  $- 3' 4''$ ; dip  $- 3' 40''$ ; refr.  $- 0' 38''$ ; par.  $+ 4''$ ; semid.  $+ 16' 16''$ ; true alt.  $57^{\circ} 5' 54''$ ; latitude  $16^{\circ} 23' 12''$  N.

*Norie.*  
 Obs. alt. sun's L.L.  $56^{\circ} 56' 56''$  S.  
 Index correction  $- 3 \ 4$   
 Dip (Table 5, Norie)  $56 \ 53 \ 52$   
 $- 3 \ 36$   
 App. alt. sun's L.L.  $56 \ 50 \ 16$   
 Corr. Alt. (Table 18)  $- 0 \ 32$   
 True alt. sun's L.L.  $56 \ 49 \ 44$   
 Semi-diameter  $+ 16 \ 16$   
 True altitude  $57 \ 6 \ 0$   
 $90 \ 0 \ 0$   
 Zenith distance  $32 \ 54 \ 0$  N.  
 Declination  $16 \ 30 \ 18$  S.  
 Latitude  $16 \ 23 \ 42$  N.

The difference of zenith distance and declination is taken because they are of contrary names. See No. 5<sup>o</sup> of Rule.

+

Ex. 3 1876, March 20th, longitude  $37^{\circ} 45'$  E., observed meridian altitude of the sun's L.L.  $52^{\circ} 52' 50''$ , bearing South: index correction  $+ 1' 5''$ ; height of eye 12 feet.

|   |                      |                          |
|---|----------------------|--------------------------|
| Long. in time $2^h 30^m$ , or $2.5$ .                 | Obs. alt. sun's L.L. | $52^{\circ} 52' 50''$ S. |
| Hourly diff., noon, 20th, $59'' \cdot 24$             | Index correction     | $+ 1' 5''$               |
| T. from noon, 20th, at $2^h 31^m \times 2.5$          |                      | <hr/>                    |
|   | Dip (Norie)          | $52^{\circ} 53' 55''$    |
|   |                      | $- 3' 19''$              |
|   | App. alt. sun's L.L. | $52^{\circ} 50' 36''$    |
|   | Corr. of alt.        | $- 38''$                 |
|   | True alt. sun's L.L. | $52^{\circ} 49' 58''$    |
|   | Semi-diameter        | $+ 16' 5''$              |
|   | True altitude        | $53^{\circ} 6' 3''$      |
|   |                      | $90^{\circ} 0' 0''$      |
|   | Zenith distance      | $36^{\circ} 53' 57''$ N. |
|   | Declination          | $0^{\circ} 2' 25''$ N.   |
|   | Latitude             | $36^{\circ} 56' 22''$ N. |
| Correction $6,0)14,8100$                              |                      | $36^{\circ} 57,2921$     |
|   |                      |                          |
|   |                      |                          |
| Decl. 20th, noon $0^{\circ} 5' 53''$ N., <i>incr.</i> |                      |                          |
| Correction $- 2' 28''$                                |                      |                          |
|   |                      |                          |
| Red. decl. $0^{\circ} 2' 25''$ N.                     |                      |                          |
|   |                      |                          |
|   |                      |                          |

By Raper: dip  $- 3' 20''$ ; ref.  $- 0' 44''$ ; par.  $+ 5''$ ; semid.  $+ 16' 5''$ . True alt.  $53^{\circ} 6' 1''$ , and latitude  $36^{\circ} 56' 38''$  N.

The longitude  $37^{\circ} 45'$  in time is  $2^h 31^m$ , or  $2.5$ , and being *east*, the Greenwich date is  $2^h 31^m$  before the noon of March 20th (the noon of the ship date), then the decl. and hourly diff. is taken out of the *Nautical Almanac*, page I, for the *nearest* noon to Greenwich date, viz., noon of March 20th, and hourly diff. is multiplied by  $2.5$ ; the resulting figures are  $148'' \cdot 100$ , or  $2' 28''$ , the correction. The decl. at noon 20th, *increasing*, would evidently be less,  $2^h 31^m$  *earlier*, therefore the correction  $- 2' 28''$  is *subtractive*. See Rule LXXXIV, page 229.

Ex. 4. 1876, April 16th, longitude  $139^{\circ} 50'$  E., observed meridian altitude sun's L.L.  $89^{\circ} 46' 10''$ , bearing North; index correction  $+ 1' 56''$ ; height of eye 18 feet.

|  |                      |                          |
|--|----------------------|--------------------------|
| Long. in time ( $139^{\circ} 50'$ E.) $= 9^h 19^m 20^s$ , or $9.3$ . | Obs. alt. sun's L.L. | $89^{\circ} 46' 10''$ N. |
| Decl. page I, N.A.   | Index correction     | $+ 1' 56''$              |
| Hourly diff., noon, 16th $52'' \cdot 91$                             |                      | <hr/>                    |
| Green. time $9^h 19^m = \times 9.3$                                  | Dip (Norie)          | $89^{\circ} 48' 6''$     |
|  |                      | $- 4' 4''$               |
|  | Corr. alt.           | $89^{\circ} 44' 2''$     |
|  |                      | $0''$                    |
|  | Semi-diameter        | $89^{\circ} 44' 2''$     |
|  |                      | $+ 15' 58''$             |
|  |                      | <hr/>                    |
|  | Zenith distance      | $90^{\circ} 0' 0''$      |
|  | Declination          | $90^{\circ} 0' 0''$      |
|  | Latitude             | $10^{\circ} 12' 40''$ N. |
| Correction $6,0)49,2063$   |                      | $10^{\circ} 12' 40''$ N. |
|  |                      |                          |
|  |                      |                          |
| Decl. noon, 16th $10^{\circ} 20' 52''$ N. <i>incr.</i>               |                      |                          |
| Correction $- 8' 12''$   |                      |                          |
|  |                      |                          |
| Red. decl. $10^{\circ} 12' 40''$ N.                                  |                      |                          |
|  |                      |                          |
|  |                      |                          |

By Raper: index corr.  $+ 1' 56''$ ; dip  $- 4' 10''$ ; ref. &c.,  $0'$ ; semid.  $+ 15' 58''$ . True alt.  $89^{\circ} 59' 54''$ , latitude  $10^{\circ} 12' 34''$  N.

Ex. 5. 1876, July 13th, longitude  $50^{\circ} 0' E.$ , observed meridian altitude sun's L.L.  $68^{\circ} 2' 0''$ , bearing north; index correction,  $- 25''$ , height of eye 17 feet.

| Long. in time             | or,    | $3^h 20^m 0^s$<br>$3\frac{1}{3}^h$                               | Norie.   |
|---------------------------|--------|--|--|
| Hourly diff., 13th, noon  |        | $22'' 32$  | Obs. alt. sun's L.L. $68^{\circ} 2' 0'' N.$                          |
| Time from noon $3^h 20^m$ |        | $3$  | Index correction $- 25$  |
|                           | $20^m$ | $\left  \begin{array}{r} 3^h \\ 6696 \\ 744 \end{array} \right $ | Dip (Table 5) $68 \quad 1 \quad 35$<br>$- \quad 3 \quad 57$          |
|                           |        | $6,07,440$   | Corr. alt. (Table 18) $67 \quad 57 \quad 38$<br>$- \quad 20$         |
| Correction                | $+$    | $1 \quad 14$   | Semi-diameter (N.A.) $67 \quad 57 \quad 18$<br>$+ \quad 15 \quad 46$ |
| Decl. noon, 13th          |        | $21 \quad 45 \quad 42 \quad N.$                                  | True alt. $68 \quad 13 \quad 4$<br>$90 \quad 0 \quad 0$              |
| Red. decl.                |        | $21 \quad 46 \quad 56 \quad N.$                                  | Zenith distance $21 \quad 46 \quad 56 \quad S.$                      |
|                           |        |  | Declination $21 \quad 46 \quad 56 \quad N.$                          |
|                           |        |  | Latitude $0 \quad 0 \quad 0$   |

The ship on the Equator.

When the zenith distance and declination are numerically equal, and of contrary names, the ship is on the Equator.

Ex. 6. 1876, December 17th, longitude  $175^{\circ} 45' W.$ , observed meridian altitude sun's L.L.  $89^{\circ} 54' 20''$  bearing north, index correction  $+ 4' 4''$ , height of eye 24 feet.

|   |                          |   |
|---|--------------------------|---|
| Green. date (A.T.) Dec. 17th, $11^h 43^m$<br>or, $11^h 7$               | Obs. alt. sun's L.L.     | $89^{\circ} 54' 20'' N.$                        |
|   | Index correction         | $+ \quad 4 \quad 4$                             |
| Decl. page I, N.A. Dec., 17th, $23^{\circ} 23' 46''$<br>S., increasing. | Dip (Table 5) 24 feet    | $89 \quad 58 \quad 24$<br>$- \quad 4 \quad 42$  |
| H. diff. Dec. 17th, noon  |                          | $89 \quad 53 \quad 42$                          |
| Time from noon  |                          | $0 \quad 0$                                     |
|   | Corr. of alt. (Table 18) | $89 \quad 53 \quad 42$<br>$+ \quad 16 \quad 18$ |
|   | Semi-diameter            | $90 \quad 10 \quad 0$                           |
|   | True altitude            | $0 \quad 10 \quad 0 \quad N.$                   |
|   | Zenith distance          | $23 \quad 24 \quad 41 \quad S.$                 |
|   | Declination              |   |
|   | Latitude                 | $23 \quad 14 \quad 41 \quad S.$                 |
| Decl. Dec. 17th, noon $23^{\circ} 23' 46'' S.$ , inc.                   |                          |   |
| Corr. for $11^h 43^m$   |                          |   |
| Red. decl.  |                          |   |

The true altitude by Raper's Tables is  $90^{\circ} 9' 52''$ , Zenith dist.  $0^{\circ} 9' 52''$ , latitude  $23^{\circ} 14' 49'' S.$

$90^{\circ}$  is subtracted from the true altitude, the remainder is zenith distance, North.

Ex. 7. 1876, September 22nd, long.  $76^{\circ} 30' W.$ , observed meridian altitude sun's L.L.  $40^{\circ} 9'$ , bearing North, index correction  $+ 20''$ , height of eye 18 feet.

|  |                       |                          |
|--|-----------------------|--------------------------|
| Green. date (A.T.) Sept. 22nd, $5^h 6^m$ .                     | Obs. alt. sun's L.L.  | $40^{\circ} 9' 0'' N.$   |
| Decl. page I, N.A., Sept. 22nd, at noon                        | Index correction      | $+ 20$                   |
| $0^{\circ} 4' 58'' N.$ , decreasing, Hourly diff. $58'' .50$ . |                       | <hr/>                    |
| H. diff. Sept. 22nd, noon $58'' .50$                           | Dip 18 feet (Table 5) | $40^{\circ} 9' 20$       |
| Time from noon $5^h 1$   |                       | $- 4 4$                  |
| $58^{\circ} 50$  | Corr. alt. (Table 18) | $40^{\circ} 5' 16$       |
| $292^{\circ} 50$   |                       | $- 1 1$                  |
| $6,0) 29,8^{\circ} 35^{\circ}$                                 | Semi-diameter, N.A.   | $40^{\circ} 4' 15$       |
| $- 4' 58''$  | True altitude         | $+ 15' 59$               |
| Decl. Sept. 22nd $0^{\circ} 4' 58'' N.$                        |                       | $40^{\circ} 20' 14$      |
| Red. decl. $0^{\circ} 0' 0''$                                  | Zenith distance       | $90^{\circ} 0' 0''$      |
|  | Declination           | $49^{\circ} 39' 46'' S.$ |
|  | Latitude              | $49^{\circ} 39' 46'' S.$ |

By Raper: index corr.  $+ 20''$ ; dip  $- 4' 10''$ ; refr.  $- 1' 9''$ ; par.  $+ 7''$ ; semid.  $+ 15' 59''$ ; true alt.  $49^{\circ} 39' 54''$ ; latitude  $49^{\circ} 39' 54'' S.$

Ex. 8. 1876, June 25th, longitude  $59^{\circ} 15' E.$ , observed meridian altitude sun's U.L.  $60^{\circ} 24' 10''$  (zenith South of observer); index correction  $- 3' 17''$ ; height of eye 30 feet.

|  |                          |                          |
|--|--------------------------|--------------------------|
| Ship's date (A.T.) June $25^d 0^h 0^m$                 | Obs. alt. sun's U.L.     | $60^{\circ} 24' 10'' N.$ |
| Long. $59^{\circ} 15' E.$                              | Index correction         | $- 3' 17$                |
| Green. date (A.T.) June 24th $20 3$                    |                          | <hr/>                    |
| Decl. p. I, N.A., 25th $23^{\circ} 23' 29'' N.$ decr.  | Dip 30 feet (Table 5)    | $60^{\circ} 20' 53$      |
| H. diff. June 25th noon $4'' .54$                      |                          | $- 5' 15$                |
| T. from noon 25th is $3^h 57^m = 3' 95$                | Corr. of alt. (Table 18) | $60^{\circ} 15' 38$      |
| $227^{\circ} 0$  |                          | $- 29$                   |
| $4086$   | Semi-diameter            | $60^{\circ} 15' 9$       |
| $1362$   | True altitude            | $- 15' 46$               |
| Correction $17^{\circ} 9' 33''$                        |                          | <hr/>                    |
| Decl. June 25th at noon $23^{\circ} 23' 29'' N.$ decr. | Zenith distance          | $59^{\circ} 59' 23$      |
| Correction $+ 18$                                      | Declination              | $90^{\circ} 0' 0''$      |
| Reduced declination $23^{\circ} 23' 47'' N.$           | Latitude                 | $30^{\circ} 0' 37'' S.$  |
|  |                          | $23^{\circ} 23' 47'' N.$ |

By Raper: Ind. corr.  $- 3' 17''$ ; dip  $- 5' 20''$ ; refr.  $- 33'' .4$ ; par.  $+ 4'' .2$ ; Semid.  $- 15' 46''$ ; true alt.  $59^{\circ} 59' 18''$ ; latitude  $60^{\circ} 36' 55'' S.$

The decl. is taken out for the nearest noon to Green. date, viz., June 25th at noon, and corrected for the interval between it and the Green. time, which is equal to the long. in time, viz.,  $3^h 57^m (= 3^{\circ} 95')$ . We might have found the correction for  $4^h$ , and taken from this result the change for  $3^m$  or one-twentieth of the hourly difference.

Ex. 9. 1876, August 23rd, longitude  $168^{\circ} 25' W.$ , observed meridian altitude sun's L.L.  $40^{\circ} 5' 30''$ , observer N. of sun; index corr. —  $54''$ ; height of eye 12 ft.

Green. date, Aug. 23rd,  $11^h 13^m 40^s$ .

Decl. page I, N.A., August 23rd, at noon,  $11^{\circ} 15' 17'' N.$ , decreasing, Hourly diff.  $51'' \cdot 20 \times 11^h 23$  nearly =  $574'' \cdot 976$  or  $9' 35''$ , the corr. to be subtracted; whence red. decl. =  $11^{\circ} 5' 42'' N.$

By Norie: index corr. —  $54''$ ; dip —  $3' 19''$ ; corr. of alt. —  $1' 1''$ ; semid. +  $15' 52''$ ; true alt.  $40^{\circ} 16' 8''$ .

|                 |  |
|-----------------|--|
| True altitude   | $40^{\circ} 16' 8''$<br>$90 \quad 0 \quad 0$ |
| Zenith distance | $49 \quad 43 \quad 52 \quad N.$              |
| Declination     | $11 \quad 5 \quad 42 \quad N.$               |
| Latitude        | $60 \quad 49 \quad 34 \quad N.$              |

By Raper: index corr. —  $54''$ ; dip —  $3' 20''$ ; refr. —  $1' 9'' \cdot 5$ ; par. +  $6'' \cdot 5$ ; semid. +  $15' 52''$ ; true alt.  $40^{\circ} 16' 5''$ ; latitude  $60^{\circ} 49' 37'' N.$

Ex. 10. 1877, January 1st, longitude  $150^{\circ} E.$ , observed meridian altitude sun's L.L.  $70^{\circ} 20'$  (zenith N. of sun); index corr. —  $30''$ ; height of eye 19 feet.

Green. date, 1876, Dec. 31st,  $14^h 0^m$ .

Time from noon, Jan. 1st, 1877, or Dec. 32nd = longitude in time  $10^h 0^m$ .

Decl. 1876, Dec. 32nd,  $22^{\circ} 58' 47'' S.$ , increasing, Hourly diff.  $12'' \cdot 90 \times 10^h$  (long. in time E.) =  $129'' \cdot 00$  or  $2' 9''$ ; whence red. decl.  $23^{\circ} 0' 56'' S.$

By Norie: index corr. —  $30''$ ; dip —  $4' 11''$ ; corr. alt. —  $18''$ ; semid. +  $16' 18''$ ; true altitude  $70^{\circ} 31' 19''$ .

|                 |   |
|-----------------|---|
| True altitude   | $70^{\circ} 31' 19''$<br>$90 \quad 0 \quad 0$ |
| Zenith distance | $19 \quad 28 \quad 41 \quad N.$               |
| Declination     | $23 \quad 0 \quad 56 \quad S.$                |
| Latitude        | $3 \quad 32 \quad 15 \quad N.$                |

3,52.75

### EXAMPLES FOR PRACTICE.

In each of the following examples the latitude is required:—

| No.   | Civil date.      | Longitude.              | Obs. alt. sun's L.L.                 | Index corr.    | Eye.   |
|-------|------------------|-------------------------|--------------------------------------|----------------|--------|
| + 1.  | 1876, Jan. 10th, | $49^{\circ} 51' W.$     | $68^{\circ} 39' 40'' N.$             | + $5' 10''$    | 13 ft. |
| + 2.  | " Feb. 1st,      | $39 \quad 51 \quad E.$  | $72 \quad 43 \quad 50 \quad S.$      | + $1 \quad 42$ | 13     |
| + 3.  | " March 8th,     | $89 \quad 48 \quad E.$  | $51 \quad 49 \quad 30 \quad S.$      | — $3 \quad 17$ | 15     |
| + 4.  | " April 28th,    | $165 \quad 23 \quad W.$ | U.L. $82 \quad 51 \quad 10 \quad N.$ | + $4 \quad 10$ | 18     |
| — 5.  | " May 2nd,       | $32 \quad 3 \quad E.$   | U.L. $46 \quad 18 \quad 0 \quad S.$  | 0              | 20     |
| — 6.  | " June 11th,     | $62 \quad 57 \quad E.$  | L.L. $42 \quad 24 \quad 45 \quad N.$ | + $2 \quad 15$ | 21     |
| — 7.  | " July 20th,     | $156 \quad 38 \quad W.$ | $51 \quad 58 \quad 30 \quad N.$      | — $2 \quad 39$ | 16     |
| — 8.  | " Aug. 19th,     | $82 \quad 30 \quad W.$  | $57 \quad 41 \quad 0 \quad S.$       | — $1 \quad 3$  | 22     |
| — 9.  | " Aug. 26th,     | $92 \quad 3 \quad E.$   | $35 \quad 35 \quad 20 \quad N.$      | + $2 \quad 17$ | 12     |
| — 10. | " Sept. 23rd,    | $166 \quad 30 \quad E.$ | $41 \quad 36 \quad 10 \quad S.$      | — $4 \quad 41$ | 17     |
| — 11. | " Oct. 23rd,     | $90 \quad 12 \quad W.$  | $54 \quad 40 \quad 40 \quad S.$      | — $0 \quad 49$ | 18     |
| — 12. | " Nov. 15th,     | $80 \quad 11 \quad E.$  | $67 \quad 43 \quad 0 \quad S.$       | + $1 \quad 38$ | 15     |
| — 13. | " Dec. 10th,     | $55 \quad 20 \quad E.$  | $25 \quad 52 \quad 15 \quad S.$      | + $2 \quad 0$  | 17     |
| — 14. | " Sept. 21st,    | $60 \quad 1 \quad E.$   | $56 \quad 26 \quad 0 \quad N.$       | 0              | 20     |
| — 15. | " March 20th,    | $89 \quad 30 \quad E.$  | $61 \quad 49 \quad 30 \quad S.$      | — $3 \quad 17$ | 15     |
| — 16. | " April 7th,     | $139 \quad 45 \quad W.$ | $89 \quad 55 \quad 50 \quad S.$      | + $5 \quad 10$ | 12     |
| — 17. | " May 16th,      | $45 \quad 26 \quad W.$  | $86 \quad 34 \quad 19 \quad N.$      | + $4 \quad 16$ | 15     |
| — 18. | " Sept. 23rd,    | $90 \quad 45 \quad E.$  | $83 \quad 40 \quad 30 \quad S.$      | 0              | 18     |
| + 19. | " Nov. 3rd,      | $106 \quad 0 \quad E.$  | $70 \quad 29 \quad 45 \quad N.$      | + $1 \quad 22$ | 19     |
| + 20. | " Sept. 22nd,    | $173 \quad 58 \quad W.$ | $71 \quad 19 \quad 20 \quad S.$      | + $3 \quad 40$ | 18 ✕   |
| + 21. | " Feb. 12th,     | $8 \quad 12 \quad W.$   | $29 \quad 55 \quad 20 \quad S.$      | — $1 \quad 10$ | 19     |
| — 22. | " March 20th,    | $77 \quad 45 \quad E.$  | $76 \quad 58 \quad 15 \quad N.$      | — $2 \quad 20$ | 21 ✕   |
| — 23. | 1877, Jan. 1st,  | $125 \quad 32 \quad E.$ | U.L. $54 \quad 57 \quad 20 \quad S.$ | + $2 \quad 10$ | 22     |
| — 24. | 1876, Oct. 1st,  | $71 \quad 20 \quad E.$  | U.L. $82 \quad 0 \quad 15 \quad N.$  | — $3 \quad 15$ | 14     |

## ON AMPLITUDES.

281.—The Correction or Error of Compass is found by comparing the bearing of the sun or other celestial body, as shown by the compass, with the true bearing, as found by calculation.

282.—The True Amplitude is the bearing of a celestial body at rising or setting (*i.e.*, when its centre is on the *rational* horizon), from the *true* East or West point, found by calculation, from the latitude of the place and declination of the body, or taken by inspection from a table, of which these quantities are the arguments (Table XLII, Norie, or LIX, Raper).

283.—The Magnetic Amplitude is the bearing of a celestial body at rising or setting from the compass East or West points, found by direct observation with an instrument fitted with a magnetic needle, as the Azimuth Compass.

The magnetic amplitude is distinguished as *observed*, or *apparent*, and *corrected*. The *observed* or *apparent* magnetic amplitude of a celestial body is its bearing from the compass East or West point, when it appears in the sea-horizon of an observer standing on the deck of a ship. The *corrected* magnetic amplitude is the bearing of the body from the compass East or West point, when on the rational horizon, as it would appear to a spectator at the centre of the sphere through an uniform medium. The diurnal circles of the celestial bodies being, except at the equator, inclined to the horizon, and more and more the higher the latitude; any cause which affects the time of rising will affect the apparent amplitude, and in a greater degree as the latitude increases. The following are the causes:—(1) The elevation of the observer depresses the sea-horizon, while it does not effect the place of the celestial body—hence by reason of the *dip*, the body appears to rise before it is truly on the sensible horizon. (2) The great *refraction* at the horizon causes the body to appear to rise considerably before it comes to the sensible horizon. (3) When a body is in the sensible horizon, to an eye at the centre of the sphere it has already passed the rational horizon. This being the effect of *parallax*, is only of importance in the case of the moon. These corrections will be found in Table 59 A, Raper.

### RULE LXXXIX.

1°. *With the ship date and longitude in time, find the Greenwich date* (see Rule LXXXI, page 222).

The time of sunrise and sunset is generally given in apparent time.

2°. *Take out of Nautical Almanac* (page I) *the sun's declination and correct it for this date* (see Rule LXXXII, page 225).

3°. *Take from the Table the log. sine of declination, and log. secant of latitude* (rejecting 10 from the index); *the sum of these is log. sine of true amplitude, which take out of Tables.* (Table XXV, Norie, or Table LXVIII, Raper).

4°. **To name the True Amplitude.**—*If the body is rising, or A.M., mark true amplitude East; if it is setting, or P.M., mark it West. : mark it also North, when declination is North; or South when declination is South.*

The time of sun rising is always A.M., and of sun setting P.M.

(a) *When the declination is 0, the true amplitude is 0; that is, it is East if the object is rising—West, if it is setting.*

(b) *When the latitude is 0, the true amplitude is of the same amount as the declination.*



5°. **Correction or Error of the Compass for the Position of Ship's Head.**  
*Under the true amplitude write the magnetic amplitude; then—*

(a) *If both amplitudes are North or both South, take their difference.*

(b) *When one is North and the other South, take their sum.*

(c) *If one is reckoned from East and the other from West, take the True Amplitude from  $180^\circ$ , and change the name from East to West or from West to East; the name as to North or South remains unaltered; then, take their difference.*

*The sum or difference (as the case may be) is the entire correction, or error of the compass.*

The magnetic amplitude must be reckoned from East or West towards the North or South, before it is placed underneath the true. Thus: the magnetic amplitude S.E. by E.  $\frac{1}{2}$  E. is E.  $2\frac{1}{2}$  points S., or E.  $28^\circ 7' 30''$  S.

6°. **To name the Error of Compass.**—*The correction is named East when the true amplitude is to the right of magnetic amplitude; West when true is to the left of magnetic: the observer being supposed looking from the centre of the compass, in the direction of the magnetic amplitude.*

NOTE.—The learner will find it very useful to draw a figure, thus:—

Make a rough sketch of the compass by drawing two lines crossing at right-angles, the ends of which will represent the four cardinal points, which mark N., S., E., W., (see Fig., Ex. 1); then to name the error of the compass proceed as follows:—Consider the cardinal point from which the amplitude is reckoned as the origin, and draw two straight lines from the centre to represent the true and magnetic amplitudes, and mark their extremities T and M respectively—taking care to place the line T further from the origin if the true be greater than the observed (or magnetic) amplitude, but nearer the origin if the true is less. The arc between M and T is the error which will be East when T is to the right of M, but West if to the left. It is easily seen whether the error of the compass is the sum or difference of T. and M.

The result as deduced above is generally called the variation, but the effects of the iron in the ship modify the bearing by compass. Every error determined on board ship is compounded of variation proper and deviation, and is the entire correction necessary to be applied to every bearing taken, and course steered, but will vary with the position of the ship's head and the heel of the ship. If the iron of the vessel exercise no influence on the compass, the result obtained is only variation, and ought to agree with that registered on the chart. The deviation is found as follows:—

7°. **To find the Deviation.**—*Under the error of the compass place the variation; then (a). If they are of like names, i.e., are both East or both West, take their difference.*

(b) *But if they have unlike names, i.e., if one is East and the other is West, take the sum.*

*The sum or difference (as the case may be) is the deviation.*

(c) *If the variation is 0, the error of the compass is also the deviation.*

(d) *If the error of the compass is 0, the deviation is of the same amount as the variation.*

8°. **To name the Deviation.**—The observer must suppose himself in the centre of the compass, looking in the direction of the variation,—then the deviation is East when the error of compass is to the right of the variation;

West when the error of compass is to the left of the variation—both the error of the compass and the variation being reckoned from the North point of the compass.

NOTE.—It will be convenient for beginners to draw a figure for the deviation thus:—(See Fig. 2, Example 1.)

Make a rough sketch of the compass; the upper part of the vertical line being taken to represent the origin, which mark N., and mark the extremities of the horizontal line W. and E. respectively. Then from the centre of the compass draw two lines to represent the error of compass and the variation, calling them E and V respectively. The line E must be drawn to the right of N. if the error of compass is E., but to the left of N. if the error be W.; similarly, the line V must be to the right of N. when the variation is E., but to the left of N. if the variation is W. Take care to draw E further from N. than V if the error of compass is greater than the variation, but nearer to N. if the error is the less. The deviation is the distance from V to E, and is East when E is to the right of V, but West when E is to the left of V. It is easily seen whether the deviation is the sum or difference of E and V.

NOTE.—Persons who understand the algebraic signs will find it easier to use them in finding the deviation, which is always the algebraic difference between the error of compass and the variation, and which may be thus expressed,—when of contrary names, add; but when of the same name, subtract.

NOTE.—In the following examples the seconds of declination are rejected. When the seconds are 30, or above, 1 is added to the minutes; but when they are below 30 nothing is added to the minutes.

### EXAMPLES.

Ex. 1. 1876, January 6th, at 4<sup>h</sup> 44<sup>m</sup> 27<sup>s</sup> A.M., apparent time at ship, lat. 37° 59' S., long. 36° 24' W., the sun's magnetic amplitude was S.E. by E.  $\frac{1}{2}$  E.: required the true amplitude and error of compass; and supposing the variation to be 3° 40' E., required the deviation for the position of the ship's head at the time of observation.

|  |  |
|--|--|
| Ship date (A.T.) Jan.                          | 5 <sup>d</sup> 16 <sup>h</sup> 44 <sup>m</sup> 27 <sup>s</sup> |
| Long. in time                                  | + 2 25 36  |
| Green. date (A.T.) Jan.                        | 5 19 10 3  |
| H. diff. noon, Jan. 6th                        | — 17 <sup>m</sup> 71   |
| Time from noon, 4 <sup>h</sup> 50 <sup>m</sup> | × 4 <sup>m</sup> 83  |
|  | 5313   |
|  | 14168  |
|  | 7084   |

6,085,5393

|                  |             |
|------------------|-------------|
| Correction       | + 1 26      |
| Decl. 6th, noon  | 22 32 49 S. |
| Red. declination | 22 34 15 S. |

|               |                 |
|---------------|-----------------|
| Decl. 22° 34' | sine 9.584058   |
| Lat. 37 59    | secant 0.103369 |
|               | sine 9.687427   |

(A.M. and S. decl.) True amp. E. 29° 8' S.

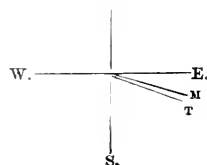
(S.E. by E.  $\frac{1}{2}$  E.) Mag. amp. E. 28 7 $\frac{1}{2}$  S. = E. 2 $\frac{1}{2}$  points.

Error of compass 1 0 $\frac{1}{2}$  E., because true amplitude is to the right of magnetic amplitude.

|                                   |                    |
|-----------------------------------|--------------------|
| Or thus, H.D.                     | 17 <sup>m</sup> 71 |
|                                   | 5 <sup>h</sup>     |
| 10 <sup>m</sup>   $\frac{1}{6}$ h | 88.55              |
|                                   | — 2.95             |
| 6,0                               | 8,5.60             |
|                                   | 1 26               |

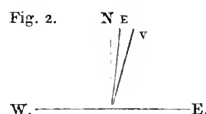
The decl. is here taken for the nearest noon, viz., the 6th, and since the Green. time wants only 4<sup>h</sup> 50<sup>m</sup> of being noon of 6th (24<sup>h</sup> 0<sup>m</sup> — 19<sup>h</sup> 10<sup>m</sup> = 4<sup>h</sup> 50<sup>m</sup>), we multiply the hourly diff. by this quantity, and apply the resulting correction the opposite way to throw it back, for since the declination is decreasing the declination at 4<sup>h</sup> 50<sup>m</sup> before noon will be more than it is at noon, hence we add the correction. Or, multiply by 5<sup>h</sup>, then since 5<sup>h</sup> is 10<sup>m</sup> in excess of 4<sup>h</sup> 50<sup>m</sup>, deducting 1-6th of H.D. from the product above, the result is correction.

Fig. 1. N.



## To find the Deviation.

$$\begin{array}{rcl}
 \text{Error of compass} & + & 1^{\circ} 0\frac{1}{2}' \text{ E.} \\
 \text{Variation by chart} & + & 3 40' \text{ E.} \\
 \hline
 \text{Deviation} & = & 2 39\frac{1}{2}' \text{ W., because} \\
 & & \text{the error of compass is to the left of the variation.}
 \end{array}$$



Make a rough sketch of the compass as in Fig. 1 in the above example. In this example the magnetic amplitude is reckoned from E. towards S. (S.E. by E.  $\frac{1}{2}$  E. = E.  $2\frac{1}{2}$  pts. S. = E.  $28^{\circ} 7\frac{1}{2}'$  S.) To represent this, draw a line from the centre of the compass to a point M, somewhere between E. or S. Again, the true amplitude is reckoned from E. towards S. To represent this, draw a line from the centre of the compass to point T, further from E than M is from E, because the true amplitude is greater than the magnetic amplitude. Then it is evident that the line T, or the true amplitude, is to the *right* of the line M, or the magnetic amplitude. Hence by Rule, 6<sup>o</sup>, the error of the compass is East.

Again, to name the deviation:—Draw a figure (see Fig. 2 above) and mark the end of the vertical line N, to represent the true meridian (or true North point), and the extremities of the horizontal line W and E respectively, to represent West and East. Next, from the centre of the compass draw a line E (see Fig. 2) to the *right* of North, to represent the Error of the Compass, which is E.; and since the variation is also East, draw another line V to the *right* of North, but further from N than E is, because the variation is *greater* than the error. (See Fig. 2.) It is evident that the deviation is the angle included between E and V, and is East because E the error is to the right of V the variation. It is evident too that in this instance the deviation is the difference of E and V.

Ex. 2. 1876, February 16th, at 4<sup>h</sup> 58<sup>m</sup> P.M., apparent time at ship, latitude  $51^{\circ} 9' \text{ N.}$ , longitude  $15^{\circ} \text{ W.}$ , sun's magnetic amplitude W.  $\frac{1}{4} \text{ N.}$ : required the true amplitude and error of the compass; and supposing the variation to be  $28^{\circ} 30' \text{ W.}$ : required the deviation for the position of the ship's head at the time of observation.

Ship date (A.T.), Feb. 16<sup>d</sup> 4<sup>h</sup> 58<sup>m</sup>  
 Long.  $15^{\circ} 0' \text{ W.}$  + 1 0  
 Green. date (A.T.), Feb. 16 5 58  
 H.D. =  $51^{\circ} 86'$   
           6

2 |  $\frac{1}{36}$  | 31116  
       — 1'73  
 6,0 | 30,9'43  
       — 5 9'4

H. diff., noon, Feb. 16th —  $51^{\circ} 86'$   
                                       5'97

36302  
 46674  
 25930

6,030,9'6042

5 9'5

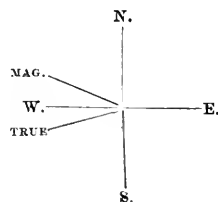
Correction — 5 10  
 Decl., noon, 16th 12 26 48 S.

Red. decl. 12 21 38 S.

Declination  $12^{\circ} 22'$  sine 9'330753  
 Latitude  $51 9$  secant 0'202536  
                                       sine 9'533289

(P.M. and S. decl.) True amp. W.  $19^{\circ} 58' \text{ S.}$   
 (W.  $\frac{1}{4}$  pt. N.) Mag. amp. W. 2 49 N.

Error of compass 22 47 W., the true  
 amplitude being to the left of magnetic.

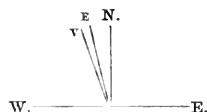


*To find the Deviation.*

Error of compass —  $22^{\circ} 47' W.$   
 Variation —  $28^{\circ} 30' W.$   


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 Deviation +  $5^{\circ} 43' E.$ , because the  
 error is to the *right* of the variation.



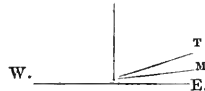
Make a rough sketch of the compass by drawing two lines crossing at right-angles; and since the magnetic amplitude is reckoned from W. and N., draw a line M somewhere between W. and N. to represent it. Again, the true amplitude is reckoned from W. towards S.; draw another line T somewhere between W. and S. to represent the true amplitude. It is easily seen that the error of the compass is the angle included between M and T, *i.e.*, the sum of the true and magnetic amplitudes; and it is evident T, the true amplitude, is to the *left* of the magnetic amplitude, the observer being supposed looking from the centre of the compass in the direction of magnetic amplitude; whence, according to Rule, 6<sup>o</sup>, the error of the compass is marked West.

*To name the Deviation.*—Draw another compass, and taking N. as the origin, and to represent the error of compass, draw a line E from the centre of the compass, but to the left of N., because the error is West. Again, the variation also being West, draw another line V to the left of N., but further than E is from N., because the variation is greater than error. It is easily seen that, in this instance, the deviation is the difference of V and E, and the deviation is named East, because the error is to the right of the variation; the observer being supposed looking from the centre of the compass, in the direction of the variation.

Ex. 3. 1876, April 13th, at  $5^h 47^m 20^s$  A.M., apparent time at ship, latitude  $20^{\circ} 2' N.$ , longitude  $107^{\circ} 56' E.$ , sun's magnetic amplitude  $E. \frac{1}{4} N.$ , variation  $1^{\circ} 40' E.$

|   |                       |                            |                      |
|---|-----------------------|----------------------------|----------------------|
| Ship date, (A.T.) April                 | $12^d 17^h 47^m 20^s$ | H. diff., April 12th, noon | + $54^m 48^s$        |
| Long. $107^{\circ} 56' E.$              | — $7^h 11^m 44^s$     |                            | $10^h 6^m$           |
| Green. date, (A.T.) April 12th          | $10^d 35^h 36^m$      |                            | $32688$              |
|   |                       |                            | $54480$              |
| Declination $9^{\circ} 42' \frac{1}{2}$ | sine                  | $9^{\circ} 167907$         |                      |
| Latitude $20^{\circ} 2'$                | secant                | $0^{\circ} 027106$         | $577^{\circ} 488$    |
|   |                       |                            | $9^{\circ} 37' 5$    |
|   | sine                  | $9^{\circ} 225013$         |                      |
| (A.M. and N. decl.) True amp.           | E. $9^{\circ} 40' N.$ | Correction                 | + $9' 37''$          |
| (E. $\frac{1}{4}$ point N.) Mag. amp.   | E. $2^{\circ} 49' N.$ | Decl. 12th noon            | $8^{\circ} 54' 55''$ |
|   |                       | Red. decl.                 | $9^{\circ} 4' 32''$  |

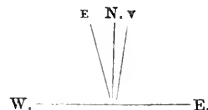
Error of compass  $6^{\circ} 51' W.$  the true  
 amplitude being to the *left* of magnetic.

*To find the Deviation.*

Error of compass  $6^{\circ} 51' W.$   
 Variation  $1^{\circ} 40' E.$   


---

 Deviation  $8^{\circ} 31' W.$   
 the error is to the *left* of the variation.



Ex. 4. 1876, June 10th, at  $4^h 45^m$  P.M., apparent time at ship, latitude  $36^{\circ} 42' S.$ , longitude  $120^{\circ} 30' E.$ , magnetic amplitude W.  $29^{\circ} 15' N.$ , variation  $7^{\circ} 20' W.$ : required the deviation for the position of the ship's head at the time of observation.

|                                  |  |  |                    |
|----------------------------------|--|--|--------------------|
| Ship date (A.T.), June           | 10 <sup>d</sup> 4 <sup>h</sup> 45 <sup>m</sup> | H. diff., noon, June 10th, +                   | 10 <sup>m</sup> 90 |
| or June                          | 9 28 45  | T. from noon, 3 <sup>h</sup> 17 <sup>m</sup> = | 3 <sup>h</sup> 3   |
| Long. 120° 30' E.                | — 8 2  |  | 3270               |
|                                  |  |  | 3270               |
| Green. date (A.T.), June         | 9 20 43  |  | 35 970             |
| Time from noon                   | June 10 3 17                                   |  |                    |
| Declination 23° 4'               | sine 9.593067                                  | Correction                                     | — 0' 36"           |
| Latitude 36 42                   | secant 0.95947                                 | Decl., 10th, noon                              | 23° 4 16 N.        |
|                                  | sine 9.689014                                  | Red. decl.                                     | 23 3 40 N.         |
| (P.M. and N. decl.) True amp. W. | 29° 15' N.                                     |  |                    |
| Mag. amp. W.                     | 29 15 N.                                       |  |                    |
| Error of compass                 | 0 0  |  |                    |
| Variation                        | 7 20 W.  |  |                    |
| Deviation                        | 7 20 E., because the error is                  |  |                    |
|                                  | to the right of the variation.                 |  |                    |

In this instance the error of compass is 0, and the deviation is equal in amount to the variation, but of an *opposite name*.

Ex. 5. 1876, July 31st, at 4<sup>h</sup> 26<sup>m</sup> A.M., apparent time at ship, latitude 46° 3' N., longitude 165° 58' W., sun's magnetic amplitude N.E. by E., variation 13° 0' W., ship's head E. by N.

|                                  |   |                                  |                        |
|----------------------------------|---|----------------------------------|------------------------|
| Ship date, (A.T.)                | July 30 <sup>d</sup> 16 <sup>h</sup> 26 <sup>m</sup> 0 <sup>s</sup> | H. diff., July 31st, noon        | 37 <sup>m</sup> 46     |
| Long. in time                    | + 11 52   | 3 <sup>h</sup> 30 <sup>m</sup> = | 3 5                    |
| Green. date,                     | July 31 <sup>d</sup> , 3 20 52                                      |                                  | 18730                  |
|                                  | or 3 <sup>h</sup> 5 <sup>h</sup>                                    |                                  | 11238                  |
| Declination 18° 6'               | sine 9.492308   |                                  | 13,1110                |
| Latitude 46 3                    | secant 0.158622   | Correction                       | — 2' 11"               |
|                                  | sine 9.650930   | Decl. 31st noon                  | 18° 8 19 N. <i>der</i> |
| (A.M. and N. decl.) True amp. E. | 26° 36' N.  | Red. decl.                       | 18 6 8 N.              |
| (E. 2½ pts. N.) Mag. amp. E.     | 30 46 N.  |                                  |                        |
| Error of compass                 | + 4 20 E., the true amplitude being to the right of                 |                                  |                        |
| Variation                        | — 13 0 W. the magnetic.   |                                  |                        |
| Deviation                        | + 17 20 E., because the error is                                    |                                  |                        |
|                                  | to the right of variation.  |                                  |                        |

Ex. 6. 1876, Sept. 22nd, at 6<sup>h</sup> 0<sup>m</sup> P.M., apparent time at ship, latitude 24° 40' S., longitude 13° 30' E., sun's magnetic amplitude W. 2° 50' N., variation 10° 40' W.

|                         |  |                               |                    |
|-------------------------|--|-------------------------------|--------------------|
| Ship date, Sept.        | 22 <sup>d</sup> 6 <sup>h</sup> 0 <sup>m</sup> 0 <sup>s</sup> | H. diff., noon, Sept. 22nd, — | 58 <sup>m</sup> 50 |
| Long. 13° 30' in time   | — 54 0   |                               | 5 1                |
| Green. date, Sept. 22nd | 5 6 0  |                               | 5850               |
|                         | or, 5 <sup>h</sup> 1 <sup>h</sup>                            |                               | 29250              |
|                         |  |                               | 6,029,8350         |
|                         |  | Correction                    | — 4 58             |
|                         |  | Decl., 22nd noon              | 0 4 58 N.          |
|                         |  | Red. decl.                    | 0 0 0              |

The decl. being 0° the true amplitude is 0°, or W. 0° 0', whence the error of compass is 2° 50' W., because the *true* amplitude is to *left* of magnetic.

To find the Deviation.

Error of compass —  $2^{\circ} 50'$  W.  
Variation —  $10^{\circ} 40'$  W.

Deviation  $+ 7^{\circ} 50'$  E., because the error of compass  
is to the *right* of variation.

Ex. 7. 1876, December 10th, at  $8^h 27^m$  A.M., apparent time at ship, latitude  $54^{\circ} 35'$  N., longitude  $53^{\circ} 15'$  W., sun's magnetic amplitude S.E.  $\frac{1}{2}$  E., variation  $36^{\circ} 20'$  W., ship's head S.W. by W.

Green. date, Dec.  $9^d 24^h 0^m 0^s$

or Dec.  $10^{\circ} 0' 0'' 0'''$

Decl. at noon, Dec. 10th,  $22^{\circ} 59' 18''$  S.

The Green. date being noon, Dec. 10th, one of the instants for which the declination is put down in the Almanac, nothing more is necessary than to transcribe the quantity as there put down.

|             |                  |        |            |
|-------------|------------------|--------|------------|
| Declination | $22^{\circ} 59'$ | sine   | $9.591580$ |
| Latitude    | $54^{\circ} 35'$ | secant | $0.236933$ |
|             |                  | sine   | $9.828513$ |

(A.M. and S. decl.) True amp. E.  $42^{\circ} 22'$  S.  
(E.  $3\frac{1}{2}$  pts. S.) Mag. amp. E.  $39^{\circ} 22'$  S.

Error of compass  $+ 3^{\circ} 0'$  E., the true amplitude being to the  
Variation —  $36^{\circ} 20'$  W. *right* of magnetic.

Deviation  $+ 39^{\circ} 20'$  E., because the error is to the *right*  
of variation.

Ex. 8. 1876, December 20th, at  $4^h 31^m$  P.M., apparent time at ship, latitude  $41^{\circ} 12'$  N., longitude  $110^{\circ} 45'$  E., sun's setting amplitude S.W.  $\frac{1}{4}$  W., variation 0.

Green. date, Dec.  $19^d 21^h 8^m$

Declination  $23^{\circ} 27'$  sine  $9.599827$   
Latitude  $41^{\circ} 12'$  secant  $0.123543$

sine  $9.723370$

Decl. noon, Dec. 20th,  $23^{\circ} 27' 15''$  S., *incr.*

H. diff., noon, 20th,  $+ 1''.13 \times$  time  
from noon,  $2^h 52^m (= 2^h.87) = 3'.2431$   
 $=$  corr.  $- 3''$ ; Red. decl.  $23^{\circ} 27' 12''$ .

(P.M. and S. decl.) True amp. W.  $31^{\circ} 56'$  S.  
(W.  $3\frac{3}{4}$  pts. S.) Mag. amp. W.  $42^{\circ} 11'$  S.

Error of compass  $+ 10^{\circ} 15'$  E., the *true* amplitude being to the  
Variation  $+ 0$  *right* of magnetic.

Deviation  $10^{\circ} 15'$  E.

The Variation being 0, the error of the compass is also the deviation.

Ex. 9. 1876, November 15th, at  $6^h 45^m$  P.M., apparent time at ship, latitude  $31^{\circ} 56'$  N., longitude  $75^{\circ} 30'$  W., sun's setting amplitude W. by S.  $\frac{3}{4}$  S., variation  $6^{\circ} 30'$  W., ship's head N.N.E.

Green. date, November  $15^d 11^h 47^m$   
Declination  $18^{\circ} 47'$  sine  $9.507843$   
Latitude  $31^{\circ} 56'$  secant  $0.071264$

sine  $9.579107$

H. diff. noon, 15th  $+ 37''.83 \times$  time from  
noon  $11^h 47^m (= 11^h.8) = 446''.394 =$  corr.  
 $+ 7''.26$ ; Red. decl.  $18^{\circ} 47' 14''$  S.

(P.M. and S. decl.) True amplitude W.  $22^{\circ} 18'$  S.  
(W.  $1\frac{3}{4}$  pts. S.) Mag. amplitude W.  $19^{\circ} 41'$  S.  $=$  W. by S.  $\frac{3}{4}$  S.

Error of compass —  $2^{\circ} 37'$  W. the *true* amplitude being to *left*  
Variation —  $6^{\circ} 30'$  W. *of* magnetic.

Deviation  $+ 3^{\circ} 53'$  E. the error being to the *right* of  
[variation.]

Ex. 10. 1876, June 19th, at 9<sup>h</sup> 40<sup>m</sup> P.M., apparent time at ship, lat. 62° 31' N., long. 60° 24' W., sun's magnetic amplitude, N.N.E.; and supposing the variation of the compass is 57° 50' W., required the deviation for the position of the ship's head at the time the observation was taken.

|                              |                      |   |                       |                                   |
|------------------------------|----------------------|---|-----------------------|-----------------------------------|
| Ship date (A.T.),            | June 19 <sup>d</sup> | 9 <sup>h</sup> 40 <sup>m</sup> 0 <sup>s</sup> | H. diff., 19th        | 1 <sup>m</sup> 66                 |
| Long. (60° 24' W.) in time + | 4                    | 1   | T. from noon          | × 13 <sup>m</sup> 7               |
| Green. date (A.T.) June 19   | 13                   | 41  | Corr. of decl.        | 22 <sup>m</sup> 74 <sup>s</sup> 2 |
| Declination                  | 23° 27'              | 13 <sup>h</sup> 7 <sup>m</sup> sine           | Decl. June 19th, noon | 23° 26' 56"                       |
| Latitude                     | 62 31                | secant  | corr.                 | 23                                |
|                              |                      | sine  | Red. decl.            | 23 27 19                          |
|                              |                      |   |                       |                                   |

(P.M. and N. decl.) True amplitude W. 59° 35' S.  
180 0

(E. 6 points N.) Mag. amplitude E. 120 25 N.  
E. 67 30 N. = N.N.E.

|                  |   |
|------------------|---|
| Error of compass | 52 55 W., because <i>true</i> amplitude is to the <i>left</i> |
| Variation        | 57 50 W. of mag. amplitude.                                   |
| Deviation        | 4 55 E., because error is to the <i>right</i> of variation.   |

Before comparing the true and magnetic amplitudes, they must both be reckoned from the same point of the compass, E. or W., but in this instance one is reckoned from W. and the other from E.; therefore, by taking either of them from 180°, they would both be reckoned from the same point—the true amplitude, in this example, is taken from 180°, and it is then reckoned from E. instead of W. Next take the difference of the amplitudes, as they are both marked N.; and since the true amplitude is to the *left* of the magnetic—looking from the centre of the compass in the direction of the magnetic—the error of compass is W. The error of compass and variation being of the same name, take their difference for the deviation, which mark E, because the error of the compass is to the right of variation, looking from the centre of the compass in the direction of the variation.

Ex. 11. 1876, July 20th, at 7<sup>h</sup> 0<sup>m</sup> P.M., apparent time at ship, lat. 34° 51' S., long. 172° 28' E., sun's magnetic amplitude W.  $\frac{1}{4}$  N., variation 8° 30' E.

|                                   |  |   |                                       |
|-----------------------------------|--|---|---------------------------------------|
| Green. date, July 19 <sup>d</sup> | 19 <sup>h</sup> 30 <sup>m</sup> 8 <sup>s</sup> | H. diff. noon, 20th —                               | 28 <sup>m</sup> 63 × time from noon   |
| Declination                       | 20° 36 $\frac{1}{2}$ ' sine                    | 4 <sup>h</sup> 30 <sup>m</sup> (4 <sup>h</sup> 5) = | 128 <sup>m</sup> 835 = corr. + 2' 9"; |
| Latitude                          | 34 51 secant                                   | 0 <sup>o</sup> 08 <sup>m</sup> 58 <sup>s</sup> 42   | Red. decl. 20° 36' 24" N.             |
|                                   | sine   | 9 <sup>o</sup> 63 <sup>m</sup> 2357                 |                                       |

(P.M. and N. decl.) True amplitude W. 25° 24' N.  
(W  $\frac{1}{4}$  N.) Mag. amplitude W. 8 26 N.

|                  |   |
|------------------|---|
| Error of Compass | + 16 58 E., the <i>true</i> amplitude being to                |
| Variation        | + 8 30 E. [the <i>right</i> of the <i>magnetic</i> .          |
| Deviation        | + 8 28 E., because error is to the <i>right</i> of variation. |

Ex. 12. 1876, March 24<sup>d</sup> 5<sup>h</sup> 58<sup>m</sup> P.M. apparent time at ship, latitude 22° 15' S., longitude 179° 12' W., sun's magnetic amplitude S.W. by W.  $\frac{1}{4}$  W. variation 9° 40' E.

The Green. date is March 24<sup>d</sup> 17<sup>h</sup> 54<sup>m</sup> 48<sup>s</sup>. Then 24<sup>h</sup> — 17<sup>h</sup> 55<sup>m</sup> = 6<sup>h</sup> 5<sup>m</sup>, or 6<sup>h</sup> 1 nearly, the time from noon, March 25th.

The decl. noon, March 25th is 2° 4' 4" N., increasing; H. diff., 25th, noon 58<sup>m</sup> 88 × 6<sup>h</sup> 1 = 359<sup>m</sup> 168, or 5<sup>h</sup> 59<sup>m</sup> subtractive; the decl. increasing, will be less 6<sup>h</sup> 5<sup>m</sup> before noon than at noon. Red. decl. 1° 58' 5" N.

|                             |        |            |
|-----------------------------|--------|------------|
| Declination $1^{\circ} 58'$ | sine   | $8.535523$ |
| Latitude $22\ 15$           | secant | $0.033605$ |
|                             | sine   | $8.569128$ |

(P.M. and N. decl.) True amp. W.  $2^{\circ} 7\frac{1}{2}'$  N.  
 (W.  $2\frac{1}{4}$  pts. S.) Mag. amp. W.  $25\ 19$  S.

Corr. of compass  $+ 27\ 26\frac{1}{2}$  E.  
 Variation  $+ 9\ 40$  E.

Deviation  $+ 17\ 46\frac{1}{2}$  E.

Ex. 13. 1876, July 1st, at  $8^h\ 36^m$  P.M., lat.  $56^{\circ} 4' N.$ , long.  $64^{\circ} 50' W.$ , sun's magnetic amplitude North, variation  $36^{\circ} 0' W.$

Green. date, July  $1^d\ 12^h\ 55^m\ 20^s$   
 or,  $12^h\ 92$

Decl. Page I, N.A. July 1st, at noon,  
 $23^{\circ} 5' 12'' .5 N.$  decr., H. D.  $10'' .66$ : H. D.  
 $10'' .66 \times 12.92$  gives correction  $- 2' 17'' .7$ ,  
 whence *Red. Decl.* is  $23^{\circ} 2' 54'' .8 S.$

Declination  $23^{\circ} 3'$  sine  $9.592770$   
 Latitude  $56\ 4$  sec.  $0.253188$

sine  $9.845958$

(P.M. and N. decl.) True amplitude W.  $44^{\circ} 32' N.$   
 (N., or W. 8 pts. N.) Mag. amplitude W.  $90\ 0$  N. (8 pts. =  $90^{\circ}$ )

Error of compass  $- 45\ 28$  W.  
 Variation  $- 36\ 0$  W.

Deviation  $- 9\ 28$  W.

#### EXAMPLES FOR PRACTICE.

In each of the following examples the Error of Compass and Deviation are required for the position of the ship's head at the time of observation.

| No.          | Civil date.    | App. time.   | Latitude.    | Longitude.    | Sun's Mag. Amp.           | Variation.   |
|--------------|----------------|--------------|--------------|---------------|---------------------------|--------------|
| <b>1876.</b> |                |              |              |               |                           |              |
| 1            | Jan. 27th....  | 6 55 40 A.M. | $35\ 42\ N.$ | $12\ 52\ W.$  | S.E. by S.                | $21\ 50\ W.$ |
| 2            | Feb. 17th....  | 6 48 0 P.M.  | $34\ 57\ N.$ | $40\ 8\ E.$   | S.W. by W.                | $7\ 40\ E.$  |
| 3            | March 29th ..  | 5 50 0 A.M.  | $25\ 50\ S.$ | $127\ 35\ W.$ | E.S.E.                    | $23\ 40\ W.$ |
| 4            | April 5th .... | 6 15 0 P.M.  | $20\ 20\ S.$ | $155\ 30\ E.$ | W. $6^{\circ} 40' N.$     | $6\ 40\ E.$  |
| 5            | Nov. 7th ....  | 5 25 0 A.M.  | $27\ 41\ S.$ | $70\ 2\ W.$   | E. $\frac{1}{2} N.$       | $13\ 50\ E.$ |
| 6            | May 26th ....  | 7 56 0 A.M.  | $51\ 22\ S.$ | $48\ 0\ E.$   | E. $\frac{3}{4} S.$       | $35\ 20\ W.$ |
| 7            | June 2nd ....  | 8 8 2 P.M.   | $52\ 30\ N.$ | $27\ 6\ W.$   | N.N.W. $\frac{1}{4} W.$   | $37\ 20\ W.$ |
| 8            | July 14th .... | 6 50 58 A.M. | $28\ 59\ S.$ | $111\ 11\ W.$ | N.E. $\frac{1}{4} N.$     | $11\ 40\ E.$ |
| 9            | Aug. 27th ..   | 5 44 0 P.M.  | $21\ 4\ S.$  | $36\ 19\ E.$  | N.W. $\frac{3}{4} W.$     | $23\ 10\ W.$ |
| 10           | Sept. 8th .... | 5 47 0 A.M.  | $24\ 22\ N.$ | $57\ 30\ W.$  | E.                        | $0\ 0$       |
| 11           | Oct. 1st ....  | 5 48 50 A.M. | $42\ 44\ S.$ | $175\ 15\ W.$ | E. $\frac{3}{4} N.$       | $18\ 50\ E.$ |
| 12           | Sept. 23rd ..  | 6 0 0 A.M.   | $56\ 41\ S.$ | $179\ 42\ E.$ | E. $\frac{1}{4} S.$       | $11\ 0\ E.$  |
| 13           | Nov. 3rd ....  | 6 34 0 P.M.  | $29\ 20\ S.$ | $136\ 35\ E.$ | W.S.W.                    | $2\ 50\ W.$  |
| 14           | Dec. 4th ....  | 7 56 48 P.M. | $49\ 59\ S.$ | $160\ 45\ E.$ | S.W. by W.                | $16\ 0\ E.$  |
| 15           | March 20th ..  | 6 0 0 P.M.   | $55\ 10\ N.$ | $179\ 24\ E.$ | W. $\frac{1}{2} N.$       | $15\ 0\ E.$  |
| 16           | Sept. 22nd ..  | 6 0 0 P.M.   | $60\ 1\ S.$  | $13\ 54\ E.$  | West.                     | $21\ 50\ W.$ |
| 17           | June 9th ....  | 6 0 0 A.M.   | $0\ 0$       | $10\ 21\ W.$  | E. $\frac{1}{2} N.$       | $20\ 15\ W.$ |
| 18           | Feb. 26th .... | 7 49 0 A.M.  | $62\ 5\ N.$  | $12\ 52\ W.$  | S.S.E.                    | $35\ 45\ W.$ |
| 19           | April 30th ..  | 6 28 12 P.M. | $24\ 58\ N.$ | $138\ 52\ W.$ | W. by N. $\frac{1}{2} N.$ | $10\ 0\ E.$  |
| 20           | May 27th ....  | 7 40 0 P.M.  | $47\ 40\ N.$ | $148\ 3\ W.$  | W. by N.                  | $20\ 15\ E.$ |
| 21           | June 18th ..   | 1 47 0 A.M.  | $63\ 54\ N.$ | $174\ 20\ W.$ | N. by W. $\frac{1}{4} W.$ | $25\ 0\ E.$  |
| 22           | March 6th ..   | 6 14 0 P.M.  | $31\ 24\ S.$ | $2\ 10\ E.$   | W. $16^{\circ} 52' N.$    | $17\ 50\ W.$ |
| 23           | April 10th ..  | 6 45 0 P.M.  | $53\ 58\ N.$ | $178\ 33\ E.$ | W. $\frac{3}{4} S.$       | $16\ 10\ E.$ |
| 24           | Dec. 14th....  | 4 35 0 A.M.  | $42\ 0\ S.$  | $74\ 56\ E.$  | South.                    | $19\ 20\ W.$ |



## ON FINDING THE TIME OF HIGH WATER.

### “BY THE ADMIRALTY TIDE TABLES.”

284. These Tide Tables, published annually, give the *time* (A.M. and P.M.) of high water, and the *height* for every day in the year, at the following places, viz.:—Brest, Devonport, Portsmouth, Dover, Sheerness, London, Harwich, Hull, Sunderland, North Shields, Leith, Thurso, Greenock, Liverpool, Pembroke, Weston-super-mare, Holyhead, Kingston, Belfast, Londonderry, Sligo Bay, Galway, Queenstown, and Waterford.

285. To find the times of high water from the Tide Tables if the place is one of the Standard Ports, proceed by

#### RULE XC.

*Turn to the month in the Tide Tables and find the given place; then opposite the given date will stand the morning (A.M.) and afternoon (P.M.) times of high water required.*

NOTE.—When the mark — occurs it shows that there is but one tide during that day; no high water, therefore, takes place in the morning or afternoon in which the mark appears.

Thus, wishing to know the time of high water at North Shields on the 7th of February, 1875—on turning to February under the head of North Shields (see page 13), it is seen at a glance that high water takes place at 4<sup>h</sup> 8<sup>m</sup> A.M., and that the height of tide is 12ft. 10in. above the mean low water level of spring tides, and that the time of high water on the afternoon of same day is 4<sup>h</sup> 27<sup>m</sup>, while the height of tide above the low water level of spring tides is 13ft. 2in. Similarly, desiring to know the particulars of the tide at Brest on the morning of March 3rd, 1875 (see page 18), the mark — shows that no tide occurs in the morning of that day; there will be a high water at 11<sup>h</sup> 41<sup>m</sup> P.M. on the 2nd, and again at 0<sup>h</sup> 27<sup>m</sup> P.M. (i.e., 27<sup>m</sup> past noon) of the 3rd, but none in the interval.

Again, if it be required to know the times of high water on May 1st, 1875, at Weston-super-mare—on turning to May, and under Weston-super-mare (see page 39), and opposite the 1st we find that the times of high water are 2<sup>h</sup> 24<sup>m</sup> A.M., and 2<sup>h</sup> 57<sup>m</sup> P.M. respectively.

286 If the place at which the time of high water is required be not a standard port, it is to be referred (if in the west of Europe) to a **standard port**, by adding or subtracting a certain constant to the time of that standard port, as directed in the Tables.

In pages 103 to 108 of the Admiralty Tables, 1875, will be found upwards of two hundred ports on the coasts of the United Kingdom, and in Europe, for which standard ports of reference are given, and the time which is to be added to or subtracted from the time of high water at such standard port.

287. To find the times of high water by the Tidal Constants.

#### RULE XCI.

1°. *Seek in the “Tide Tables,” pages 104—108, in the left hand column for the given place, and in the column headed “Standard Port of Reference” will be found the Standard Port for the given place; also, from the column headed “Time,” and opposite the given place, take out the “Constant,” being careful to note whether it is additive (marked +), or subtractive (marked —).*

2°. Take out of "*Admiralty Tide Tables*," pages 1—97, the morning (A.M.) and afternoon (P.M.) times of high water at the "Standard Port of Reference," being careful to annex the letters A.M. or P.M. to the tides so taken out.

(a) If a blank (—) occurs in either morning (A.M.) or afternoon (P.M.) column, use the preceding tide instead when the Constant is marked additive (+), but use the tide following the blank (—) when the difference is marked subtractive (—).

3°. To the times of high water at the Standard Port just taken out, apply the Constant (No. 2°), adding or subtracting said constant according as it marked + or —; the result in each case, if less than 12<sup>h</sup>, is respectively the morning (A.M.) and afternoon (P.M.) times of high water required.

(a) When the sum of the Constant and the morning (A.M.) time of high water at the Standard Port exceeds 12<sup>h</sup>, deduct 12<sup>h</sup>, the remainder is the afternoon (P.M.) time of high water at the given place. To obtain the morning (A.M.) time of high water at a given place, if any, add the Constant to the preceding afternoon (P.M.) time of high water at the Standard Port, and if the sum exceeds 12<sup>h</sup>, deduct 12<sup>h</sup>, the remainder is the morning (A.M.) tide sought, but if the sum be less than 12<sup>h</sup>, it is the afternoon (P.M.) tide of the day before, and there is no morning (A.M.) tide that day at the given place.

(b) When the Constant added to the morning (A.M.) tide at the Standard Port is less than 12<sup>h</sup> (i.e., gives morning (A.M.) tide at given place); but when added to the afternoon (P.M.) tide at the Standard Port is greater than 12<sup>h</sup>, there is only a morning (A.M.) tide at the given place on that day.

NOTE.—When the sum of the constant and the tide taken from the Tables is less than 12<sup>h</sup>, it remains a tide of the same name as that used, but when the sum exceeds 12<sup>h</sup>, the time over 12<sup>h</sup> will be a tide of the name following that taken out.

(c) When the Constant is subtractive, and exceeds the morning (A.M.) tide at the Standard Port, reject this last and use the following afternoon (P.M.) tide at the Standard Port. If the subtractive Constant exceeds the afternoon (P.M.) tide at Standard Port, 12<sup>h</sup> must be added to this last before subtraction is made; the remainder will be the morning (A.M.) tide at the given place. For the afternoon (P.M.) tide use the following tide at Standard Port, that is, the morning tide of next day, borrowing 12<sup>h</sup> if Constant exceeds it; the remainder is afternoon (P.M.) tide at the given place.

(d) If Constant being subtractive, exceeds the Standard morning (A.M.) tide, but is less than the Standard afternoon (P.M.) tide, there is only an afternoon (P.M.) tide at the given place on that day.

(e) If when the Constant is subtractive, the Standard afternoon (P.M.) tide has to be increased 12<sup>h</sup>, but Constant is less than the Standard morning (A.M.) tide following; there is only a morning (A.M.) tide at the given place that day.

#### EXAMPLES.

Ex. 1. 1875, January 3rd: find the times of high water A.M. and P.M. at the Needles Point.

Turning to the "*Admiralty Tide Table*" for 1875, at page 107, in the left hand column, we find Needles Point, and in the right hand column, immediately abreast, we find that the Standard Port of Reference which in this instance is Portsmouth, and in the column under Time we have the Constant — 1<sup>h</sup> 55<sup>m</sup>, that is, we have to subtract 1<sup>h</sup> 55<sup>m</sup> from the time of high water at Portsmouth on any day in order to obtain the corresponding time of high water at Needles Point. The work will stand as follows:—

|                              |                                    |                                     |
|------------------------------|------------------------------------|-------------------------------------|
| Port of reference—Portsmouth | 8 <sup>h</sup> 1 <sup>m</sup> A.M. | 8 <sup>h</sup> 34 <sup>m</sup> P.M. |
| Constant for Needles         | — 1 55                             | — 1 55                              |
| Time H.W. Needles, Jan. 3rd  | 6 6 A.M.                           | 6 39 P.M.                           |

Ex. 2. 1875, Feb. 12th: find times of high water A.M. and P.M. at Bordeaux.

Turning to page 107, Admiralty Tide Tables, it is seen that the Port of Reference for Bordeaux is Brest, and the constant is + 3<sup>h</sup> 3<sup>m</sup>, that is, the Bordeaux tides are 3<sup>h</sup> 3<sup>m</sup> later than the Brest tides, and consequently 3<sup>h</sup> 3<sup>m</sup> must be added to the time of high water at Brest on any day, to obtain the corresponding time of high water at Bordeaux.

|                                     |                                     |                                     |
|-------------------------------------|-------------------------------------|-------------------------------------|
| Port of reference—Brest, Feb. 12th, | 7 <sup>h</sup> 47 <sup>m</sup> A.M. | 8 <sup>h</sup> 10 <sup>m</sup> P.M. |
| Constant for Bordeaux               | + 3 3                               | + 3 3                               |
| Times H.W. Bordeaux                 | 10 50 A.M.                          | 11 13 P.M.                          |

It may be here remarked, that on adding a *constant* to the standard, a morning tide frequently becomes an afternoon tide, and an afternoon tide may become a morning tide *for the next day*. (See 3° (a) of Rule.)

Ex. 3. 1875, March 16th: find times of high water, A.M. and P.M. at Cherbourg.

The Standard Port of Reference for Cherbourg (see page 108, Admiralty Tide Tables) is Brest, and the Constant is + 4<sup>h</sup> 2<sup>m</sup>, that is, for the times of high water at Cherbourg, we must always add 4<sup>h</sup> 2<sup>m</sup> to the times of high water at Brest.

In this instance, high water at Brest, March 16th, occurs at 11<sup>h</sup> 0<sup>m</sup> A.M. (*i.e.*, 51<sup>m</sup> before noon); consequently 4<sup>h</sup> 2<sup>m</sup> (the Cherbourg constant) added to that time must evidently give a P.M. tide at Cherbourg; the A.M. high water at Cherbourg must, therefore, be sought from the previous (P.M.) tide at Brest, thus:—

|                                   |                                     |                                      |
|-----------------------------------|-------------------------------------|--------------------------------------|
| Port of reference—Brest, H.W.,    | 11 <sup>h</sup> 9 <sup>m</sup> A.M. | 10 <sup>h</sup> 14 <sup>m</sup> P.M. |
| Constant for Cherbourg            | + 4 2                               | + 4 2                                |
|                                   | 15 11                               | 14 16                                |
|                                   | — 12                                | — 12                                 |
| Times H.W. Cherbourg, March 16th, | 3 11 P.M.                           | 2 16 A.M.                            |

If the morning tide, by adding a Constant, becomes an afternoon tide, and the afternoon tide of the day before *remain less than 12<sup>h</sup>* when the Constant is added there is *no morning high water* at the required port thus:—

Ex. 4. 1875, April 19th: find A.M. and P.M. tides at Flushing.

The Standard Port of Reference in this case is Dover, and the Constant + 1<sup>h</sup> 42<sup>m</sup>.

In this case it is high water at Dover, April 19th, at 10<sup>h</sup> 21<sup>m</sup> A.M. (*i.e.*, 1<sup>h</sup> 39<sup>m</sup> before noon), and the Constant 1<sup>h</sup> 42<sup>m</sup> added to that will evidently give a P.M. tide at Flushing. The preceding time of high water at Dover *i.e.*, the time of high water in the afternoon (P.M.) of the previous day must be employed to obtain the morning (or A.M.) tide at Flushing—if any. In this example it will be seen that when the *additive* constant is applied to the preceding afternoon tide at Dover, the sum is less than 12<sup>h</sup>, consequently, the tide does not flow *past midnight*—the result being P.M. tide of April 18th. There is, therefore, no A.M. tide on the 19th of April at Flushing.

|                                |                                      |  |
|--------------------------------|--------------------------------------|--|
| Time H.W. Dover, April 19th    | 10 <sup>h</sup> 21 <sup>m</sup> A.M. | April 18th 10 <sup>h</sup> 4 <sup>m</sup> P.M. |
| Constant                       | + 1 42                               | + 1 42   |
|                                | 12 3                                 | April 18th 11 46 P.M.                          |
|                                | 12                                   |  |
| Time H.W. Flushing, April 19th | 0 3 P.M.                             | (No A.M. tide.)                                |

When the constant is subtractive, the morning tide at the Standard Port frequently becomes an afternoon tide of the day before, and the afternoon tide of the given day becomes a morning tide, in which case the morning tide of the succeeding day must be employed to find the afternoon tide at the given port, as in the example following:—

Ex. 5. 1875, May 11th: find A.M. and P.M. tides at Portland Breakwater.

In this case the Standard Port of Reference is Portsmouth, and the first tide at Portsmouth occurs at 3<sup>h</sup> 30<sup>m</sup> A.M. (i.e., 3<sup>h</sup> 30<sup>m</sup> after midnight), consequently, since Portland Constant shows that high water occurs there 4<sup>h</sup> 40<sup>m</sup> earlier than at Portsmouth, and since that quantity, subtracted from May 11th, 3<sup>h</sup> 30<sup>m</sup> A.M., would give a P.M. tide of the 10th at Portland; we therefore use the Portsmouth tide of the 11th P.M., and of the 12th A.M. thus:—

|                                |                                     |          |                                     |
|--------------------------------|-------------------------------------|----------|-------------------------------------|
| Time H.W. Portsmouth, May 11th | 3 <sup>h</sup> 58 <sup>m</sup> P.M. | May 12th | 4 <sup>h</sup> 30 <sup>m</sup> A.M. |
|                                | + 12                                |          | + 12                                |
|                                | 15 58                               |          | 16 30                               |
| Constant for Portland          | — 4 40                              |          | — 4 40                              |

Time H.W. Portland B'kwater, May 11th 11 18 A.M. 11 50 P.M.

Ex. 6. 1875, June 28th: find A.M. and P.M. tides at Falmouth.

The Standard Port of Reference is Devonport, and the Constant is — 0<sup>h</sup> 46<sup>m</sup>. A blank (—) occurs in the morning column of the 28th, we therefore use the next tide (as the constant is *subtractive*), viz., the P.M. tide, 12<sup>h</sup> being added to make the subtraction, thus:—

|                                |                                     |                       |                                     |
|--------------------------------|-------------------------------------|-----------------------|-------------------------------------|
| Time H.W. Devonport, June 28th | 0 <sup>h</sup> 21 <sup>m</sup> P.M. | (next tide) June 29th | 0 <sup>h</sup> 57 <sup>m</sup> A.M. |
|                                | 12                                  | Constant              | — 0 46                              |
|                                | 12 21                               |                       | June 29th 0 11 A.M.                 |
| Constant for Falmouth          | — 0 46                              |                       |                                     |

Times H.W. Falmouth, June 28th 11 35 A.M.

Here there is no P.M. tide on June 28th at Falmouth.

Ex. 7. 1875, July 12th: find A.M. and P.M. times of high water at Milford Haven (entrance).

The Standard Port of Reference is Pembroke, and the Constant — 0<sup>h</sup> 20<sup>m</sup> (see page 105, Admiralty Tide Tables). Constant *exceeds* Standard A.M. tide, therefore reject it; but it is less than P.M.; there is only a P.M. tide at Milford Haven.

|                               |                                    |                                     |
|-------------------------------|------------------------------------|-------------------------------------|
| Time H.W. Pembroke, July 12th | 0 <sup>h</sup> 5 <sup>m</sup> A.M. | 0 <sup>h</sup> 33 <sup>m</sup> P.M. |
| Constant                      | — 20                               | — 20                                |
|                               |                                    | 0 13 P.M.                           |

No A.M. tide on 12th at Milford Haven.

Ex. 8. 1875, February 15th: find A.M. and P.M. times of high water at Ballycotton.

The Standard Port of Reference is Waterford, and the Constant — 0<sup>h</sup> 20<sup>m</sup>.

(Only tide) Time H.W. Waterford, Feb. 15th 0<sup>h</sup> 26<sup>m</sup> P.M.

Constant — 26

Time H.W. Ballycotton, Feb. 15th 0 0

There is only one high water on the 15th, and this occurs at Noon.

### EXAMPLES FOR PRACTICE.

In each of the following examples it is required to find the times of high water, A.M. and P.M.:—

| No. | Civil Date.      | Place.             | No. | Civil Date.      | Place.         |
|-----|------------------|--------------------|-----|------------------|----------------|
| 1.  | 1875, Dec. 14th, | Cherbourg.         | 12. | 1875, Jan. 19th, | Cadiz.         |
| 2.  | „ Dec. 23rd,     | Aberdeen.          | 13. | „ Sept. 24th     | Lundy Island.  |
| 3.  | „ Nov. 8th       | Stromness.         | 14. | „ Oct. 22nd,     | Havre.         |
| 4.  | „ May 14th,      | St. Nazaire.       | 15. | „ Oct. 8th,      | Cardiff.       |
| 5.  | „ April 18th,    | Ushant.            | 16. | „ Sept. 17th,    | Ramsey.        |
| 6.  | „ May 12th,      | Portland B'kwater. | 17. | „ July 21st,     | Maryport.      |
| 7.  | „ June 27th,     | Dartmouth.         | 18. | „ March 16th,    | Wexford.       |
| 8.  | „ Oct. 23rd,     | Ballycotton.       | 19. | „ May 16th,      | Gibraltar.     |
| 9.  | „ Dec. 6th,      | King Road.         | 20. | „ May 22nd,      | Dublin Bay.    |
| 10. | „ Oct. 9th,      | Falmouth.          | 21. | „ Aug. 11th,     | Milford Haven. |
| 11. | „ Sept. 11th,    | Ferrol.            | 22. | „ Sept. 17th,    | Nieuport.      |

288. In pages 151 to 232 of Admiralty Tide Tables for 1875, are given the times of high water at full and change of a great number of Ports, by which we are enabled to calculate approximately the time of high water on each day. The constant is found by taking Brest as the standard port, at which place the time of high water, full and change, is  $3^h 47^m$ . The difference between the full and change at the given port and Brest will be the constant to be employed, as in the preceding Rules, except there be a great difference of longitude; in which case the correction for the moon's meridian passage must be employed, since for the greatest longitude this correction may amount to half an hour. Should the longitude, however, not exceed  $5^\circ$ , it may be neglected, as doing so will scarcely make more than a difference of one minute. It must also be observed that the longitude of Brest is  $4\frac{1}{2}^\circ$  W. of Greenwich, and in strictness, therefore, in determining this correction  $4^\circ$  should be subtracted, if the longitude of the place be east, or added if it be west. The correction is found in Table XVI, Norie, or Table XXVIII, Raper. Hence:

289. To find the time of high water at Foreign Ports whose constants are not given in the Tide Tables.

# RULE XCII.

1°. To find the Constant — In the Alphabetical List of Ports at the end of the Admiralty Tide Tables (for 1875 p. 189—232), find the time of high water, Full and Change, at Brest, and also that corresponding to the given port; subtract the less from the greater of these two times, and the remainder will be the CONSTANT, additive if the full and change (F. & C.) at the given port is greater than that of Brest, but subtractive if less.

2°. Take out the times of high water at Brest for the given day, and apply the constant as directed in the preceding Rule, XCI pages 253—254; the result is the time of high water (nearly) at the given place.

3°. Take out the longitude of Brest and also of the given place; take the sum if the names are alike, but take the difference if the names are unlike.

4°. Take out (from the column to the left of those containing the times of high water at Brest) the moon's transit for the proposed day and the following one, if the long. is west; but for the given day and the preceding one if the long. is east. Their difference, in either case, is the Daily Variation, or Retardation.

5°. Take from Table 28, Raper, or Table 16, Norie, the correction corresponding to the daily variation and longitude.

6°. Apply this correction by addition in west longitude, but by subtraction in east longitude, to the approximate times of high water already found, the result is the times of high water on the proposed day at the given place.

# EXAMPLES.

Ex. 1. 1875, March 30th: required the time of high water at Victoria River, Turtle Point (N.W. coast of Australia), longitude  $130^\circ$  E.

|  |                     |
|--|---------------------|
| Time of H.W. full and change, Victoria River | $7^h 15^m$ (p. 229) |
| „ Brest.....                                 | $3 47$ (p. 194)     |

Constant  $+ 3 28$

D's transit, March 30th,  $6^h 16^m$  P.M.  
29th,  $5 23$

Long. Victoria River,  $130^\circ$  E.  
„ Brest .....  $4$  W.

53

126

Under  $53^m$  and against  $126^\circ$  longitude, in Raper, Table 28, or Norie, 16, we find  $18^m$  to be subtracted because the longitude is E.

|   |                                     |  |                                     |
|---|-------------------------------------|--|-------------------------------------|
| Time H.W. Brest, March 30th                     | 8 <sup>h</sup> 45 <sup>m</sup> A.M. | Time H.W., Brest, March 30th                     | 9 <sup>h</sup> 25 <sup>m</sup> P.M. |
| Constant  | + 3 28                              | Constant   | + 3 28                              |
| Correction for longitude                        | <u>12 13</u><br>— 0 18              |  | <u>12 53</u><br>— 0 18              |
| Time H.W. at Victoria {<br>River, March 30th, } | 11 55 A.M.                          | Time H.W. at Victoria {<br>River, March 30th.. } | 12 35 P.M.                          |
| No P.M. tide.                                   |                                     | on March 31st                                    | 0 35 A.M.                           |

Ex. 2. 1875, October 20th: find the times of high water at Sandy Hook, longitude 74° W.

|  |                                |   |
|--|--------------------------------|---|
| Time of H.W. full and change, Sandy Hook | ....                           | 7 <sup>h</sup> 29 <sup>m</sup> (p. 222) |
| "  | "                              | Brest ..... 3 47 (p. 194)               |
|  |                                | Constant + 3 42                         |
| D's transit 20th,                        | 4 <sup>h</sup> 44 <sup>m</sup> | Long. Sandy Hook, 74° W.                |
| 21st,                                    | 5 46                           | " Brest ..... + 4 W.                    |
|  | <u>1 2</u>                     | 78                                      |
|  | 62 <sup>m</sup>                |   |

Under 62<sup>m</sup> and against 78° in longitude, in Raper, Table 28, or Norie, 16, we find 13<sup>m</sup> to be added, because the longitude is West.

|  |                                     |  |                                     |
|--|-------------------------------------|--|-------------------------------------|
| Time H.W., Brest, Oct. 20th                | 7 <sup>h</sup> 10 <sup>m</sup> A.M. | Time H.W., Brest, Oct. 20th                | 7 <sup>h</sup> 39 <sup>m</sup> P.M. |
| Constant                                   | + 3 42                              | Constant                                   | + 3 42                              |
| Correction for longitude                   | <u>10 52 A.M.</u><br>+ 13           | Correction for longitude                   | <u>11 21 P.M.</u><br>+ 13           |
| Time H.W. Sandy Hook, {<br>Oct. 20th ..... | 11 5 A.M.                           | Time H.W. Sandy Hook, {<br>Oct. 20th ..... | 11 34 P.M.                          |

Ex. 3. 1875, May 21st: required the times of high water at Nelson, New Zealand, longitude 173° E.

|   |                                     |   |
|---|-------------------------------------|---|
| Time of H.W. full and change, at Nelson | .....                               | 9 <sup>h</sup> 50 <sup>m</sup> (p. 215) |
| "                                       | "                                   | Brest ..... 3 47 (p. 194)               |
|   |                                     | Constant + 6 3                          |
| D's transit, May 21st,                  | 0 <sup>h</sup> 23 <sup>m</sup> A.M. |   |
| 19th,                                   | 11 36 P.M.                          |   |
|   | <u>47</u>                           |   |

Under 47<sup>m</sup> and opposite 169° (173° — 4°) in Table 16, Norie, or 28, Raper, stands the correction 21<sup>m</sup> to be subtracted.

|                            |                                    |                             |                                     |
|----------------------------|------------------------------------|-----------------------------|-------------------------------------|
| Time H.W., Brest, May 21st | 4 <sup>h</sup> 8 <sup>m</sup> A.M. | Time H.W., Brest, May 21st  | 4 <sup>h</sup> 24 <sup>m</sup> P.M. |
| Constant                   | + 6 3                              | Constant                    | + 6 3                               |
| Correction for longitude   | <u>10 11 A.M.</u><br>— 21          | Correction for longitude    | <u>10 27 P.M.</u><br>— 21           |
| Time H.W. Nelson, May 21st | 9 50 A.M.                          | Time H.W., Nelson, May 21st | 10 6 P.M.                           |

Ex. 4. 1875, August 3rd: find the times of high water at Cape Virgin, Straits of Magellan, longitude 68° W.

|   |                                |   |
|---|--------------------------------|---|
| Time of H.W. full and change, Cape Virgin | ....                           | 8 <sup>h</sup> 30 <sup>m</sup> (p. 229)                                   |
| "   | "                              | Brest ..... 3 47 (p. 194)   |
|   |                                | Constant + 4 43   |
| D's transit, August 3rd,                  | 1 <sup>h</sup> 51 <sup>m</sup> | 45 <sup>m</sup> and long. 72° W. (68° + 4°) give corr. + 8 <sup>m</sup> . |
| August 4th,                               | 2 36                           |   |

Time H.W. Brest, Aug. 3rd  $4^h 51^m$  A.M.  
Constant  $+ 4 \ 43$

Correction for longitude....  $\begin{array}{r} 9 \ 34 \\ + \ 8 \end{array}$

Time H.W.C. Virgin Aug. 3rd  $9 \ 42$  A.M.

Time H.W. Brest, Aug. 3rd  $5^h 11^m$  P.M.  
Constant  $+ 4 \ 43$

Correction for longitude....  $\begin{array}{r} 9 \ 54 \\ + \ 8 \end{array}$

Time H.W.C. Virgin, Aug. 3rd  $10 \ 2$  P.M.

### EXAMPLES FOR PRACTICE.

Ex. 1. 1875, Aug. 12th: find the times of high water at Caracas River, Ecuador, longitude  $67^\circ$  W.

Ex. 2. 1875, September 22nd: find the times of high water at Auckland, New Zealand, longitude  $175^\circ$  E.

Ex. 3. 1875, May 15th: find the times of high water at Point de Galle, Ceylon, longitude  $80^\circ$  E.

Ex. 4. 1875, February 22nd: find the times of high water at San Francisco Bay, longitude  $122^\circ$  W.

Ex. 5. 1875, September 23rd: find the times of high water at Malacca Fort, longitude  $102^\circ 15'$  E.

Ex. 6. 1875, July 22nd: find times of high water at Port Jackson, North Head, longitude  $151^\circ 16'$  E.

Ex. 7. 1875, July 27th: find times of high water at St. Julian, longitude  $67^\circ 38'$  W.

Ex. 8. 1875, July 26th: find times of high water at Awatska Bay, longitude  $158^\circ 47'$  E.

Ex. 9. 1875, July 18th: find times of high water at Cape Cod, longitude  $70^\circ 6'$  W.

Ex. 10. 1875, June 3rd: find times of high water at Point de Galle, longitude  $80^\circ$  E.

## GREENWICH DATE BY CHRONOMETER.

290. **The Error of Chronometer** on mean time at any place is the difference between the time indicated by the chronometer and the mean time at that place. *The error of chronometer on Mean Time at Greenwich* is the difference between the time indicated by the chronometer and the mean time at Greenwich. The error is said to be *fast* or *slow* as the chronometer is in advance of or behind the mean time at Greenwich.

291. **Rate of Chronometer** is the daily change in its error, or the interval it shows more or less than twenty-four hours in a mean solar day. If the instrument is going too fast, the rate is called *gaining*; if too slow, *losing*.

292. **To find the rate.**—The rate of a chronometer is determined by comparing its errors for mean time, as found by observation at a given place, on different days. Thus, if by observation a chronometer is found  $20''$  *slow*, and at the end of ten days is found to be  $50''$  *slow* for mean time at the same place, it has evidently lost  $30''$  in ten days, whence its mean daily rate is  $3''$  *losing*. If on a given day, chronometer be  $12''$  *fast*, and at the end of thirteen days  $57''$  *fast* for mean time at any place, it must have gained  $45''$  in thirteen days, or its rate is about  $3''.5$  a day *gaining*. Hence the amount of the daily rate (supposed uniform) is found by dividing the change of the error by the number of days in the interval between observations.

293. To name the rate.—When the chronometer is *fast* either on Greenwich mean time, or on the time at place, if the error is *increasing*, the rate is *gaining*; if *decreasing*, the rate is *losing*. When the chronometer is *slow*, if the error is *increasing*, it is *losing*; if *decreasing*, it is *gaining*. When the chronometer is *fast* and the error changes to *slow*, the rate is *losing*; if the error changes from *slow* to *fast*, the rate is *gaining*.

## EXAMPLES.

Ex. 1. A chronometer was  $25^m 20^s$  *slow* for mean time at Greenwich on Nov. 20th, and on November 30th, was  $24^m 45^s$  *slow* on Greenwich mean time: required the daily rate.

|                            |             |                        |
|----------------------------|-------------|------------------------|
| November 20th, chronometer | <i>slow</i> | $25^m 20^s$            |
| November 30th, „           | <i>slow</i> | $24 \quad 45$          |
| Change of error in 10 days |             | <u>35</u>              |
| Rate for 1 day             |             | $3.5$ <i>gaining</i> . |

In this example the chronometer is *slow* on November 20th, and the error is *decreasing*, therefore the chronometer is *gaining*.

Ex. 2. A chronometer was  $28^m 5^s$  *slow* on mean time at Greenwich, Feb. 27th, 1876, and on March 11th was  $29^m 36^s$  *slow* on mean time at Greenwich: find daily rate.

|                                  |             |                      |       |                 |
|----------------------------------|-------------|----------------------|-------|-----------------|
| 1876, February 27th, chronometer | <i>slow</i> | $28^m 5^s$           | Feb.  | 29 (leap year). |
| 1876, March 11th, „              | <i>slow</i> | $29 \quad 36$        | Feb.  | <u>27</u>       |
| Change of error in 13 days       |             | <u>1 \quad 31</u>    |       | <u>2</u>        |
|                                  |             | $13) 91(7^{\circ} 0$ | March | <u>11</u>       |
|                                  |             | <u>91</u>            | Int.  | <u>13^d</u>     |

The error of chronometer, which is *slow*, is *increasing*, it is therefore *losing*  $7^{\circ} 0$ .

Ex. 3. A chronometer was  $1^m 23^s$  *fast* on mean time at Greenwich, June 2nd, and on July 1st, was  $1^m 37^{\circ} 5$  *fast* on mean time at Greenwich: find daily rate.

|                       |             |                |      |             |
|-----------------------|-------------|----------------|------|-------------|
| June 2nd, chronometer | <i>fast</i> | $1^m 23^s$     | June | 30          |
| July 1st, „           | <i>fast</i> | $1 \quad 37.5$ | June | <u>2</u>    |
| Change in 29 days     |             | <u>14.5</u>    |      | <u>28</u>   |
|                       |             | $29) 14.5(0.5$ | July | <u>1</u>    |
|                       |             | <u>14.5</u>    | Int. | <u>29^d</u> |

The error of chronometer is *fast* and *increasing*, hence the daily rate is  $0.5$  *gaining*.

Ex. 4. A chronometer was  $1^m 51^s$  *fast* on mean time at Greenwich, May 1st, and on May 15th was  $0 \quad 41$  *fast* on mean time at Greenwich: find daily rate.

|                      |             |  |      |           |
|----------------------|-------------|--|------|-----------|
| May 1st, chronometer | <i>fast</i> | $1^m 51^s$   | May  | 1         |
| May 15th, „          | <i>fast</i> | $0 \quad 41$   | May  | <u>15</u> |
| Change in 14 days    |             | <u>1 \quad 10</u>  | Int. | <u>14</u> |
|                      |             | $14 \left\{ \begin{array}{l} 2 \quad 70 \\ 7 \quad 35 \end{array} \right.$ |      |           |
|                      |             | <u>5</u>   |      |           |

In this example the chronometer is *fast* and the error *decreasing*, the rate therefore is *losing*.



294. When the error is found to have changed from *fast* to *slow*, or from *slow* to *fast*, the rate is the sum of the errors divided by the number of days elapsed.

## EXAMPLES.

Ex. 1. July 28th, at 3<sup>h</sup> P.M., the chronometer was 0<sup>m</sup> 6<sup>s</sup>·0 *fast*, and on August 4th at same time, it was 0<sup>m</sup> 17<sup>s</sup>·1 *slow*: required the daily rate.

|  |                                  |
|--|----------------------------------|
| July 28th, at 3 <sup>h</sup> P.M., chronometer <i>fast</i> | 0 <sup>m</sup> 6 <sup>s</sup> ·0 |
| August 4th, „ „ „ <i>slow</i>                              | 0 17·1                           |
| Change of error in 7 days                                  | <u>23·1</u>                      |
|  | 3·3 <i>losing</i> .              |

In this example the error has changed from *fast* to *slow*, the chronometer therefore is *losing*.

Ex. 2. A chronometer was *slow* 1<sup>m</sup> 4<sup>s</sup> on mean time at Greenwich, March 1st, and on March 23rd, was 0<sup>m</sup> 19<sup>s</sup>·6 *fast* on mean time at Greenwich: required the rate of chronometer.

|                                    |                               |       |                       |
|------------------------------------|-------------------------------|-------|-----------------------|
| March 1st, chronometer <i>slow</i> | 1 <sup>m</sup> 4 <sup>s</sup> | March | 23                    |
| March 23rd, „ „ <i>fast</i>        | 0 19·6                        | March | 1                     |
| Change of error in 22 days         | <u>1 23·6</u>                 | Int.  | <u>22<sup>d</sup></u> |
| 22 {                               | 2   83·6                      |       |                       |
|                                    | 11   41·8                     |       |                       |
| Rate                               | <u>3·8</u>                    |       | <i>gains</i> .        |

In this example the error of chronometer has changed from *slow* to *fast*, it is evident, therefore, that the chronometer is *gaining*.

## EXAMPLES FOR PRACTICE.

Ex. 1. A chronometer was *slow* 2<sup>m</sup> 14<sup>s</sup> on mean time at Greenwich, March 3rd, and on March 25th was *slow* 50<sup>s</sup>·4 on mean time at Greenwich: find the daily rate.

Ex. 2. A chronometer was *slow* 5<sup>m</sup> 19<sup>s</sup> on mean time at Greenwich, January 30th, and on February 17th was *slow* 6<sup>m</sup> 13<sup>s</sup> on mean time at Greenwich: find the daily rate.

Ex. 3. A chronometer was 2<sup>m</sup> 2<sup>s</sup> *fast* on mean time at Greenwich, January 24th, and on February 10th was *fast* 3<sup>m</sup> 18<sup>s</sup>·5 for mean time at Greenwich: find the daily rate.

Ex. 4. A chronometer was *slow* 49<sup>s</sup>·3 on mean time at Greenwich, March 17th, and on April 1st was 1<sup>m</sup> 58<sup>s</sup>·7 *fast* for mean time at Greenwich: find daily rate of chronometer.

Ex. 5. A chronometer was *fast* 1<sup>m</sup> 4<sup>s</sup> on mean time at Greenwich, January 10th, and on February 10th was 1<sup>m</sup> 5<sup>s</sup>·2 *slow* for mean time at Greenwich: required the daily rate.

Ex. 6. A chronometer was *fast* 1<sup>m</sup> 29<sup>s</sup> on mean time at Greenwich, July 1st, and on July 23rd was *fast* 1<sup>m</sup> 5<sup>s</sup>·9 on mean time at Greenwich: find daily rate.

Ex. 7. A chronometer was *fast* 48<sup>s</sup> on mean time at Greenwich, February 28th, and on March 15th was *slow* 48<sup>s</sup> on mean time at Greenwich: find daily rate.

Ex. 8. A chronometer was *slow* 20<sup>s</sup> on mean time at Greenwich, September 1st, and on September 15th was *fast* 1<sup>m</sup> 18<sup>s</sup> on mean time at Greenwich: find daily rate.

295. To find the accumulated rate proceed thus:—

### EXAMPLES.

Ex. 1. If a chronometer gains  $2^s.6$  in a day, what will it gain in  $32^d 16^h$ ?

$$\begin{array}{r|l}
 12^h & \frac{1}{2}^d \\
 \hline
 & 2^s.6 \\
 & 32 \\
 & \hline
 & 52 \\
 & 78 \\
 4 & \frac{1}{3} \\
 & 13 \\
 & 4 \\
 \hline
 6,0 & 8,4.9 \\
 \hline
 & 1^m 24^s.9 \\
 \hline
 & \text{or, } 1^m 25^s
 \end{array}$$

*Explanation.*—Multiply the decimal  $2^s.6$  by the number of whole days, namely, 32. Next consider that 12 hours is the  $\frac{1}{2}$  of 1 day, and 4 hours is the  $\frac{1}{3}$  of 12 hours. 12 and 4 make up the whole number of hours, namely, 16. Divide  $2^s.6$  by 2 and the quotient 13 by 3 (see example). Add the products and quotients together; its sum is  $84.9 = 1^m 24^s.9$ ; and observe that the decimal is rejected, and since it is above '5, therefore 1 is added to the seconds.

Ex. 2. If a chronometer loses  $9^s.4$  in a day, what will be the accumulated loss in  $12^d 9^h 34^m$ ?

$$\begin{array}{r|l}
 12^d 9^h 34^m & \text{may be reckoned as } 8^d 9^h 30^m \\
 6^h & \frac{1}{4}^d \\
 \hline
 & 9^s.4 \\
 & 12 \\
 & \hline
 & 112.8 \\
 3 & \frac{1}{2}^h \\
 30^m & \frac{1}{6}^h \\
 & 23 \\
 & 11 \\
 & 2 \\
 \hline
 6,0 & 11,6.4 \\
 \hline
 & 1^m 56^s.4 \\
 \hline
 & \text{or, } 1^m 56^s
 \end{array}$$

*Explanation.*—Multiply by 12; then 6 hours is  $\frac{1}{4}$  of 1 day, and 3 hours  $\frac{1}{2}$  of 6 hours, and 30 minutes is  $\frac{1}{6}$  of 3 hours. Divide the daily rate,  $9^s.4$ , by 4, which will give  $2.3$ , the proportional part of rate in 6 hours ( $\frac{1}{4}$  of a day); next, divide  $2.3$  by 2, which gives the rate for 3 hours ( $\frac{1}{2}$  of 6 hours); again, divide  $1.1$  by 6, which gives the change for 30 minutes ( $\frac{1}{6}$  of 3 hours); then, add the product and several quotients together, the result is the accumulated rate for the interval.

296. The accumulated rate may also be found by decimals; thus:—

### RULE XCIII.

1°. Affix two cyphers to the hours, and divide the result by 6 and the quotient by 4, (i.e., divide by 24); the last quotient is the hours expressed as decimals of a day. (See Rule XVIII, page 44).

2°. Multiply the days and decimals of a day by the seconds and decimals of a second (if any) for the daily rate; the product is the accumulated rate.

### EXAMPLES.

Ex. 1. A chronometer gains  $2^s.6$  in a day; what does it gain in  $32^d 16^h$ ?

$$\begin{array}{r}
 24 \left\{ \begin{array}{l} 6) 16.00 \\ \hline 4) 2.66 \\ \hline \end{array} \right. \begin{array}{l} 32.66 \\ 2.6 \\ \hline 19596 \\ 6532 \\ \hline 6,0) 8,4.916 \\ \hline 1^m 24^s.9 \end{array}
 \end{array}$$

Prefixing the days }  
to the decimals of }  
a day. }

Ex. 2. If a chronometer loses  $9^s.4$  in a day, what is its loss in  $12^d 9^h 34^m = 12^d 10^h$  (nearly)?

$$\begin{array}{r}
 24 \left\{ \begin{array}{l} 6) 10 \\ \hline 4) 1.66 \\ \hline \end{array} \right. \begin{array}{l} 12.41 \\ 9.4 \\ \hline 4964 \\ 11169 \\ \hline 6,0) 11,6.654 \\ \hline 1^m 56^s.7 \\ \hline \text{or } 1^m 57^s \end{array}
 \end{array}$$

Prefixing the days }  
to the decimals of }  
a day. }

The result obtained by this rule in these examples is a little more than by the previous one of aliquot parts, as we have taken  $9^h 34^m$  as  $10^h$  in this, while in the other it was reckoned  $9^h 30^m$ .

297. Before going to sea, the error of the chronometer on Greenwich mean time, and its daily rate, are supposed to have been accurately determined, either at an observatory by means of daily comparison with an astronomical clock, or by observations taken by a sextant at a place whose longitude is known.

298. When the error of a chronometer on Greenwich mean time, and also its daily rate, are known, we may determine Greenwich mean time at some other instant, as when an observation is taken, by the following:—

### RULE XCIV.

1°. To the time by chronometer apply the original error, adding it if the chronometer was slow, rejecting  $24^h$  if greater than  $24^h$ , and putting the day one forward; but if the chronometer is fast, subtract original error, increasing time shown by chronometer by  $24^h$ , if necessary, and putting the day one back.

2°. Find the number of days and parts of a day, to the nearest hour, elapsed since the original error was ascertained.

3°. Multiply the daily rate of chronometer by the elapsed time, and add thereto the proportionate part for the fraction of a day, found by proportion or otherwise; the result is the accumulated rate in the interval.

4°. To the result found by 1°, add the accumulated rate, if chronometer is losing; but subtract if gaining; the result will be mean time at Greenwich, at the instant of observation.

### EXAMPLES.

Ex. 1. 1876, Jan. 30th, r.m. at ship, time by a chronometer, Jan.  $29^d 15^h 47^m 48^s.3$ , which was  $9^m 19^s.6$  slow for Greenwich mean time Dec. 1st, 1875, and on January 1st, 1876, was  $10^m 24^s.7$  slow on Greenwich mean time.

|                              |  |                      |
|------------------------------|--|----------------------|
| 1875, Dec. 1st slow          | $9^m 19^s.6$   | Dec. 31 <sup>d</sup> |
| 1876, Jan. 1st slow          | $10 \quad 24.7$  | Dec. 1               |
| Change of error in 31 days = | $\begin{array}{r} 1 \quad 5.1 \\ 60 \end{array}$   | Jan. 30              |
|                              | $\begin{array}{r} 31)65.1(2.1 \text{ losing} \\ 62 \\ \hline 3.1 \\ 3.1 \\ \hline \end{array}$ | Int. 31 <sup>d</sup> |

The chronometer being *slow* and the error *increasing*, the rate must be marked *losing*.

|                      |                                   |   |   |                    |             |
|----------------------|-----------------------------------|---|---|--------------------|-------------|
| Time by chron., Jan. | $29^d 15^h 47^m 48^s.3$           | Interval from<br>January 1st<br>to January<br>29th $15^h 58^m$<br>is $28^d 16^h$<br>nearly. | { | Daily rate         | $2^s.1$     |
| Original error       | $+ 10 \quad 24.7$                 |   |   |                    | 28          |
| Jan.                 | $29 \quad 15 \quad 58 \quad 13.0$ |   |   |                    | 168         |
| Accumulated rate     | $+ 1 \quad 0.1$                   |   |   |                    | 42          |
| Greenwich date, Jan. | $29 \quad 15 \quad 59 \quad 13.1$ |   |   | h   d              |             |
|                      |                                   |   |   | 12   $\frac{1}{3}$ | 58.8        |
|                      |                                   |   |   | 4   $\frac{1}{3}$  | 1.0         |
|                      |                                   |   |   |                    | 3           |
|                      |                                   |   |   |                    | 6,06,0.1    |
|                      |                                   |   |   | Acc. rate          | $1^m 0^s.1$ |

Ex. 2. 1876, March 20th, P.M. at ship, an observation was made when the time by chronometer was March 20<sup>d</sup> 0<sup>h</sup> 7<sup>m</sup> 55<sup>s</sup>, which was 50<sup>m</sup> 51<sup>s</sup> *fast* on Greenwich mean time, November 22nd, 1875, and on December 21st, 1875, was *fast* 47<sup>m</sup> 33<sup>s</sup>.8 for mean noon at Greenwich: required the Greenwich date by chronometer.

|                                   |  |      |                 |
|-----------------------------------|--|------|-----------------|
| November 22nd, chron. <i>fast</i> | 50 <sup>m</sup> 51 <sup>s</sup> .0                     | Nov. | 30 <sup>d</sup> |
| December 21st, <i>fast</i>        | 47 33 <sup>s</sup> .8                                  | Nov. | 22              |
| Change of rate in 29 <sup>d</sup> | = 3 17 <sup>s</sup> .2                                 |      | 8               |
|                                   | 60   | Dec. | 21              |
|                                   | 29)197 <sup>s</sup> .2(6 <sup>s</sup> .8 <i>losing</i> | Int. | 29 <sup>d</sup> |
|                                   | 174  |      |                 |
|                                   | 232  |      |                 |
|                                   | 232  |      |                 |
|                                   | —  |      |                 |

The chronometer is *fast* and the error *decreasing*, the rate is therefore *losing*.

|                       |   |       |       |  |
|-----------------------|---|-------|-------|--|
| Time by chron. March  | 20 <sup>d</sup> 0 <sup>h</sup> 7 <sup>m</sup> 55 <sup>s</sup> | Dec.  | 31    | <div style="display: inline-block; vertical-align: middle;"> <div style="display: inline-block; vertical-align: middle;">Rate</div> <div style="display: inline-block; vertical-align: middle;">6<sup>s</sup>.8</div> </div>   |
|                       | or 19 24 7 55   |       | 21    |  |
| Original error        | — 47 33 <sup>s</sup> .8                                       |       | 10    |  |
|                       | 23 20 21 <sup>s</sup> .2                                      | Jan.  | 31    |  |
| Accumulated rate      | + 10 11 <sup>s</sup> .7                                       | Feb.  | 29    |  |
| Greenwich date, March | 19 23 30 32 <sup>s</sup> .9                                   | March | 19 23 | <div style="display: inline-block; vertical-align: middle;"> <div style="display: inline-block; vertical-align: middle;">h   d</div> <div style="display: inline-block; vertical-align: middle;">12   1</div> <div style="display: inline-block; vertical-align: middle;">8   3</div> <div style="display: inline-block; vertical-align: middle;">605<sup>s</sup>.2</div> </div> |
|                       |   | Intr. | 89 23 |  |
|                       |   |       |       |  |
|                       |   |       |       |  |
|                       |   |       |       |  |
|                       |   |       |       | 3 <sup>s</sup> .4  |
|                       |   |       |       | 2 <sup>s</sup> .3  |
|                       |   |       |       | .8   |
|                       |   |       |       | 6,0)61,1 <sup>s</sup> .7   |
|                       |   |       |       | Acc. rate 10 11 <sup>s</sup> .7  |

In finding accumulated rate, as the interval is within half an hour of 90 days (23<sup>d</sup> 1<sup>h</sup>), we might have multiplied by 90 and deducted 1-48th ( $\frac{1}{48}$  is 1-48th of a day) from the daily rate.

Ex. 3. Time by a chronometer, Sept. 7<sup>d</sup> 23<sup>h</sup> 16<sup>m</sup> 28<sup>s</sup>, which was 57<sup>m</sup> 47<sup>s</sup> *slow* on Greenwich mean time, June 30th, and on July 12th, was 56<sup>m</sup> 53<sup>s</sup> *slow* on mean time at Greenwich.

|                               |                                    |      |                 |
|-------------------------------|------------------------------------|------|-----------------|
| June 30th, chron. <i>slow</i> | 57 <sup>m</sup> 47 <sup>s</sup>    | June | 30 <sup>d</sup> |
| July 12th, „ <i>slow</i>      | 56 53                              |      | 30              |
| Change in rate in 12 days     | = 54                               |      | 0               |
| Daily rate                    | 4 <sup>s</sup> .5 <i>gaining</i> . | July | 12              |
|                               |                                    | Int. | 12 <sup>d</sup> |

In this instance the chronometer is *slow* and the error *decreasing*, the rate 4<sup>s</sup>.5 is therefore to be marked *gaining*.

|                       |  |       |    |  |
|-----------------------|--|-------|----|--|
| Time by chron. Sept.  | 7 <sup>d</sup> 23 <sup>h</sup> 16 <sup>m</sup> 28 <sup>s</sup> | July  | 31 | <div style="display: inline-block; vertical-align: middle;"> <div style="display: inline-block; vertical-align: middle;">Rate</div> <div style="display: inline-block; vertical-align: middle;">4<sup>s</sup>.5</div> </div> |
| Original error        | + 56 53  |       | 12 |  |
|                       | 8 0 13 21  |       | 19 |  |
| Accumulated rate      | — 4 21   | Aug.  | 31 |  |
| Greenwich date, Sept. | 8 0 9 0  | Sept. | 8  |  |
|                       |  | Int.  | 58 | <div style="display: inline-block; vertical-align: middle;"> <div style="display: inline-block; vertical-align: middle;">6,0)26,1<sup>s</sup>.0</div> </div>   |
|                       |  |       |    |  |
|                       |  |       |    | Acc. rate 4 21 <sup>s</sup> .0   |

#### EXAMPLES FOR PRACTICE.

Ex. 1. 1876, February 16th, A.M. at ship, an observation was taken, when the corresponding time by a chronometer was Feb. 16<sup>d</sup> 8<sup>h</sup> 59<sup>m</sup> 25<sup>s</sup>, which was 1<sup>h</sup> 20<sup>m</sup> 23<sup>s</sup>.4 *fast* on Greenwich mean time, December 1st, 1875, and on January 23rd, 1876, was 1<sup>h</sup> 14<sup>m</sup> 23<sup>s</sup> *fast* on Greenwich mean time: required the Greenwich date by chronometer.

Ex. 2. A chronometer showed April 29<sup>d</sup> 5<sup>h</sup> 0<sup>m</sup> 0<sup>s</sup>, which was *fast* 33<sup>m</sup> 30<sup>s</sup>.3 on Greenwich mean time, March 19th, and on March 26th was 34<sup>m</sup> 20<sup>s</sup> *fast* for mean time at Greenwich: required the Greenwich date by chronometer.

Ex. 3. A chronometer showed May 7<sup>d</sup> 6<sup>h</sup> 9<sup>m</sup> 48<sup>s</sup>, which was *slow* 11<sup>m</sup> 9<sup>s</sup>·4 on Greenwich mean time, February 16<sup>th</sup>, and on February 26<sup>th</sup> was 11<sup>m</sup> 41<sup>s</sup>·6 *slow* for Greenwich mean time: required the Greenwich date by chronometer.

Ex. 4. The chronometer showed June 25<sup>d</sup> 21<sup>h</sup> 29<sup>m</sup> 53<sup>s</sup>, which was 30<sup>m</sup> 12<sup>s</sup> *fast* on Greenwich mean time, March 31<sup>st</sup>, and on April 15<sup>th</sup>, was 30<sup>m</sup> 45<sup>s</sup> *fast*, for mean time at Greenwich: required the Greenwich date by chronometer.

Ex. 5. 1876, October 25<sup>th</sup>, P.M. at ship, time by chronometer Oct. 25<sup>d</sup> 8<sup>h</sup> 31<sup>m</sup> 10<sup>s</sup>, which was 12<sup>m</sup> 9<sup>s</sup>·2 *slow* on Greenwich mean time, July 20<sup>th</sup>, and on August 13<sup>th</sup> was 10<sup>m</sup> 2<sup>s</sup> *slow* for Greenwich mean time: required the Greenwich date by chronometer.

Ex. 6. Time by chronometer January 19<sup>d</sup> 13<sup>h</sup> 21<sup>m</sup> 25<sup>s</sup>, which was 53<sup>m</sup> 47<sup>s</sup> *fast* on mean time at Greenwich, October 24<sup>th</sup>, and on October 31<sup>st</sup> was 53<sup>m</sup> 16<sup>s</sup> *fast* for mean time at Greenwich: required the Greenwich date by chronometer.

Ex. 7. Time by chronometer November 8<sup>d</sup> 16<sup>h</sup> 2<sup>m</sup> 3<sup>s</sup>, which was 33<sup>m</sup> 0<sup>s</sup> *slow* on mean time at Greenwich, July 31<sup>st</sup>, and on August 12<sup>th</sup> was 32<sup>m</sup> 2<sup>s</sup>·4 *slow* on mean time at Greenwich.

Ex. 8. Time by chronometer August 1<sup>d</sup> 0<sup>h</sup> 3<sup>m</sup> 0<sup>s</sup>, which was 6<sup>m</sup> 4<sup>s</sup> *fast* on mean noon at Greenwich, May 31<sup>st</sup>, and on June 14<sup>th</sup> was 4<sup>m</sup> 2<sup>s</sup>·2 *fast* for Greenwich mean time.

Ex. 9. Time by chronometer May 1<sup>d</sup> 13<sup>h</sup> 23<sup>m</sup> 10<sup>s</sup>, chronometer *slow* 3<sup>m</sup> 23<sup>s</sup> on mean time at Greenwich, February 2<sup>nd</sup>, and on February 28<sup>th</sup> was 3<sup>m</sup> 49<sup>s</sup>·0 *slow* on Greenwich mean time.

Ex. 10. Time by chronometer January 20<sup>d</sup> 0<sup>h</sup> 4<sup>m</sup> 21<sup>s</sup>, which was 20<sup>s</sup> *fast* on mean time at Greenwich, November 20<sup>th</sup>, 1875, and on December 10<sup>th</sup>, 1875, was 4<sup>s</sup> *fast* on mean time at Greenwich: required the Greenwich date by chronometer.

Ex. 11. Time by chronometer September 27<sup>d</sup> 16<sup>h</sup> 34<sup>m</sup> 31<sup>s</sup>, which was 0<sup>m</sup> 20<sup>s</sup> *fast* on mean time at Greenwich, April 19<sup>th</sup>, and on May 9<sup>th</sup> was 0<sup>m</sup> 18<sup>s</sup> *slow* for Greenwich mean time: required the Greenwich date by chronometer.

Ex. 12. Time by chronometer April 16<sup>d</sup> 5<sup>h</sup> 36<sup>m</sup> 12<sup>s</sup>, which was 1<sup>m</sup> 2<sup>s</sup> *slow* for mean time at Greenwich, January 24<sup>th</sup>, and on February 28<sup>th</sup> was 29<sup>s</sup> *fast* for Greenwich mean time.

299 When the "chronometer question" is given in a form similar to that below, we have to determine for ourselves the day of the month at Greenwich, that is, if the time shown by chronometer was 1<sup>h</sup>, 2<sup>h</sup>, 3<sup>h</sup>, &c., on the civil or on the astronomical day; for, a frequent source of embarrassment in interpreting the indications of a chronometer arises from the division of its face into twelve instead of twenty-four parts, so that the same position of the pointer represents two periods of the day twelve hours distant. Thus, at 2<sup>h</sup> past noon, and again at 14<sup>h</sup> past noon the hands are in the same place, and it is necessary to determine whether it should be read as 2<sup>h</sup> or 14<sup>h</sup>, 5<sup>h</sup> or 17<sup>h</sup>, 6<sup>h</sup> or 18<sup>h</sup> past noon, and so on. To determine this point proceed according to this rule:—

### RULE XCV.

1°. *Get an approximate Greenwich date by means of ship mean time nearly and the longitude by account (Rule LXXXI, page 222).*

2°. *Proceed, as directed in Rule XCIV, page 263, to apply the original error and accumulated rate to the time by chronometer.*

If the difference between Greenwich dates thus found by the two methods, is nearly 12<sup>h</sup>, then the Greenwich date by *chronometer* found as above, must be increased by 12<sup>h</sup>, and the day put one back, so as to make the two dates agree both in the day and hour nearly.

## EXAMPLES.

Ex. 1. August 3rd, at about 3<sup>h</sup> P.M., longitude by acct. 75° W., the chronometer marks 8<sup>h</sup> 11<sup>m</sup> 7<sup>s</sup>, and is 6<sup>m</sup> 10<sup>s</sup> *fast* on Greenwich mean time: what is the Greenwich astronomical date?

|                           |  |                             |   |
|---------------------------|--|-----------------------------|---|
| Approx. T. at ship, Aug.  | 3 <sup>d</sup> 3 <sup>h</sup> 0 <sup>m</sup> | Time by chron.              | 8 <sup>h</sup> 11 <sup>m</sup> 7 <sup>s</sup> |
| Longitude 75° W.          | + 5 0  | Error of chron. <i>fast</i> | — 6 10  |
| Approx. Green. date, Aug. | 3 8 0  | Green. date, Aug. 3rd       | 8 4 57  |

In this example the approximate Greenwich time is 8<sup>h</sup>, it is evident that the chronometer must have shown 8<sup>h</sup> from noon also.

Ex. 2. June 18th, at 10<sup>h</sup> 52<sup>m</sup> P.M., mean time at ship nearly, long. 60° W., an observation was taken, when a chronometer showed 2<sup>h</sup> 48<sup>m</sup> 40<sup>s</sup>, on June 6th its error was known to be 3<sup>m</sup> 10<sup>s</sup>·2 *fast* on Greenwich mean time, and its mean daily rate 3<sup>s</sup>·5 *gaining*: required the mean time at Greenwich when the observation was taken.

|                        |   |   |                    |                   |
|------------------------|---|---|--------------------|-------------------|
| Approx. Ship date June | 18 <sup>d</sup> 10 <sup>h</sup> 52 <sup>m</sup> | Interval from                                   | Daily rate         | 3 <sup>s</sup> ·5 |
| Longitude 60° W.       | + 4 0   | June 6th to                                     | 12                 | —                 |
| Approx. Green. date    | 18 14 52  | June 18th                                       | h   d              | 42 <sup>o</sup> 0 |
|                        |   | 14 <sup>h</sup> 52 <sup>m</sup> is              | 12   $\frac{1}{2}$ | 1 <sup>o</sup> 7  |
|                        |   | 12 <sup>d</sup> 14 <sup>h</sup> 52 <sup>m</sup> | 3   $\frac{1}{4}$  | 4                 |
|                        |   | = 12 <sup>d</sup> 15 <sup>h</sup>               | Acc. rate          | 44 <sup>o</sup> 1 |
|                        |   | nearly.   |                    |                   |
| Chronometer showed     | 2 <sup>h</sup> 48 <sup>m</sup> 40 <sup>s</sup>  |   |                    |                   |
| Original error         | — 3 10 <sup>s</sup> ·2 <i>fast</i>              |   |                    |                   |
| Accumulated rate       | 2 45 29 <sup>s</sup> ·8                         |   |                    |                   |
|                        | — 44 <sup>o</sup> 1 <i>gaining</i> .            |   |                    |                   |
| June                   | 19 <sup>d</sup> 2 44 45 <sup>s</sup> ·7 A.M.    |   |                    |                   |
|                        | — 12 0 0  |   |                    |                   |
| Green. date, June      | 18 14 44 45 <sup>s</sup> ·7                     |   |                    |                   |

In this instance we see that 2<sup>h</sup> by the chronometer must be reckoned as 14<sup>h</sup>, that is, 12<sup>h</sup> must be added to the indication of chronometer, and the day put one back.

## TO FIND THE HOUR-ANGLE.

Given the true altitude of an object, its declination, and the latitude of the observer, to find the meridian distance or hour-angle.

## RULE XCVI.

- 1°. Find the polar distance by Rule LXXXV, page 231.
- 2°. Add together the true altitude, latitude, and polar distance; take half their sum, and from the half sum subtract the true altitude, which call the remainder.
- 3°. Add together the secant of latitude, cosecant of polar distance, cosine of half sum, and sine of remainder; the sum of these logs. (rejecting 10 from the index), will be the log. of sun's hour-angle (Table 31, Norie); or sine square of sun's hour-angle (Table 69, Raper).

When the polar distance exceeds 90°, take out the secant of reduced declination; or subtract the polar distance from 180°, and take the cosecant of the remainder. (See Rules XL and LXI, pages 76—77.)

(a.) When both the latitude and declination are 0, take the true altitude from  $90^\circ$ , and so get the zenith distance, which convert into time by Rule LXXIX, page 220, or by Table 19, Norie, or Table 17, Raper; the result is the hour-angle.

The hour-angle can also be found without a special table, as follows:—Find the sum of the four logs. as above, and divide by 2: the result is the log. sine of half the hour-angle in arc. From the Table of log. sines find the arc corresponding thereto, which multiplied by 2, and converted into time (Rule LXXIX, page 220), is the hour-angle sought. It is thus evident that the complete solution may be obtained by means of the Table of log. sines, &c., alone.

### EXAMPLES.

Ex. 1. Given the true alt.  $25^\circ 23' 41''$ , lat.  $31^\circ 17' N.$ , decl.  $17^\circ 9' 8'' S.$ , whence pol. dist.  $107^\circ 9' 8''$ : find the hour-angle.

|             |                     |        |             |
|-------------|---------------------|--------|-------------|
| Altitude    | $25^\circ 23' 41''$ |        |             |
| Latitude    | $31^\circ 17' 0''$  | sec.   | $0.0068232$ |
| Polar dist. | $107^\circ 9' 8''$  | cosec. | $0.0197538$ |

2)163 49 49

81 54 54 cos.  $9.148115$

56 31 13 sine  $9.921208$

Hour-angle =  $2^h 58^m 11^s$  log.  $9.15731, 3$   
15724

$7 = 1^s$

NOTE.—In Norie, Table XXXI, the next less log. to 15731 is 15724, which gives  $2^h 58^m 10^s$ , and diff 7 gives  $1^s$  to add, whence the term corresponding to  $9.15731$  is  $2^h 58^m 11^s$ .

Ex. 2. Given the true altitude  $17^\circ 16' 12''$ , latitude  $50^\circ 42' S.$ , reduced declination  $20^\circ 6' 17'' S.$  (when polar dist. is  $69^\circ 53' 43''$ ): find the hour-angle.

|             |                     |        |            |
|-------------|---------------------|--------|------------|
| Altitude    | $17^\circ 16' 12''$ |        |            |
| Latitude    | $50^\circ 42' 0''$  | sec.   | $0.198335$ |
| Polar dist. | $69^\circ 53' 43''$ | cosec. | $0.027304$ |

Sum 137 51 55

Half sum 68 55 57 cos.  $9.555660$

$\frac{1}{2}$  sum—alt. 51 39 45 sine  $9.894521$

Hour-angle  $5^h 48^m 6^s$  log.  $9.67582, 0$   
79

$1^s = 3$

In Norie, Table 31, we seek for the nearest log. to  $9.67582$ , the nearest to which is  $9.67579$ , which corresponds to  $5^h 48^m 5^s$ ; then in column prop. part we seek for 3, which gives  $1^s$  to add, whence hour-angle is  $5^h 48^m 6^s$ .

The pol. dist. being greater than  $90^\circ$ , take the secant of decl. for the cosec. of pol. dist., and add the prop. part for  $8''$ .

|                    |        |            |          |
|--------------------|--------|------------|----------|
| $107^\circ 9' 0''$ | cosec. | $0.019753$ | Diff. 65 |
| Parts for 8        |        | +          | 5        |

$107^\circ 9' 8''$  cosec.  $0.019758$  5,20

Observation.—Always cut off two figures when working for seconds of arc.

|                    |      |            |            |
|--------------------|------|------------|------------|
| $81^\circ 54' 0''$ | cos. | $9.148915$ | Diff. 1481 |
| Parts for 54       |      | —          | 800        |

$81^\circ 54' 54''$  cos.  $9.148115$  5924

7405

79974

|                    |      |            |           |
|--------------------|------|------------|-----------|
| $56^\circ 31' 0''$ | sine | $9.921190$ | Diff. 139 |
| Parts for 13       |      | +          | 18        |

$56^\circ 31' 13''$  sine  $9.921208$  417

139

18,07

Ex. 3. Given the true altitude  $13^\circ 28' 42''$ , latitude  $10^\circ 35' S.$ , reduced declination  $23^\circ 23' 54'' N.$  (or polar distance  $113^\circ 23' 54''$ ): find the hour-angle.

|             |                      |        |            |
|-------------|----------------------|--------|------------|
| Altitude    | $13^\circ 28' 42''$  |        |            |
| Latitude    | $10^\circ 35' 0''$   | sec.   | $0.007451$ |
| Polar dist. | $113^\circ 23' 54''$ | cosec. | $0.037268$ |

Sum 137 27 36

Half sum 68 43 48 cos.  $9.559623$

$\frac{1}{2}$  sum—alt. 55 15 6 sine  $9.914694$

Hour-angle  $4^h 40^m 41^s$  log.  $9.51903, 6$   
898

$1^s = 6$

The nearest log. to  $9.51903$  is  $9.51898$ , which gives  $4^h 40^m 40^s$ , the diff. 6 found at right hand in prop. parts gives  $1^s$ , whence hour-angle is  $4^h 40^m 41^s$ .

Ex. 4. Latitude  $0^{\circ}$ , declination  $0^{\circ}$ , true altitude  $30^{\circ}$ : required the hour-angle.

|                 |  |
|-----------------|--|
| True altitude   | $30^{\circ} 0'$<br>$90 \quad 0$                        |
| Zenith distance | $60 \quad 0$<br>$\quad 4$<br>$\hline 6,0)24,0 \quad 0$ |
| Hour-angle      | $4^h 0^m 0^s$  |

Ex. 5. Given true altitude  $75^{\circ}$ , latitude  $0^{\circ}$ , declination  $0^{\circ}$ : find the hour angle.

|                 |   |
|-----------------|---|
| True altitude   | $75^{\circ} 0'$<br>$90 \quad 0$                       |
| Zenith distance | $15 \quad 0$<br>$\quad 4$<br>$\hline 6,0)6,0 \quad 0$ |
| Hour-angle      | $1^h 0^m 0^s$   |

#### EXAMPLES FOR PRACTICE.

Required the hour-angle or meridian distance in each of the following examples:—

|    | True altitude, $11^{\circ} 21' 29''$ | Latitude $30^{\circ} 15' S.$ | Declination $15^{\circ} 21' 4'' N.$ |
|----|--------------------------------------|------------------------------|-------------------------------------|
| 1. | $30 \quad 2 \quad 4$                 | $39 \quad 27 \quad S.$       | $5 \quad 48 \quad 23 \quad N.$      |
| 2. | $27 \quad 48 \quad 22$               | $40 \quad 10 \quad N.$       | $23 \quad 26 \quad 44 \quad N.$     |
| 3. | $34 \quad 49 \quad 46$               | $39 \quad 20 \quad S.$       | $21 \quad 15 \quad 7 \quad S.$      |
| 4. | $25 \quad 38 \quad 11$               | $0 \quad 29 \quad N.$        | $23 \quad 1 \quad 55 \quad N.$      |
| 5. | $15 \quad 59 \quad 13$               | $60 \quad 5 \quad N.$        | $7 \quad 25 \quad 38 \quad S.$      |
| 6. | $29 \quad 2 \quad 27$                | $0 \quad 0 \quad 0$          | $0 \quad 0 \quad 0$                 |
| 7. | $20 \quad 34 \quad 4$                | $0 \quad 0 \quad 0$          | $23 \quad 27 \quad 21 \quad N.$     |
| 8. | $37 \quad 40 \quad 0$                | $0 \quad 0 \quad 0$          | $0 \quad 0 \quad 0$                 |
| 9. |                                      |                              |                                     |

## LONGITUDE BY CHRONOMETER,

FROM AN OBSERVED ALTITUDE OF THE SUN.

### RULE XCVII.

1°. To the time by Chronometer apply its original error and accumulated rate, as directed in Rule XCIV; the result is the Greenwich date at the instant of observation.

2°. Take out of Nautical Almanac, page II, the sun's declination and the equation of time for the noon of Greenwich date, and the corresponding hourly difference for each: also take out the sun's semi-diameter.

3°. Reduce the sun's declination and equation of time to the Greenwich time (Rules LXXXII and LXXXVI); also find the polar distance (Rule LXXXV).

4°. Correct observed altitude for index error, dip, correction in altitude, and semi-diameter, and thus get the true altitude. (Rule LXXXVII).

5°. Find the hour-angle or meridian distance by Rule XCVI.\*

6°. When the observation is made in the afternoon, the hour-angle is apparent time past noon of the given day at ship—before which write the date at ship, but if the observation is made in the morning, take the hour-angle from  $24^h$ , the remainder is apparent time at ship reckoned from noon of the preceding day, the time at place in both instances being expressed in astronomical time.

\* In finding longitude by chronometer the logs. used in finding the hour-angle are required to be taken out for seconds of arc.



## EXAMPLES.

Ex. 1. January 6th, P.M. at ship; suppose the sun's hour-angle to be  $3^h 40^m 18^s$ : what is the apparent time at ship?

Here the time being P.M., we have the ship date app. time, January 6<sup>d</sup>  $3^h 40^m 18^s$ .

Ex. 2. January 6th, A.M. at ship; suppose the sun's hour-angle to be  $3^h 40^m 18^s$ : what is the apparent time at ship?

Here the Hour-angle is  $3^h 40^m 18^s$   
 $\underline{24 \quad 0 \quad 0}$

Ship date app. T., Jan. 5th  $\underline{20 \quad 19 \quad 42}$

Ex. 3. June 1st, P.M. at ship; suppose the hour-angle to be  $3^h 54^m 39^s$ : required the apparent time at ship.

Here the time being P.M., we have the app. T. at ship, June 1<sup>d</sup>  $3^h 54^m 39^s$ .

Ex. 4. June 1st, A.M. at ship; suppose the hour-angle to be  $3^h 54^m 39^s$ : what is the apparent time at ship?

Hour-angle  $3^h 54^m 39^s$   
 $\underline{24 \quad 0 \quad 0}$

App. T. at ship, May 31st  $\underline{20 \quad 5 \quad 21}$

On comparing these examples with paragraph 6°, which they are intended to illustrate, the seamen will have no difficulty in understanding that, since the sun's Hour-angle is the Distance (in time) of the object from the meridian, if the observation is made in the afternoon (P.M.), as in Ex. 1, the time will be  $3^h 40^m 10^s$  past noon of the 5th day; that is, the ship date (astronomical time) is January 6<sup>d</sup>  $3^h 40^m 10^s$ —the astronomical day commences always at noon; but if the observation be made in the morning (A.M.), the hour-angle will be the time before noon of the 6th day; or, as shown in Ex. 2,  $20^h 19^m 42^s$  past noon of the day before,—that is, January 5<sup>d</sup>  $20^h 19^m 42^s$ . In Ex. 3, similarly, the observation being P.M., the time will be  $3^h 54^m 39^s$  past noon of June 1st, while in Ex. 4, the observation being A.M., the time will be  $3^h 54^m 39^s$  before noon of June 1st, i.e.,  $20^h 5^m 21^s$  past noon, May 31st.

In the new edition of Norie's Tables the hour-angle is so arranged that when the observation is made P.M. at ship it is read from the top of the page; when A.M. from the bottom; in which case the necessity of deducting from  $24^h$  (as explained in paragraph 6°) is obviated.

7°. To apparent time apply the reduced equation of time, adding or subtracting as directed in page I, Nautical Almanac, and so get mean time.

8°. Under ship mean time put Greenwich mean time—not forgetting the day in each case:—subtract the less from the greater; the remainder is longitude in time, which convert into arc  $^{\circ}'''$ ; see Rule LXXX, or Table 17, Raper, or Table 19, Norie.

In taking the difference of Greenwich mean time and ship mean time, if the days of the month be different, it will be necessary to add 24 to the hours of the more advanced (that is the one whose days are most), in order to enable the subtraction to be made.

9°. Call the longitude West when Greenwich time is greater than ship mean time; but East when Greenwich mean time is least.

NOTE.—When the latitude at noon is given, the latitude in at the time of observation must be found by means of the course steered and distance sailed. The diff. of lat. from noon is to be named North and South, according as the ship at the time of observation is north or south of her latitude at noon. When the longitude is found as in examples 1 to 10 (or according to paragraph No. 8° and 9°, page 269), the diff. of long. between the ship at the time of observation and noon must be applied to find the longitude at noon. The diff. of long. is to be named East or West, according as the ship is east or west of its position at noon.

## EXAMPLES.

Ex. 1. 1876, January 11th, P.M. at ship, latitude  $49^{\circ} 30'$  N., the observed altitude sun's L.L. was  $12^{\circ} 20' 30''$ , height of eye 18 feet, time by a chronometer January 11<sup>d</sup> 6<sup>h</sup> 44<sup>m</sup> 36<sup>s</sup> (being P.M. at Greenwich), which was 6<sup>m</sup> 8<sup>s</sup>·3 *fast* for mean noon at Greenwich, September 1st, 1875, and on September 30th, 1875, was 8<sup>m</sup> 42<sup>s</sup> *fast* on Greenwich mean time; required the longitude by chronometer.

|   |  |   |                                |
|---|--|---|--------------------------------|
| September 1st, chronometer <i>fast</i> 6 <sup>m</sup> 8 <sup>s</sup> ·3 |  | 30th, „ <i>fast</i> 8 42 <sup>o</sup>   |                                |
| Change in 29 days   |  | 2 33 <sup>7</sup>   |                                |
|   |  | 29) 153 <sup>7</sup> (5 <sup>s</sup> ·3   |                                |
| T. by chron., Jan.  | 11 <sup>d</sup> 6 <sup>h</sup> 44 <sup>m</sup> 36 <sup>s</sup> | (a) Interval from   | Obs. alt. $\odot$ 's L.L.      |
| Original error  | = 0 8 42   | Oct. 1st to Jan. 11th   | Dip                            |
|   |  | 6 <sup>h</sup> 10 <sup>m</sup> 3 <sup>s</sup> ·3 is 103 <sup>d</sup> 6 <sup>h</sup> . |                                |
| Accumulated rate  | 11 6 35 54   | Daily rate  | 12 16 26                       |
|   | 9 7  | 5 <sup>s</sup> ·3   | 4 9                            |
| Green. date, Jan.   | 11 6 26 47   | 103   |                                |
|   |  | 159   | 12 12 17                       |
|   |  | 53 <sup>o</sup>   | + 16 18                        |
|   |  |   | True alt. 12 28 35             |
|   |  | 6   $\frac{1}{4}$   545 <sup>9</sup>  | By Raper's Tables; dip —       |
|   |  | $\frac{1}{2}$   $\frac{1}{2}$   1 <sup>3</sup>  | 4' 10", refr. — 4' 23", par. + |
|   |  |   | 9, semid. + 16' 18", and true  |
|   |  | 6,0) 54,7 <sup>3</sup>  | alt. 12° 28' 24".              |

(a) The chronometer having been rated September 30th, there are no days left in September.

|                     |                             |                           |                      |                               |                    |
|---------------------|-----------------------------|---------------------------|----------------------|-------------------------------|--------------------|
| Decl. page II, N.A. |                             | H.D.                      | Eq. T. page II, N.A. |                               | H.D.               |
| 11th noon           | 21° 51' 58" S. <i>decr.</i> | 23 <sup>14</sup>          | 11th noon            | 8 2 <sup>4</sup> <i>incr.</i> | 992                |
| Correction          | — 2 29                      | 6 <sup>45</sup>           | Correction           | + 6 <sup>4</sup>              | 6 <sup>45</sup>    |
| Red. decl.          | 21 49 29 S.                 | 1157 <sup>o</sup>         | Red. Eq. T.          | 8 8 <sup>8</sup>              | 496 <sup>o</sup>   |
|                     |                             | 9256                      |                      |                               | 3968               |
| Polar dist.         | 111 49 29                   | 13884                     | To be added to A.T.  |                               | 5952               |
|                     |                             | 6,0) 14,9 <sup>2530</sup> |                      |                               | 6 <sup>39840</sup> |
| Corr. — 2 29        |                             |                           |                      |                               |                    |

|             |  |        |                     |
|-------------|--|--------|---------------------|
| Altitude    | 12° 28' 35"                                    |        |                     |
| Latitude    | 49 30 0  | sec.   | 0 <sup>187456</sup> |
| Polar dist. | 111 49 29                                      | cosec. | 0 <sup>032299</sup> |
|             | 173 48 4                                       |        |                     |
|             | 86 54 2  | cos.   | 8 <sup>732949</sup> |
|             | 74 25 27                                       | sine   | 9 <sup>983751</sup> |
| Hour-angle  | 2 <sup>h</sup> 16 <sup>m</sup> 45 <sup>s</sup> | log.   | 8 <sup>936455</sup> |

|  |  |
|--|--|
| App. T. at ship Jan.                   | 11 <sup>d</sup> 2 <sup>h</sup> 16 <sup>m</sup> 45 <sup>s</sup> |
| Eq. T.                                 | + 8 9  |
| M.T. ship Jan.                         | 11 2 24 54   |
| M.T. Green. Jan.                       | 11 6 26 47   |
| Long. in time                          | 4 1 53   |
| Longitude                              | 60° 28' 15" W.   |
| By Raper: log. sin. sq. (sum of logs.) |  |
| 8 <sup>936693</sup> gives hour-angle   | 2 <sup>h</sup> 16 <sup>m</sup> 47 <sup>s</sup> , <i>long.</i>  |
| 60° 27' 45" W.                         |  |

Ex. 2. 1876, May 20th, P.M. at ship, latitude  $50^{\circ} 43'$  N., obs. alt. sun's L.L.  $17^{\circ} 10'$ , index corr. —  $1' 50''$ , height of eye 28 feet, time by a chronometer May 20<sup>d</sup> 0<sup>h</sup> 19<sup>m</sup> 53<sup>s</sup> (or 0<sup>h</sup> 19<sup>m</sup> 53<sup>s</sup> P.M.), which was 33<sup>s</sup> *fast* on mean noon at Greenwich, March 20th, and on April 1st, was 23<sup>s</sup>·4 *fast* on Greenwich mean time.

|   |                       |
|---|-----------------------|
| March 20th chronometer <i>fast</i> 0 <sup>m</sup> 33 <sup>s</sup> |                       |
| April 1st „ <i>fast</i> 0 23 <sup>4</sup>                         |                       |
| Change in 12 days   | 12) 9 <sup>6</sup>    |
| Daily rate  | 0 <sup>8</sup> losing |

|  |   |                    |  |
|--|---|--------------------|--|
| T. by chronometer May 20 <sup>d</sup> 0 <sup>h</sup> 19 <sup>m</sup> 53 <sup>s</sup>       | Interval from   | Obs. alt. ☉'s L.L. | 17° 10' 0"                                     |
| Original error <i>fast</i> — 23 <sup>·</sup> 4   | April 1st to May 20th is 49 <sup>d</sup> .  | Index corr.        | — 1 50   |
| Accumulated rate   | Rate 0 <sup>s</sup> ·8  | Dip                | 17 8 10  |
| Green. date, May   | Interval × 49   | Corr. alt.         | — 5 5  |
|  | Acc. Rate 39 <sup>·</sup> 2   |                    | 17 3 5   |
|  |   |                    | — 2 55   |
| By Raper: dip — 5' 10", refr. — 3' 9", par. — 8", semid. + 15' 50", true alt. 17° 15' 49". |   | Semi-diameter      | 17 0 10  |
|  |   |                    | + 15 50  |
| H. diff. + 30 <sup>s</sup> ·80   | H. diff.  | True alt.          | 17 16 0  |
| 20 <sup>m</sup>   $\frac{1}{3}$ h   30 <sup>s</sup> ·80                                    |   |                    | — 0 <sup>s</sup> ·148                          |
| Correction + 10 <sup>·</sup> 27  | Correction  |                    | — 0 <sup>·</sup> 49                            |
| Decl. 20th, noon 20 6 52   | Eq. T., 20th, noon  |                    | 3 <sup>m</sup> 41 <sup>s</sup> ·09             |
| Red. decl. 20 7 2  | Red. eq. time   |                    | 3 41 <sup>·</sup> 04                           |
| 90   | (To be subtracted from A.T.)  |                    |  |
| Polar dist. 69 52 58   |   |                    |  |
| Altitude 17° 16' 0"  | App. T. Ship, May 20th  |                    | 5 <sup>h</sup> 48 <sup>m</sup> 12 <sup>s</sup> |
| Latitude 50 43 0 sec. 0 <sup>·</sup> 198489  | Eq. Time  |                    | — 3 41   |
| Polar dist. 69 52 58 cosec. 0 <sup>·</sup> 027339  | Mean T. Ship, May 20th  |                    | 5 44 31  |
| 137 51 58  | Mean T. Green., May 20th  |                    | 0 20 9   |
| Half sum alt. 68 55 59 cos. 9 <sup>·</sup> 555649  | Long. in time   |                    | 5 24 22  |
| 51 39 59 sin. 9 <sup>·</sup> 894544  | Longitude   |                    | 81° 5' 30" E.                                  |
| Hour-angle 5 <sup>h</sup> 48 <sup>m</sup> 12 <sup>s</sup> log. 9 <sup>·</sup> 676021       | By Raper: Log. sine sq. (sum of logs.)  |                    |  |
|  | 9 <sup>·</sup> 676062 gives Hour-angle 5 <sup>h</sup> 48 <sup>m</sup> 13 <sup>s</sup> , |                    |  |
|  | Longitude 81° 5' 45" E.   |                    |  |

Since the sun's hour-angle is the distance (time) of the object from the meridian, if the observation is P.M., as in this example, the time (or hour-angle) will be 5<sup>h</sup> 48<sup>m</sup> 12<sup>s</sup> *past noon* of the 20th day; hence the app. time at ship is May 20<sup>d</sup> 5<sup>h</sup> 48<sup>m</sup> 12<sup>s</sup> (see Rule XCVII, 6°, page 269).

Ex. 3. 1876, July 3rd, A.M. at ship, latitude 32° 10' S., obs. alt. sun's L.L. 14° 10' 15", index corr. + 1' 22", height of eye 19 feet, time by a chronometer July 2<sup>d</sup> 16<sup>h</sup> 33<sup>m</sup> 22<sup>s</sup> (being 3<sup>d</sup> 4<sup>h</sup> 33<sup>m</sup> 22<sup>s</sup> A.M. at Greenwich), which was 17<sup>m</sup> 16<sup>s</sup>·4 *fast* for Greenwich mean noon May 16th, and on June 1st was 16<sup>m</sup> 22<sup>s</sup> *fast* for mean time at Greenwich: required the longitude.

May 16th, Chronometer *fast* 17<sup>m</sup> 16<sup>s</sup>·4  
June 1st, „ *fast* 16 22<sup>·</sup>0

Change in 16 days 54<sup>·</sup>4

|   |  |                                  |             |
|---|--|----------------------------------|-------------|
|   | Daily rate   | 3 <sup>·</sup> 4 <i>losing</i> . |             |
| T. by chron., July 2 <sup>d</sup> 16 <sup>h</sup> 33 <sup>m</sup> 22 <sup>s</sup> | Interval from  | Obs. alt. ☉'s L.L.               | 14° 10' 15" |
| Original error — 16 22  | June 1st to July 2nd, 16 <sup>d</sup> , is 31 <sup>d</sup> 16 <sup>h</sup> . | Index corr.                      | + 1 22      |
| Accumulated rate  | Daily rate 3 <sup>s</sup> ·4   | Dip                              | 14 11 37    |
| Green. date, July 2 16 18 48  | Interval 31  | Corr. alt.                       | — 4 11      |
|   | 34   |                                  | 14 7 26     |
|   | 102  |                                  | — 3 35      |
|   | 12   $\frac{1}{3}$   1054  | Semi-diameter                    | 14 3 51     |
|   | 4   $\frac{1}{3}$   17   |                                  | + 15 46     |
|   | 6  | True alt.                        | 14 19 37    |
|   | 6,0)107 <sup>·</sup> 7   | By Raper: index corr +           |             |
| Acc. rate 1 47 <sup>·</sup> 7   |  | 1' 22", dip — 4' 15", ref. —     |             |
|   |  | 3' 47", par. + 8", semid. +      |             |
|   |  | 15' 46", true alt. 14° 19' 29".  |             |

| Decl. page II, N.A.                            | H.D.            | Eq. T. page II, N.A.                    | H.D.                    |
|--|-----------------|---|-------------------------|
| 2nd, noon $23^{\circ} 0' 45''$ N. <i>Deer.</i> | — 11'66         | 2nd, noon <i>add</i> $3^m 48^s \cdot 4$ | + 0'463                 |
| Correction — 3 10                              | + 16'3          | Correction + 7'5                        | × 16'3                  |
| Red. decl. $22^{\circ} 57' 35''$ N.            | 3498            | Red. eq. time $3^h 55^m 9^s$            | 1389                    |
| 90   | 6996            | (To be added to A.T.)                   | 2778                    |
|  | 1166            |   | 463                     |
| Polar dist. $112^{\circ} 57' 35''$             | 6,019,0058      |   | Corr. + 7.5469          |
|  | Corr. — 3 10    |   |                         |
| Altitude $14^{\circ} 19' 37''$                 |                 | Hour-angle $3^h 37^m 6^s$               |                         |
| Latitude $32^{\circ} 10' 0''$                  | sec. 0'072371   |   | 24                      |
| Polar dist. $112^{\circ} 57' 35''$             | cosec. 0'035844 | App. T. ship, July 2nd                  | 20 22 54                |
|  |                 | Eq. T.                                  | + 3 56                  |
| $159^{\circ} 27' 12''$                         |                 | Mean time Ship, July 2nd                | 20 26 50                |
| $79^{\circ} 43' 36''$                          | cos. 9'251260   | Mean time Green., July 2nd              | 16 18 48                |
| $65^{\circ} 23' 59''$                          | sin. 9'958676   | Longitude in time                       | 4 8 2                   |
| Hour-angle $3^h 37^m 6^s$                      | log. 9'318151   | Longitude                               | $62^{\circ} 0' 30''$ E. |

By Raper: Log. sin. sq.  $9'318201$  gives  
Hour-angle  $3^h 37^m 6^s$ , longitude  $62^{\circ} 0' 30''$  E.

In this example the time of observation is A.M. at ship, the hour-angle is therefore the time *before noon* of July 3rd, and as all calculations are made in the astronomical day, we take the hour-angle from  $24^h$ , the remainder is A.T. at ship, reckoned from *noon* of the *preceding day*, viz., that of July 2nd. (See Rule XC VII, page 269.)

Ex. 4. 1876, April 14th, A.M. at ship, latitude  $52^{\circ} 10' N.$ , observed altitude sun's L.L.  $18^{\circ} 20' 25''$ , index corr. +  $55''$ , height of eye 12 feet, time by chron.  $14^d 5^h 5^m 5^s$  (being P.M. at Greenwich), which was *fast*  $5^m 52^s \cdot 4$  for mean noon at Greenwich, February 14th, and on February 26th was *fast*  $6^m 38^s$  for mean noon at Greenwich.

|  |                              |   |
|--|------------------------------|---|
| T. by chron., Ap. $14^d 5^h 5^m 5^s$       | Interval from                | Obs. alt. $\odot$ 's L.L. $18^{\circ} 20' 25''$ |
| Original error — 6 38                      | Feb. 26th, to April          | Index corr. + 55                                |
|  | $14^d 5^h$ , is $48^d 5^h$ . |   |
|  | Rate 3'8                     |   |
| Accumulated rate — 3 3                     | Interval 48                  | Dip   |
|  |                              | 18 21 20  |
| Green. date, April 14 4 55 24              |                              | — 3 19  |
|  | $4 \frac{1}{10} \frac{1}{4}$ | 18 18 1   |
|  | 1                            | — 2 42  |
|  |                              | 18 15 19  |
| By Raper: Index corr. + $55''$ ,           | 6,018,31                     | Corr. alt. — 2 42                               |
| Dip — $3' 20''$ , refr. — $2' 55''$ , par. | 3 31                         | Semid. + 15 58                                  |
| + $8''$ , semid. + $15' 58''$ , true alt.  |                              | True alt. 18 31 17                              |
| $18^{\circ} 31' 11''$ .                    |                              |   |

| Decl., page II, N.A.                                | H.D.            | Eq. T., page II, N.A.                                  | H.D.                    |
|---|-----------------|--|-------------------------|
| Ap. 14th, noon $9^{\circ} 38' 12''$ N. <i>incr.</i> | + 53'73         | 14th, noon, <i>add</i> $0^m 8^s \cdot 52$ <i>decr.</i> | 0'627                   |
| Correction + 4 23                                   | × 4'9           | Correction — 3'07                                      | × 4'9                   |
| Red. decl. $9^{\circ} 42' 35''$ N.                  | 6,026,3277      | Red. Eq. T. $0^h 5'45^s$                               | 3'0723                  |
|   | + 4 23 corr.    | (To be added to A.T.)                                  |                         |
| Polar dist. $80^{\circ} 17' 25''$                   |                 | App. T. ship, April                                    | $13^d 19^h 11^m 3^s$    |
| Altitude $18^{\circ} 31' 17''$                      |                 | Eq. time   | + 5                     |
| Latitude $52^{\circ} 10' 0''$                       | sec. 0.212280   | Mean T. ship, April                                    | 13 19 11 8              |
| Polar dist. $80^{\circ} 17' 25''$                   | cosec. 0'006267 | Mean T. Green., April                                  | 14 4 55 24              |
| $150^{\circ} 58' 42''$                              |                 | Longitude in time                                      | 9 44 16                 |
| $75^{\circ} 29' 21''$                               | cos. 9'398917   | Longitude  | $146^{\circ} 4' 0''$ W. |
| $56^{\circ} 58' 4''$                                | sine 9'923432   |  |                         |
| Hour-angle $4^h 48^m 57^s$                          | log. 9'540896   |  |                         |
| 24  |                 |  |                         |

By Raper: Log. sine sq.  $9'540927$  gives  
Hour-angle  $4^h 48^m 57^s$ . Long.  $146^{\circ} 4' 0''$  W.

A.T.S. Ap.  $13^d 19 11 3$

The observation having been made A.M. at ship, the hour-angle is the time *before noon at ship*, viz., April 14<sup>h</sup>; therefore take the hour-angle from 24<sup>h</sup>, and the remainder is apparent time at ship reckoned from the noon preceding, viz., April 13<sup>h</sup>. The mean time at Greenwich is in *advance* of mean time at ship, therefore subtract the latter from the former (borrowing 24<sup>h</sup> to enable the subtraction to be made).

Ex. 5. 1876, March 6th, P.M. at ship, latitude 40° 20' S., obs. alt. sun's L.L. 16° 20', index corr. + 30", height of eye 18 feet, time by a chronometer 5<sup>d</sup> 20<sup>h</sup> 10<sup>m</sup>, (being 6<sup>d</sup> 8<sup>h</sup> 10<sup>m</sup> A.M. at Greenwich), which was 6<sup>m</sup> 14<sup>s</sup> *fast* for mean noon at Greenwich, January 30th, and on February 13th was *fast* 4<sup>m</sup> 29<sup>s</sup> for mean time at Greenwich.

|                                       |                                |                                   |
|---------------------------------------|--------------------------------|-----------------------------------|
| January 30th, chronometer <i>fast</i> | 6 <sup>m</sup> 14 <sup>s</sup> | 1 45                              |
| Feb. 13th, " <i>fast</i>              | 4 29                           | 60                                |
| Change in 14 days.                    | 1 45                           | 14)105(7.5<br>98<br>70<br>70<br>— |

|   |  |                    |                    |
|---|--|--------------------|--------------------|
| T. by chron. March 5 <sup>d</sup> 20 <sup>h</sup> 10 <sup>m</sup> 0 <sup>s</sup>                                  | Interval from Feb. 13th to Mar. 5th, 20 <sup>h</sup> | Obs. alt. ☉'s L.L. | 16° 20' 0"         |
| Original error — 4 29   | is 21 <sup>d</sup> 20 <sup>h</sup> .                 | Index corr.        | + 30               |
| Accumulated rate 5 20 5 31<br>+ 2 44  | Rate 7 <sup>m</sup> 5 21                             | Dip                | 16 20 30<br>— 4 4  |
| Green. date March 5 20 8 15   | 12   1/2   157.5<br>8   3/4   3.7<br>2.5             | Corr. alt.         | 16 16 26<br>— 3 5  |
| By Raper: Index corr. + 30",<br>dip — 4' 10", refr. 3' 18", par. + 8",<br>semid. + 16' 9", true alt. 16° 29' 19". | 6,0)16,3.7<br>2 43.7                                 | Semid.             | 16 13 21<br>+ 16 9 |
|   |  | True alt.          | 16 29 30           |

|                         |               |   |       |
|-------------------------|---------------|---|-------|
| Decl., page II, N.A.    | H.D.          | Eq. time, page II, N.A.                       | H.D.  |
| 6th noon, 5° 24' 35" S. | — 58.23       | 6th noon + 11 <sup>m</sup> 20 <sup>s</sup> .4 | 0.604 |
| Correction + 3 45       | 3.87          | Correction + 2.4                              | × 4   |
| Red. decl. 5 28 20 S.   | 6,0)22,5.3501 | Red. Eq. time 11 22.8                         | 2.416 |
| Polar dist. 84 31 40    | Corr + 3 45   | (To be added to A.T.)                         |       |

Declination and equation of time are both taken out for the nearest noon at Greenwich, viz., 6th, and corrected for the time wanting to noon, that is, for 3<sup>h</sup> 52<sup>m</sup> or 3<sup>h</sup> 87.

|   |   |
|---|---|
| Altitude 16° 29' 30"  | A.T. ship, March 6 <sup>d</sup> 4 <sup>h</sup> 51 <sup>m</sup> 54 <sup>s</sup>    |
| Latitude 40 20 0 sec. 0.117879  | Equation time + 11 23   |
| Polar dist. 84 31 40 cosec. 0.001984  | M.T. ship, March 6 5 3 17   |
| 141 21 10   | M.T. Green., March 5 20 8 15  |
| 70 40 35 cosin. 9.519701  | Longitude in time 8 55 2  |
| 54 11 5 sine 9.908972   | Longitude 133° 45' 30" E.   |
| A.T.S. Mar. 6 <sup>d</sup> 4 <sup>h</sup> 51 <sup>m</sup> 54 <sup>s</sup> log. 9.548536 | By Raper: Log. sin. sq. 9.548579 gives  |
|   | hour-angle 4 <sup>h</sup> 51 <sup>m</sup> 55 <sup>s</sup> , long. 133° 45' 45" E. |

The observation having been made P.M. at ship, the hour-angle is the app. time at ship, before which write the date at ship, viz., March 6th: then mean time at ship being one day in advance of mean time at Greenwich, we subtract the latter from mean time at ship (borrowing 24<sup>h</sup>) to enable us to complete the subtraction.

Ex. 6. 1876, November 19th, A.M. at ship, latitude 39° 20' S., obs. alt. sun's L.L. 34° 37' 55", index corr. + 1' 10", height of eye 14 feet, time by chronometer 18<sup>d</sup> 23<sup>h</sup> 49<sup>m</sup> 32<sup>s</sup> (or 19<sup>d</sup> 11<sup>h</sup> 49<sup>m</sup> 32<sup>s</sup> A.M.), which was *slow* 56<sup>m</sup> 57<sup>s</sup> .1 for mean noon at Greenwich, September 1st, and on September 19th was 58<sup>m</sup> 52<sup>s</sup> .3 *slow* on Greenwich mean time.

|  |  |  |  |                      |
|--|--|--|--|----------------------|
| Sept. 1st, chronometer <i>slow</i>       | 56 <sup>m</sup> 57 <sup>s</sup> ·1                                       | 1 55 <sup>s</sup> ·2   |  |                      |
| Sept. 19th, „ <i>slow</i>                | 58 52 <sup>s</sup> ·3  | 60   |  |                      |
| Change in 18 days                        | 1 55 <sup>s</sup> ·2   | 18) 115 <sup>s</sup> ·2 (6 <sup>s</sup> ·4                                     |  |                      |
|  |  | 108  |  |                      |
|  |  | 72   |  |                      |
|  |  | 72   |  |                      |
| T. by chron. Nov.                        | 18 <sup>d</sup> 23 <sup>h</sup> 49 <sup>m</sup> 32 <sup>s</sup>          | Sept. 30 days  | Obs. alt. ☉'s L.L.                           | 34° 37' 55"          |
| Original error                           | + 58 52 <sup>s</sup> ·3  | 19   | Index error                                  | + 1 10               |
|  | 18 24 48 24 <sup>s</sup> ·3  | Sept. 11   |  | 34 39 5              |
| or                                       | 19 0 48 24 <sup>s</sup> ·3   | Oct. 31  | Dip for 14 feet                              | — 3 36               |
| Accumulated rate                         | + 6 30 <sup>s</sup> ·6   | Nov. 19 1 <sup>h</sup> nearly  |  | 34 35 29             |
| Green. date Nov.                         | 19 0 54 54 <sup>s</sup> ·9   | Intr. 61 1   | Corr. altitude                               | — 1 15               |
|  |  | Daily rate 6 <sup>s</sup> ·4   |  | 34 34 14             |
|  |  | Interval 61  | Semi-diameter                                | + 16 14              |
|  |  | 390 <sup>s</sup> ·4  |  | 34 50 28             |
| By Raper: index cor. + 1' 10", dip       |  | Prop. par. 1 <sup>h</sup> 2  | True altitude                                |                      |
| — 3' 40", ref. — 1' 25", par. + 7",      |  | 6,0) 39,06   |  |                      |
| semid. + 16' 14", true alt. 34° 50' 21", |  |  |  |                      |
|  |  | Acc. rate 6 30 <sup>s</sup> ·6   |  |                      |
| Decl. page II, N.A.                      | H.D.   | Eq. T. page II, N.A.   | H.D.   |                      |
| Nov. 19th noon, 19° 37' 44" S.           | + 34 <sup>s</sup> ·39  | Nov. 19th noon <i>sub.</i> 14 <sup>m</sup> 19 <sup>s</sup> ·57                 | — 0 <sup>s</sup> ·594                        |                      |
| Correction                               | + 31   | Correction   | — 53   | × 9                  |
| Red. decl.                               | 19 38 15 S.  | Red. Eq. T.  | 14 19 <sup>s</sup> ·04                       | 0 <sup>s</sup> ·5346 |
|  | 30 <sup>s</sup> ·951   | (To be <i>subt.</i> from A.T.)   |  |                      |
| Polar dist.                              | 70 21 45   |  |  |                      |
| Altitude                                 | 34° 50' 28"  | Hour-angle   | 4 <sup>h</sup> 2 <sup>m</sup> 9 <sup>s</sup> |                      |
| Latitude                                 | 39 20 0 sec. 0 <sup>s</sup> ·111556                                      |  | 24   |                      |
| Polar dist.                              | 70 21 45 cosec. 0 <sup>s</sup> ·026025                                   | App. T. ship, Nov. 18 <sup>d</sup>   | 19 57 51                                     |                      |
|  | 144 32 13  | Eq. Time   | — 14 19                                      |                      |
|  | 72 16 6 cos. 9 <sup>s</sup> ·483672                                      | Mean T. ship, Nov. 18 <sup>d</sup>   | 19 43 32                                     |                      |
|  | 37 25 38 sine 9 <sup>s</sup> ·783727                                     | Mean T. Green, Nov. 19 <sup>d</sup>  | 0 54 55                                      |                      |
| Hour-angle                               | 4 <sup>h</sup> 2 <sup>m</sup> 9 <sup>s</sup> log. 9 <sup>s</sup> ·404980 | Longitude in time  | 5 11 23                                      |                      |
|  |  | Longitude  | 77° 50' 45" W.                               |                      |
|  |  | By Raper: Log. sin. sq. 9 <sup>s</sup> ·405015, gives                          |  |                      |
|  |  | Hour-angle 4 <sup>h</sup> 2 <sup>m</sup> 10 <sup>s</sup> , Long. 77° 51' 0" W. |  |                      |

In this example, the observation is made A.M. at ship, the hour-angle is therefore the *time before noon*, Nov. 19<sup>d</sup>, and since all our computations are made in astronomical time—which dates from noon—we take the hour-angle from 24<sup>h</sup>, which gives apparent time at ship reckoned from noon of the preceding day. The mean time at ship and mean time at Greenwich are of different dates, mean time at Greenwich being more advanced, take the mean time at ship from mean time at Greenwich, borrowing 24<sup>h</sup> to enable the subtraction to be made.

Ex. 7. 1876, June 15th, P.M. at ship, latitude 13° 54' S., obs. alt. sun's L.L. 16° 16' 16", index cor. + 0' 16", height of eye 16 feet, time by a chronometer 15<sup>d</sup> 0<sup>h</sup> 16<sup>m</sup> 16<sup>s</sup> (or 0<sup>h</sup> 16<sup>m</sup> 16<sup>s</sup> P.M.) which was 2<sup>h</sup> 13<sup>m</sup> 37<sup>s</sup> *fast* for mean noon at Greenwich, April 1st, and on April 16th was 2<sup>h</sup> 16<sup>m</sup> 16<sup>s</sup> *fast* on mean time at Greenwich.

|                                    |  |                             |
|------------------------------------|--|-----------------------------|
| April 1st, chronometer <i>fast</i> | 2 <sup>h</sup> 13 <sup>m</sup> 37 <sup>s</sup> | 2 39                        |
| 16th, „ <i>fast</i>                | 2 16 16  | 60                          |
| Change in 15 days                  | 2 39   | 15) 159 (10 <sup>s</sup> ·6 |
| Daily rate                         | 10 <sup>s</sup> ·6 <i>gaining</i> .            | 15                          |
|                                    |  | 90                          |
|                                    |  | 90                          |

|   |  |                    |             |
|---|--|--------------------|-------------|
| T. by chron., June 15 <sup>d</sup> 0 <sup>h</sup> 16 <sup>m</sup> 16 <sup>s</sup> | Interval from  | Obs. alt. ☉'s L.L. | 16° 16' 16" |
| Original error — 2 16 16  | April 16 <sup>th</sup> to June 14 <sup>th</sup> 22 <sup>h</sup> , is 59 <sup>d</sup> 22 <sup>h</sup> . | Index corr.        | + 0 16      |
| Accumulated rate — 14 22 0 0  | Daily rate 10'6  | 16 feet            | 16 16 32    |
| Green. date, June 14 21 49 25   | Interval 59  | Corr. altitude     | — 3 50      |
|   | 954  |                    | 16 12 42    |
|   | 530  |                    | — 3 5       |
| By Raper: Index corr. + 0' 16",   | 12   1/2   625'4   | Semi-diameter      | 16 9 37     |
| dip — 4' 0", refr. — 3' 18", par.   | 8   1/2   5'3  |                    | + 15 47     |
| + 8", semid. + 15' 47", true alt.   | 2   1/2   3'5  | True altitude      | 16 25 24    |
| 16° 25' 9".   |  |                    |             |

6,0)63,5'1

10 35'1

|   |        |   |                  |
|---|--------|---|------------------|
| Decl., page II, N.A.                        | H.D.   | Eq. T., page II, N.A.   | H.D.             |
| June 15 <sup>th</sup> , noon 23° 20' 58" N. | 5'79   | 15 <sup>th</sup> , noon, add 0 <sup>m</sup> 14 <sup>s</sup> 7 | + 0' 532         |
| Correction — 13                             | 2'2    | Correction — 1'1  | X 2 <sup>h</sup> |
| Red. decl. 23 20 45 N.                      | 1158   | Red. Eq. T. 0 13'6  | 1'064            |
| Polar dist. 113 20 45                       | 1158   | (To be added to A.T.)   |                  |
|   | 12'738 |   |                  |

|   |   |
|---|---|
| Altitude 16° 25' 24"  | App. time at ship, June 15 <sup>d</sup> 4 <sup>h</sup> 19 <sup>m</sup> 38 <sup>s</sup>                                |
| Latitude 13 54 0 sec. 0'012908  | Equation time + 0 14  |
| Polar dist. 113 20 45 cossec. 0'037096                                  | Mean time at ship, June 15 4 19 52  |
| 143 40 9  | Mean time at Green. June 14 21 49 25  |
| 71 50 4 cos. 9'493825   | Longitude in time 6 30 27   |
| 55 24 40 sine 9'915530  | Longitude 97° 36' 45" E.  |
| Hour-angle 4 <sup>h</sup> 19 <sup>m</sup> 38 <sup>s</sup> log. 9'459359 | By Raper: Log. sine sq. 9'459415, Hour-angle 4 <sup>h</sup> 19 <sup>m</sup> 39 <sup>s</sup> . Longitude 97° 37' 0" E. |

In this example the observation is made P.M.: hence the hour-angle is apparent time at ship, before which we write the date at ship, viz., June 15<sup>th</sup> (see head of question); and since the mean time at ship is June 15<sup>th</sup> 4<sup>h</sup> 19<sup>m</sup> 52<sup>s</sup>, which is in advance of mean time at Greenwich, the latter being June 14<sup>th</sup> 21<sup>h</sup> 49<sup>m</sup> 25<sup>s</sup>; we subtract mean time at ship from mean time at Greenwich, and 24<sup>h</sup> is borrowed from subtracting.

Ex. 8. 1876, September 23<sup>rd</sup>, A.M. at ship, latitude 59° 30' N., observed altitude sun's L.L. 10° 50' 10", index correction + 6' 10", height of eye 18 feet, time by chronometer 22<sup>d</sup> 11<sup>h</sup> 44<sup>m</sup> 20<sup>s</sup> (or 22<sup>d</sup> 11<sup>h</sup> 44<sup>m</sup> 20<sup>s</sup> P.M.) which was 35<sup>m</sup> 19<sup>s</sup> fast for mean noon at Greenwich, July 14<sup>th</sup>, and on August 13<sup>th</sup> was 30<sup>m</sup> 4<sup>s</sup> fast on Greenwich mean time.

July 14<sup>th</sup> fast 35<sup>m</sup> 19<sup>s</sup>  
August 13<sup>th</sup> fast 30 4

July 31

14

Change in 30 days 5 15

17

Aug. 13

Daily rate 10'5

Interval 30

|  |  |                    |             |
|--|--|--------------------|-------------|
| T. by chron. Sept. 22 <sup>d</sup> 11 <sup>h</sup> 44 <sup>m</sup> 20 <sup>s</sup> | Interval from  | Obs. alt. ☉'s L.L. | 10° 50' 10" |
| Original error — 30 4  | Aug. 13 <sup>th</sup> to Sept. 22 <sup>nd</sup> , 11 <sup>h</sup> , is 40 <sup>d</sup> 11 <sup>h</sup> | Index corr.        | + 6 10      |
| Accumulated rate 22 11 14 16   | Daily rate 10'5  | Dip                | 10 56 20    |
| Green. date, Sept. 22 11 21 21   | 40   | Corr. alt.         | — 4 4       |
|  | 8 <sup>h</sup>   1/2   420'0   |                    | 10 52 16    |
|  | 3   1/2   3'5  |                    | — 4 42      |
|  | 1'3  |                    |             |
| By Raper: Index corr. + 6' 10",  | 6,0)42,4'8   | Semi-diameter      | 10 47 34    |
| dip — 4' 10", refr. — 4' 56", par. +   |  |                    | + 15 59     |
| 8", semid. + 15' 59", true alt. 11° 3' 21"   | 7 4'8  | True altitude      | 11 3 33     |

| Decl. page II, N.A.                     | H.D.                         | Eq. T. page II, N.A.           | H.D.                     |
|---|------------------------------|--------------------------------|--------------------------|
| Sept. 22nd, noon $0^{\circ} 4' 51''$ N. | — $58^{\circ} 50'$           | 22nd, noon $7^m 30^s 2$        | + $0^s 866$              |
| Correction — $11 4$                     | $11^h 20^m = 11^{\circ} 35'$ | Correction + $9^{\circ} 8'$    | $11^{\circ} 35'$         |
| Red. decl. $0 6 13$ S.                  | $6,0)66,3)9750$              | Red. Eq. T. $7 40^{\circ} 0$   | $9^{\circ} 829 10$       |
|   |                              | (To be <i>subt.</i> from A.T.) |                          |
| Polar dist. $90 6 13$                   | $11^{\circ} 4''$             | Hour-angle                     | $4^h 30^m 25^s$          |
| Altitude $11^{\circ} 3' 33''$           |                              |                                | $24$                     |
| Latitude $59 30 0$ sec.                 | $0^{\circ} 294531$           | App. T. at ship, Sept.         | $22^d 19 29 35$          |
| Polar dist. $90 6 13$ cosec.            | $0^{\circ} 000001$           | Equation of Time               | — $7 40$                 |
| $160 39 46$                             |                              | Mean T. at ship, Sept.,        | $22 19 21 55$            |
| $80 19 53$ cos.                         | $9^{\circ} 225178$           | Mean T. at Green., Sept.,      | $22 11 21 21$            |
| $69 16 20$ sine                         | $9^{\circ} 970938$           | Longitude in time              | $8 0 34$                 |
| Hour-angle $4^h 30^m 25^s$ log.         | $9^{\circ} 490648$           | Longitude                      | $120^{\circ} 8' 30''$ E. |

Ex. 9. 1876, June 23rd P.M. at ship, latitude  $0^{\circ}$ , observed altitude sun's L.L.  $20^{\circ} 25'$ , height of eye 20 feet, time by chronometer June 23<sup>d</sup> 6<sup>h</sup> 4<sup>m</sup> 40<sup>s</sup>, which was *fast*  $13^m 11^s$  on Greenwich mean time, April 6th, and on May 1st, was  $12^m 1^s$  *fast* for mean noon at Greenwich.

Interval from April 6th to May 1st is 25 days; the change in rate in that time is  $70^s$ : then  $70^s \div 25 = 2^s 8$  *losing*.

|   |  |                           |                      |
|---|--|---------------------------|----------------------|
| T. of chron., Jan. $23^d 6^h 4^m 40^s$                                | Interval from May 1st to June 23rd, 6 <sup>h</sup> , is $53^d 6^h$ | Obs. alt. $\odot$ 's L.L. | $20^{\circ} 25' 0''$ |
| Original error — $12 1$   | Daily rate $2^s 8$   | Dip                       | — $4 17$             |
| Acc. rate $23 5 52 39$  | Interval $53$  | Corr. alt.                | $20 20 43$           |
|   |  |                           | — $2 25$             |
| Green. date, June $23 5 55 8$   | $84$   | Semi-diameter             | $20 18 18$           |
|   | $140$  |                           | + $15 46$            |
| By Raper: dip — $4' 20''$ , refr. — $2' 36''$                         |  | True altitude             | $20 34 4$            |
| par. + $8''$ , semid. + $15' 46''$ , and true $6 \frac{1}{4}   148.4$ |  |                           |                      |
| alt. $20^{\circ} 33' 58''$ .  | $7$  |                           |                      |

$6,0)14,971$

$2 29^{\circ} 1'$

| Decl. page II, N.A.                | H.D.               | Eq. T. page II, N.A.               | H.D.               |
|------------------------------------|--------------------|------------------------------------|--------------------|
| 23rd noon $23^{\circ} 26' 17''$ N. | $2^{\circ} 48'$    | 23rd noon $1^m 58^s 8$             | $540$              |
| Correction — $15$                  | $5^{\circ} 9'$     | Correction $3^{\circ} 2'$          | $5^{\circ} 9'$     |
| Red. decl. $23 26 2$ N.            | $2232$             | Red. Eq. T.                        | $2 2^{\circ} 0$    |
|                                    | $1240$             | (Added to A.T.)                    |                    |
| Polar dist. $66 33 58$             | $14^{\circ} 632$   |                                    | $3^{\circ} 1860$   |
| Altitude $20^{\circ} 34' 4''$      |                    | Altitude $20^{\circ} 34' 4''$      |                    |
| Latitude $0 0 0$ sec.              | $0^{\circ} 000000$ | Latitude $0 0 0$ sec.              | $0^{\circ} 000000$ |
| Polar dist. $66 33 58$ cosec.      | $0^{\circ} 037385$ | Polar dist. $113 26 2$ cosec.      | $0^{\circ} 037385$ |
| $87 8 2$                           |                    | $134 0 6$                          |                    |
| $43 34 1$ cos.                     | $9^{\circ} 860080$ | $67 0 3$ cos.                      | $9^{\circ} 591863$ |
| $22 59 57$ sine                    | $9^{\circ} 591863$ | $46 25 59$ sine                    | $9^{\circ} 860080$ |
| Hour-angle $4^h 29^m 57^s$ log.    | $9^{\circ} 489328$ | Hour-angle $4^h 29^m 57^s$ log.    | $9^{\circ} 489328$ |
| Eq. T. $+ 2 2$                     |                    | Eq. T. $+ 2 2$                     |                    |
| M. T. S. $23^d 4 31 59$            |                    | M. T. S. $23^d 4 31 59$            |                    |
| M. T. G. $23^d 5 55 8$             |                    | M. T. G. $23^d 5 55 8$             |                    |
| Long. in T. $1 23 9$               |                    | Long. in T. $1 23 9$               |                    |
| Longitude $20^{\circ} 47' 15''$ W. |                    | Longitude $20^{\circ} 47' 15''$ W. |                    |

By Raper the answer comes out the same.



Ex. 10. 1876, Sept. 22nd, P.M. at ship, lat.  $0^{\circ} 0'$ , obs. alt. sun's L.L.  $28^{\circ} 52'$ , height of eye 17 feet, time by chronometer Sept. 22<sup>d</sup> 4<sup>h</sup> 59<sup>m</sup> 41<sup>s</sup>, which was *slow* 15<sup>s</sup> on Greenwich mean time, April 30th, and on June 1st was *fast* 10<sup>m</sup> 6 on Greenwich mean time.

|  |          |    |
|--|----------|----|
| April 30th, chronometer <i>slow</i> 0 <sup>m</sup> 15 <sup>s</sup> | April    | 30 |
| June 1st, „ <i>fast</i> 0 10 <sup>m</sup> 6                        |          | 30 |
| Change in 32 days  |          | 0  |
| Daily rate   |          | 31 |
|  | May      | 31 |
|  | June     | 1  |
|  | Interval | 32 |

|   |          |     |                               |
|---|----------|-----|-------------------------------|
| T. by chronometer, Sept. 22 <sup>d</sup> 4 <sup>h</sup> 59 <sup>m</sup> 41 <sup>s</sup> | June     | 30  | Interval 113 days.            |
| Original error — 10 <sup>m</sup> 6  |          | 1   | Rate 0 <sup>m</sup> 8         |
| Accumulated rate 22 <sup>d</sup> 4 59 30 <sup>m</sup> 4                                 | July     | 29  | 6,0)9,0 <sup>m</sup> 4        |
| Greenwich date, Sept. 22 4 58 0   | Aug.     | 31  | Acc. rate 1 30 <sup>m</sup> 4 |
| or, 4 <sup>h</sup> 97   | Sept.    | 22  |                               |
|   | Interval | 113 |                               |

|   |                            |   |                    |
|---|----------------------------|---|--------------------|
| Decl., page II, N.A.                                    | H.D.                       | Fq. T.  | H.D.               |
| Sept. 22nd, $0^{\circ} 4' 50'' \cdot 5$ N. <i>decr.</i> | — 58 <sup>m</sup> 50       | Sept. 22nd, <i>sub.</i> 7 <sup>m</sup> 30 <sup>s</sup> 21 | 0 <sup>m</sup> 866 |
| Corr. for 5 <sup>h</sup> 89 — 4 50 <sup>m</sup> 7       | 4 <sup>m</sup> 97          | Corr. 5 <sup>h</sup> 9 + 4 <sup>m</sup> 33                | 5 <sup>m</sup>     |
| Red. decl. 0 0 0  | 6,0)29,0 <sup>m</sup> 7450 | Red. Eq. T. 7 34 <sup>m</sup> 54                          | 4 <sup>m</sup> 330 |
|   | 4 50 <sup>m</sup> 7        | (To be <i>subt.</i> from A.T.)                            |                    |

|   |                                    |   |   |
|---|------------------------------------|---|---|
| Obs. alt. sun's L.L.  | 28 <sup>o</sup> 52' 0 <sup>o</sup> | App. T. ship, Sept.   | 22 <sup>d</sup> 4 <sup>h</sup> 3 <sup>m</sup> 50 <sup>s</sup> 2 |
| Dip — 3 57  |                                    | Eq. T.  | — 7 34 <sup>m</sup> 5   |
| Corr. altitude 28 48 3                                      |                                    | Mean T. ship, Sept.   | 22 <sup>d</sup> 3 56 15 <sup>m</sup> 7                          |
| Semi-diameter + 1 35  |                                    | Mean T. Green., Sept.   | 22 <sup>d</sup> 4 58 0 <sup>m</sup> 0                           |
| True alt. 28 46 28  |                                    | Long. in time   | 1 1 44 <sup>m</sup> 3   |
| Zenith distance 60 57 33*                                   |                                    | Longitude   | 15 <sup>o</sup> 26' 4 <sup>o</sup> W.                           |
| Do. in time 4 <sup>h</sup> 3 <sup>m</sup> 50 <sup>s</sup> 2 |                                    | By Raper: True alt. 29 <sup>o</sup> 2' 16 <sup>m</sup> , whence                 |   |
|   |                                    | H.A. (or zen. dist.) in time = 4 <sup>h</sup> 3 <sup>m</sup> 50 <sup>s</sup> 9. |   |
|   |                                    | Long. 15 <sup>o</sup> 25' 54 <sup>m</sup> W.                                    |   |

Ex. 11. 1876, October 10th, P.M. at ship, latitude at noon  $20^{\circ} 41' S.$ , ship had sailed N.E. (true) 54 miles since noon, obs. alt. sun's L.L.  $18^{\circ} 45'$ , height of eye 15 feet, time by chronometer October 9<sup>d</sup> 16<sup>h</sup> 28<sup>m</sup> 42<sup>s</sup>, which was *slow* 11<sup>m</sup> 44<sup>s</sup> on mean time at Greenwich, August 26th, and on September 10th was *slow* 10<sup>m</sup> 26<sup>s</sup>: required the longitude at time of observation, and also at noon.

To find the difference of latitude and difference of longitude.—The course 4 points and distance 54 miles give diff. lat.  $38^{\circ} 2'$  and dep.  $38^{\circ} 2'$ . The diff. of lat. is named North, because the ship at the time of sights was to the north of the position at noon; and is subtracted from the lat. at noon, viz.,  $20^{\circ} 41' S.$  to get the lat. at sights, the result is  $20^{\circ} 2' 48'' S.$ , and the dep. is named East, because the ship at the time of sights was to the east of the position at noon. The mid. lat.  $20^{\circ} 22'$  as a course, and dep.  $38^{\circ} 2'$  as a diff. lat., give the distance 41' as diff. of long. and is named East, because the ship at time of sights is east of her position at noon.

\* Both latitude and declination being 0, the zenith distance converted into time is the hour-angle.

The daily rate is  $5^{\text{m}} 2^{\text{s}}$  *gaining*; the interval  $29^{\text{d}} 16^{\text{h}} \times 5^{\text{m}} 2^{\text{s}}$  gives accumulated rate  $2^{\text{m}} 34^{\text{s}} 3$ ; Greenwich date October  $9^{\text{d}} 16^{\text{h}} 36^{\text{m}} 34^{\text{s}}$ ; polar distance  $83^{\circ} 14' 2''$ ; red. eq. T.  $13^{\text{m}} 2^{\text{s}} 25$  *subt.* from A.T.; true alt. (Norie)  $18^{\circ} 54' 43''$ ; latitude in at sights  $20^{\circ} 2' 48''$  S.; hour-angle  $4^{\text{h}} 49^{\text{m}} 10^{\text{s}}$ ; mean time at ship October  $10^{\text{d}} 4^{\text{h}} 36^{\text{m}} 8^{\text{s}}$ ; long. at time of observation  $179^{\circ} 53' 30''$  E.; diff. long.  $41$ ; also longitude at noon  $179^{\circ} 25' 30''$  W.

### EXAMPLES FOR PRACTICE.

Ex. 1. 1876, January 2nd, A.M. at ship, latitude  $36^{\circ} 59' \text{ S.}$ , observed altitude sun's L.L.  $49^{\circ} 10'$ , index correction —  $2' 40''$ , height of eye 14 feet, time by a chronometer  $1^{\text{d}} 19^{\text{h}} 8^{\text{m}} 50^{\text{s}}$  (being  $7^{\text{h}} 8^{\text{m}} 50^{\text{s}}$  A.M. at Greenwich), which was *slow*  $18^{\text{m}} 2^{\text{s}}$  for mean noon at Greenwich, November 30th, 1875, and on December 7th was  $19^{\text{m}} 10^{\text{s}} 6$  *slow* for mean time at Greenwich: required the longitude.

Ex. 2. 1876, February 19th, A.M. at ship, latitude  $38^{\circ} 18' \text{ S.}$ , observed altitude sun's L.L.  $21^{\circ} 30' 40''$ , index correction —  $6' 45''$ , height of eye 14 feet, time by a chronometer  $18^{\text{d}} 19^{\text{h}} 53^{\text{m}} 37^{\text{s}} 6$  (being  $7^{\text{h}} 53^{\text{m}} 37^{\text{s}} 6$  A.M. at Greenwich), which was  $4^{\text{m}} 16^{\text{s}} 6$  *fast* for mean noon at Greenwich, January 23rd, and on January 30th was  $5^{\text{m}} 9^{\text{s}} 8$  *fast* for mean time at Greenwich.

Ex. 3. 1876, March 28th, P.M. at ship, latitude  $20^{\circ} 19' \text{ S.}$ , observed altitude sun's L.L.  $30^{\circ} 14'$ , index correction —  $2' 10''$ , height of eye 30 feet, time by chronometer  $28^{\text{d}} 0^{\text{h}} 10^{\text{m}}$  (being  $0^{\text{h}} 10^{\text{m}}$  P.M. at Greenwich), which was  $54^{\text{m}} 48^{\text{s}}$  *fast* for mean noon at Greenwich, October 20th, 1875, and on December 2nd, 1875, was  $51^{\text{m}} 56^{\text{s}}$  *fast* for mean noon at Greenwich.

Ex. 4. 1876, April 6th, A.M. at ship, latitude  $53^{\circ} 5' \text{ N.}$ , observed altitude sun's L.L.  $16^{\circ} 8' 40''$ , index correction —  $40''$ , height of eye 15 feet, time by a chronometer  $5^{\text{d}} 19^{\text{h}} 18^{\text{m}} 49^{\text{s}}$  (being  $7^{\text{h}} 18^{\text{m}} 49^{\text{s}}$  A.M. at Greenwich), which was  $0^{\text{m}} 4^{\text{s}} 4$  *slow* for mean noon at Greenwich, February 11th, and on March 11th was  $2^{\text{m}} 38^{\text{s}}$  *fast* for mean noon at Greenwich.

Ex. 5. 1876, May 19th, P.M. at ship, latitude  $2^{\circ} 58' \text{ S.}$ , obs. alt. sun's L.L.  $30^{\circ} 30'$ , index correction  $+ 52''$ , height of eye 19 feet, time by chronometer  $19^{\text{d}} 0^{\text{h}} 23^{\text{m}} 58^{\text{s}}$ , which was  $28^{\text{s}}$  *fast* for mean noon at Greenwich, January 3rd, and on January 31st was  $42^{\text{s}}$  *slow* on mean time at Greenwich.

Ex. 6. 1876, June 15th, A.M. at ship, latitude  $12^{\circ} 11' \text{ N.}$ , observed altitude sun's L.L.  $39^{\circ} 39' 40''$ , index correction  $+ 20''$ , height of eye 17 feet, time by a chronometer  $14^{\text{d}} 17^{\text{h}} 59^{\text{m}} 30^{\text{s}}$  (being  $5^{\text{h}} 59^{\text{m}} 30^{\text{s}}$  A.M. at Greenwich), which was *slow*  $5^{\text{m}} 56^{\text{s}} 3$  for mean time at Greenwich, April 20th, and on May 12th was  $2^{\text{m}} 29^{\text{s}} 5$  *slow* for mean noon at Greenwich.

Ex. 7. 1876, July 5th, A.M. at ship, latitude  $23^{\circ} 48' \text{ N.}$ , observed altitude sun's L.L.  $48^{\circ} 36' 50''$ , index correction —  $50''$ , height of eye 17 feet, time by chronometer  $5^{\text{d}} 0^{\text{h}} 42^{\text{m}} 38^{\text{s}}$  (being  $0^{\text{h}} 42^{\text{m}} 38^{\text{s}}$  P.M. at Greenwich), which was *fast*  $4^{\text{m}} 47^{\text{s}} 8$  for mean noon at Greenwich, May 6th, and on June 1st was *fast*  $6^{\text{m}} 50^{\text{s}}$  for mean noon at Greenwich.

Ex. 8. 1876, August 13th, A.M. at ship, latitude  $30^{\circ} 46' \text{ S.}$ , observed altitude sun's L.L.  $27^{\circ} 15'$ , index correction —  $1' 15''$ , height of eye 21 feet, time by a chronometer  $13^{\text{d}} 2^{\text{h}} 0^{\text{m}}$  (being  $2^{\text{h}} 0^{\text{m}}$  P.M. at Greenwich), which was *slow*  $26^{\text{m}} 7^{\text{s}} 6$  for mean noon at Greenwich, April 10th, and on May 1st, was *slow*  $25^{\text{m}} 13^{\text{s}}$  for mean noon at Greenwich.

Ex. 9. 1876, September 1st, P.M. at ship, latitude  $35^{\circ} 49' \text{ N.}$ , observed altitude sun's L.L.  $44^{\circ} 32' 10''$ , index correction  $+ 1' 46''$ , height of eye 20 feet, time by chronometer August  $31^{\text{d}} 19^{\text{h}} 24^{\text{m}} 57^{\text{s}}$  (being  $7^{\text{h}} 24^{\text{m}} 57^{\text{s}}$  A.M. at Greenwich), which was *fast*  $11^{\text{m}} 57^{\text{s}} 4$  for mean noon at Greenwich, July 3rd, and on July 31st was *fast*  $12^{\text{m}} 17^{\text{s}}$  for mean noon at Greenwich.

Ex. 10. 1876, October 25th, P.M. at ship, latitude  $51^{\circ} 30' \text{ S.}$ , observed altitude sun's L.L.  $40^{\circ} 22'$ , index correction —  $1' 50''$ , eye 20 feet, time by chronometer  $25^{\text{d}} 8^{\text{h}} 22^{\text{m}} 1^{\text{s}}$  (or  $8^{\text{h}} 22^{\text{m}} 1^{\text{s}}$  P.M.), which was *slow*  $24^{\text{m}} 8^{\text{s}} 2$  for mean noon at Greenwich, June 14th, and on July 20th was *slow*  $21^{\text{m}} 19^{\text{s}}$  for mean noon at Greenwich.

Ex. 11. 1876, November 27th, A.M. at ship, latitude  $39^{\circ} 20' S.$ , observed altitude sun's L.L.  $34^{\circ} 37' 55''$ , index corr.  $+ 1' 15''$ , eye 18 feet, time by a chronometer  $27^d 7^h 41^m 30^s$  (being P.M. at Greenwich), which was *fast*  $31^m 54^s$  for mean noon at Greenwich, October 20th, and on November 9th was  $29^m 40^s$  *fast* on mean noon at Greenwich.

Ex. 12. 1876, December 24th, A.M. at ship, latitude  $9^{\circ} 59' S.$ , observed altitude sun's L.L.  $10^{\circ} 38' 45''$ , index correction  $- 3' 12''$ , eye 18 feet, time by a chronometer  $23^d 17^h 36^m 0^s$  (being A.M. at Greenwich), which was *slow*  $34^m 19^s$  for mean noon at Greenwich, July 1st, and on July 29th was *slow*  $38^m 39^s$  for mean noon at Greenwich.

Ex. 13. 1876, January 1st, P.M. at ship, latitude  $38^{\circ} 28' S.$ , observed altitude sun's L.L.  $39^{\circ} 0'$ , index correction  $- 2' 25''$ , eye 12 feet, time by chronometer  $1^d 11^h 58^m 29^s$  (being P.M. at Greenwich), which was *slow*  $1^h 49^m 19^s$  for mean noon at Greenwich, on September 12th, 1875, and on October 13th was  $1^h 52^m 53^s$  *slow* for mean noon at Greenwich.

Ex. 14. 1876, February 11th, A.M. at ship, latitude  $53^{\circ} 12' N.$ , observed altitude sun's L.L.  $12^{\circ} 10'$ , index corr.  $- 49''$ , eye 12 feet, time by chronometer  $10^d 22^h 22^m 22^s$  (being A.M. at Greenwich), which was *fast*  $34^m 41^s$  for mean noon at Greenwich, October 31st, and on December 1st, 1875, was *fast*  $38^m 59^s$  for mean noon at Greenwich.

Ex. 15. 1876, October 26th, A.M. at ship, latitude  $28^{\circ} 10' N.$ , observed altitude sun's L.L.  $25^{\circ} 32' 20''$ , index correction  $0''$ , eye 17 feet, time by chronometer  $0^h 54^m 6^s$  (being P.M. at Greenwich), which was *fast*  $31^m 31^s$  on mean time at Greenwich, August 1st, and on Sept. 4th was *fast*  $30^m 6^s$  for mean noon at Greenwich.

Ex. 16. 1876, February 6th, P.M. at ship, latitude  $6^{\circ} 58' N.$ , observed altitude sun's L.L.  $21^{\circ} 43' 40''$ , index corr.  $0''$ , eye 18 feet, time by a chronometer  $11^h 40^m 26^s$  (being A.M. at Greenwich), which was *slow*  $16^m 4^s$  on mean noon at Greenwich, January 2nd, and on January 20th was *slow*  $17^m 42^s$  on mean noon at Greenwich.

Ex. 17. 1876, May 1st, P.M. at ship, latitude  $21^{\circ} 8' N.$ , observed altitude sun's L.L.  $28^{\circ} 5' 30''$ , index corr.  $+ 2' 50''$ , height of eye 16 feet, time by a chronometer April  $30^d 18^h 50^m 29^s$  (being  $6^h 50^m 29^s$  A.M. at Greenwich), which was  $10^m 12^s$  *slow* for mean noon at Greenwich, December 31st, 1875, and on February 17th, 1876, was  $7^m 33^s$  *slow* for mean noon at Greenwich.

Ex. 18. 1876, April 21st, P.M. at ship, latitude at noon  $0^{\circ} 20' N.$ , observed altitude sun's L.L.  $32^{\circ} 21' 10''$ , index correction  $- 1' 10''$ , eye 12 feet, time by a chronometer  $3^h 44^m 1^s$  (being A.M. at Greenwich) which was *slow*  $9^m 7^s$  for mean noon at Greenwich, November 14th, 1875, and on January 11th, 1876, was *slow*  $7^m 34^s$  for mean noon at Greenwich, course since noon S.W. by W. (true), distance 36 miles: required the longitude at the time of observation, and also at noon.

Ex. 19. 1876, August 21st, A.M. at ship, latitude at noon  $0^{\circ} 20' S.$ , observed altitude sun's L.L.  $33^{\circ} 49'$ , index correction  $+ 2' 10''$ , eye 15 feet, time by chronometer  $8^h 14^m 0^s$  (being P.M. at Greenwich), which was *slow*  $4^m 40^s$  for mean noon at Greenwich, March 13th, and on April 30th was *slow*  $5^m 40^s$  for mean noon at Greenwich, course till noon S.W. by W., distance 36 miles: required the longitude at time of sights, and also at noon.

Ex. 20. 1876, March 20th, A.M. at ship, latitude  $0^{\circ}$ , observed altitude sun's L.L.  $28^{\circ} 50' 10''$ , index corr.  $+ 1'$ , eye 23 feet, time by chronometer  $20^d 1^h 35^m$  (being P.M. at Greenwich), which was  $1^m 59^s$  *fast* for mean noon at Greenwich, February 1st, and on February 28th was *fast*  $2^m 8^s$  for mean noon at Greenwich.

Ex. 21. 1876, June 14th, A.M. at ship, latitude  $29^{\circ} 10' S.$ , observed altitude sun's L.L.  $30^{\circ} 40'$ , eye 25 feet, time by chronometer, June  $13^d 22^h 59^m 20^s$  (being P.M. on 14th at Greenwich), which was *fast*  $4^m 35^s$  for mean noon at Greenwich, March 20th, and on May 3rd was *slow*  $1^m 17^s$  for mean noon at Greenwich.

## VARIATION BY AN AZIMUTH.

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IN this problem the Error of the Compass is required by computing the true bearing of the sun, and taking the difference between the true bearing and the bearing by an Azimuth Compass.

300. **The Azimuth** of a heavenly body is the arc of the horizon intercepted between the cardinal point adjacent to the elevated pole, and the circle of altitude passing through the body, or it is the angle at the Zenith contained between the vertical circle passing through the elevated pole (the meridian) and the vertical circle passing through the object. Azimuth is usually reckoned from the north or south point, eastward and westward from  $0^{\circ}$  to  $180^{\circ}$ .

301. **True Azimuth** is the bearing of an object from the *true* north or south point, and is the azimuth found by calculation from the observed altitude or hour-angle of the body. It is in general simply called *The "Azimuth"* but it is thus qualified as the *True* Azimuth to distinguish it from the *Magnetic* Azimuth, which is the bearing of the object from the compass North or South point, and which is found by direct observation with an instrument carrying a magnetic needle. The difference between the true and magnetic azimuth gives the entire correction of the compass—variation and deviation combined.

301\*. Given the latitude, altitude, and declination of an object, to find the true azimuth.

### RULE XCVIII.

1°. *Add together the polar distance, the latitude, and the altitude,\* take half the sum, and take the difference between the half sum and the polar dist.*

NOTE.—When the latitude is 0, suppose it to be of *contrary* name to the declination when finding the polar distance.

2°. *Add together the log. sec. of latitude, the log. sec. of altitude, (rejecting tens), the log. cosines of the half sum and remainder; the sum (rejecting tens) is log. sine square of true azimuth (Table 69 Raper). Or half the sum of the four logs. is the log. sine of half of the true azimuth, which take out of the table (Table 24 Norie), and double it; the result is the true azimuth.*

3°. *Reckon the true azimuth from S., when the latitude is N., but from the N. when the latitude is S.; towards E. when it is A.M., or when the altitude is increasing, but towards W. when it is P.M., or when the altitude is decreasing.*

(a) *When latitude is  $0^{\circ}$ , if declination is N. reckon the azimuth from the South; if declination is S., reckon the azimuth from the North.*

(b) *When both latitude and declination are  $0^{\circ}$ , the object moves on the prime vertical, or is E. while the altitude is increasing and W. while the altitude is decreasing.*

NOTE.—The logs. are taken out in these examples to the nearest second.

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\* The learner will observe that in this formulæ the pol. dist., lat., and alt. occur in the reverse order of that in Rule XCVI (finding hour angle) in which the initials form the word *alp*. In finding the azimuth the initials form *pla*. The 2nd and 3rd terms, take secants; the last two, cosines. By this arrangement the term which has to be taken for the half sum is always on the top.

EXAMPLES.

Ex. 1. Given the latitude  $47^{\circ} 32' 38''$  S.; declination  $22^{\circ} 27' 22''$  (or polar distance  $67^{\circ} 32' 38''$ ): true altitude  $26^{\circ} 44'$  decreasing or (being P.M.)

|             |                       |      |                       |
|-------------|-----------------------|------|-----------------------|
| Polar dist. | $67^{\circ} 32' 38''$ |      |                       |
| Latitude    | $47^{\circ} 46' 0''$  | sec. | $0^{\circ} 17' 25.33$ |
| Altitude    | $26^{\circ} 44' 0''$  | sec. | $0^{\circ} 04' 9.095$ |

Sum  $142^{\circ} 2' 38''$

Half sum  $71^{\circ} 1' 19''$  cos.  $9^{\circ} 51' 15.9$

Half sum—p.d.  $3^{\circ} 28' 41''$  cos.  $9^{\circ} 99' 20.0$

$2) 19^{\circ} 73' 29.87$

$47^{\circ} 20' 12''$  sine  $9^{\circ} 86' 6.493$   
 $2$   $47^{\circ}$

True az. N.  $94^{\circ} 40' W.$   $12'' = 23$

The true azimuth is here marked N. because the latitude is S., and W. because the altitude is decreasing, it being P.M.

Ex. 3. Latitude  $28^{\circ} 3' N.$ , declination  $12^{\circ} 39' 50'' S.$ , true altitude  $25^{\circ} 12' 4'' +$  (A.M.)

|             |                        |      |                       |
|-------------|------------------------|------|-----------------------|
| Polar dist. | $102^{\circ} 39' 50''$ |      |                       |
| Latitude    | $28^{\circ} 3' 0''$    | sec. | $0^{\circ} 05' 42.67$ |
| Altitude    | $25^{\circ} 12' 4''$   | sec. | $0^{\circ} 04' 34.38$ |

Sum  $155^{\circ} 54' 54''$

Half sum  $77^{\circ} 57' 27''$  cos.  $9^{\circ} 31' 9.32$

P. dist.— $\frac{1}{2}$  sum  $24^{\circ} 42' 23''$  cos.  $9^{\circ} 95' 8.307$

$2) 19^{\circ} 375.404$

Half azimuth  $29^{\circ} 10' 22''$  sine  $9^{\circ} 68' 7.02$   
 $2$

True az. S.  $58^{\circ} 19' E.$

The sum of the four logs., rejecting 10 from the index is the log. sine square of true azimuth; seek for log. in Table 69, Raper, and the corresponding arc is  $58^{\circ} 19'$ , whence true azimuth is S.  $58^{\circ} 19' E.$ , the same as by Norie's Table.

Ex. 5. Latitude  $34^{\circ} 19' S.$ , declination  $7^{\circ} 5' 27'' S.$ , true altitude  $40^{\circ} 55' 57'' +$  (P.M.)

|             |                       |      |                       |
|-------------|-----------------------|------|-----------------------|
| Polar dist. | $82^{\circ} 54' 33''$ |      |                       |
| Latitude    | $34^{\circ} 19' 0''$  | sec. | $0^{\circ} 08' 30.54$ |
| Altitude    | $40^{\circ} 55' 57''$ | sec. | $0^{\circ} 12' 17.76$ |

Sum  $158^{\circ} 9' 30''$

Half sum  $79^{\circ} 4' 45''$  cos.  $9^{\circ} 27' 5.00$

Remainder  $3^{\circ} 49' 48''$  cos.  $9^{\circ} 99' 0.29$

$2) 19^{\circ} 481.359$

$33^{\circ} 23' 40''$  sine  $9^{\circ} 40' 6.79$   
 $2$

True az. N.  $66^{\circ} 47' 20'' E.$

00

Ex. 2. Latitude  $37^{\circ} 15' N.$ , declination  $22^{\circ} 22' 58'' N.$ , true altitude  $39^{\circ} 20' 8''$ —(P.M.)

|             |                      |      |                       |
|-------------|----------------------|------|-----------------------|
| Polar dist. | $67^{\circ} 37' 2''$ |      |                       |
| Latitude    | $37^{\circ} 15' 0''$ | sec. | $0^{\circ} 09' 9.86$  |
| Altitude    | $39^{\circ} 20' 8''$ | sec. | $0^{\circ} 11' 15.70$ |

Sum  $144^{\circ} 12' 10''$

Half sum  $72^{\circ} 6' 5''$  cos.  $9^{\circ} 48' 6.10$

Half sum—p.d.  $4^{\circ} 29' 3''$  cos.  $9^{\circ} 99' 8.68$

$2) 19^{\circ} 69' 69.34$

$44^{\circ} 51' 58''$  sine  $9^{\circ} 84' 8.67$   
 $2$

True azimuth S.  $89^{\circ} 44' W.$

The sum of logs. (less 10 in the index) being found in the log. sine square (Table 69, Raper), gives true azimuth as above—without the trouble of halving the sum of logs. and multiplying the arc corresponding thereto by 2.

Ex. 4. Latitude  $38^{\circ} 46' N.$ , declination  $7^{\circ} 41' 56'' S.$ , true altitude  $27^{\circ} 16' 8''$ —(P.M.)

|             |                       |      |                       |
|-------------|-----------------------|------|-----------------------|
| Polar dist. | $97^{\circ} 41' 56''$ |      |                       |
| Latitude    | $38^{\circ} 46' 0''$  | sec. | $0^{\circ} 10' 8.071$ |
| Altitude    | $27^{\circ} 16' 8''$  | sec. | $0^{\circ} 05' 11.64$ |

Sum  $163^{\circ} 44' 4''$

Half sum  $81^{\circ} 52' 2''$  cos.  $9^{\circ} 15' 0.657$

Remainder  $15^{\circ} 49' 54''$  cos.  $9^{\circ} 98' 3.206$

$2) 19^{\circ} 293.098$

$26^{\circ} 18' \frac{1}{2}$  sine  $9^{\circ} 64' 6.549$   
 $2$

True azimuth S.  $52^{\circ} 36' \frac{1}{2} W.$

Ex. 6. Latitude  $0^{\circ}$  declination  $15^{\circ} 2' 27'' N.$  True altitude  $24^{\circ} 12' 10''$ —

|             |                       |      |                       |
|-------------|-----------------------|------|-----------------------|
| Polar dist. | $105^{\circ} 2' 27''$ |      |                       |
| Latitude    | $0^{\circ} 0' 0''$    |      |                       |
| Altitude    | $24^{\circ} 12' 10''$ | sec. | $0^{\circ} 03' 9.957$ |

Sum  $129^{\circ} 14' 37''$

Half sum  $64^{\circ} 37' 18''$  cos.  $9^{\circ} 63' 20.45$

Remainder  $40^{\circ} 25' 9''$  cos.  $9^{\circ} 88' 1.568$

$2) 19^{\circ} 553.570$

$36^{\circ} 44'$  sine  $9^{\circ} 77' 6.785$   
 $2$

S.  $73^{\circ} 28' W.$

## EXAMPLES FOR PRACTICE.

In each of the following examples it is required to find the true azimuth :  
(The sign + means A.M., and the sign — means P.M.)

|    |               |                         |             |                                  |          |                             |
|----|---------------|-------------------------|-------------|----------------------------------|----------|-----------------------------|
| 1. | True altitude | $7^{\circ} 43' 27'' +$  | Declination | $11^{\circ} 28' 32'' \text{ N.}$ | Latitude | $51^{\circ} 10' \text{ N.}$ |
| 2. | "             | $28^{\circ} 30' 53'' +$ | "           | $21^{\circ} 56' 45'' \text{ S.}$ | "        | $26^{\circ} 20' \text{ N.}$ |
| 3. | "             | $12^{\circ} 50' 46'' -$ | "           | $9^{\circ} 36' 51'' \text{ N.}$  | "        | $15^{\circ} 47' \text{ S.}$ |
| 4. | "             | $29^{\circ} 41' 59'' +$ | "           | $2^{\circ} 38' 14'' \text{ N.}$  | "        | $4^{\circ} 22' \text{ N.}$  |
| 5. | "             | $7^{\circ} 15' 55'' -$  | "           | $12^{\circ} 14' 38'' \text{ S.}$ | "        | $51^{\circ} 2' \text{ N.}$  |
| 6. | "             | $13^{\circ} 47' 28'' -$ | "           | $17^{\circ} 50' 57'' \text{ N.}$ | "        | $42^{\circ} 36' \text{ S.}$ |
| 7. | "             | $45^{\circ} 30' 0'' -$  | "           | $23^{\circ} 2' 0'' \text{ S.}$   | "        | $0^{\circ} 0'$              |
| 8. | "             | $25^{\circ} 40' 10'' +$ | "           | $0^{\circ} 0' 0''$               | "        | $0^{\circ} 0'$              |
| 9. | "             | $40^{\circ} 7' 21'' -$  | "           | $17^{\circ} 4' 3'' \text{ S.}$   | "        | $33^{\circ} 51' \text{ S.}$ |

301. Given the true bearing and compass bearing, to find the error of the compass.

## RULE XCIX.

1°. To find the amount of the Error of the Compass.—*Reckon the True and Magnetic Azimuths from the same point of the compass—North or South.*

(a) *If one of the azimuths be expressed from the North and the other from the South, take either of them from  $180^{\circ}$ , and it will then be reckoned from the same point as the other.*

(b) *If the bearing by compass be reckoned from East or West, towards North or South, take it from  $90^{\circ}$ , and reverse the position of the letters; or, add  $90^{\circ}$ , and it will then be expressed from the opposite point to that from which it is reckoned when taken from  $90^{\circ}$ .*

## EXAMPLE.

Ex. Suppose magnetic azimuth to be W.  $78^{\circ} 30' \text{ N}$ ; then subtract the magnetic azimuth from  $90^{\circ}$  thus:—

$$\begin{array}{r} 90^{\circ} 00' \\ \text{W. } 78^{\circ} 30' \text{ N.} \\ \hline \end{array}$$

The azimuth is thus reckoned N.  $11^{\circ} 30' \text{ W.}$  from the north pole.

(c) *When the magnetic azimuth is either East or West, it is to be reckoned as  $90^{\circ}$  from North or South, according as the true azimuth is North or South.*

2°. *Take the difference of the true and magnetic azimuths when measured towards the same point of the compass, East or West; but when measured towards different points, i.e., when one is reckoned towards East and the other towards West, take the sum; the result is the error of the compass or correction.*

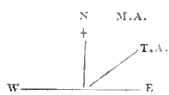
3°. To name the Correction of Compass.—*Let the observer look at the two azimuths (or bearings) from the centre of the compass—then if the true azimuth is to the right of the magnetic azimuth, the correction is East; but if the true azimuth is to the left of the magnetic azimuth, the error is West.*

EXAMPLES.

Ex. 1. Given true azimuth N.  $44^{\circ} 20'$  E. and the sun's bearing by compass (or magnetic azimuth) N.  $17^{\circ} 10'$  E.: required the error of compass.

True az. N.  $44^{\circ} 20'$  E.  
Mag. az. N.  $17^{\circ} 10'$  E.

Error  $\underline{27^{\circ} 10'}$  E.

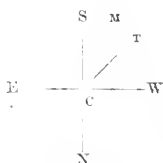


The observer being supposed looking from the centre of the compass in the direction of the magnetic azimuth, then the *true azimuth* lies to the *right* hand of the magnetic azimuth, whence the error of compass is to be marked *East*.

Ex. 3. Given true azimuth S.  $69^{\circ}$  W., magnetic azimuth S.  $47^{\circ}$  W.: required the error of compass.

True az. S.  $69^{\circ}$  W.  
Mag. az. S.  $47^{\circ}$  W.

Error  $\underline{22^{\circ}}$  E.



The observer being supposed looking from the centre of the compass in the direction of the magnetic azimuth C M, then the true azimuth, C T, lies to the *right* hand of the magnetic azimuth, whence the error of the compass is *East*.

Ex. 5. The true azimuth S.  $62^{\circ} 41'$  E., and magnetic azimuth E.S.E.: required the error of compass.

True az. S.  $62^{\circ} 41'$  E.  
S. 6 pts. E. = Mag. az. S.  $67^{\circ} 30'$  E.

Error of compass  $\underline{4^{\circ} 49'}$  E.

Here the error of compass is East, since the *true azimuth* is on the *right* of the magnetic azimuth, the observer looking from the centre of the compass in the direction of the magnetic azimuth.

Ex. 7. True azimuth N.  $72^{\circ}$  E., magnetic azimuth East.

True azimuth N.  $72^{\circ}$  E.  
Mag. azimuth East = N.  $90^{\circ}$  E.

Error of compass  $\underline{18^{\circ}}$  W.

Ex. 9. The true azimuth S.  $90^{\circ} 33'$  E., and magnetic azimuth N.  $81^{\circ} 20'$  E.: find the error of compass.

True azimuth S.  $90^{\circ} 33'$  E.  
 $\underline{180^{\circ} 0'}$

or, N.  $89^{\circ} 27'$  E.  
Mag. azimuth N.  $81^{\circ} 20'$  E.

Error of compass  $\underline{8^{\circ} 7'}$  E.

The *true azimuth* being reckoned from S., while the magnetic azimuth is expressed from N., the true is subtracted from  $180^{\circ}$ , in order to reckon it from the same point as the magnetic azimuth, viz., from N.

Ex. 2. Given true azimuth S.  $70^{\circ} 57'$  E. the magnetic azimuth S.E. by E.  $\frac{3}{4}$  E.: required the error of compass.

Mag. az. S.E. by E.  $\frac{3}{4}$  E. = S.  $64^{\circ} 41' 15''$  E.

True az. S.  $70^{\circ} 57' 0''$  E. M.A. 8  
Mag. az. S.  $64^{\circ} 41' 15''$  E.

Error  $\underline{6^{\circ} 15' 45''}$  W.

The error of compass is in this instance West, because when looking from the centre of the compass in the direction of the magnetic azimuth, the *true azimuth* is on the *left* hand of the magnetic.

Ex. 4. True azimuth N.  $50^{\circ} 12'$  E., and the magnetic azimuth N.  $61^{\circ} 50'$  E.: required the correction of compass.

True azimuth N.  $50^{\circ} 12'$  E.  
Magnetic azimuth N.  $61^{\circ} 50'$  E.

Error of compass  $\underline{11^{\circ} 38'}$  W.

The error of compass is here West, because the *true azimuth* is to the *left* hand of the magnetic azimuth, the observer being supposed to look from the centre of the compass in the direction of the magnetic azimuth.

Ex. 6. The true azimuth S.  $82^{\circ} 50'$  W., and magnetic azimuth W.  $15^{\circ}$  N.

True az. S.  $82^{\circ} 50'$  W.  
W.  $15^{\circ}$  N. = Mag. az. S.  $105^{\circ} 0'$  W.

Error of compass  $\underline{22^{\circ} 10'}$  W.

The error of compass is West, the *true azimuth* being to the *left* of magnetic,  $90^{\circ}$  is added to the compass-bearing in order to reckon it from the same point as the true azimuth; thus, from S. to W. is  $90^{\circ}$ , and from W. to W.  $15^{\circ}$  N. is  $15^{\circ}$  more; hence magnetic azimuth is S.  $105^{\circ}$  W.

Ex. 8. The true azimuth is S.  $76^{\circ}$  W., and the magnetic azimuth West.

True azimuth S.  $76^{\circ} 0'$  W.  
Mag. azimuth S.  $90^{\circ} 0'$  W.

Error of compass  $\underline{14^{\circ} 0'}$  W.

The magnetic azimuth West is reckoned as  $90^{\circ}$  from S., because the true azimuth is reckoned from S.

Ex. 10. The true azimuth N.  $69^{\circ} 39'$  W., and magnetic azimuth S.  $93^{\circ} 30'$  W.: find the error of compass.

True azimuth N.  $69^{\circ} 39'$  W.  
 $\underline{180^{\circ} 0'}$

or, S.  $110^{\circ} 21'$  W.  
Mag. azimuth S.  $93^{\circ} 30'$  W.

Error of compass  $\underline{16^{\circ} 51'}$  E.

The *true azimuth* is here taken from  $180^{\circ}$ , in order to reckon it from the same point as the magnetic azimuth.

Ex. 11. True azimuth S.  $36^{\circ}$  W., magnetic azimuth S.  $9^{\circ}$  E.

True azimuth S.  $36^{\circ}$  W.  
Mag. azimuth S.  $9^{\circ}$  E.

Error of compass  $\underline{\hspace{1cm}} 45^{\circ}$  E.

Ex. 12. True azimuth N.  $68^{\circ}$  W., magnetic azimuth N.  $5^{\circ}$  E.

True azimuth N.  $68^{\circ}$  W.  
Mag. azimuth N.  $5^{\circ}$  E.

Error of compass  $\underline{\hspace{1cm}} 73^{\circ}$  W.

Ex. 13. True azimuth N.  $49^{\circ}$  E., magnetic azimuth N.  $3^{\circ}$  W.

True azimuth N.  $49^{\circ}$  E.  
Mag. azimuth N.  $3^{\circ}$  W.

Error of compass  $\underline{\hspace{1cm}} 52^{\circ}$  E.

Ex. 14. True azimuth S.  $50^{\circ}$  E., magnetic azimuth S.  $8^{\circ}$  W.

True azimuth S.  $50^{\circ}$  E.  
Mag. azimuth S.  $8^{\circ}$  W.

Error of compass  $\underline{\hspace{1cm}} 58^{\circ}$  W.

### RULE C.

1°. *With ship time and longitude in time find the Greenwich date (Rule LXXXI, page 222.)*

2°. *Take from page II, Nautical Almanac, the sun's declination and reduce it to Greenwich date (Rule LXXXII, page 222); also take out sun's semi-diameter.*

If apparent time is given, use Nautical Almanac, page I.

3°. *Correct observed altitude for index error, dip, refraction, parallax, and semi-diameter, and thus get the true altitude (Rule LXXXVII, page 236).*

4°. *Proceed according to Rule XCVIII, page 280, to find the true azimuth.*

5°. *Having found the true azimuth, proceed by Rule XCIX, page 282, to find the entire correction or error of the compass.*

6°. *Next apply the variation to the error of compass according to Rules 7° and 8° of Rule LXXXIX, page 245, the result is the deviation for the position of the ship's head at the time of observation.*

### EXAMPLES.

Ex. 1. 1876, May 19th,  $3^h 7^m 44^s$  P.M., mean time at ship, latitude  $41^{\circ} 53'$  N., longitude  $60^{\circ} 19'$  W., sun's bearing by compass S.  $104^{\circ} 40'$  W., observed altitude sun's L.L.  $43^{\circ} 56' 7''$ , height of eye 18 feet, index correction  $0'$ ; required the true azimuth and error of the compass; and supposing the variation to be  $17^{\circ} 10'$  W.: required the deviation of the compass for the position of the ship's head at the time of observation.

Ship date (M.T.) May  $19^d 3^h 7^m 44^s$   
Long.  $60^{\circ} 19'$  W. in time  $\underline{\hspace{1cm}} + 4 \quad 1 \quad 16$   
Green. date (M.T.) May  $19 \quad 7 \quad 9 \quad 0$

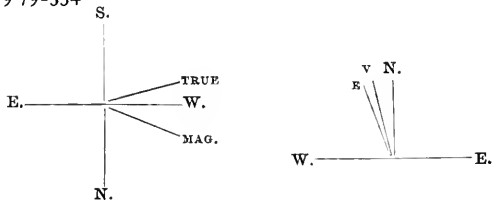
Obs. alt.  $\odot$ 's L.L.  $43^{\circ} 56' 7''$   
Dip  $\underline{\hspace{1cm}} - 4 \quad 4$   
 $\underline{\hspace{1cm}} 43 \quad 52 \quad 3$   
Corr. altitude  $\underline{\hspace{1cm}} - 53$

By Raper: Dip  $- 4' 10''$ , ref.  $- 1' 1''$ , par.  $+ 6''$ , semid.  $+ 15' 50''$ . True altitude  $44^{\circ} 6' 54''$ .

$\underline{\hspace{1cm}} 43 \quad 51 \quad 10$   
Semi-diameter  $\underline{\hspace{1cm}} + 15 \quad 50$   
 $\underline{\hspace{1cm}} 44 \quad 7 \quad 0$   
True altitude



|                           |            |      |             |                            |          |
|---------------------------|------------|------|-------------|----------------------------|----------|
| Polar dist.               | 70° 1' 52" |      |             | Decl. page II, N.A.        | H.D.     |
| Latitude                  | 41 53 0    | sec. | 0°128132    | 19th, noon, 19° 54' 22" N. | + 31"65  |
| Altitude                  | 44 7 0     | sec. | 0°143922    | Correction                 | + 3 46   |
| Sum                       | 156 1 52   |      |             | Red. decl.                 | 19 58 8  |
| Half sum                  | 78 0 56    | cos. | 9°317284    |                            | 90 0 0   |
| Remainder                 | 7 59 4     | cos. | 9°995771    | Polar dist.                | 70 1 52  |
|                           |            |      | 2)19°585109 | Correction                 | + 3' 46" |
| Half azimuth              | 38° 20'    | sine | 9°792554    |                            |          |
| True azimuth S. 76 40 W.  |            |      |             |                            |          |
| Mag. azimuth S. 104 40 W. |            |      |             |                            |          |
| Error of compass          | 28 0 W.    |      |             |                            |          |
| Variation                 | 17 10 W.   |      |             |                            |          |
| Deviation                 | 10 50 W.   |      |             |                            |          |



The true azimuth being to the left of the magnetic, the error of compass being to the left of the variation.

Ex. 2. 1876, September 2nd, mean time at ship 8<sup>h</sup> 59<sup>m</sup> A.M., latitude 39° 31' S., longitude 127° 45' W., sun's bearing by compass N. 29° 50' E., observed altitude sun's L.L., 26° 40' 37", height of eye 18 feet: required the true azimuth and error of the compass: and supposing the variation to be 9° 50' E.: required the deviation of the compass for the position of the ship's head at the time of observation.

|                        |  |                                  |              |
|------------------------|--|----------------------------------|--------------|
| Ship date (M.T.) Sept. | 1 <sup>d</sup> 20 <sup>h</sup> 59 <sup>m</sup> | Obs. alt ☉'s L.L.                | 26° 40' 37"  |
| Long. 127° 45' W.      | + 8 31   | Dip. (T. 4)                      | — 4 4        |
| Grn. date (M.T.) Sept. | 2 5 30   | Corr. altitude                   | 26 36 33     |
|                        |  |                                  | — 1 45       |
|                        |  | Semi-diameter                    | 26 34 48     |
|                        |  |                                  | + 15 54      |
|                        |  | True altitude                    | 26 50 42     |
| Decl. 2nd, p. II, N.A. | 7° 42' 31" N.                                  | Hourly diff., noon,              | 54" 95       |
| Correction             | — 5 2  | 5 <sup>h</sup> 30 <sup>m</sup> = | × 5'5        |
| Reduced declination    | 7 37 29 N.                                     |                                  | 27475        |
|                        | 90 0 0   |                                  | 27475        |
| Polar distance         | 97 37 29                                       |                                  | 6,0)30,2'225 |
|                        |  |                                  | 5' 2"        |

|              |             |  |              |
|--------------|-------------|--|--------------|
| Polar dist.  | 97° 37' 29" | Half true azimuth                                | 26° 11' 50"  |
| Latitude     | 39 31 0     |  | 2            |
| Altitude     | 26 50 42    | True azimuth                                     | N. 52 24 E.  |
| Sum          | 163 59 11   | Magnetic azimuth                                 | N. 29 50 E.  |
| Half sum     | 81 59 35    | Error of compass                                 | 22 34 E.     |
| Remainder    | 15 37 54    | The true azimuth being to the right of magnetic, |              |
|              |             | To find the Deviation.                           |              |
|              |             | Error of compass                                 | + 22° 34' E. |
| Half azimuth | 26° 11' 50" | Variation  | 9 50 W.      |
|              |             | Deviation  | + 12 44 E.   |

Ex. 3. 1876, July 5th, mean time at ship  $6^h 55^m 51^s$  P.M., latitude  $50^\circ 53' N.$ , longitude  $119^\circ 8' E.$ , sun's bearing by compass N.  $69^\circ 0' W.$ , observed altitude sun's L.L.  $9^\circ 40'$ , index correction  $+ 3' 50''$ , height of eye 18 feet, variation  $4^\circ 0' W.$

|                               |   |  |                   |
|-------------------------------|---|--|-------------------|
| Ship date (M.T.) July         | 5 <sup>d</sup> 6 <sup>h</sup> 55 <sup>m</sup> 51 <sup>s</sup> | Obs. alt. $\odot$ 's L.L.                  | 9° 40' 0"         |
| Long. 119° 8' E.              | — 7 56 32   | Index correction                           | + 3 50            |
| Green. date (M.T.) July       | 4 22 59 19  | Dip  | 9 43 50           |
| Hourly diff.                  | 14" 64  |  | — 4 4             |
| Time from noon 1 <sup>h</sup> | 1   | Corr. altitude                             | 9 39 46           |
| Correction                    | 14" 64  |  | — 5 17            |
|                               | or + 15"  | Semi-diameter                              | 9 34 29           |
| Decl., noon, July 5th,        | 22 44 58 N.   | True altitude                              | + 15 46           |
| Red. decl.                    | 22 45 13 N.   |  | 9 50 15           |
|                               | 90  | By Raper: Index corr. + 3' 50", dip —      |                   |
| Polar dist.                   | 67 14 47  | 4' 10", ref. — 5' 31", par. + 8", semid. + |                   |
|                               |   | 15' 46". True alt. 9° 50' 3".              |                   |
| Polar dist                    | 67° 14' 47"   | True azimuth                               | N. 65° 51' 40" W. |
| Latitude                      | 50 53 0   | Magnetic azimuth                           | N. 69 0 0 W.      |
| Altitude                      | 9 50 15   | Error of compass                           | 3 8 20 E.         |
| Sum                           | 127 58 2  |  |                   |
| Half sum                      | 63 59 1   |  |                   |
| Remainder                     | 3 15 46   |  |                   |
| Half azimuth                  | 57° 4' 10"  |  |                   |
| True azimuth S. 114 8 20 W.   |   |  |                   |
| or, N. 65 51 40 W.            |   |  |                   |

The true and magnetic azimuths being reckoned from opposite points, the true is taken from  $180^\circ$ , and the remainder reckoned from the opposite point, whence true azimuth is N.  $65^\circ 52' W.$  The true azimuth being to the right of magnetic, the error of compass is East.

To find the Deviation.

|                  |            |
|------------------|------------|
| Error of compass | + 3° 8' E. |
| Variation        | — 4 0 W.   |
| Deviation        | + 7 8 E.   |

Ex. 4. 1876, February 10th, at  $8^h 2^m$  A.M., mean time at ship, latitude  $50^\circ 48' N.$ , longitude  $77^\circ 30' W.$ , sun's bearing by compass S.E. by E.  $\frac{1}{4}$  E., observed altitude sun's L.L.  $7^\circ 10' 40''$ , index correction  $- 1' 6''$ , height of eye 15 feet: required the true azimuth and error of compass; variation  $14^\circ 0' W.$

|   |   |                           |            |
|---|---|---------------------------|------------|
| Ship date, M.T., Feb.                         | 9 <sup>d</sup> 20 <sup>h</sup> 2 <sup>m</sup> | Obs. alt. $\odot$ 's L.L. | 7° 10' 40" |
| Long. 77° 30' W.                              | + 5 10  | Index correction          | — 1 6      |
| Feb.  | 9 25 12                                       | Dip for 15 feet           | 7 9 34     |
|   | — 24  |                           | — 3 42     |
| Green. date, M.T., Feb.                       | 10 1 12                                       | Correction of altitude    | 7 5 52     |
| Hourly diff. decl. noon                       | — 48" 55                                      |                           | — 7 6      |
| Time from noon 1 <sup>h</sup> 12 <sup>m</sup> | × 1' 2  | Semi-diameter             | 6 58 46    |
| Correction                                    | — 58" 260                                     | True altitude             | + 16 14    |
| Decl. 10th, noon                              | 14 27 36 S.                                   |                           | 7 15 0     |
| Red. declination                              | 14 26 38 S.                                   |                           |            |
|   | 90  |                           |            |
| Polar distance                                | 104 26 38                                     |                           |            |

By Raper: Index corr. — 1' 4", dip — 3' 50", ref. — 7' 19", par. + 9", semid. + 16' 14", true alt.  $7^\circ 14' 50''$ .

|              |              |      |             |   |
|--------------|--------------|------|-------------|---|
| Polar dist.  | 104° 26' 38" |      |             | 28° 11'   |
| Latitude     | 50 48 0      | sec. | 0°199263    | 2   |
| Altitude     | 7 15 0       | sec. | 0°003486    |   |
| Sum          | 162 29 38    |      |             |   |
| Half sum     | 81 14 49     | cos. | 9°182347    |   |
| Remainder    | 23 11 49     | cos. | 9°963389    |   |
|              |              |      | 2)19°348485 |   |
| Half azimuth | 28° 11' 7"   | sine | 9°674242    |   |
|              |              |      |             | The error is East, the <i>true</i> azimuth being to the <i>right</i> of the <i>magnetic</i> . |

Ex. 5. 1876, January 21st, at 10<sup>h</sup> 14<sup>m</sup> A.M. app. time at ship, lat. 39° 3' S., longitude 96° 28' E., sun's bearing by compass E. 2° 30' S., observed altitude sun's U.L. 46° 15', index correction — 2' 43", height of eye 19 feet: required the true azimuth and error of compass; variation 17° 0' W.: find the deviation.

|                          |  |   |               |
|--------------------------|--|---|---------------|
| Ship date, M.T. Jan.     | 20 <sup>d</sup> 22 <sup>h</sup> 14 <sup>m</sup> 0 <sup>s</sup> | Obs. alt. ☉'s U.L.  | 46° 15' 0"    |
| Long. 96° 28' E.         | — 6 25 52  | Index correction  | — 2 43        |
| Green. date, M.T. Jan.   | 20 15 48 8   | Dip for 19 feet   | 46 12 17      |
| Hourly diff. 21st, noon  | — 33' 17"  |   | — 4 11        |
|                          | × 8.2  | Correction of altitude  | 46 8 6        |
|                          | 6634   |   | — 0 49        |
|                          | 26536  | Semi-diameter   | 46 7 17       |
|                          | 6,0)27,1'994   | True altitude   | — 16 17       |
| Correction               | + 4' 32"   |   | 45 51 0       |
| Decl. 21st, noon, page I | 19 58 58 S.  | By Raper: Index corr. — 2' 43", dip — 4' 15", ref. — 56", par. + 6", semid. — 16' 17", true alt. 45° 50' 55". |               |
| Red. decl.               | 20 3 30 S.   | True azimuth  | N. 78° 22' E. |
| Polar distance           | 69 56 30   | Mag. azimuth  | N. 92 30 E.   |
| Polar dist.              | 69° 56' 30"  | Error of compass  | — 14 8 W.     |
| Latitude                 | 39 3 0   | Variation   | — 17 0 W.     |
| Altitude                 | 45 51 0  |   |               |
| Sum                      | 154 50 30  | Deviation   | + 2 52 E.     |
| Half sum                 | 77 25 15   |   |               |
| Polar dist. — do.        | 7 28 45  |   |               |
|                          |  |   |               |
|                          | 39° 11' 4"   |   |               |
|                          | 2  |   |               |
| True azimuth             | 78 22 8  |   |               |

Ex. 6. 1876, June 1st, at 9<sup>h</sup> 40<sup>m</sup> A.M. mean time at ship, latitude 60° N., longitude 40° 20' W., observed altitude sun's L.L. 44° 48' 50", index correction + 3' 17", height of eye 18 feet, sun's bearing by compass S.  $\frac{1}{2}$  W.: required the true azimuth and error of compass; variation 51° 15' W.

The Greenwich date is June 1<sup>d</sup> 0<sup>h</sup> 21<sup>m</sup> 20<sup>s</sup>. True altitude (Norie) 45° 3' 0", hourly diff. of decl.  $19^{\circ}81' \times \frac{1}{3}^h = 7'$ , which, *add'd* to decl. June 1st at noon, viz., 22° 8' 52" N., gives the red. decl. 22° 8' 59" N., polar distance 67° 51' 1", sum of logs. 19°220455, true azimuth S. 48° 6' E.

True azimuth S.  $48^{\circ} 6' 26''$  E.  
 S.  $\frac{1}{3}$  point W. = Mag. azimuth S.  $53^{\circ} 37' 30''$  W.

Error of compass —  $53^{\circ} 43' 56''$  W. true azimuth left of mag.  
 Variation —  $51^{\circ} 15' 0''$  W.

Deviation —  $2^{\circ} 28' 56''$  W. because error is left of variation

### EXAMPLES FOR PRACTICE.

In each of the following examples it is required to find the true azimuth, also the error of compass and deviation for the position of the ship's head at the time of observation.

| No. | Civil date.<br>1876. | M.T. ship.  | Latitude. | Longitude. | Sun's<br>bearing by<br>compass. | Obs.<br>alt. sun's<br>L.L. | Ht.<br>of<br>eye. | Variation. |
|-----|----------------------|---|-----------|------------|---------------------------------|----------------------------|-------------------|------------|
| 1   | Jan. 24th .....      | 8 <sup>h</sup> 22 <sup>m</sup> 35 <sup>s</sup> A.M. | 26° 5' S. | 50° 53' W. | E. by N.                        | 38° 23' 10                 | 16                | 4° 36' E.  |
| 2   | Feb. 28th .....      | 3 14 0 P.M.   | 38 46 N.  | 97 16 W.   | S. 42° 35' W.                   | 26 57 14                   | 17                | 11 30 E.   |
| 3   | March 27th .....     | 4 0 40 P.M.   | 4 22 N.   | 53 7 E.    | W. by N.                        | 20 30 50                   | 20                | 3 30 W.    |
| 4   | April 3rd .....      | 6 20 0 P.M.   | 42 59 N.  | 169 58 E.  | West.                           | 11 43 0                    | 17                | 9 16 E.    |
| 5   | May 27th .....       | 9 3 20 A.M.   | 55 0 N.   | 1 33 W.    | S. 61 45 E.                     | 43 8 51                    | 18                | 15 45 W.   |
| 6   | June 20th .....      | 6 10 0 P.M.   | 43 45 N.  | 11 26 W.   | N. 43 20 W.                     | 16 40 20                   | 18                | 23 0 W.    |
| 7   | July 31st .....      | 8 46 30 A.M.  | 38 18 N.  | 65 4 W.    | S. 75 20 E.                     | 43 24 58                   | 18                | 8 50 W.    |
| 8   | Aug. 23rd .....      | 5 54 58 A.M.  | 51 10 N.  | 135 40 W.  | N. 66 20 E.                     | 7 38 0                     | 15                | 25 30 E.   |
| 9   | Sept. 1st .....      | 3 47 50 P.M.  | 10 40 S.  | 138 42 E.  | W. $\frac{1}{2}$ N.             | 30 4 10                    | 15                | 3 30 W.    |
| 10  | Nov. 25th .....      | 4 7 0 P.M.  | 39 58 S.  | 50 52 W.   | W. $\frac{1}{2}$ N.             | 33 51 0                    | 14                | 9 22 E.    |
| 11  | Dec. 17th .....      | 9 10 30 A.M.  | 29 10 S.  | 26 53 W.   | S. 84 20 E.                     | 51 1 43                    | 16                | 9 45 W.    |
| 12  | July 3rd .....       | 8 26 50 A.M.  | 32 10 S.  | 62 0 E.    | N. 62 0 E.                      | 14 11 37                   | 19                | 17 0 W.    |
| 13  | Jan. 6th .....       | 5 2 14 P.M.   | 47 46 S.  | 33 11 E.   | N. 84 40 W.                     | 26 37 27                   | 28                | 33 15 W.   |
| 14  | April 25th .....     | 7 56 41 A.M.  | 27 20 S.  | 86 43 W.   | N. 61 50 E.                     | 18 44 55                   | 30                | 14 30 W.   |
| 15  | Jan. 25th .....      | 3 36 35 P.M.  | 42 26 N.  | 49 18 W.   | W. 9 10 S.                      | 13 38 46                   | 16                | 20 30 W.   |
| 16  | Feb. 1st .....       | 3 44 51 P.M.  | 33 51 S.  | 20 37 E.   | N. 70 50 W.                     | 39 56 10                   | 18                | 29 40 W.   |
| 17  | March 26th .....     | 9 5 50 A.M.   | 43 6 N.   | 51 2 W.    | S. 44 50 E.                     | 32 40 0                    | 18                | 26 0 W.    |
| 18  | Feb. 26th .....      | 2 48 0 P.M.   | 5 0 N.    | 167 0 E.   | N. 118 34 W.                    | 60 37 0                    | 19                | 9 15 E.    |
| 19  | June 21st .....      | 3 22 0 P.M.   | 66 40 N.  | 55 20 W.   | N. $\frac{1}{2}$ E.             | 15 38 0                    | 18                | 67 50 W.   |
| 20  | Sept. 11th .....     | 7 0 0 A.M.  | 37 0 S.   | 19 0 W.    | N. 44 50 E.                     | 42 28 0                    | 20                | 12 20 W.   |
| 21  | April 25th .....     | 8 50 0 A.M.   | 5 35 N.   | 94 30 E.   | N. 75 46 E.                     | 42 55 0                    | 13                | 2 30 E.    |
| 22  | March 1st .....      | 0 35 0 P.M.   | 15 30 N.  | 65 0 E.    | S. $\frac{1}{2}$ E.             | 66 14 0                    | 12                | 0 0        |
| 23  | 1877, Jan. 1st ...   | 9 27 10 A.M.  | 0 0       | 0 25 E.    | S.E.                            | 45 10 50                   | 17                | 21 0 W.    |

## ON FINDING THE LATITUDE BY REDUCTION TO THE MERIDIAN.

302. The latitude of a place is most simply determined by observation of the meridian altitude of a known heavenly body. When such an observation cannot be obtained by reason of the state of the weather, the altitude of the body may often be obtained a little before or a little after its meridian passage. And if at the time of observing such an altitude near the meridian, the hour-angle of the body is known, we may find by computation very nearly the difference of altitude by which to reduce the observed to the Meridian altitude. The correction is called the "Reduction to the meridian." This method, in point of simplicity, is little inferior to the meridian altitude, to which it is next in importance. The altitude may also be determined by a direct process, deduced from spherical trigonometry. The former is the method used in the following pages. The Term "near the meridian" implies a meridian distance limited according to the latitude and declination, and also the degree of precision with which the time is known (see Raper, Table 47).

## RULE CI.

1°. To the time shown by the watch, expressed astronomically, apply the error of the watch for apparent time,\* adding when the watch is slow (rejecting  $24^h$  when the sum exceeds  $24^h$  and putting the day one forward), subtracting when the watch is fast (increasing the time shown by watch by  $24^h$ , if necessary, and putting the day one back.)

2°. Next turn into time the difference of longitude made since the error of the watch was determined; adding when the difference of longitude is East, subtracting when difference of longitude is West; the result is apparent time at ship when the observation was made.†

3°. If apparent time at ship is P.M., it is the time from noon; when it is A.M., (reckoning from the preceding noon) subtract it from  $24^h$ , the remainder is the time from noon.

## EXAMPLES.

Ex. 1. Suppose it is P.M. at ship, and the watch when corrected shows January  $2^d$   $0^h$   $16^m$   $56^s$  (see example 1 following): then the time from noon is  $16^m$   $56^s$  past noon of the 2nd.

Ex. 2. Again, suppose it is A.M. at ship, and the watch when corrected indicates Feb.  $5^d$   $23^h$   $37^m$   $16^s$  (see example 2 following), then we have

$$\begin{array}{r} 24^h \ 0^m \ 0^s \\ 23 \ 37 \ 16 \\ \hline 22 \ 44 \end{array}$$

In this instance it is  $22^m$   $44^s$  before noon of the 6th.

4°. With apparent time at ship and longitude, find Greenwich date in apparent time (Rule LXXXI, page 222.)

5°. Take out of Nautical Almanac, page I, the declination, and reduce it to the Greenwich date (Rule LXXXII, page 225.)

6°. Correct the observed altitude of sun's upper or lower limb, and so get the true altitude of sun's centre (Rule LXXXVII, page 236).

## METHOD I.

7°. Take out log. rising of time from noon (Table 29, Norie), log. cos. declination (Table 25, Norie), and log. cos. of latitude (Table 25, Norie).

NOTE.—In using the natural sines and cosines to six places, it will be necessary to add 1 to the index of the log. rising, because, as given in the Table, it is only adapted to five places of figures.

\* The error of chronometer for apparent time at place, should be noted when the morning sights are taken for determining the longitude. This with the diff. long. made in the interval between this last time and the time of observing the ex-meridian altitude, will give the apparent time at ship. If the ship has not changed her meridian since the time of morning sights the result obtained by applying the error of chronometer is, of course, the apparent time at ship.

† The reason for this rule will appear on considering that if a watch is set to the time at any given meridian, it will be slow for any meridian to the eastward, but fast for any meridian to the westward, at the rate of  $1^m$  for  $15'$  diff. long., since the sun comes to the easterly meridian earlier, and to the westerly meridian later.

CAUTION.—In the use of the table of log. rising (XXIX, Norie), care must be taken that the correct indices are used when the minutes of the time from noon are 1, 3, 10, or 32. It is necessary to notice, that the indices in the table sometimes change in the column where they could not be inserted for want of room; this may, however, be easily known by observing that the first figure of the decimal part of the log. changes from 9 to 0.

Thus the log. rising of  $0^h 1^m 0^s$  is 9.97860

but the log. rising of  $0^h 1^m 5^s$  is 0.04813.

The index, as given in the table, is in the form  $\frac{9}{10}$ , which means that it changes from 9 to 0 somewhere in that line. Similarly, opposite  $10^m$ , the index is in the form  $\frac{1}{2}$ , and the numerator 1 is the index of the log. rising of  $10^m 0^s$ ,  $10^m 5^s$ ,  $10^m 10^s$ , and of  $10^m 15^s$ , and changes to 2 somewhere between  $10^m 15^s$  and  $10^m 20^s$ .

8°. Take the sum of these and find the natural number corresponding thereto. (Table 24, Norie).

9°. To the natural number just found add the natural sine of the true altitude, (Table 26, Norie); the sum is natural cosine of meridian zenith distance, which take out of the Table, and name it North or South, according as the observer is North or South of the sun. See Rule LXXXVIII, 4°, page 238.

10°. Apply the reduced declination to the zenith distance, taking their sum if they are of the same name, but their difference if of contrary names; the result, in either case, is the latitude of the same name as the greater.

NOTE.—The foregoing Method (Method I) is only convenient when the computer is provided with a table of natural sines and cosines, as well as a table of log. versed sines, or the logarithmic value of  $2 \sin^2 \frac{1}{2} t$ .

303. We may also compute directly the reduction of the observed altitude to the meridian altitude by the following:—

#### METHOD II.

1°. Add together the following logarithms:—

Constant log. 5.615455; (this is the log. of  $\frac{2}{\sin 1''}$ ).\*

Log. cosine of latitude by account (Table 25, Norie):

Log. cosine of declination (Table 25, Norie).

Log. cosecant of meridian zenith distance as deduced from latitude by D.R. and declination (Table 25, Norie).

The log. of time from noon; (this is twice the log. sine of half the hour-angle).—(Table 31, Norie, and 69, Raper).

The sum of these logs., rejecting tens from the index, will be the log. of the reduction in seconds ( $''$ ).—(Table 24, Norie).

The zenith distance from latitude by D.R. is found as follows:—When the latitude and declination are both of the same name, take their difference; when latitude and declination have different names, take their sum: the result in either case will be zenith distance by D.R.

\* If we use the constant log. 0.301030 (this is log. of 2) instead of that given above, viz., 5.615455, the sum of logs., rejecting tens from index, will be log. sine of reduction in minutes ( $'$ ) and seconds ( $''$ ). Table 66, Raper, or Table 25, Norie.

2°. Add the reduction to the true altitude: the result is the meridian altitude.\*

3°. Having the meridian altitude: find the latitude as by the method of meridian altitudes (Rule LXXXVIII, page 238).

NOTE.—This Method (Method II) does not approximate so rapidly as the preceding (Method I), but the objection is of little weight when the observations are very near the meridian. On the other hand, it has the great advantage of not requiring the use of the table of Natural sines.

304. At the Liverpool Local Marine Board Examinations the Candidate is expected to solve this problem by means of Towson's ex-meridian Tables: hence we have

#### METHOD III.

1°. Enter Table I (Towson) under nearest declination and find nearest hour-angle, against which stands Augmentation I, which add to declination, at the same time take out corresponding index number in the margin.

2°. Enter Table II under true altitude and opposite index number, find Augmentation II, which add to true altitude, and thence find latitude as in meridian altitude.

305. In the following method the latitude is obtained by a direct process, deduced from spherical trigonometry, and wholly independent of the latitude by account.

#### METHOD IV.

1°. To find Arc I.—To the secant of the hour-angle (or time from noon) add the tangent of the declination; the sum (rejecting 10 in the index) will be the tangent of Arc I, which is named North or South according to the declination.

2°. To find Arc II.—Add together cosecant of declination, sine of Arc I, and sine of true altitude; the sum is the cosine of Arc II, to be marked of a contrary name to the bearing of the sun.

3°. If Arcs I and II are of the same name take their sum; but their difference if of contrary names; the result in either case is the latitude of the same name as the greater.

NOTE.—As a check against any gross mistake, it should be borne in mind that Arc I is always a little greater than the declination, and Arc II is (nearly) the complement of the altitude when the hour-angle is small. The tang. of decl. and the cosec. of the same arc, of course, found on the same page, and generally, also tang. Arc I and the corresponding sin. of same will be found on that page; while the sin. of alt. and cos. Arc II are found in another page. In example I, page 292, the logs. which are found at the same opening of the Tables are marked with the same letter.

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\* This is only an approximate meridian altitude, in strictness a second reduction should be computed.

## EXAMPLES.

Ex. 1. 1876, January 2nd P.M. at ship, latitude by account  $52^{\circ} 6' S.$ , longitude  $71^{\circ} 23' W.$ , observed altitude sun's L.L. North of observer  $60^{\circ} 20' 30''$ , index correction  $+ 2' 58''$ , height of eye 20 feet, time by watch, January  $2^d 0^h 48^m 22^s$ , which was found to be  $29^m 16^s$  *fast* on apparent time at ship, difference of longitude 32.4 miles to West: required the latitude by reduction to meridian.

Time by watch, Jan.  $2^d 0^h 48^m 22^s$   
 Watch *fast*  $- 0 29 16$

Diff. long.  $\frac{32.4 \times 4}{60}$   $2 0 19 6$   
 $- 2 10$

Time from noon, Jan.  $2 0 16 56$

Obs. alt.  $\odot$ 's L.L.  $60^{\circ} 20' 30''$   
 Index correction  $+ 2 58$

$60 23 28$   
 Dip for 20 feet  $- 4 17$

$60 19 11$   
 Correction of alt.  $- 0 28$

$60 18 43$   
 Semi-diameter  $+ 16 18$

True altitude  $60 35 1$

## Method I.

Time from noon  $16^m 56^s$  rising\*  $3.435880$   
 Latitude  $52^{\circ} 6' S.$  cos.  $9.788370$   
 Declination  $22 56 \frac{1}{2}$  cos.  $9.964211$

$1542$  nat. no.  $3.188461$

T. alt.  $60^{\circ} 35' 1''$  nat. sine  $871073$   
 $1542$

Z. dist.  $29 14 10 S.$  nat. cos.  $872615$   
 Decl.  $22 56 28 S.$  (next greater)  $638$

Lat.  $52 10 38 S.$   $239)2300(10$   
 nearly.

(\* The index of log. rising is increased by 1. See Note to 7<sup>th</sup> page 289).

## Method III.—By Townsen's Ex-Meridian Tables.

$\odot$ 's red. declination  $22^{\circ} 56' 28'' S.$

Aug. Table 1, Index 30  $+ 3 21$

Augmented declination  $22 59 49 S.$

App. time at ship, Jan.  $2^d 0^h 16^m 56^s$   
 Long. in time  $+ 4 45 32$

Greenwich date, Jan.  $2 5 2 28$

Decl., page I, N.A., January 2nd, at noon,  $22^{\circ} 57' 34'' S.$ , (decreasing).

H. diff., Jan. 2nd, noon,  $13'' 20$

Greenwich date  $5^h 2^m$ , or  $\times 5$

$6,0)6,600$

Correction  $- 1' 6''$

Decl., Jan. 2nd, noon,  $22^{\circ} 57' 34'' S.$  decr.

Correction  $- 1 6$

Red. decl.  $22 56 28 S.$

## Method II.

Constant log.  $5.61546$

Lat. by D. R.  $52^{\circ} 6' S.$  cos.  $9.78837$

Declination  $22 56 \frac{1}{2} S.$  cos.  $9.96421$

Mer. zen. dist.  $29 9 \frac{1}{2}$  cosec.  $0.31227$

Time from noon  $16^m 56^s$  log.  $7.13485$

$6,0)65,3$  log.  $2.81516$

Reduction  $+ 10' 53''$

True altitude  $60 35 1$

Meridian alt.  $60 45 54$

$90$

Zenith distance  $29 14 6 S.$

Declination  $22 56 28 S.$

Latitude  $52 10 34 S.$

True altitude  $60^{\circ} 35' 0'' S.$

Aug. Table 2, Index 30  $+ 14 4$

$60 49 4$

Meridian zen. dist.  $29 10 56 S.$

Declination  $22 59 49 S.$

Latitude  $52 10 45 S.$

This is the method required of Candidates at Liverpool.

## Method IV.

Time from noon  $4^h 14' 0''$  sec.  $0.001187$

Declination  $22 56 28 S.$  tang.  $9.626609$  cosec.  $0.409165$

Arc I  $22 59 50 S.$  tang.  $9.627796$  sine  $9.591828$

True alt.  $60^{\circ} 35' 1''$  sine  $9.940055$

Arc II  $29 10 50 S.$  cos.  $9.941048$

Latitude  $52 10 40 S.$



Ex 2. 1876, February 6th, A.M. at ship, lat. acct.  $51^{\circ} 50' N.$ , long.  $105^{\circ} 41' W.$ , obs. alt. sun's L.L. South of observer  $22^{\circ} 10' 30''$ , index corr.  $+ 56''$ , height of eye 22 feet, time by watch  $6^h 0^m 4^s$ , found to be  $28^m 47^s$  fast on app. time at ship, diff. of long. made to East  $29^{\circ} 8'$  miles since error of watch on app. time at ship was determined: required the latitude by reduction to meridian.

Time by watch, February  $6^h 0^m 4^s$   
Watch fast  $- 28 47$

App. time at ship, February  $5^h 23^m 37^s 16^s$   
Long.  $105^{\circ} 41' W.$   $+ 7 2 44$

Diff. long.  $\frac{29^{\circ} 8' \times 4}{60}$   $+ 1 59$

Greenwich date, February  $6 6 40 0$   
or,  $6^h 67$

App. time at ship, February  $5 23 37 16$   
 $24 0 0$

Hourly diff.  $- 46'' 02$   
 $6^h 40^m = \times 6 67$

Time from noon, February  $6 0 22 44$

Obs. alt.  $\odot$ 's L.L.  $22^{\circ} 10' 30''$   
Index correction  $+ 56$

$32214$   
 $27612$   
 $27612$

Dip  $22 11 26$   
 $- 4 30$

$6,0)30,6^{\circ}9534$

Correction of alt.  $22 6 56$   
 $- 2 11$

Declination, page I, N.A.  
Feb. 6th, noon,  $15^{\circ} 43' 7'' S.$  decr.  
Correction  $- 5 7$

Semi-diameter  $22 4 45$   
 $+ 16 15$

Red decl.  $15 38 0 S.$

True altitude  $22 21 0$

#### Method I.

Time from noon  $22^m 44^s$  rising  $3^h 68^m 03^s$   
Latitude  $51^{\circ} 50'$  cos.  $9^{\circ} 79^m 09^s 4$   
Declination  $15 38$  cos.  $9^{\circ} 98^m 36^s 29$

$2926$  nat. no.  $3^{\circ} 466^m 21^s 3$

True altitude  $22^{\circ} 21' 0''$  nat. sine  $380263$

Zen. distance  $67^{\circ} 28' 7'' N.$  nat. cos.  $383189$   
Declination  $15 38 0 S.$

Latitude  $51 50 7 N.$

(The nat. sine being worked to six places of figures, 1 is added to index of log. rising).

#### Method III.—By Towson's Ex-Meridian Tables.

$\odot$ 's Red. declination  $15^{\circ} 38' 0'' S.$   
Aug. Table 1, Index 57  $+ 4 23$   
Augmented declination  $15 42 23$

Constant log.  $5^{\circ} 615455$   
Latitude  $51^{\circ} 50' N.$  cos.  $9^{\circ} 79^m 09^s 4$   
Declination  $15 38 S.$  cos.  $9^{\circ} 98^m 36^s 29$   
Mer. zen. dist.  $67 28$  cosec.  $0^{\circ} 34489$   
T. from noon  $22^m 44^s$  log.  $7^{\circ} 39^m 05^s 40$

$6,0)65,3$  log.  $2^{\circ} 815067$

Reduction  $+ 10' 53''$   
True altitude  $22^{\circ} 21' 0''$

Mer. altitude  $22 31 53$

Zenith distance  $67 28 7 N.$   
Declination  $15 38 0 S.$

Latitude  $51 50 7 N.$

Meridian zen. dist.  $67 32 25 N.$   
Augmented declination  $15 42 23 S.$

Latitude  $51 50 2 N.$

#### Method IV.

Time from noon  $22^m 44^s = 5^{\circ} 41'$  sec.  $0^{\circ} 002140$   
Declination  $15^{\circ} 38' S.$  tang.  $9^{\circ} 446898$ ..... cosec.  $0^{\circ} 569473$

Arc I  $15 42 24^{\circ} S.$  tang.  $9^{\circ} 449038$ ..... sine  $9^{\circ} 432508$   
True alt.  $22^{\circ} 21'$  sine  $9^{\circ} 580085$

Arc II  $67 32 32 N.$ ..... cos.  $9^{\circ} 582066$

Latitude  $51 50 8 N.$

Ex. 3. 1876, April 7th, A.M. at ship, lat. by acct.  $58^{\circ} 50' N.$ , long.  $51^{\circ} 42' W.$ , obs. alt. sun's L.L. South of observer  $37^{\circ} 42' 15''$ , index corr. —  $1' 6''$ , height of eye 10 feet, time by watch  $7^h 0^m 59^s 50^{\circ}$ , found to be  $1^h 22^m$  fast on app. time at ship, the diff. of long. made to East was  $20.7$  miles after the error on apparent time at ship was determined: required the latitude by reduction to meridian.

Time by watch, April  $7^h 0^m 59^s 50^{\circ}$   
Watch fast  $- 1 22 0$

App. time at ship, April  $6^h 23^h 39^m 13^s$   
Long.  $51^{\circ} 42' W.$   $+ 3 26 48$

April  $6 23 37 50$   
Diff. log.  $\frac{20.7 \times 4}{60} + 1 23$

Greenwich date, April  $7 3 6 1$   
or,  $3^h 1$

App. time at ship, April  $6 23 39 13$   
 $24 0 0$

By Raper: True altitude  $37^{\circ} 53' 2''$

Time from noon, April  $7 0 20 47$

H.D.  $56'' 15$   
 $3^h 6^m = 3^h 1$

Obs. alt.  $\odot$ 's L.L.  $37^{\circ} 42' 15''$   
Index correction  $- 1 6$

$5615$   
 $16845$

Dip  $37 41 9$   
 $- 3 2$

$6,0)17,4^{\circ} 065$

Corr. altitude  $37 38 7$   
 $- 1 7$

$2 54$

Semi-diameter  $37 37 0$   
 $+ 16 0$

Decl. apparent noon  
 $7^h 4' 14'' N.$   
Correction  $+ 2 54$

True altitude  $37 53 0$

Red. decl.  $7 7 8 N.$

#### Method I.

Time from noon  $20^m 47^s$  rising  $1300$   
Latitude acct.  $58^{\circ} 50'$  cos.  $2'612340$   
Declination  $7 7$  cos.  $9'996639$

$2110$  nat. no.  $2'324214$

True altitude  $37^{\circ} 53'$  nat. no.  $2110$   
nat. sine  $614056$

Mer. zen. dist.  $51 57 48'' N.$  nat. cos.  $616166$   
Declination  $7 7 8 N.$

Latitude  $59 4 56 N.$

#### Method II.

Constant log.  $5'615455$   
Latitude D.R.  $58^{\circ} 50' N.$  cos.  $9'713935$   
Declination  $7 7 N.$  cos.  $9'996639$   
Mer. zen. dist.  $51 43$  cosec.  $0'105167$   
Time from noon  $20^m 47^s$  log.  $7'312710$

$6.0)55,5$  log.  $2'743906$

Reduction  $+ 9' 15''$   
True altitude  $37^{\circ} 53' 0$

Meridian altitude  $38 2 15$

Zenith distance  $51 57 45 N.$   
Declination  $7 7 8 N.$

Latitude  $59 4 53 N.$

#### Method III.—By *Townson's Ex-Meridian Tables*.

$\odot$ 's red. declination  $7^{\circ} 7' 8'' N.$   
Aug. Table 1, Index 53  $+ 1 44$

True altitude  $37^{\circ} 53' 0'' N.$   
Aug. Table 2, Index 53  $+ 11 3 N.$

Augmented declination  $7 8 52 N.$

$38 4 3$

Mer. zen. dist.  $51 55 57 N.$   
Augmented declination  $7 8 52 N.$

Latitude  $59 4 49 N.$

#### Method IV.

Time from noon  $20^m 47^s = 5^{\circ} 11' 45''$  sec.  $0.001788$   
Declination  $7^{\circ} 7' 8'' N.$  tang.  $9.096532$  ..... cosec.  $0.906828$

Arc I  $7 8 53 N.$  tang.  $9.098320$  ..... sine  $9.094938$   
True alt.  $57^{\circ} 53'$  sine  $9.788208$

Arc II  $51 56 5 N.$  ..... cos.  $9.789974$

Latitude  $59 4 58 N.$

Ex. 4. 1876, August 7th, A.M. at ship, lat. acct.  $40^{\circ} 52' N.$ , long.  $36^{\circ} 47' W.$ , obs. alt. sun's L.L. South of observer  $65^{\circ} 1'$ , index corr.  $+ 17'$ , eye 14 feet, time by watch  $11^h 15^m 46^s$ , found to be  $26^m 16^s$  slow of app. time at ship, the diff. of long. made to East was 17 miles after the error on app. time at ship was determined: required the latitude.

|                           |                          |                                   |                      |
|---------------------------|--------------------------|-----------------------------------|----------------------|
| Time by watch, Aug.       | $6^d 23^h 15^m 46^s$     | App. time at ship, Aug.           | $6^d 23^h 43^m 10^s$ |
| Watch slow                | $+ 26 16$                | Long. $36^{\circ} 47' W.$         | $+ 2 27 8$           |
| Diff. of long.            | $6 23 42 2$<br>$+ 1 8$   | Greenwich date, Aug.              | $7 2 10 18$          |
| App. time at ship, Aug.   | $6 23 43 10$<br>$24 0 0$ | By Raper: True altitude           | $65^{\circ} 13' 3''$ |
| Time from noon, Aug.      | $7 0 16 50$              | H.D.                              | $42'' 34$            |
| Obs. alt. $\odot$ 's L.L. | $65^{\circ} 1' 0''$      | $2^h 10^m =$                      | $\times 2.2$         |
| Index correction          | $+ 17$                   |                                   | $8468$               |
| Dip                       | $65 1 17$<br>$- 3 36$    |                                   | $8468$               |
| Corr. altitude            | $64 57 41$<br>$- 23$     | Decl. apparent noon.              |                      |
| Semi-diameter             | $64 57 18$<br>$+ 15 49$  | Aug. 7th $16^{\circ} 16' 28'' N.$ |                      |
| True altitude             | $65 13 7$                | Correction $- 1 33$               |                      |
|                           |                          | Red. decl. $16 14 55 N.$          |                      |

## Method I.

|                |                  |        |               |
|----------------|------------------|--------|---------------|
| Time from noon | $16^m 50^s$      | rising | $3' 43 07 50$ |
| Latitude       | $40^{\circ} 52'$ | cos.   | $9' 87 86 56$ |
| Declination    | $16 15$          | cos.   | $9' 98 22 97$ |
|                | 1958 nat. no.    |        | $3' 29 17 03$ |

|                                    |           |          |
|------------------------------------|-----------|----------|
| True altitude $65^{\circ} 13' 7''$ | nat. no.  | 1958     |
|                                    | nat. sine | $907913$ |

|                             |           |          |
|-----------------------------|-----------|----------|
| Zen. distance $24 30 45 N.$ | nat. cos. | $909871$ |
| Declination $16 14 55 N.$   |           |          |

|                        |  |  |
|------------------------|--|--|
| Latitude $40 45 40 N.$ |  |  |
|------------------------|--|--|

## Method II.

|                                    |        |               |
|------------------------------------|--------|---------------|
| Constant log.                      |        | $5' 61 54 55$ |
| Latitude acct. $40^{\circ} 52' N.$ | cos.   | $9' 87 86 56$ |
| Declination $16 15 N.$             | cos.   | $9' 98 22 97$ |
| Mer. zen. dist. $24 37$            | cosec. | $0' 38 03 25$ |
| Time from noon $16^m 50^s$         | log.   | $7' 12 97 20$ |

|  |           |      |               |
|--|-----------|------|---------------|
|  | $6,096,9$ | log. | $2' 98 64 53$ |
|--|-----------|------|---------------|

|           |             |
|-----------|-------------|
| Reduction | $+ 16' 9''$ |
|-----------|-------------|

|               |                      |
|---------------|----------------------|
| True altitude | $65^{\circ} 13' 7''$ |
|---------------|----------------------|

|               |            |
|---------------|------------|
| Meridian alt. | $65 29 16$ |
|---------------|------------|

|                 |               |
|-----------------|---------------|
| Mer. zen. dist. | $24 30 44 N.$ |
|-----------------|---------------|

|             |               |
|-------------|---------------|
| Declination | $16 14 55 N.$ |
|-------------|---------------|

|          |               |
|----------|---------------|
| Latitude | $40 45 39 N.$ |
|----------|---------------|

## Method III.—By Towson's Ex-Meridian Tables.

|                             |                       |                        |                      |
|-----------------------------|-----------------------|------------------------|----------------------|
| $\odot$ 's red. declination | $16^{\circ} 14' 55''$ | True altitude          | $65^{\circ} 13' 7''$ |
| Aug. Table 1, Index 33      | $+ 2 30$              | Aug. Table 2, Index 33 | $+ 19 2$             |
| Augmented declination       | $16 17 25 N.$         | Augmented altitude     | $65 32 9$            |
|                             |                       | Zenith distance        | $24 27 51 N.$        |
|                             |                       | Augmented declination  | $16 17 25 N.$        |
|                             |                       | Latitude               | $40 45 16 N.$        |

## Method IV.

|                |                |                                |                    |
|----------------|----------------|--------------------------------|--------------------|
| Time from noon | $4^h 12' 30''$ | sec.                           | $0' 00 11 73$      |
| Declination    | $16 14 55 N.$  | tang.                          | $9' 46 45 60$      |
| Arc I          | $16 17 25 N.$  | tang.                          | $9' 46 57 33$      |
|                |                | True alt. $65^{\circ} 13' 7''$ | sine $9' 44 79 40$ |
|                |                |                                | sine $9' 95 80 45$ |
| Arc II         | $24 28 10 N.$  | cos.                           | $9' 95 91 28$      |
| Latitude       | $40 45' 35 N.$ |                                |                    |

Ex. 5. 1876, March 9th, A.M. at ship, lat. acct.  $30^{\circ} 21' S.$ , long.  $16^{\circ} 45' W.$ , obs. alt. sun's L.L. North of observer was  $63^{\circ} 37'$ , index corr. —  $1' 57''$ , eye 21 feet, time by watch, March  $8^h 21^m 49^s 25^s$  (being  $9^h 49^m 25^s$  A.M. on 9th), found to be  $1^h 59^m 10^s$  slow of apparent time at ship, the diff. of long. made to East was  $23\frac{1}{2}$  miles after the error on apparent time at ship was determined: required the latitude.

|                      |                      |                        |                     |
|----------------------|----------------------|------------------------|---------------------|
| Time by watch, March | $8^h 21^m 49^s 25^s$ | Ship date (A.T.) March | $8^h 23^m 50^m 9^s$ |
| Watch slow           | $1^m 59^s 10^s$      | Long. in time          | $1^m 7^s 0^s$       |

|   |                       |
|---|-----------------------|
| Diff. long. $\frac{23^{\circ} 5' \times 4}{60}$ | $23^{\circ} 48' 35''$ |
|   | $+ 1^{\circ} 34'$     |

|                          |                     |
|--------------------------|---------------------|
| App. time at ship, March | $8^h 23^m 50^s 9^s$ |
|--------------------------|---------------------|

|                       |                    |
|-----------------------|--------------------|
| Time from noon, March | $9^h 0^m 9^s 51^s$ |
|-----------------------|--------------------|

|                           |                         |
|---------------------------|-------------------------|
| Obs. alt. $\odot$ 's L.L. | $63^{\circ} 37' 0'' N.$ |
| Index correction          | $- 1^{\circ} 57'$       |

|     |                      |
|-----|----------------------|
| Dip | $63^{\circ} 35' 3''$ |
|     | $- 4^{\circ} 23'$    |

|               |                       |
|---------------|-----------------------|
| Corr. of alt. | $63^{\circ} 30' 40''$ |
|               | $- 24''$              |

|               |                       |
|---------------|-----------------------|
| Semi-diameter | $63^{\circ} 30' 16''$ |
|               | $+ 16' 8''$           |

|               |                       |
|---------------|-----------------------|
| True altitude | $63^{\circ} 46' 24''$ |
|---------------|-----------------------|

## Method I.

|                |                  |        |                      |
|----------------|------------------|--------|----------------------|
| Time from noon | $9^m 51^s$       | rising | $2^{\circ} 96' 5410$ |
| Latitude       | $30^{\circ} 21'$ | cos.   | $9^{\circ} 935988$   |
| Declination    | $4^{\circ} 13'$  | cos.   | $9^{\circ} 998820$   |

|          |     |      |                    |
|----------|-----|------|--------------------|
| nat. no. | 795 | log. | $2^{\circ} 900218$ |
|----------|-----|------|--------------------|

|               |                       |           |          |
|---------------|-----------------------|-----------|----------|
| True altitude | $63^{\circ} 46' 24''$ | nat. no.  | 795      |
|               |                       | nat. sine | $897052$ |

|               |                         |             |          |
|---------------|-------------------------|-------------|----------|
| Mer. Z. dist. | $26^{\circ} 7' 25'' S.$ | nat. cosine | $897847$ |
| Declination   | $4^{\circ} 13' 18'' S.$ |             |          |

|          |                          |
|----------|--------------------------|
| Latitude | $30^{\circ} 20' 43'' S.$ |
|----------|--------------------------|

|                          |                    |
|--------------------------|--------------------|
| Green. date (A.T.) March | $9^h 0^m 57^s 9^s$ |
|                          | or, $0^h 95^s$     |

|              |                  |
|--------------|------------------|
| Hourly diff. | $58^{\circ} 69'$ |
| $0^h 57^m =$ | $0^{\circ} 95'$  |

|            |         |
|------------|---------|
| Correction | $29345$ |
|            | $52821$ |

|            |                    |
|------------|--------------------|
| Correction | $55^{\circ} 7555'$ |
|            | or, $56''$         |

|                               |                               |
|-------------------------------|-------------------------------|
| Decl. app. noon, page I, N.A. |                               |
| March 9th                     | $4^{\circ} 14' 14'' S. decr.$ |
| Correction                    | $- 56''$                      |

|            |                         |
|------------|-------------------------|
| Red. decl. | $4^{\circ} 13' 18'' S.$ |
|------------|-------------------------|

## Method II.

|              |                         |                |                         |
|--------------|-------------------------|----------------|-------------------------|
| Constant log |                         |                | $5^{\circ} 615455$      |
| Latitude     | $30^{\circ} 21'$        | $0^{\circ} S.$ | cos. $9^{\circ} 935988$ |
| Declination  | $4^{\circ} 13' 18'' S.$ |                | cos. $9^{\circ} 998820$ |

|               |                      |        |                    |
|---------------|----------------------|--------|--------------------|
| Mer. Z. dist. | $26^{\circ} 7' 42''$ | cosec. | $0^{\circ} 356170$ |
| T. from noon  | $9^m 51^s$           | log.   | $6^{\circ} 664380$ |

|              |      |                    |
|--------------|------|--------------------|
| $6,0)37,2''$ | log. | $2^{\circ} 570813$ |
|--------------|------|--------------------|

|               |                                   |
|---------------|-----------------------------------|
| Reduction     | $+ 6' 12''$                       |
| True altitude | $63^{\circ} 46' 24''$ (By Norie). |

|               |                       |
|---------------|-----------------------|
| Mer. altitude | $63^{\circ} 52' 36''$ |
|---------------|-----------------------|

|                 |                         |
|-----------------|-------------------------|
| Zen. mer. dist. | $26^{\circ} 7' 24'' S.$ |
| Declination     | $4^{\circ} 13' 18'' S.$ |

|          |                          |
|----------|--------------------------|
| Latitude | $30^{\circ} 20' 42'' S.$ |
|----------|--------------------------|

## Method III.—By Towson's Ex-Meridian Tables.

|                             |                         |
|-----------------------------|-------------------------|
| $\odot$ 's red. declination | $4^{\circ} 13' 18'' S.$ |
| Aug. Table 1, Index 12      | $+ 13''$                |

|                                  |                         |
|----------------------------------|-------------------------|
| $\odot$ 's Augmented declination | $4^{\circ} 13' 31'' S.$ |
|----------------------------------|-------------------------|

|                        |                       |
|------------------------|-----------------------|
| True altitude          | $63^{\circ} 46' 24''$ |
| Aug. Table 2, Index 13 | $+ 6' 27''$           |

|                    |                       |
|--------------------|-----------------------|
| Augmented altitude | $63^{\circ} 52' 51''$ |
|--------------------|-----------------------|

|                            |                         |
|----------------------------|-------------------------|
| Zenith distance            | $26^{\circ} 7' 9'' S.$  |
| $\odot$ 's Augmented decl. | $4^{\circ} 13' 31'' S.$ |

|          |                          |
|----------|--------------------------|
| Latitude | $30^{\circ} 20' 40'' S.$ |
|----------|--------------------------|

## Method IV.

|                |                                 |       |  |
|----------------|---------------------------------|-------|--|
| Time from noon | $9^m 51^s = 2^{\circ} 27' 45''$ | sec.  | $0^{\circ} 000400$                                 |
| Declination    | $4^{\circ} 13' 18''$            | tang. | $8^{\circ} 868150$ ..... cosec. $1^{\circ} 133031$ |

|       |                         |                                 |  |
|-------|-------------------------|---------------------------------|--|
| Arc I | $4^{\circ} 13' 32'' S.$ | tang.                           | $8^{\circ} 868550$ ..... sine $8^{\circ} 367367$ |
|       |                         | True alt. $63^{\circ} 46' 24''$ | sine $9^{\circ} 952818$                          |

|        |                         |      |                    |
|--------|-------------------------|------|--------------------|
| Arc II | $26^{\circ} 7' 12'' S.$ | cos. | $9^{\circ} 953216$ |
|--------|-------------------------|------|--------------------|

|          |                          |
|----------|--------------------------|
| Latitude | $30^{\circ} 20' 44'' S.$ |
|----------|--------------------------|

Ex. 6. 1876, Sept. 23rd, P.M. at ship, lat. acct.  $51^{\circ} 2' N.$ , long.  $173^{\circ} 53' E.$ , obs. alt. sun's L.L. South of observer  $38^{\circ} 44' 20''$ , index corr.  $+ 1' 8''$ , height of eye 21 feet, time by watch  $50^m 0^s$ , (or  $23^d 0^h 50^m$ ) found to be  $39^m 2^s$  fast on app. time at ship, diff. of long. made to West was 8.2 miles after the error on app. time was determined: required the latitude.

Time by watch, Sept.  $23^d 0^h 50^m 0^s$   
Watch fast  $39 2$

App. time at ship, Sept.  $23^d 0^h 10^m 25^s$   
Long.  $173^{\circ} 53' E.$

Diff. of longitude  $23 0 10 58$   
 $33$

Greenwich date, Sept.  $22 12 34 53$

App. time at ship, Sept.  $23 0 10 25$

By Raper: True altitude  $38^{\circ} 55' 55''$

Time from noon 23rd is  $10 25$

H.D.  $- 58^m 50$   
 $12^h 35^m \times 12^{\circ} 6$

Obs. alt.  $\odot$ 's L.L.  $38^{\circ} 44' 20''$   
Index correction  $+ 1 8$

$35100$   
 $11700$   
 $5850$

Dip  $38 45 28$   
 $- 4 23$

$6,0)73,7100$   
 $12' 17$

Corr. altitude  $38 41 5$   
 $- 1 4$

Semi-diameter  $38 40 1$   
 $+ 15 59$

True altitude  $38 56 0$

Decl. page I, N.A.  
Sept. 22nd  $0^{\circ} 4' 58'' N.$ , *decr.*  
Correction  $- 12 17$

Red. decl.  $0 7 19 S.$

## Method I.

Time from noon  $10^m 25^s$  rising  $3^o 1399$   
Latitude  $51^{\circ} 2'$  cos.  $9^{\circ} 798560$   
Declination  $0 7$  cos.  $9^{\circ} 999999$   
 $650 \text{ nat. no. } 2^{\circ} 812549$

True altitude  $38^{\circ} 56'$  nat. no.  $650$   
nat. sine  $628416$

Mer. zen. dist.  $51^{\circ} 1' 7'' N.$  nat. cos.  $629066$   
Declination  $0 7 19 S.$

Latitude  $50 53 48 N.$

In taking out log. rising for  $10^m 25^s$ , it will be noticed that the index given at the beginning of the line is  $\frac{1}{2}$ , meaning that the index at the commencement of the line is 1, but that it changes somewhere along the line, which may easily be known by observing that when the first figure of the decimal part of the log. changes from 9 to 0, the index changes from 1 to 2.

Method III.—By Towson's *Ex-Meridian Tables*.

$\odot$ 's Red. declination  $0^{\circ} 7' 19'' S.$   
Aug. Table 1, Index 13  $+ 0$

Augmented declination  $0 7 19 S.$

As the decl. is less than any given in the head of Table I, augmentation is alone required. In this case enter Table I, under least declination, and with given hour-angle find corresponding Index number; with this and the altitude, augmentation II is determined as in other case.

True altitude  $38^{\circ} 56' 0''$   
Aug. Table 2, Index 13  $+ 2 47$

Augmented altitude  $38 58 47$

Zenith distance  $51 1 13 N.$

Augmented declination  $0 7 19 S.$

Latitude  $50 53 54 N.$

Ex. 7. 1876, May 5th, P.M. at ship, latitude account  $5^{\circ} 13' N.$ , longitude  $61^{\circ} E.$ , observed altitude sun's L.L.  $78^{\circ} 41' N.$ , eye 17 feet, time by watch  $5^h 1^m 7^s$ , which was found fast  $4^h 50^m 57^s$ , difference of longitude made since,  $20\frac{1}{2}$  miles West.

App. time at ship, May  $5^d 0^h 8^m 48^s$

Green. date app. time, May  $4^d 20^h 4^m 48^s$

Time from noon is  $8 48$

Hourly diff. 5th noon,  $42^{\circ}34' \times$  Green. time  $3^h 9^m = 165^{\circ} 9728 \div 60 = 2^{\circ} 46'$ , decl. noon 5th,  $16^{\circ} 26' 4''$  N. —  $2^{\circ} 46' =$  red. decl.  $16^{\circ} 23' 18''$  N.

By Norie: True altitude  $78^{\circ} 52' 47''$ .

By Raper: True altitude  $78^{\circ} 52' 36''$ .

*Method I.*

|                |                  |          |                    |
|----------------|------------------|----------|--------------------|
| Time from noon | $8^m 48^s$       | rising   | $2^{\circ} 867510$ |
| Latitude acct. | $5^{\circ} 13'$  | cos.     | $9^{\circ} 998197$ |
| Declination    | $16^{\circ} 23'$ | cos.     | $9^{\circ} 981986$ |
|                |                  | 704 log. | $2^{\circ} 847693$ |

nat. no. 704  
nat. sine  $981227$

True altitude  $78^{\circ} 52' 47''$

M. Z. dist.  $10^{\circ} 54' 31''$  S. nat. cos.  $981931$   
Declination  $16^{\circ} 23' 18''$  N.

Latitude  $5^{\circ} 28' 45''$  N.

This example cannot be solved by means of Towson's Ex-meridian Tables, as the altitude exceeds the limits of the Tables.

*Method II.*

|                 |                     |                   |                   |
|-----------------|---------------------|-------------------|-------------------|
| Constant log.   |                     |                   | $5^{\circ} 61546$ |
| Latitude D.R.   | $5^{\circ} 13'$ N.  | cos.              | $9^{\circ} 99820$ |
| Declination     | $16^{\circ} 23'$ N. | cos.              | $9^{\circ} 98199$ |
| Mer. zen. dist. | $11^{\circ} 10'$    | cos <sup>cc</sup> | $0^{\circ} 71276$ |
| Time from noon  | $8^m 48^s$          | log.              | $6^{\circ} 56649$ |

$6,075,0$  log.  $2^{\circ} 87489$

Reduction  $+ 12' 30''$

True altitude  $78^{\circ} 52' 47''$

Meridian altitude  $79^{\circ} 5' 17''$

Mer. zen. dist.  $10^{\circ} 54' 43''$  S.

Declination  $16^{\circ} 23' 18''$  N.

Latitude  $5^{\circ} 28' 35''$  N.

### EXAMPLES FOR PRACTICE.

Ex. 1. 1876, January 4th, A.M. at ship, latitude by account  $34^{\circ} 47'$  N., long.  $27^{\circ} 12'$  W., observed altitude sun's L.L. South of the observer was  $32^{\circ} 12' 10''$ , index corr  $+ 4' 19''$ , height of eye 28 feet, time by watch  $0^h 13^m 24^s$ , which had been found to be  $25^m 35^s$  fast of app. time at ship, difference of longitude made to West was  $29^{\circ} 2'$  after the error on apparent time at ship was determined: required the latitude.

Ex. 2. 1876, February 28th, P.M. at ship, lat. acct.  $43^{\circ} 46'$  N., long.  $12^{\circ} 31'$  W., obs. alt. sun's L.L.  $38^{\circ} 1' 15''$  S., index corr. —  $5' 10''$ , eye 23 feet, time by watch  $22^m 31^s$ , which had been found to be  $8^m 14^s$  fast of app. time at ship, diff. of long. made to East was  $14'$  after error on app. time at ship was found: required the latitude.

Ex. 3. 1876, March 20th, A.M. at ship, lat. acct.  $41^{\circ} 24'$  S., long.  $105^{\circ}$  E., obs. alt. sun's L.L.  $47^{\circ} 46'$  N., index corr.  $+ 26''$ , eye 22 feet, time by chron.  $19^d 16^h 58^m 12^s$ , which had been found to be  $6^h 34^m 34^s$  slow on app. time at ship, diff. of long. made to East was  $23'$  after the error on app. time at ship was determined: required the latitude.

Ex. 4. 1876, April 21st, A.M. at ship, lat. acct.  $39^{\circ} 54'$  N., long.  $6^{\circ} 6'$  E., obs. alt. sun's L.L.  $61^{\circ} 26' 35''$  S., index. corr.  $+ 1'$ , eye 18 feet, time by watch  $21^d 0^h 8^m 10^s$ , which had been found to be  $27^m 0^s$  fast of app. time at ship, diff. of long. made to East was  $5'$  after the error on app. time at ship was determined.

Ex. 5. 1876, May 29th, P.M. at ship, lat. acct.  $37^{\circ} 15'$  S., long.  $107^{\circ}$  W., obs. alt. sun's L.L.  $30^{\circ} 22' 30''$  N., index corr.  $+ 49''$ , eye 22 feet, time by watch  $29^d 7^h 9^m 11^s$ , which had been found to be  $6^h 36^m 56^s$  fast on app. time at ship, diff. of long. made to West was  $27'$  after the error on app. time at ship was determined.

Ex. 6. 1876, June 19th, A.M. at ship, lat. acct.  $44^{\circ} 24'$  N., long.  $14^{\circ} 5'$  W., obs. alt. sun's L.L.  $68^{\circ} 37' 5''$  South of observer, eye 18 feet, time by watch  $11^h 40^m 40^s$ , which was found to be  $2^m 2^s$  slow on app. time at ship, diff. of long. made to East was  $32\frac{1}{2}'$  after the error on app. time at ship was determined.

Ex. 7. 1876, July 16th, P.M. at ship, lat. acct.  $0^{\circ} 38'$  S., long.  $2^{\circ}$  E., obs. alt. sun's L.L.  $67^{\circ} 41'$  (zen. S.), eye 15 feet, time by watch  $0^h 11^m 9^s$ , found fast on app. time at ship  $56^s$ , diff. of long. made since  $1\frac{1}{2}'$  to East.

Ex. 8. 1876, August 30th, P.M. at ship, lat. acct.  $41^{\circ} 5'$  N., long.  $139^{\circ} 25'$  E., obs. alt. sun's L.L.  $57^{\circ} 20'$  S., index corr.  $+ 2' 21''$ , eye 14 feet, time by watch  $22^m 22^s$ , found to be  $18^s$  slow of app. time at ship, diff. of long. made to West was  $34'$ .

Ex. 9. 1876, Sept. 9th, P.M. at ship, lat. acct.  $9^{\circ} 20'$  N., long.  $178^{\circ} 30'$  E., obs. alt. sun's L.L.  $85^{\circ} 19'$  (zen. N.), eye 20 feet, time by watch  $11^h 59^m 40^s$ , slow on app. time at ship  $9^m 21^s$ , diff. of long. made to East was  $10\frac{1}{2}'$ .

- + Ex. 10. 1876, Oct. 11th, P.M. at ship, lat. acct.  $45^{\circ} 51' N.$ , long.  $85^{\circ} 3' E.$ , obs. alt. sun's L.L.  $36^{\circ} 38' 15'' S.$ , index corr.  $- 5' 15''$ , eye 16 feet, time by watch  $10^d 18^h 50^m 10^s$  which was  $5^h 40^m 12^s$  slow on app. time, diff. of long.  $33' W.$
- + Ex. 11. 1876, Nov. 3rd, P.M. at ship, lat. acct.  $32^{\circ} S.$ , long.  $109^{\circ} 39' E.$ , obs. alt. sun's L.L.  $71^{\circ} 50' N.$ , index corr.  $+ 32''$ , eye 18 feet, time by watch  $2^d 22^h 22^m$ , which was found  $2^h$  slow, diff. of long.  $28^h 7' West.$
- + Ex. 12. 1876, Dec. 23rd, A.M. at ship, lat. acct.  $47^{\circ} 22' S.$ , long.  $27^{\circ} 3' W.$ , obs. alt. sun's L.L.  $65^{\circ} 10' 15'' N.$ , index corr.  $+ 45''$ , eye 12 feet, time by watch  $11^h 29^m 42^s$ , found to be  $18^m 40^s$  slow, diff. of long. was  $36' East.$
- + Ex. 13. 1876, Jan. 5th, P.M. at ship, lat. acct.  $8^{\circ} 50' N.$ , long.  $130^{\circ} 14' W.$ , obs. alt. sun's L.L.  $58^{\circ} 6' 10'' S.$ , eye 21 feet, time by watch  $0^h 2^m 40^s$ , found  $13^m 48^s$  slow on app. time, diff. of long. made since  $16' East.$
- + Ex. 14. 1876, April 28th, A.M. at ship, lat. acct.  $18^{\circ} 46' S.$ , long.  $34^{\circ} 12' W.$ , obs. alt. sun's L.L.  $56^{\circ} 28' (zen. S.)$ , index corr.  $+ 1' 5''$ , eye 21 feet, time by watch  $11^h 49^m 50^s$ , found  $fast 2^m 17^s$  on app. time at ship, diff. of long. made since  $17\frac{1}{2}' West.$
- + Ex. 15. 1876, July 13th, A.M. at ship, lat. acct.  $54^{\circ} 35' S.$ , long.  $152^{\circ} 20' W.$ , obs. alt. sun's L.L.  $13^{\circ} 17' N.$ , index corr.  $+ 47''$ , eye 12 feet, time by watch  $13^d 7^h 54^m 12^s$ , which had been found to be  $8^h 14^m 17^s$  fast on app. time at ship, diff. of long. made to *West* was  $34'$  after error on app. time was determined.
- + Ex. 16. 1876, March 20th, A.M. at ship, lat. acct.  $19^{\circ} S.$ , long.  $33^{\circ} 33' E.$ , obs. alt. sun's L.L.  $70^{\circ} 21' N.$ , index corr.  $- 2' 10''$ , eye 16 feet, time by watch  $8^m 17^s$ , found *fast* on app. time at ship  $26^m 11^s$ , diff. long. made since  $14\frac{1}{2}' East.$
- + Ex. 17. 1876, April 12th, A.M. at ship, lat. acct.  $0^{\circ}$ , long.  $164^{\circ} 12' W.$ , obs. alt. sun's L.L.  $80^{\circ} 30' N.$ , index corr.  $- 5' 10''$ , eye 21 feet, time by watch  $12^d 0^h 0^m 2^s$ , *fast* on app. time at ship  $10^m 51^s$ , diff. of long. made to *East*  $7\frac{1}{2}'$ .
- + Ex. 18. 1876, Sept. 16th, A.M. at ship, lat. acct.  $42^{\circ} 36' S.$ , long.  $137^{\circ} 10' E.$ , obs. alt. sun's L.L.  $44^{\circ} 6' N.$ , index corr.  $+ 2' 10''$ , eye 19 feet, time by watch  $16^d 8^h 41^m 43^s$ , which had been found to be  $9^h 2^m 47^s$  fast on app. time at ship, the diff. of long. made to *West* was  $14'$  after the error on app. time at ship was determined.
- + Ex. 19. 1876, March 16th, A.M. at ship, lat. acct.  $37^{\circ} 42' N.$ , long.  $61^{\circ} 40' E.$ , obs. alt. sun's L.L.  $50^{\circ} 0' 30'' S.$ , index corr.  $+ 34''$ , eye 15 feet, time by watch  $10^h 53^m 31^s$ , found *slow* on app. time at ship  $1^h 3^m 22^s$ , diff. of long. made since  $18' West.$
- + Ex. 20. 1876, December 31st, A.M. at ship, lat. acct.  $52^{\circ} N.$ , long.  $12^{\circ} 53' W.$ , obs. alt. sun's L.L.  $14^{\circ} 46' S.$ , eye 19 feet, time by watch  $0^h 56^m$ , which was *fast* on app. time at ship  $1^h 5^m 20^s$ , diff. of long.  $21^h 4' West.$
- + Ex. 21. 1876, March 5th, P.M. at ship, lat. acct.  $33^{\circ} 35' N.$ , long.  $78^{\circ} E.$ , obs. alt. sun's L.L.  $49^{\circ} 53' 15'' S.$ , index corr.  $- 3' 15''$ , eye 22 feet, time by watch  $4^d 19^h 2^m 12^s$ , found to be  $5^h 17^m 12^s$  slow, diff. of long. was  $10' E.$
- + Ex. 22. 1876, September 22nd, A.M. at ship, lat. acct.  $45^{\circ} 45' S.$ , long.  $111^{\circ} 42' W.$ , obs. alt. sun's L.L.  $43^{\circ} 50' N.$ , index corr.  $- 5' 40''$ , height of eye 18 feet, time by watch  $22^d 7^h 41^m 10^s$ , found to be  $8^h 4^m 10^s$  fast, diff. of long. was  $13^h 5' East.$
- + Ex. 23. 1876, December 23rd, P.M. at ship, lat. acct.  $42^{\circ} 16' N.$ , long.  $4^{\circ} 39' W.$ , obs. alt. sun's L.L.  $24^{\circ} 14' 10'' S.$ , eye 11 feet, time by watch  $0^h 50^m 58^s$ , *fast* on app. time at ship  $19^m 38^s$ , diff. of long.  $21^h 3' West.$

## MERIDIAN ALTITUDE OF A FIXED STAR.

### RULE CII.

- 1°. Take from Nautical Almanac the star's declination.
- 2°. To the observed altitude apply the index error, as the sign attached directs.
- 3°. Subtract the dip answering to the height of eye (Table 5, Norie; Table 30, Raper).

4°. Subtract the refraction (Table 4, Norie; Table 31, Raper), and thus get the true altitude.

5°. Subtract the true altitude from 90; the remainder is the zenith distance.

6°. Mark the zenith distance N. or S., according as the observer is North or South of the star.

7°. Underneath this last place the declination, and take their sum if they have the same names; but take their difference if they have unlike names; the result, in either case, will be the latitude.

The declination of a fixed star changes so slowly that it may be taken out of the *Nautical Almanac* by inspection, without any practical error resulting; a Greenwich date, therefore, is clearly unnecessary.

8°. When the zenith distance and declination are of the same name, the latitude is of that name; when the zenith distance and declination are of different names, the latitude takes the name of the greater.

The stars are inserted in the *Nautical Almanac* in the order of their Right Ascension, from 0<sup>h</sup> to 24<sup>h</sup>; it will, therefore, very much facilitate the finding of the given star in the *Nautical Almanac*, to turn, in the first instance, to the three pages (297—299, *Nautical Almanac*, 1876, and seek the given star under the head "Mean Places of stars" for January, and thence obtain the star's Right Ascension, which find at the top of one of the pages following 317—373, *Nautical Almanac*, 1876), which will give the star, and the declination will be found opposite the day in the side column which is nearest the given day. The degrees (°) and minutes (′) are placed at the top of the column (as annexed), and the seconds (″) are ranged below, for the sake of economizing space in the second column below the name of the star. If the seconds exceed 60″, only take the excess of 60″ and increase the minutes (′) at the top by 1. Thus, on May 10th, (see table annexed) the declination of  $\alpha$  Andromedæ is 28° 22′ 49″ N., and on January 1st, the declination is 28° 23′ 3″ N., 62″·8 being 1′ 3″, which being added to 28° 22′, which stands at the head of the column, gives the declination 28° 23′ 3″.

#### EXAMPLES.

Ex. 1. 1876, Dec. 29th, long. 140° W., the obs. mer. alt. of the star  $\alpha$  Leonis (*Regulus*), bearing South, was 52° 7′ 30″, index corr. — 27″, height of eye 15 feet: required the latitude.

|                            |                |
|----------------------------|----------------|
| Observed altitude of star  | 52° 7′ 30″ S.  |
| Index correction           | — 27           |
|                            | <hr/>          |
|                            | 52° 7′ 3       |
| Dip 15 feet                | — 3 42         |
|                            | <hr/>          |
|                            | 52° 3 21       |
| Refraction                 | — 44           |
|                            | <hr/>          |
| True altitude              | 52° 2 37       |
|                            | <hr/>          |
|                            | 52° 2 37       |
|                            | <hr/>          |
|                            | 90° 0 0        |
|                            | <hr/>          |
| Zenith distance            | 37 57 23 N.    |
| Declination (N.A., p. 345) | 12 34 1 N.     |
|                            | <hr/>          |
| Latitude                   | 50° 31′ 24″ N. |

By Raper: Index corr. — 27″, Dip — 3′ 50″, ref. — 46″, true alt. 52° 2′ 27″, latitude 50° 31′ 34″ N.

Ex. 2. 1876, March 12th, long. 10° E., obs. mer. alt. of the star *Pollux*, bearing North, was 71° 59′ 10″, index corr. + 1′ 15″, height of eye 18 feet: required the latitude.

|                            |                |
|----------------------------|----------------|
| Observed altitude of star  | 71° 59′ 10″ N. |
| Index correction           | + 1 15         |
|                            | <hr/>          |
|                            | 72° 0 25       |
| Dip 18 feet                | — 4 4          |
|                            | <hr/>          |
|                            | 71° 56 21      |
| Refraction                 | — 18           |
|                            | <hr/>          |
| True altitude              | 71° 56 3       |
|                            | <hr/>          |
|                            | 90° 0 0        |
|                            | <hr/>          |
|                            | 18 3 57 S.     |
| Zenith distance            |                |
| Declination (N.A., p. 341) | 28 19 33 N.    |
|                            | <hr/>          |
| Latitude                   | 10 15 36 N.    |

By Raper: Index corr. + 1′ 15″, dip — 3′ 10″, ref. — 19″, true alt. 71° 55′ 56″, latitude 10° 15′ 29″ N.



Ex. 3. 1876, March 11th, long.  $84^{\circ}$  W., the obs. mer. alt. of the star  $\alpha$  Argus (*Canopus*), bearing South, was  $37^{\circ} 26'$  index corr.  $+ 1' 12''$ , height of eye 16 feet.

Observed altitude of star  $37^{\circ} 26' 0''$  S.  
Index correction  $+ 1' 12''$

Dip 16 feet  $37^{\circ} 27' 12''$   
 $- 3' 50''$

Refraction  $37^{\circ} 23' 22''$   
 $- 1' 15''$

True altitude  $37^{\circ} 22' 7''$   
 $90^{\circ} 0' 0''$

Zenith distance  $52^{\circ} 37' 53''$  N.  
Declination (N.A., p. 338)  $52^{\circ} 37' 53''$  S.

Latitude  $0^{\circ} 0' 0''$

By Raper: Index corr.  $+ 1' 12''$ , dip  $- 4' 0''$ , ref.  $- 1' 16''$ , true alt.  $37^{\circ} 21' 56''$ , latitude  $0^{\circ} 0' 11''$  N.

Ex. 4. 1876, January 1st, long.  $100^{\circ}$  E., the obs. mer. alt. of the star  $\alpha$  Canis Majoris (*Sirius*), bearing South, was  $59^{\circ} 59' 50''$ , index corr.  $+ 4' 12''$ , height of eye 24 feet.

Observed altitude of star  $59^{\circ} 59' 50''$  S.  
Index correction  $+ 4' 12''$

Dip 24 feet  $60^{\circ} 4' 2''$   
 $- 4' 42''$

Refraction  $59^{\circ} 59' 20''$   
 $- 33''$

True altitude  $59^{\circ} 58' 47''$   
 $90^{\circ} 0' 0''$

Zenith distance  $30^{\circ} 1' 13''$  N.  
Declination (N.A., p. 339)  $16^{\circ} 32' 44''$  S.

Latitude  $13^{\circ} 28' 29''$  N.

By Raper: Index corr.  $+ 4' 12''$ , dip  $- 4' 50''$ , ref.  $- 34''$ , true alt.  $59^{\circ} 58' 38''$ , latitude  $13^{\circ} 28' 38''$  N.

### EXAMPLES FOR PRACTICE.

In each of the following examples it is required to find the latitude:—

| NO. | CIVIL DATE.<br>1876. | LONG.            | STAR.  | OBS. ALT.                | CORR.       | EYE.  |
|-----|----------------------|------------------|--|--------------------------|-------------|-------|
| 1.  | Nov. 7th,            | $90^{\circ}$ W.  | $\alpha$ Andromedæ .....                       | $75^{\circ} 10' 30''$ S. | $+ 0' 27''$ | 25ft. |
| 2.  | Jan. 1st,            | $27^{\circ}$ W.  | $\alpha$ Aurigæ ( <i>Capella</i> ) .....       | $54^{\circ} 0' 15''$ N.  | $- 1' 45''$ | 18    |
| 3.  | Aug. 19th,           | $84^{\circ}$ E.  | $\alpha$ Lyre ( <i>Vega</i> ) .....            | $50^{\circ} 0' 20''$ N.  | $0' 0''$    | 22    |
| 4.  | Dec. 22nd,           | $82^{\circ}$ E.  | $\alpha$ Persei .....                          | $51^{\circ} 51' 45''$ N. | $+ 0' 40''$ | 26    |
| 5.  | April 11th,          | $142^{\circ}$ W. | $\alpha$ Virginæ ( <i>Spica</i> ) .....        | $63^{\circ} 14' 30''$ S. | $+ 3' 47''$ | 22    |
| 6.  | June 10th,           | $151^{\circ}$ E. | $\alpha$ Eridani ( <i>Achernar</i> ) .....     | $40^{\circ} 10' 25''$ S. | $+ 0' 55''$ | 24    |
| 7.  | Dec. 27th,           | $91^{\circ}$ W.  | ( <i>Algenib</i> ) .....                       | $78^{\circ} 16' 45''$ S. | $- 0' 25''$ | 24    |
| 8.  | Nov. 30th,           | $24^{\circ}$ W.  | $\alpha$ Arietis .....                         | $68^{\circ} 23' 0''$ N.  | $- 1' 38''$ | 28    |
| 9.  | Feb. 2nd,            | $76^{\circ}$ E.  | $\alpha$ Tauri ( <i>Aldebaran</i> ) .....      | $29^{\circ} 52' 10''$ N. | $+ 5' 20''$ | 15    |
| 10. | June 1st,            | $97^{\circ}$ E.  | $\alpha^1$ Crucis .....                        | $75^{\circ} 10' 30''$ S. | $- 1' 40''$ | 14    |
| 11. | May 22nd,            | $178^{\circ}$ W. | $\alpha$ Hydræ .....                           | $30^{\circ} 28' 53''$ S. | $- 7' 38''$ | 11    |
| 12. | July 17th,           | $29^{\circ}$ E.  | $\alpha$ Cygni .....                           | $20^{\circ} 13' 50''$ N. | $0' 0''$    | 18    |
| 13. | Oct. 17th,           | $165^{\circ}$ E. | $\alpha$ Aquilæ ( <i>Altair</i> ) .....        | $60^{\circ} 49' 10''$ N. | $+ 0' 55''$ | 17    |
| 14. | March 2nd,           | $154^{\circ}$ W. | $\alpha$ Canis Majoris ( <i>Sirius</i> ) ....  | $58^{\circ} 58' 50''$ N. | $+ 1' 10''$ | 20    |
| 15. | April 3rd,           | $111^{\circ}$ E. | $\alpha$ Bootis ( <i>Arcturus</i> ) .....      | $79^{\circ} 49' 40''$ S. | $- 2' 5''$  | 25    |
| 16. | Aug. 7th,            | $40^{\circ}$ W.  | $\alpha$ Scorpii ( <i>Antares</i> ) .....      | $68^{\circ} 49' 30''$ S. | $- 1' 54''$ | 21    |
| 17. | May 1st,             | $8^{\circ}$ E.   | $\alpha^2$ Centauri .....                      | $10^{\circ} 2' 50''$ S.  | $- 0' 45''$ | 20    |
| 18. | Oct. 29th,           | $5^{\circ}$ W.   | $\alpha$ Piscis Australis ( <i>Fomalhaut</i> ) | $70^{\circ} 6' 0''$ N.   | $+ 0' 55''$ | 12    |
| 19. | March 31st,          | $36^{\circ}$ E.  | $\alpha$ Pegasi ( <i>Markab</i> ) .....        | $33^{\circ} 20' 50''$ N. | $+ 1' 20''$ | 20    |
| 20. | Sept. 11th,          | $12^{\circ}$ W.  | $\alpha$ Cassiopeiæ .....                      | $62^{\circ} 24' 50''$ N. | $- 7' 30''$ | 19    |

# ORDINARY EXAMINATION.

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## EXAMINATION PAPER

*To be used by all Candidates when appearing for Examination for the first time only.*

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### DEFINITIONS.

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*The Candidate is requested to write at least ten of the following definitions. The writing should be clear, and the spelling should not be disregarded.*

- 1.—The Equator is a great circle passing round the earth at an equal distance from the two poles.
2. The Poles are the extremities of the axis of the earth.
3. A Meridian is a great circle passing through both poles, perpendicular to the equator.
4. The Ecliptic is the great circle of the celestial sphere in which the sun appears to move in consequence of the earth's motion in its orbit.
5. The Tropics of Cancer and Capricorn are the parallels of latitude  $23^{\circ} 28'$  N. and S.
6. Latitude is that portion of the meridian which is contained between the equator and the given place, and is reckoned in degrees, minutes, and seconds.
7. Parallels of Latitude are small circles parallel to the equator.
8. Longitude is an arc of the equator between the "first meridian" and the meridian of the place.
9. The Visible Horizon is the circle bounding the spectator's view at sea.
10. The Sensible Horizon is the plane on which the spectator stands, produced to meet the celestial concave.
11. The Rational Horizon is an imaginary plane parallel to the sensible horizon, and passing through the centre of the earth.
12. Artificial Horizon and its use. It is a small shallow trough, containing quicksilver, or any other fluid, the surface of which affords a reflected image of a heavenly body. It is used for observing altitudes on shore.
13. True Course of a ship is the angle which the ship's track makes with the meridian, or N. and S. line of the horizon.
14. Magnetic Course (correct magnetic) is the angle which the ship's track makes with the magnetic meridian.
15. Compass Course is the angle which the ship's track makes with the N. and S. line of the compass card.
16. Variation of the Compass is the angle which the magnetic needle, under the influence of terrestrial magnetism only, makes with the meridian.
17. Deviation of the compass is the angle the compass needle makes with the (correct) magnetic meridian.
18. The Error of the Compass is the angle the compass needle makes with the true meridian, being the combined effect of the variation and deviation.
19. Leeway is the angle included between the direction of the ship's keel and the direction of the wake she leaves on the surface of the water.
20. Meridian Altitude of a celestial object is the angular height of that object above the horizon when it is on the meridian of the place of observation.
21. Azimuth of a celestial object is the arc of the horizon between the N. and S. points, and a vertical circle drawn through the object.

22. Amplitude is the arc of the horizon between the East point and the centre of the object when rising, or the West point when setting.

23. Declination of a celestial object is the arc of a circle of declination between the object and the equator.

24. Polar distance is an arc of a circle of declination between the body and the pole (complement of the declination).

25. Right Ascension of a body is an arc of the equator, or an angle at the pole intercepted between the meridian passing through the first point of Aries, and that over the object.

26. Dip is the angle through which the sea horizon is depressed in consequence of the elevation of the spectator above the surface of the earth.

27. Refraction is the correction to be applied to the place of a heavenly body as actually viewed through the atmosphere, which bends the rays of light which pass through it, into a position more nearly vertical, and thus causes the apparent places of the heavenly bodies to be above the true place.

28. Parallax is a correction to reduce an altitude as observed from the surface of the earth, to what it would be if taken from the centre. It is the angle subtended at the object by that radius of the earth which is drawn to the place of observation.

29. Semi-diameter of a heavenly body is half the angle subtended by the diameter of the visible disc at the eye of the observer.

30. Moon's Augmented Semi-diameter is an increase of the moon's apparent dimension due to increase of altitude, because the Moon's distance from the spectator decreases as the altitude increases.

31. Observed Altitude is the angular distance of a heavenly body from the horizon, as observed with the sextant or other instrument.

32. Apparent Altitude is the altitude of a celestial body as seen from the surface of the earth; or, the observed altitude corrected for index error and dip.

33. True altitude is the altitude of a celestial body as seen from the centre of the earth; that is, the apparent altitude corrected for refraction, semi-diameter, and parallax.

34. Zenith Distance is an arc of a circle of altitude between the body and the zenith (complement of the altitude).

35. Vertical circles are great circles passing through the zenith and nadir, perpendicular to the horizon. They are also called *Circles of Altitude*, because altitudes are measured on them; and *Circles of Azimuth*, as marking out all the points that have the same azimuth.

36. Prime vertical is a great circle passing through the zenith and nadir, and the East and West (true) points of the horizon.

37. Civil time is the time used in ordinary life to record events. It begins at midnight and ends at the following midnight, and its hours are reckoned through twice 12, from midnight to noon, denoted by A.M.; and then from noon to midnight, denoted by P.M.

38. Astronomical Time is the time used in all astronomical calculations; it begins at noon and ends at the following noon, its hours being reckoned from 0<sup>h</sup> to 24<sup>h</sup>.

39. Sidereal Time is the westerly hour-angle of the first point of Aries.

40. Mean Time is the hour-angle which the mean sun is westward of the meridian.

41. Apparent Time is the hour-angle of the apparent or true sun, always reckoning westward.

42. Equation of Time is an angle at the pole between a meridian over the true sun, and one over the mean sun.

43. Hour-angle of a Celestial Object is an angle at the pole included between the meridian of the observer and that over the object.

44. Complement of an Arc or Angle is that arc or angle which must be added to it to make a right-angle (90°).

45. Supplement of ditto is that angle which must be added to it to make two right-angles (180°).

## EXAMINATION PAPER.—No. I.

## FOR SECOND MATE.

1. Multiply 7654 by 95 by common logarithms.
2. Divide 3654000 by 7308 by common logarithms.
- 3.—

| II. | COURSES.              | K. | $\frac{1}{10}$ | WINDS.     | LEE-<br>WAY.          | DEVI-<br>TION. | REMARKS, &c.  |
|-----|-----------------------|----|----------------|------------|-----------------------|----------------|---|
| 1   | W.S.W.                | 10 | 8              | N.W.       | pts.<br>$\frac{1}{2}$ | 11° W.         | A point, lat. 37° 3' N.<br>long. 9° 0' W., bearing<br>by compass N.E. $\frac{1}{4}$ E.<br>dist. 15 miles. (Ship's<br>head W.S.W.) Dev.<br>as per log.         |
| 2   |                       | 11 | 4              |            |                       |                |   |
| 3   |                       | 11 | 4              |            |                       |                |   |
| 4   |                       | 11 | 4              |            |                       |                |   |
| 5   | N.W. $\frac{1}{2}$ N. | 12 | 2              | W.S.W.     | $\frac{1}{4}$         | 17° W.         |   |
| 6   |                       | 12 | 3              |            |                       |                |   |
| 7   |                       | 12 | 3              |            |                       |                |   |
| 8   |                       | 12 | 2              |            |                       |                |   |
| 9   | N.N.W.                | 9  | 6              | West.      | $\frac{3}{4}$         | 11° W.         |   |
| 10  |                       | 9  | 5              |            |                       |                |   |
| 11  |                       | 9  | 5              |            |                       |                |   |
| 12  |                       | 9  | 4              |            |                       |                |   |
| 1   | N.W. by W.            | 7  | 8              | S.W. by W. | $1\frac{1}{4}$        | 20° W.         | Var. 22° 30' W.   |
| 2   |                       | 7  | 6              |            |                       |                |   |
| 3   |                       | 7  | 4              |            |                       |                |   |
| 4   |                       | 8  | 2              |            |                       |                |   |
| 5   | S.W. $\frac{1}{2}$ S. | 9  | 3              | S.S.E.     | 1                     | 6° W.          |   |
| 6   |                       | 8  | 7              |            |                       |                |   |
| 7   |                       | 9  | 2              |            |                       |                |   |
| 8   |                       | 8  | 7              |            |                       |                |   |
| 9   | W. $\frac{1}{2}$ S.   | 10 | 3              | S. by W.   | $\frac{1}{2}$         | 14° W.         | A current set the ship<br>S.W. by W. $\frac{3}{4}$ W. (cor-<br>rect magnetic) 8 miles<br>from the time the de-<br>parture was taken to<br>the end of the day. |
| 10  |                       | 10 | 2              |            |                       |                |   |
| 11  |                       | 10 | 2              |            |                       |                |   |
| 12  |                       | 10 | 3              |            |                       |                |   |

Correct the courses for deviation, variation, and leeway, and find the course and distance from the given point, and the latitude and longitude in by inspection.

4. 1876, January 1st, in longitude 102° 41' W., the observed meridian altitude of the sun's L.L. was 59° 59' 50", bearing South, index error + 50", height of eye 15 feet: required the latitude.

5. In latitude 37° N., the departure made good was 89.2 miles: required the difference of longitude by parallel sailing.

6. Required the course and distance from Toulon to Valencia, by Mercator's sailing.

Lat. Toulon 43° 8' N.

Long. Toulon 5° 56' E.

Lat. Valencia 39 29 N.

Long. Valencia 0 24 W.

## ADDITIONAL FOR ONLY MATE.

7. 1875, January 6th: find the time of high water, A.M. and P.M., at Cherbourg and Portland Breakwater.

8. 1876, January 1st, at 8<sup>h</sup> 4<sup>m</sup> A.M. apparent time at ship, in latitude 50° 32' N., longitude 139° 51' W., the sun's magnetic amplitude E. by S.  $\frac{1}{2}$  S.: required the true amplitude and error of the compass; and supposing the variation to be 23° 52' E.: required the deviation of the compass for the position of the ship's head when the observation was taken.

9. 1876, January 29th, P.M. at ship, latitude 42° 26' N., observed altitude sun's L.L. 13° 40', index error — 1' 14", height eye 16 feet, time by chronometer 29<sup>d</sup> 6<sup>h</sup> 48<sup>m</sup> 40<sup>s</sup>, which was slow 11<sup>m</sup> 22<sup>s</sup>.3 for mean noon at Greenwich, December 1st, 1875, and on January 1st, 1876, was 8<sup>m</sup> 7<sup>s</sup> slow for Greenwich mean noon: required the longitude by chronometer.

ADDITIONAL FOR FIRST MATE.

10. 1876, January 15th, mean time at ship  $9^h 39^m 44^s$  A.M., latitude  $23^\circ 39'$  S., longitude  $127^\circ 52'$  W., sun's magnetic azimuth S.  $103^\circ$  E., observed altitude sun's L.L.  $55^\circ 8' 30''$ , index error —  $2' 30''$ , height of eye 12 feet: required the true azimuth and error of the compass: and supposing the variation be  $7^\circ 50'$  E.: required the deviation of the compass for the position of the ship's head at the time the observation was taken.

11. 1876, January 17th, P.M. at ship, latitude by account  $36^\circ 2'$  N., longitude  $149^\circ 28'$  E., observed altitude sun's L.L. South of observer was  $32^\circ 54' 15''$ , index error +  $2' 18''$ , height of eye 22 feet, time by watch  $11^h 59^m$ , which had been found to be  $20^m 24^s$  slow on apparent time at ship, the difference of longitude made to the *West* since the error of watch on app. time at ship was determined, was  $39' 2''$ : required the latitude by reduction to meridian.

ADDITIONAL FOR MASTER ORDINARY.

12. 1876, January 24th, the observed meridian altitude of the star  $\alpha$  Tauri (*Aldebaran*) was  $52^m 36^s$  bearing South, index correction —  $23''$ , height of eye 20 feet: required the latitude.

DEVIATION OF THE COMPASS.

N.B.—*The Candidate is to answer correctly at least eight of such of the following questions as are marked with a cross by the Examiner. The Examiner will not mark less than twelve.*

1. What do you mean by Deviation of the Compass?

A. The deflection of the compass needle from the magnetic meridian caused by the attraction of the iron of the ship.

2. How do you determine the deviation (*a*) when in port, (and *b*) when at sea?

A. By bringing the ship's head successively upon each of the thirty two points of the Standard Compass, or on each alternate point, and then (*a*) by taking reciprocal simultaneous bearings; or by the observer on board taking the bearings of a distant object whose correct magnetic bearing is known, or of some conspicuous object in a line with figures on a dock wall. (*b*) At sea, by bearings of well known conspicuous objects in a line on the coast, or by amplitudes and azimuths and the known variation at the place of the ship.

3. Having determined the deviation with the ship's head on the various points of the compass, how do you know when it is Easterly and when Westerly?

A. When the *correct* magnetic bearing of the distant object is to the *right* of the reading of the compass on board, the deviation is easterly, when to the *left*, westerly.

4. Why is it necessary, in order to ascertain the deviations, to bring the ship's head in more than one direction?

A. Because the deviation alters as the direction of the ship's head is changed.

5. For accuracy, what is the least number of points to which the ship's head should be brought?

A. Eight; although, if the deviations be known on the four quadrantal points, N.E., S.E., S.W., and N.W., with the aid of Napier's diagram a good deviation curve may be formed.

6. How would you find the deviation when sailing along a well known coast?

A. By taking with the Standard Compass the bearing of two well defined objects in a line, as for instance, the bearings of two beacons, two lights, two points of land, not too near one another, and whose correct magnetic bearing is known, from the chart or otherwise; then the difference between the *correct* magnetic bearing and the compass bearing is the deviation for the direction of the ship's head when the bearing was taken.

7. In the following table give the correct magnetic bearing of the distant object, and thence the deviation.

Correct magnetic bearing.

| Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North ....                       | N. 86° W.                                      |                     | South ....                       | S. 64° W.                                      |                     |
| N.E. ....                        | S. 79 W.                                       |                     | S.W. ....                        | S. 72 W.                                       |                     |
| East .....                       | S. 69 W.                                       |                     | West ....                        | S. 89 W.                                       |                     |
| S.E. ....                        | S. 65 W.                                       |                     | N.W. ....                        | N. 80 W.                                       |                     |

8. With the deviation as above, give the courses you would steer by the Standard Compass to make the following courses correct magnetic.

Correct magnetic courses:—W.N.W.; N.N.E.; E.S.E.; S.S.W.

Compass courses:—

9. Supposing you have steered the following courses by the Standard Compass, find the correct magnetic courses made from the above deviation table.

Compass courses:—N.N.W.; E.N.E.; S.S.E.; W.S.W.

Magnetic courses:—

10. You have taken the following bearings of two distant objects by your Standard Compass as above, with the ship's head at N.W. by W., find the bearings, correct magnetic.

Compass bearings:—E. by S.  $\frac{1}{4}$  S. and N.  $\frac{1}{2}$  E.

Bearings, magnetic:—

11. Name some suitable objects by which you could readily obtain the deviation of the Compass when sailing along the coasts of the English Channel.

The South Foreland lighthouses in one, bearing W. by N., *correct* magnetic: Beachy Head lighthouse just open of the cliffs to the eastward, bearing N.W. by W., *correct* magnetic; Portland lights in one N.N.W.  $\frac{1}{4}$  W.; Prawl Point and Start lighthouse in one and Lizard lights in one.

12. Do you expect the deviation to change; if so, state under what circumstances?

A. Yes, it changes rapidly for several months after the ship is launched, an alteration also takes place by change of magnetic latitude, and in ships running long upon one course and then changing the course, by the heeling of the ship, and by taking in a cargo of iron.

13. How often is it advisable to test the accuracy of your table of deviations?

A. Frequently, in a new vessel; when nearing land; and under the circumstances stated in last question.

14. State briefly what you have chiefly to guard against in selecting a position for the compass.

A. Elongated iron, especially if vertical, such as stanchions, davits, capstan, spindles, funnels, ventilating shafts, &c., and the compass should be as far removed as possible from transverse bulk heads.

15. The Compasses of iron Ships are more or less affected by what is termed the heeling error; on what courses does this error vanish, and on what courses is it the greatest?

A. It vanishes when the Ship's head is East or West by compass, and is greatest when the Ship's head, by compass, is North or South.

16. State to which side of the ship, in the majority of cases, is the North point of the Compass drawn in the Northern hemisphere; and what effect has it on the assumed position of the Ship when she is steering on Northerly, and also on Southerly courses?

A. The North point of the Compass is drawn to the weather side in the majority of cases. The effect of this is to throw the Ship to windward on northerly courses, and to leeward on southerly courses.

17. The effect being as you state, on what courses would you keep away, and on what courses would you keep closer to the wind, in order to make good a given Compass course?

A. I would keep her away on either tack on northerly courses, but on either tack on southerly I would keep her close to the wind.

18. Does the same rule hold good in both hemispheres with regard to the heeling error?

A. No, ships which have a large heeling error to windward in northern latitudes, will probably have as large a heeling error to leeward in high southern latitudes; but it is recommended in order to determine it, that observations be made in every ship.

19. Your steering compass having a large error, how would you proceed to correct that compass by compensating magnets and soft iron in order to reduce the error within manageable limits.

A. Draw a line upon the deck, fore-and-aft, through the centre of the binnacle. Draw another line across the deck at right-angles to the former, through the same centre.

Bring the ship's head either North or South (correct magnetic), and placing a magnet on the deck athwartship, with its centre exactly on a fore-and-aft line drawn on the deck at some distance from the binnacle; move it gradually to or from the foot of the binnacle until the compass points correctly. If the compass needle deviates to the left, the north end of the magnet must be placed to the left, and conversely. Next swing the ship's head round to the East or West (correct magnetic) and steady her on one of these points, and place a magnet fore-and-aft, either on the port or starboard side of the binnacle, with its centre on the athwartship line drawn on the deck; move it to or from the foot of the binnacle until the compass points correctly.

Again: the semicircular deviation having thus been corrected, and the binnacle being properly fitted with two small brass boxes, one on each side of, and on a level with the compass; steady the ship's head on one of the quadrantal points, N.E., S.E., S.W., or N.W.: if there is any deviation fill one of the chain boxes with a quantity of small chain until the compass points correctly; if one chain box be not sufficient, fill the other. For greater certainty, swing the ship's head to each of the other quadrantal points.

### EXAMINATION PAPER.—No. II.

#### FOR SECOND MATE.

1. Multiply 50030 by 800 by common logarithms.
2. Divide 9999.46 by 67.8 by common logarithms.

3.—

| H. | COURSES.   | K. | $\frac{1}{10}$ | WINDS.     | LEE-<br>WAY.   | DEVI-<br>ATION. | REMARKS, &c.  |
|----|------------|----|----------------|------------|----------------|-----------------|---|
| 1  | S.E. by E. | 13 | 2              | N.         | pts.           | 11° E.          | A point of land in<br>lat. 47° 31' N., long.<br>52° 33' W., bearing<br>by compass W.S.W.,<br>dist. 18 miles. (Ship's<br>head S.E. by E.) De-<br>viation as per log. |
| 2  |            | 13 | 3              |            | 0              |                 |   |
| 3  |            | 12 | 5              |            |                |                 |   |
| 4  | S.E.       | 13 |                | E.N.E.     | $\frac{1}{2}$  | 9° E.           |   |
| 5  |            | 11 |                |            |                |                 |   |
| 6  |            | 10 | 5              |            |                |                 |   |
| 7  | E. by N.   | 10 | 4              | S.E. by S. | 1              | 17° E.          |   |
| 8  |            | 11 | 1              |            |                |                 |   |
| 9  |            | 8  | 8              |            |                |                 |   |
| 10 | E.N.E.     | 8  | 4              | S.E.       | $1\frac{1}{2}$ | 15° E.          | Variation 28° W.  |
| 11 |            | 9  | 4              |            |                |                 |   |
| 12 |            | 9  |                |            |                |                 |   |
| 1  | E.N.E.     | 6  | 8              | S.E.       | $1\frac{1}{2}$ | 15° E.          |   |
| 2  |            | 6  | 7              |            |                |                 |   |
| 3  |            | 6  | 5              |            |                |                 |   |
| 4  | S.S.E.     | 7  | 8              | East.      | 2              | 7° E.           |   |
| 5  |            | 5  | 8              |            |                |                 |   |
| 6  |            | 5  | 8              |            |                |                 |   |
| 7  | S.E. by S. | 6  | 4              | E. by N.   | $1\frac{1}{4}$ | 8° E.           | A current set (cor-<br>rect magnetic) S. $\delta$ E.,<br>12 miles, from the time<br>the departure was<br>taken to the end of the<br>day.                            |
| 8  |            | 7  |                |            |                |                 |   |
| 9  |            | 7  | 3              |            |                |                 |   |
| 10 |            | 7  | 4              |            |                |                 |   |
| 11 |            | 7  | 4              |            |                |                 |   |
| 12 |            | 7  | 3              |            |                |                 |   |

4. 1876, February 1st, in longitude  $78^{\circ} 14'$  E., the observed meridian altitude of sun's L.L. was  $78^{\circ} 4' 10''$ , bearing South, index error  $+ 55'$ , height of eye 12 feet: required the latitude.

5. In latitude  $47^{\circ} 30'$  N., the departure made good was 115.5 miles: required the difference of longitude by parallel sailing.

6. Required the course and distance from St. Helena to Cape Horn, by calculation on Mercator's principle.

Latitude St. Helena  $15^{\circ} 55'$  S.

Longitude St. Helena  $5^{\circ} 44'$  W.

Latitude Cape Horn  $55^{\circ} 59'$  S.

Longitude Cape Horn  $67^{\circ} 16'$  W.

#### ADDITIONAL FOR ONLY MATE.

7. 1875, February 5th: find A.M. and P.M. tides at Filey Bay, Milford Haven, and Cromarty.

8. 1876, February 20th, at  $6^h 9^m$  P.M., apparent time at ship, latitude  $11^{\circ} 58'$  S., longitude  $179^{\circ} 42'$  E., sun's magnetic amplitude S.W. by W.  $\frac{1}{4}$  W.: required the true amplitude and error of compass; and supposing the variation to be  $10^{\circ} 20'$  E., required the deviation of the compass for the position of the ship's head at the time of observation.

9. 1876, February 10th, A.M. at ship, latitude  $50^{\circ} 48'$  N., observed altitude sun's L.L.  $9^{\circ} 10' 50''$ , index correction  $- 3' 20''$ , height of eye 18 feet, time by chronometer February  $9^h 9^m 59^s$ , which was  $37^m 58^s.8$  fast for mean noon at Greenwich, December 20th, 1875, and on January 10th, 1876, was  $34^m 12^s$  fast for mean noon at Greenwich: required the longitude.

#### ADDITIONAL FOR FIRST MATE.

10. 1876, February 16th, mean time at ship  $8^h 7^m 35^s$  A.M., latitude  $51^{\circ} 2'$  N., longitude  $140^{\circ} 34'$  W., sun's magnetic azimuth S.  $36^{\circ} 20'$  E., observed altitude sun's L.L.  $7^{\circ} 16' 40''$ , index correction  $- 6' 10''$ , height of eye 15 feet: required the error of compass; and supposing the variation to be  $25^{\circ}$  W.: required the deviation for the position of the ship's head at the time of observation.

11. 1876, February 15th, A.M. at ship, latitude acct.  $55^{\circ} 59'$  S., longitude  $54^{\circ} 18'$  E., observed altitude sun's L.L. North of observer was  $46^{\circ} 22' 10''$ , index correction  $- 1' 50''$ , height of eye 19 feet, time by watch  $0^m 5^s$ , which had been found to be  $30^m$  fast on apparent time at ship, the difference of longitude made to the East was  $16^{\circ} 8'$ : required the latitude.

#### ADDITIONAL FOR MASTER ORDINARY.

12. 1876, February 12th, the observed meridian altitude of star Procyon, South of observer, was  $77^{\circ} 18' 10''$ , index correction  $+ 19''$ , height of eye 16 feet: required the latitude.

In the following table give the correct magnetic bearing of the distant object, and thence the deviation:—

Correct magnetic bearing.

| Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North ....                       | S. $34^{\circ}$ E.                             |                     | South ....                       | S. $43^{\circ}$ E.                             |                     |
| N.E. ....                        | S. $58^{\circ}$ E.                             |                     | S.W. ....                        | S. $31^{\circ}$ E.                             |                     |
| East .....                       | S. $62^{\circ}$ E.                             |                     | West ....                        | S. $17^{\circ}$ E.                             |                     |
| S.E. ....                        | S. $52^{\circ}$ E.                             |                     | N.W. ....                        | S. $15^{\circ}$ E.                             |                     |



With the deviation as above, give the courses you would steer by the Standard Compass to make the following courses correct magnetic.

Correct magnetic courses:—N.E. by E.  $\frac{1}{2}$  E.; W.  $\frac{1}{4}$  S.; W.  $\frac{3}{4}$  N.; E. by S.  $\frac{1}{2}$  S.

Compass courses:—

Supposing you have steered the following courses by the Standard Compass, find the correct magnetic courses made from the above deviation table.

Compass courses:—W. by N.  $\frac{1}{2}$  N.; N.E.  $\frac{3}{4}$  N.; S.W.  $\frac{1}{4}$  S.; S.E. by S.

Magnetic courses:—

You have taken the following bearings of two distant objects by your Standard Compass as above, with the ship's head at W.  $\frac{1}{2}$  S., find the bearings, correct magnetic.

Compass bearings:—N.  $79^{\circ}$  W., and S.  $19^{\circ}$  W.

Bearings, magnetic:—

# EXAMINATION PAPER.—No. III.

## FOR SECOND MATE.

- Multiply  $84.8$  by  $62.8$ , by common logarithms, and prove the result.
- Divide  $666.666$  by  $8.88$ , by common logarithms, and prove the result by decimals.

3.—

| H. | COURSES.                | K. | $\frac{1}{10}$ | WINDS.   | LEE-WAY.            | DEVIATION.      | REMARKS, &c.  |
|----|-------------------------|----|----------------|----------|---------------------|-----------------|---|
| 1  | S.S.E.                  | 5  | 6              | East.    | pts. $2\frac{1}{4}$ | $3^{\circ}$ E.  | A point of land in lat. $62^{\circ}$ N. long. $150^{\circ}$ E. bearing by compass W. by S. $\frac{1}{4}$ S., distance 17 miles. (Ship's head S.S.E.) Dev. as per log. |
| 2  |                         | 5  | 6              |          |                     |                 |   |
| 3  |                         | 5  | 8              |          |                     |                 |   |
| 4  | S.S.W. $\frac{1}{2}$ W. | 4  | 7              | West.    | $2\frac{3}{4}$      | $4^{\circ}$ W.  |   |
| 5  |                         | 4  | 8              |          |                     |                 |   |
| 6  |                         | 5  | 2              |          |                     |                 |   |
| 7  |                         | 5  | 3              |          |                     |                 |   |
| 8  | W.S.W.                  | 5  | 6              | South.   | $2\frac{1}{2}$      | $9^{\circ}$ W.  |   |
| 9  |                         | 6  | 5              |          |                     |                 | Variation $31^{\circ}$ E.   |
| 10 |                         | 6  | 5              |          |                     |                 |   |
| 11 | W. $\frac{1}{2}$ N.     | 6  | 6              | N. by E. | o                   | $11^{\circ}$ W. |   |
| 12 |                         | 7  | 4              |          |                     |                 |   |
| 1  |                         | 6  | 6              |          |                     |                 |   |
| 2  | East.                   | 4  | 6              | S.S.E.   | $2\frac{1}{2}$      | $10^{\circ}$ E. |   |
| 3  |                         | 5  | 8              |          |                     |                 |   |
| 4  |                         | 4  | 6              |          |                     |                 |   |
| 5  | E.S.E.                  | 4  | 5              | S. by W. | o                   | $9^{\circ}$ E.  | A current set the ship (correct magnetic) N.N.E., 21 miles from the time the departure was taken to the end of the day.   |
| 6  |                         | 4  | 5              |          |                     |                 |   |
| 7  |                         | 5  | 5              |          |                     |                 |   |
| 8  |                         | 5  | 5              |          |                     |                 |   |

4. 1876, March 20th, longitude  $173^{\circ} 18'$  E., the observed meridian altitude of sun's L.L. was  $89^{\circ} 38' 10''$  bearing North, index correction  $+ 4' 27''$ , height of eye 18 feet: required the latitude.

5. In latitude  $34^{\circ} 28'$  S., the departure made good was  $394.2$  miles: required the difference of longitude by parallel sailing.

6. Required the course and distance from the Cape of Good Hope to Cape Frio.

Lat. Cape of Good Hope  $34^{\circ} 28'$  S.

Long. Cape of Good Hope  $18^{\circ} 28'$  E.

Lat. Cape Frio  $23^{\circ} 0'$  S.

Long. Cape Frio  $41^{\circ} 57'$  W.

## ADDITIONAL FOR ONLY MATE.

7. 1875, March 11th: find the times of high water, A.M. and P.M. (by Admiralty Tables) at Quillebauc, Havre, Poole, Yarmouth Roads, Lerwick, and Beaumaris.

8. 1876, March 6th, at 5<sup>h</sup> 31<sup>m</sup> 52<sup>s</sup> P.M. apparent time at ship, in latitude 52° 12' N, longitude 138° 54' W., the sun's magnetic amplitude was W. by S.  $\frac{1}{2}$  S.: required the error of compass, and supposing the variation to be 24° E.: required the deviation for the position of the ship's head at the time of observation.

9. 1876, March 31st, A.M. at ship, latitude 26° 9' N., observed altitude sun's L.L. 29° 10' 20", height of eye 26 feet, time by chronometer 31<sup>d</sup> 0<sup>h</sup> 4<sup>m</sup> 50<sup>s</sup>, which was 58<sup>m</sup> 58<sup>s</sup> fast for mean noon at Greenwich, November 20th, 1875, and on December 31st, 1875, was 1<sup>h</sup> 2<sup>m</sup> 55<sup>s</sup>.8 fast for mean time at Greenwich: required the longitude.

## ADDITIONAL FOR FIRST MATE.

10. 1876, March 10th, mean time at ship, 7<sup>h</sup> 35<sup>m</sup> 25<sup>s</sup> A.M., latitude 42° 41' S., longitude 148° 5' E., sun's bearing by compass S. 108° 37' 30" E., observed altitude sun's L.L. 17° 57' 40", height of eye 19 feet: required the error of the compass; and supposing the variation to be 10° 50' E.: required the deviation for the position of the ship's head at the time of observation.

11. 1876, March 25th, P.M. at ship, latitude acct. 20° 1' N., longitude 89° 10' E., observed altitude sun's L.L. South of observer was 71° 9', height of eye 18 feet, time by watch 11<sup>h</sup> 38<sup>m</sup> 12<sup>s</sup> (or 24<sup>d</sup> 23<sup>h</sup> 38<sup>m</sup> 12<sup>s</sup>), which had been found to be 31<sup>m</sup> 8<sup>s</sup> slow on apparent time at ship, the difference of longitude made to East was 13 $\frac{1}{2}$  miles after the error on apparent time was determined: required the latitude by reduction to meridian.

## ADDITIONAL FOR MASTER ORDINARY.

12. 1876, March 19th, the observed meridian altitude of *a Bootis (Areturus)*, 36° 10' 20", bearing North, index correction + 2' 42", height of eye 20 feet: required the latitude.

In the following table give the correct magnetic bearing of the distant object and thence the deviation.

## Correct magnetic bearing.

| Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North ....                       | S. 67° E.                                      |                     | South ....                       | S. 72° E.                                      |                     |
| N.E. ....                        | East.  |                     | S.W. ....                        | S. 46° E.                                      |                     |
| East .....                       | N. 85° E.                                      |                     | West ....                        | S. 45° E.                                      |                     |
| S.E. ....                        | N. 87° E.                                      |                     | N.W. ....                        | S. 52° E.                                      |                     |

With the deviation as above, give the courses you would steer by the Standard Compass to make the following courses correct magnetic.

Correct magnetic courses:—N.E.  $\frac{1}{2}$  E.; S.W. by W.; W. by S.  $\frac{3}{4}$  S.; S.S.E.  $\frac{1}{4}$  E.

Compass courses:—

Supposing you have steered the following courses by the Standard Compass, find the correct magnetic courses made from the above deviation table.

Compass courses:—S.E. by E.  $\frac{1}{4}$  E.; N.E. by E.  $\frac{1}{2}$  E.; N.W. by W.  $\frac{3}{4}$  W.; N.N.W.

Correct magnetic courses:—

You have taken the following bearings of two distant objects by your Standard Compass as above; with the ship's head at N. 24° E., find the bearings, correct magnetic.

Compass bearings:—W.  $\frac{3}{4}$  S. and E.N.E.

Bearings, magnetic:—

## EXAMINATION PAPER.—No. IV.

## FOR SECOND MATE.

1. Multiply, by common logarithms, 456 by 28.9.
2. Divide, by common logarithms, 462927 by 142.8.

3.—

| H. | COURSES.                  | K. | $\frac{1}{10}$ | WINDS.                | LEE-WAY.        | DEVIATION. | REMARKS, &c.   |
|----|---------------------------|----|----------------|-----------------------|-----------------|------------|--|
| 1  | S.W. $\frac{1}{2}$ W.     | 14 | 5              | S.E.                  | pts.<br>0       | 6° W.      | A point, lat. 50° 12' S.<br>long. 179° 40' W., bearing by compass N. $\frac{3}{4}$ W.<br>dist. 19 miles. (Ship's head S.W. $\frac{1}{2}$ W.) Deviation as per log. |
| 2  |                           | 14 | 2              |                       |                 |            |  |
| 3  |                           | 14 | 6              |                       |                 |            |  |
| 4  |                           | 14 | 7              |                       |                 |            |  |
| 5  | N. $\frac{3}{4}$ E.       | 4  |                | E.N.E.                | 3 $\frac{1}{4}$ | 3° E.      |  |
| 6  |                           | 3  | 6              |                       |                 |            |  |
| 7  |                           | 3  | 6              |                       |                 |            |  |
| 8  |                           | 3  | 8              |                       |                 |            |  |
| 9  | S. by E. $\frac{1}{2}$ E. | 2  | 4              | S.W. $\frac{1}{2}$ W. | 2 $\frac{3}{4}$ | 6° E.      |  |
| 10 |                           | 2  | 3              |                       |                 |            |  |
| 11 |                           | 2  | 3              |                       |                 |            |  |
| 12 |                           | 2  |                |                       |                 |            |  |
| 1  | W. by S.                  | 12 | 2              | S. by W.              | $\frac{1}{4}$   | 14° W.     | Variation 14° East.  |
| 2  |                           | 12 | 4              |                       |                 |            |  |
| 3  |                           | 12 | 6              |                       |                 |            |  |
| 4  |                           | 12 | 8              |                       |                 |            |  |
| 5  | E.N.E.                    | 3  |                | S.E.                  | 2 $\frac{1}{2}$ | 19° E.     |  |
| 6  |                           | 2  | 3              |                       |                 |            |  |
| 7  |                           | 3  | 4              |                       |                 |            |  |
| 8  |                           | 3  | 3              |                       |                 |            |  |
| 9  | S.S.W. $\frac{1}{2}$ W.   | 5  | 6              | S.E.                  | 1 $\frac{3}{4}$ | 4° W.      | A current set (correct mag.) S.W. $\frac{1}{4}$ W., 42 miles, from the time the departure was taken to the end of the day.   |
| 10 |                           | 5  | 7              |                       |                 |            |  |
| 11 |                           | 5  | 3              |                       |                 |            |  |
| 12 |                           | 5  | 4              |                       |                 |            |  |

4. 1876, April 1st, in longitude 87° 42' W., observed meridian altitude sun's L.L. South of observer was 48° 42' 30", index correction + 1' 42", height of eye 18 feet: required the latitude.

5. In latitude 49° 57' N., the departure made good was 149 miles: required the difference of longitude by parallel sailing.

6. Required the course and distance from A to B.

|            |            |             |           |
|------------|------------|-------------|-----------|
| Latitude A | 56° 35' S. | Longitude A | 2° 15' E. |
| Latitude B | 51 10 S.   | Longitude B | 3 10 W.   |

#### ADDITIONAL FOR ONLY MATE.

7. 1875, April 13th: required the times of high water, A.M. and P.M., at Erehous, Blakeney, Portree, Llanelly, Cardiff, and New Ross.

8. 1876, April 28th, at 5<sup>h</sup> 14<sup>m</sup> 2<sup>s</sup> P.M. apparent time at ship, latitude 38° 19' S., longitude 88° 48' E., sun's magnetic amplitude N.W. by W., variation 19° 10' W.: required the deviation.

9. 1876, April 15th, P.M. at ship, latitude 37° 49' S., observed altitude sun's L.L. was 26° 27' 30", index correction — 49", height of eye 13 feet, time by chronometer 14<sup>h</sup> 21<sup>m</sup> 48<sup>s</sup> 17<sup>s</sup>, which was 4<sup>m</sup> 51<sup>s</sup> fast for Greenwich mean noon, January 22nd, and on February 3rd, was 2<sup>m</sup> 35<sup>s</sup> 4 fast for mean time at Greenwich: required the longitude.

#### ADDITIONAL FOR FIRST MATE.

10. 1876, April 17th, mean time at ship 2<sup>h</sup> 49<sup>m</sup> 45<sup>s</sup> P.M., latitude 39° 50' N., longitude 1° 35' E., sun's bearing by compass West, observed altitude sun's L.L. 42° 10', index corr. — 45", height of eye 14 feet: required the error of compass; and supposing the variation to be 19° 50' W.: required the deviation of the compass for the position of the ship's head when the observation was taken.

11. 1876, April 19th, A.M. at ship, latitude account 46° 15' N., longitude 178° 12' E., observed altitude of sun's L.L. South of observer 54° 7', index correction + 2' 12", height of eye 20 feet, time by watch 11<sup>h</sup> 24<sup>m</sup> 22<sup>s</sup>, or 13<sup>h</sup> 23<sup>m</sup> 24<sup>m</sup> 22<sup>s</sup>, which had been found to be 5<sup>m</sup> slow on apparent time at ship, the difference of longitude made to the East was 30 miles, after the error on apparent time was determined.

## ADDITIONAL FOR MASTER ORDINARY.

12. 1876, April 12th, the observed meridian altitude of the star Spica, South of observer, was  $20^{\circ} 58' 40''$ , index correction  $-45''$ , height of eye 25 feet: required the latitude.

In the following table give the correct magnetic bearing of the distant object, and thence the deviation:—

Correct magnetic bearing.

| Ship Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. |
|--------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North. ....                    | S. $2^{\circ}$ W.                              |                     | South ....                       | S. $5^{\circ}$ E.                              |                     |
| N.E. ....                      | S. $5^{\circ}$ W.                              |                     | S.W. ....                        | S. $24^{\circ}$ E.                             |                     |
| East. ....                     | S. $10^{\circ}$ W.                             |                     | West ....                        | S. $17^{\circ}$ E.                             |                     |
| S.E. ....                      | S. $16^{\circ}$ W.                             |                     | N.W. ....                        | S. $3^{\circ}$ E.                              |                     |

With the deviation as above, give the courses you would steer by the Standard Compass to make the following courses correct magnetic.

Correct magnetic courses:—E. by N.  $\frac{1}{4}$  N.; N.W.  $\frac{3}{4}$  W.; S.W. by S.  $\frac{1}{2}$  S.; S.E. by S.  $\frac{1}{4}$  S. Compass courses:—

Supposing you have steered the following courses by the Standard Compass, find the correct magnetic courses made from the above deviation table.

Compass Courses:—N.W. by W.  $\frac{1}{2}$  W.; W. by S.  $\frac{1}{2}$  S.; E. by S.  $\frac{1}{4}$  S.; N.E.  $\frac{3}{4}$  E.

Correct magnetic courses.

You have taken the following bearing of two distant objects by your Standard Compass as above, with the ship's head at S.  $24^{\circ}$  W., find the bearings, correct magnetic.

Compass bearings:—N.  $84^{\circ}$  W. and W.S.W.

Bearings, magnetic:—

## EXAMINATION PAPER—No. V.

## FOR SECOND MATE.

1. Multiply 767 by 89.8, by common logarithms.
2. Divide 66889.2 by 99.7, by common logarithms.

3.—

| H. | COURSES.                  | K. $\frac{1}{10}$ | WINDS. | LEE-WAY.       | DEVIATION.      | REMARKS, &c.   |
|----|---------------------------|-------------------|--------|----------------|-----------------|--|
| 1  | S.E. $\frac{1}{2}$ E.     | 14                | S.W.   | pts.           | $8^{\circ}$ E.  | A point, lat. $64^{\circ} 2'S.$ , long. $140^{\circ} 21'E.$ , bearing by compass W. by S. $\frac{3}{4}$ S., distance 23 miles. (Ship's head S.S.E. $\frac{1}{2}$ E.) Deviation as per log. |
| 2  |                           | 14                |        | 0              |                 |  |
| 3  |                           | 14 $\frac{4}{10}$ |        |                |                 |  |
| 4  | E. by S. $\frac{3}{4}$ S. | 13 $\frac{6}{10}$ | N.E.   | 3              | $14^{\circ}$ E. |  |
| 5  |                           | 3 $\frac{4}{10}$  |        |                |                 |  |
| 6  |                           | 3 $\frac{3}{10}$  |        |                |                 |  |
| 7  |                           | 3 $\frac{4}{10}$  |        |                |                 |  |
| 8  |                           | 3 $\frac{5}{10}$  |        |                |                 |  |
| 9  |                           | 3 $\frac{4}{10}$  |        |                |                 |  |
| 10 | W.N.W.                    | 4 $\frac{3}{10}$  | North. | $2\frac{3}{4}$ | $19^{\circ}$ W. |  |
| 11 |                           | 4 $\frac{3}{10}$  |        |                |                 |  |
| 12 |                           | 4 $\frac{4}{10}$  |        |                |                 |  |
| 1  | N.E. $\frac{1}{4}$ N.     | 12 $\frac{2}{10}$ | N.N.W. | $\frac{1}{4}$  | $8^{\circ}$ E.  | Variation $37^{\circ}$ E.  |
| 2  |                           | 12 $\frac{5}{10}$ |        |                |                 |  |
| 3  |                           | 12 $\frac{3}{10}$ |        |                |                 |  |
| 4  | W.S.W.                    | 3 $\frac{6}{10}$  | N.W.   | $3\frac{1}{4}$ | $19^{\circ}$ W. |  |
| 5  |                           | 3 $\frac{4}{10}$  |        |                |                 |  |
| 6  |                           | 3 $\frac{3}{10}$  |        |                |                 |  |
| 7  | N.N.W.                    | 5 $\frac{7}{10}$  | West.  | 2              | $11^{\circ}$ W. | A current set the ship (correct magnetic) N.E. $\frac{1}{4}$ E., 48 miles, from the time the departure was taken to the end of the day.  |
| 8  |                           | 5 $\frac{6}{10}$  |        |                |                 |  |
| 9  |                           | 5 $\frac{7}{10}$  |        |                |                 |  |
| 10 | S.S.W.                    | 6 $\frac{5}{10}$  | West.  | $1\frac{1}{2}$ | $3^{\circ}$ W.  |  |
| 11 |                           | 6 $\frac{7}{10}$  |        |                |                 |  |
| 12 |                           | 7 $\frac{8}{10}$  |        |                |                 |  |

4. 1876, May 8th, in longitude  $105^{\circ} 17' W.$ , observed meridian altitude of sun's L.L., bearing North, was  $76^{\circ} 3'$ , index correction  $- 1' 27''$ , height of eye 10 feet: required the latitude.

5. In latitude  $3^{\circ} 24' N.$ , the departure made good was 982 miles: required the difference of longitude by parallel sailing.

6. Required the course and distance from A to B, by calculation on Mercator's principle.

|            |                     |             |                     |
|------------|---------------------|-------------|---------------------|
| Latitude A | $39^{\circ} 39' N.$ | Longitude A | $51^{\circ} 51' E.$ |
| Latitude B | $27^{\circ} 27' N.$ | Longitude B | $33^{\circ} 33' E.$ |

ADDITIONAL FOR ONLY MATE.

7. 1875, May 21st: find the times of high water A.M. and P.M. at Loch Ryan, Tarn Point, Berwick, St. Malo, and Dungeness.

8. 1876, May 21st, at  $7^h 29^m$  A.M. apparent time at ship, latitude  $45^{\circ} 53' S.$ , longitude  $50^{\circ} 39' E.$ , sun's magnetic amplitude N.E.  $\frac{1}{4} E.$ : required the true amplitude and error of the compass; and supposing the variation to be  $31^{\circ} 50' E.$ : required the deviation of the compass for the position of the ship's head at the time of observation.

9. 1876, May 22nd, A.M. at ship, latitude  $43^{\circ} 25' N.$ , observed altitude sun's L.L.  $32^{\circ} 8'$ , index correction  $+ 47''$ , height of eye 15 feet, time by chron.  $21^d 21^h 6^m 10^s$ , which was *slow*  $12^m 6$  for mean noon at Greenwich, February 24th, and on April 1st, was  $2^m 45^s$  *fast* for mean noon at Greenwich: required the longitude.

ADDITIONAL FOR FIRST MATE.

10. 1876, May 25th, mean time at ship,  $3^h 29^m 47^s$  P.M., latitude  $41^{\circ} 58' N.$ , longitude  $96^{\circ} 1' W.$ , sun's bearing by compass N.  $118^{\circ} 30' W.$ , observed altitude sun's L.L.  $40^{\circ} 40' 40''$ , index correction  $+ 2' 15''$ , height of eye 12 feet: required the true azimuth and error of the compass; and supposing the variation is  $10^{\circ} 30' E.$ : required the deviation of the compass for the position of the ship's head at the time the observation.

11. 1876, May 10th, P.M. at ship, latitude account  $28^{\circ} 13' S.$ , longitude  $112^{\circ} 15' W.$ , observed altitude of sun's L.L. North of observer was  $43^{\circ} 35' 20''$ , index correction  $- 6' 12''$ , height of eye 19 feet, time by watch  $30^m 26^s$  (or  $10^d 0^h 30^m 26^s$ ), which had been found to be  $6^m 45^s$  *fast* on apparent time at ship, the difference of longitude made to the *East* was  $26'$ , after the error on apparent time was determined: required the latitude.

ADDITIONAL FOR MASTER ORDINARY.

12. 1876, May 10th, the observed meridian altitude of Spica, bearing North, was  $70^{\circ} 10' 25''$ , index correction  $+ 42''$ , height of eye 22 feet: required the latitude.

In the following table give the correct magnetic bearing of the distant object and thence the deviation.

Correct magnetic bearing.

| Ship's Head<br>by Standard<br>Compass. | Bearing of<br>Distant Object<br>by Standard<br>Compass. | Deviation<br>required. | Ship's Head<br>by Standard<br>Compass. | Bearing of<br>Distant Object<br>by Standard<br>Compass. | Deviation<br>required. |
|--|---|------------------------|--|---|------------------------|
| North ....                             | East.   |                        | South ....                             | N. $85^{\circ} E.$                                      |                        |
| N.E. ....                              | S. $78^{\circ} E.$                                      |                        | S.W. ....                              | N. $63^{\circ} E.$                                      |                        |
| East .....                             | S. $70^{\circ} E.$                                      |                        | West ....                              | N. $64^{\circ} E.$                                      |                        |
| S.E. ....                              | S. $71^{\circ} E.$                                      |                        | N.W. ....                              | N. $74^{\circ} E.$                                      |                        |

With the deviation as above, give the courses you would steer by the Standard Compass to make the following courses correct magnetic.

Correct magnetic courses:—N.N.E.  $\frac{3}{4}$  E.; N.  $84^{\circ}$  W.; S.  $72^{\circ}$  E.; S.W. by W.  $\frac{1}{2}$  W.

Compass courses:—

Supposing you have steered the following courses by the Standard Compass, find the correct magnetic courses made from the above deviation table.

Compass courses:—N.N.W.  $\frac{1}{2}$  W.; N.  $64^{\circ}$  E.; S.E.  $\frac{3}{4}$  E.; S.  $39^{\circ}$  W.

Correct magnetic courses:—

You have taken the following bearings of two distant objects by your Standard Compass as above; with the ship's head at S.  $87^{\circ}$  E., find the bearings, correct magnetic.

Compass bearings:—S.  $15^{\circ}$  W. and N.  $72^{\circ}$  W.

Bearings, magnetic:—

## EXAMINATION PAPER—No. VI.

### FOR SECOND MATE.

1. Multiply 5900 by .00071, by common logarithms.

2. Divide 50800 by  $4^{\circ}8'35''$ , by common logarithms.

3.—

| H. | COURSE.               | K. | $\frac{1}{10}$ | WINDS.     | LEE-WAY.            | DEVIATION. | REMARKS, &c.   |
|----|-----------------------|----|----------------|------------|---------------------|------------|--|
| 1  | E. by S.              | 4  | 3              | S. by E.   | 1 $\frac{1}{4}$ ts. | 15° E.     | A point, lat. $56^{\circ}12'N$ . long. $135^{\circ}40'W$ ., bearing by compass WSW dist. $22\frac{1}{2}$ miles. (Ship's head E. by S.) Deviation as per log. |
| 2  |                       | 4  | 4              |            |                     |            |  |
| 3  |                       | 4  | 3              |            |                     |            |  |
| 4  |                       | 4  |                |            |                     |            |  |
| 5  | S.E. by E.            | 5  | 6              | S. by W.   | 1 $\frac{1}{4}$     | 12° E.     |  |
| 6  |                       | 5  | 8              |            |                     |            |  |
| 7  |                       | 5  | 6              |            |                     |            |  |
| 8  |                       | 5  |                |            |                     |            |  |
| 9  | S. by E.              | 5  | 7              | S.W. by W. | 1 $\frac{1}{2}$     | 4° E.      | Variation $25^{\circ}$ E.  |
| 10 |                       | 5  | 8              |            |                     |            |  |
| 11 |                       | 6  |                |            |                     |            |  |
| 12 |                       | 6  | 5              |            |                     |            |  |
| 1  | E. $\frac{3}{4}$ S.   | 6  | 4              | S. by E.   | 1 $\frac{3}{4}$     | 15° E.     |  |
| 2  |                       | 6  | 5              |            |                     |            |  |
| 3  |                       | 6  | 4              |            |                     |            |  |
| 4  |                       | 5  | 7              |            |                     |            |  |
| 5  | S.W. $\frac{3}{4}$ W. | 4  | 8              | S. by E.   | 3 $\frac{1}{2}$     | 7° W.      | A current set (correct mag.) N. by W. $\frac{1}{4}$ W. 16 miles, from the time the departure was taken to the end of the day.                                |
| 6  |                       | 4  | 6              |            |                     |            |  |
| 7  |                       | 4  | 2              |            |                     |            |  |
| 8  |                       | 4  | 4              |            |                     |            |  |
| 9  | S. by E.              | 4  | 5              | E. by S.   | 2 $\frac{1}{4}$     | 4° E.      |  |
| 10 |                       | 4  | 5              |            |                     |            |  |
| 11 |                       | 3  | 6              |            |                     |            |  |
| 12 |                       | 4  | 4              |            |                     |            |  |

4. 1876, June 1st, in longitude  $96^{\circ}17'E$ ., the observed meridian altitude of sun's L.L. was  $75^{\circ}38'15''$  bearing North, index correction  $+27''$ , height of eye 26 feet: required the latitude.

5. In latitude  $35^{\circ}54'S$ ., departure made good 249 miles: required the difference of longitude.

6. Required the course and distance from A to B, by Mercator's Sailing.

Latitude of A  $3^{\circ}19'N$ .

Longitude of A  $71^{\circ}42'W$ .

Latitude of B  $33^{\circ}2'S$ .

Longitude of B  $122^{\circ}20'W$ .

ADDITIONAL FOR ONLY MATE.

7. 1875, June 19th: find A.M. and P.M. tides at Rotterdam, Heligoland, and Rio Janeiro, longitude  $43^{\circ} 12' W.$

8. 1876, June 21st, at  $9^h 16^m$  P.M. apparent time at ship, latitude  $59^{\circ} 51' N.$ , longitude  $64^{\circ} 42' W.$ , sun's magnetic amplitude  $N. \frac{3}{4} E.$ : required the true amplitude and error of compass: variation  $52^{\circ} 30' W.$ : find deviation.

9. 1876, June 14th, P.M. at ship, latitude  $2^{\circ} 2' S.$ , observed altitude sun's L.L.  $28^{\circ} 38'$ , index correction  $+ 48''$ , height of eye 12 feet, time by chronometer  $14^h 0^m 3^m 18^s$ , which was  $2^h 28^m 19^s$  fast for mean noon at Greenwich, April 1st, and on April 30th, was  $2^h 24^m 19^s$  fast for mean noon at Greenwich: required the longitude.

ADDITIONAL FOR FIRST MATE.

10. 1876, June 8th, mean time at ship  $7^h 50^m$  A.M., latitude  $15^{\circ} 45' N.$ , longitude  $32^{\circ} 33' W.$  sun's bearing by compass  $N. 70^{\circ} E.$ , observed altitude sun's L.L.  $31^{\circ} 10'$ , index correction  $- 1' 22''$ , height of eye 18 feet: required the error of compass, variation  $14^{\circ} 40' W.$ : find the deviation.

11. 1876, June 5th, P.M. at ship, latitude account  $61^{\circ} 58' N.$ , longitude  $155^{\circ} 21' E.$ , observed altitude sun's L.L. South of observer was  $49^{\circ} 50' 30''$ , index corr.  $+ 2' 10''$ , height of eye 21 feet, time by watch  $11^h 48^m 26^s$  (or  $4^d 23^h 48^m 26^s$ ), which had been found to be  $50^m 10^s$  slow on apparent time at ship, the difference of longitude made to West was  $17' 5''$ , after the error on apparent time was determined.

ADDITIONAL FOR MASTER ORDINARY.

12. 1876, June 11th, the observed meridian altitude of the star Pollux, bearing North, was  $48^{\circ} 40' 24''$ , index correction  $- 1' 32''$ , height of eye 20 feet.

In the following table give the correct magnetic bearing of the distant object, and thence the deviation.

Correct magnetic bearing.

| Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North ....                       | N. $89^{\circ} W.$                             |                     | South ....                       | S. $67^{\circ} W.$                             |                     |
| N.E. ....                        | S. $79^{\circ} W.$                             |                     | S.W. ....                        | S. $75^{\circ} W.$                             |                     |
| East ....                        | S. $62^{\circ} W.$                             |                     | West ....                        | N. $83^{\circ} W.$                             |                     |
| S.E. ....                        | S. $58^{\circ} W.$                             |                     | N.W. ....                        | N. $77^{\circ} W.$                             |                     |

With the deviation as above, give the courses you would steer by the Standard Compass, to make the following courses correct magnetic.

Correct magnetic courses:—N.W. by W.; S.W. by W.  $\frac{1}{2} W.$ ; N.N.E.; S. by W.

Compass courses:—

Supposing you have steered the following courses by the Standard Compass, find the correct magnetic courses made from the above deviation table.

Compass courses:—N.W. by N.; W.S.W.; S.  $\frac{1}{2} W.$ ; S.E. by E.  $\frac{1}{2} E.$

Magnetic courses:—

You have taken the following bearings of two distant objects by your Standard Compass as above, with the ship's head at S.E. by S., find the bearings, correct magnetic.

Compass bearings:—N.  $\frac{3}{4} W.$  and S.  $73^{\circ} W.$

Bearings, magnetic:—

EXAMINATION PAPER.—No. VII.

FOR SECOND MATE.

1. Multiply 483 by 28.7, by common logarithms.
2. Divide 242880 by 704, by common logarithms.

3.—

| H. | COURSES.   | K. | $\frac{1}{16}$ | WINDS.     | LEE-WAY.               | DEVIATION. | REMARKS, &c.   |
|----|------------|----|----------------|------------|------------------------|------------|--|
| 1  | S.E. by S. | 6  |                | S.W. by S. | pts.<br>$1\frac{1}{4}$ | 8° E.      | A point, lat. $51^{\circ}25'N.$ long. $9^{\circ}29'W.$ , bearing by compass N.E. by N., dist. 17 miles. (Ship's head S.E. by S.) Deviation as per log. |
| 2  |            | 5  | 6              |            |                        |            |  |
| 3  |            | 5  | 4              |            |                        |            |  |
| 4  |            | 5  | 3              |            |                        |            |  |
| 5  | South.     | 3  | 5              | W.S.W.     | $2\frac{3}{4}$         | 2° E.      |  |
| 6  |            | 3  | 5              |            |                        |            |  |
| 7  | N.W.       | 3  | 2              | W.S.W.     | $3\frac{1}{4}$         | 17° W.     |  |
| 8  |            | 2  | 8              |            |                        |            |  |
| 9  | West.      | 6  | 6              | S.S.W.     | $\frac{3}{4}$          | 16° W.     |  |
| 10 |            | 6  | 4              |            |                        |            |  |
| 11 |            | 6  | 5              |            |                        |            |  |
| 12 |            | 6  | 5              |            |                        |            |  |
| 1  | S.S.E.     | 4  | 4              | S.W.       | $1\frac{1}{2}$         | 6° E.      | Variation 28° W.   |
| 2  |            | 4  | 4              |            |                        |            |  |
| 3  |            | 4  | 2              |            |                        |            |  |
| 4  |            | 4  |                |            |                        |            |  |
| 5  | S.W. by W. | 7  |                | S. by E.   | $\frac{1}{2}$          | 9° W.      | A current set (correct magnetic) N.W. by N. 9 miles, from the time the departure was taken to the end of day.  |
| 6  |            | 6  | 6              |            |                        |            |  |
| 7  |            | 6  | 4              |            |                        |            |  |
| 8  |            | 7  |                |            |                        |            |  |
| 9  | S.S.E.     | 7  | 4              | East.      | $\frac{1}{4}$          | 6° E.      |  |
| 10 |            | 7  | 6              |            |                        |            |  |
| 11 | South.     | 9  | 6              | East.      | 0                      | 2° E.      |  |
| 12 |            | 8  | 4              |            |                        |            |  |

4. 1876, July 26th, in longitude  $12^{\circ}19'W.$ , the observed meridian altitude of the sun's L.L. was  $15^{\circ}41'$ , bearing North, index correction  $-3'10''$ , height of eye 19 feet: required the latitude.

5. In latitude  $25^{\circ}20'S.$ , the departure made good was 389 miles: required the difference of longitude by parallel sailing.

6. Required the course and distance from Start Point to St. Michael's.

Lat. Start Point  $50^{\circ}13'N.$

Long. Start Point  $3^{\circ}38'W.$

Lat. St. Michael's  $37^{\circ}48'N.$

Long. St. Michael's  $25^{\circ}10'W.$

#### ADDITIONAL FOR ONLY MATE.

7. 1875, July 25th: find the time of high water, A.M. and P.M., at Bayonne, Ile de Noirmoutier, Port Navalo, Belle Isle, and Bordeaux (by Admiralty Tables).

8. 1876, July 12th, at  $5^h 9^m$  P.M. apparent time at ship, in latitude  $29^{\circ}3'S.$ , longitude  $21^{\circ}53'W.$ , the sun's magnetic amplitude was W. by N.  $\frac{3}{4}N.$ : required the true amplitude and error of the compass; and supposing the variation to be  $11^{\circ}20'W.$ : required the deviation for the position of the ship's head when the observation was taken.

9. 1876, July 17th, P.M. at ship, latitude  $31^{\circ}32'S.$ , observed altitude sun's L.L.  $13^{\circ}23'10''$ , index correction  $+5''$ , height of eye 16 feet, time by chronometer July  $16^d 22^h 3^m 49^s$ , which was  $9^m 17^s$  fast for mean noon at Greenwich, June 6th, and on June 14th was fast  $8^m 32^s.6$  on mean time at Greenwich: required the longitude.

#### ADDITIONAL FOR FIRST MATE.

10. 1876, July 4th, mean time at ship  $8^h 39^m 2^s$  A.M., latitude  $38^{\circ}10'S.$ , longitude  $78^{\circ}35'W.$ , sun's bearing by compass N.  $19^{\circ}16'E.$ , observed altitude sun's L.L.  $12^{\circ}16'10''$ , index correction  $-2'38''$ , height of eye 14 feet: required the true azimuth and error of the compass: and supposing the variation be  $17^{\circ}20'E.$ : required the deviation of the compass for the position of the ship's head at the time the observation was taken.

11. 1876, July 31st, P.M. at ship, latitude by account  $45^{\circ}5'S.$ , longitude  $83^{\circ}12'E.$ , observed altitude sun's L.L. North of observer was  $26^{\circ}15'10''$ , index corr.  $-40''$ , height of eye 19 feet, time by watch  $11^h 50^m$ , (or  $30^d 23^h 50^m$ ), which had been found to be  $36^m 16^s$  slow on apparent time at ship, the difference of longitude made to the West was 14 miles, after the error on apparent time was determined: required the latitude by reduction to meridian.



ADDITIONAL FOR MASTER ORDINARY.

12. 1876, July 6th, the observed meridian altitude of the star *α* Scorpii (*Antares*), bearing North,  $70^{\circ} 10' 30''$ , height of eye 21 feet: required the latitude.

In the following table give the correct magnetic bearing of the distant object, and thence the deviation:—

Correct magnetic bearing.

| Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North .....                      | West.  |                     | South .....                      | N. $85^{\circ}$ W.                             |                     |
| N.E. ....                        | S. $72^{\circ}$ W.                             |                     | S.W. ....                        | N. $78^{\circ}$ W.                             |                     |
| East .....                       | S. $70^{\circ}$ W.                             |                     | West .....                       | N. $70^{\circ}$ W.                             |                     |
| S.E. ....                        | S. $82^{\circ}$ W.                             |                     | N.W. ....                        | N. $73^{\circ}$ W.                             |                     |

With the deviation as above, give the courses you would steer by the Standard Compass to make the following courses correct magnetic.

Correct magnetic courses:—E. by N.  $\frac{3}{4}$  N.; S.E. by E.  $\frac{1}{2}$  E.; S. by W.  $\frac{1}{2}$  W.; N.  $1^{\circ}$  E.

Compass courses:—

Supposing you have steered the following courses by the Standard Compass, find the correct magnetic courses made from the above deviation table.

Compass courses:—W.  $1^{\circ}$  S.; N.  $\frac{1}{4}$  E.; N.E. by E.  $\frac{1}{4}$  E.; S.E.  $\frac{1}{2}$  S.

Magnetic courses:—

You have taken the following bearings of two distant objects by your Standard Compass as above, with the ship's head at N.W. by W., find the bearings, correct magnetic.

Compass bearings:—E.  $\frac{1}{4}$  S., and E.  $\frac{1}{2}$  N.

Bearings, magnetic:—

EXAMINATION PAPER.—No. VIII.

FOR SECOND MATE.

1. Multiply 777 by 999, by common logarithms.
  2. Divide 111111 by 234, by common logarithms.
- 3.—

| H. | COURSES.                  | K. | $\frac{1}{10}$ | WINDS.     | LEE-WAY.       | DEVIATION.      | REMARKS, &c.   |
|----|---------------------------|----|----------------|------------|----------------|-----------------|--|
|    |                           |    |                |            | pts.           |                 |  |
| 1  |                           |    |                |            |                |                 |  |
| 2  | S.S.E.                    | 9  | 2              | S.W.       | 1              | $6^{\circ}$ E.  | A point of land in lat. $0^{\circ} 10' N.$ long. $173^{\circ} 50' E.$ bearing by compass S.W., dist. 15 miles. (Ship's head S.S.E.) Dev. as per log. |
| 3  |                           | 8  | 4              |            |                |                 |  |
| 4  |                           | 8  | 4              |            |                |                 |  |
| 5  | W.N.W.                    | 7  | 3              | S.W.       | $1\frac{1}{2}$ | $18^{\circ}$ W. |  |
| 6  |                           | 7  |                |            |                |                 |  |
| 7  |                           | 6  | 7              |            |                |                 |  |
| 8  |                           | 6  |                |            |                |                 |  |
| 9  | W. $\frac{1}{2}$ N.       | 5  | 4              | S.W. by S. | 2              | $16^{\circ}$ W. |  |
| 10 |                           | 5  | 5              |            |                |                 |  |
| 11 |                           | 5  | 6              |            |                |                 |  |
| 12 |                           | 5  | 5              |            |                |                 |  |
| 1  | S. by E. $\frac{3}{4}$ E. | 6  | 3              | S.W.       | $1\frac{1}{2}$ | $5^{\circ}$ E.  | Variation $8^{\circ}$ E.   |
| 2  |                           | 6  | 3              |            |                |                 |  |
| 3  |                           | 6  | 2              |            |                |                 |  |
| 4  |                           | 6  | 2              |            |                |                 |  |
| 5  | S.S.E.                    | 5  | 2              | S.W.       | $1\frac{3}{4}$ | $5^{\circ}$ E.  |  |
| 6  |                           | 5  | 3              |            |                |                 |  |
| 7  |                           | 5  | 5              |            |                |                 |  |
| 8  |                           | 6  |                |            |                |                 |  |
| 9  | W. by N.                  | 9  | 6              | S.S.W.     | 0              | $17^{\circ}$ W. | A current set the ship (correct magnetic) S. $6^{\circ}$ W., 18 miles from the time the departure was taken to the end of the day.                   |
| 10 |                           | 10 | 4              |            |                |                 |  |
| 11 |                           | 11 | 5              |            |                |                 |  |
| 12 |                           | 11 | 5              |            |                |                 |  |

4. 1876, August 12th, longitude  $92^{\circ} 12'$  E., the observed meridian altitude of sun's L.L. bearing North, was  $42^{\circ} 42' 10''$ , index correction  $- 2' 50''$ , height of eye 17 feet: required the latitude.

5. In latitude  $56^{\circ} 11'$  S., the departure made good was 356 miles East: required the difference of longitude by parallel sailing.

6. Required the course and distance from A to B.

|            |                     |             |                     |
|------------|---------------------|-------------|---------------------|
| Latitude A | $47^{\circ} 50'$ S. | Longitude A | $42^{\circ} 16'$ E. |
| Latitude B | $40^{\circ} 49'$ S. | Longitude B | $46^{\circ} 25'$ E. |

#### ADDITIONAL FOR ONLY MATE.

7. 1875, August 13th: find the times of high water, A.M. and P.M., at Lisbon (Bar), Cadiz, and Broughty Ferry.

8. 1876, August 20th, at  $5^h 16^m$  P.M. apparent time at ship, in latitude  $42^{\circ} 5'$  S., longitude  $88^{\circ} 36'$  W., the sun's magnetic amplitude was W. by S., variation  $19^{\circ} 15'$  E.: required the deviation of the compass for the position of the ship's head at the time of observation.

9. 1876, August 7th, P.M. at ship, latitude  $6^{\circ} 4'$  N., observed altitude sun's L.L.  $24^{\circ} 5'$ , index correction  $+ 1' 30''$ , height of eye 12 feet, time by chronometer August  $6^d 20^h 30^m 36^s$ , which was  $36^{\cdot}2$  fast for Greenwich mean noon, July 14th, and on July 21st was  $10^s$  slow for Greenwich mean time: required the longitude.

#### ADDITIONAL FOR FIRST MATE.

10. 1876, August 20th, mean time at ship  $2^h 35^m 25^s$  P.M., latitude  $52^{\circ} 2'$  S., longitude  $89^{\circ} 26'$  E., sun's bearing by compass N.W.  $\frac{3}{4}$  N., observed altitude sun's L.L.  $17^{\circ} 26'$ , index correction  $+ 1' 45''$ , height of eye 21 feet: required the error of compass; and supposing the variation to be  $33^{\circ} 50'$  E.: find the deviation of the compass for the position of the ship's head at the time of observation.

11. 1876, August 11th, A.M. at ship, latitude account  $39^{\circ} 3'$  S., longitude  $157^{\circ} 25'$  E., observed altitude of sun's L.L., North of observer, was  $34^{\circ} 37'$ , height of eye 12 feet, time by watch  $7^h 41^m 25^s$  (or  $10^d 19^h 41^m 25^s$ ), which had been found to be  $3^h 41^m 8^s$  slow on apparent time at ship, the difference of longitude made to the East was  $33'$ , after the error on apparent time was determined.

#### ADDITIONAL FOR MASTER ORDINARY.

12. 1876, August 20th, the observed meridian altitude of the star  $\alpha$  Aquilæ (*Altair*), bearing North, was  $66^{\circ} 51' 10''$ , index correction  $+ 58''$ , height of eye 13 feet: required the latitude.

In the following table give the correct magnetic bearing of the distant object, and thence the deviation:—

Correct magnetic bearing.

| Ship's head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation required. | Ship's head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North ....                       | S. $12^{\circ}$ E.                             |                     | South. ....                      | S. $4^{\circ}$ E.                              |                     |
| N.E. ....                        | S. $10^{\circ}$ E.                             |                     | S.W. ....                        | S. $17^{\circ}$ E.                             |                     |
| East. ....                       | S. $6^{\circ}$ W.                              |                     | West. ....                       | S. $20^{\circ}$ E.                             |                     |
| S.E. ....                        | S. $9^{\circ}$ W.                              |                     | N.W. ....                        | S. $16^{\circ}$ E.                             |                     |

With the deviation as above, give the courses you would steer by the Standard Compass to make the following courses correct magnetic.

Correct magnetic courses:—E. by N.  $\frac{1}{2}$  N.; S.W. by W.  $\frac{1}{2}$  W.; N.N.W.  $\frac{3}{4}$  W.; E.S.E  
Compass courses:—

Supposing you have steered the following courses by the Standard Compass, find the correct magnetic courses made, from the above deviation table.

Compass courses:—N.W.  $\frac{1}{2}$  N.; W. by S.  $\frac{1}{2}$  S.; N.  $\frac{1}{2}$  W.; W.  $\frac{3}{4}$  S.

Magnetic courses:—

You have taken the following bearings of two distant objects by your Standard Compass as above; with the ship's head at W.N.W., find the bearings, correct magnetic.

Compass bearings:—S.S.E. and S.E. by S.

Bearings, magnetic:—

### EXAMINATION PAPER—No. IX.

#### FOR SECOND MATE.

1. Multiply .03948 by .01959, by common logarithms.
2. Divide 69.7565 by 97564, by common logarithms.
- 3.—

| H. | COURSES.                  | K. $\frac{1}{10}$ | WINDS.                    | LEE-WAY.           | DEVIATION. | REMARKS, &c.   |
|----|---------------------------|-------------------|---------------------------|--------------------|------------|--|
| 1  | S.E. $\frac{1}{2}$ E.     | 10 4              | S. by W. $\frac{1}{2}$ W. | pts. $\frac{3}{4}$ | 15° E.     | A point, lat. 54° 7' N., long. 0° 5' W., bearing by compass W. $\frac{3}{4}$ N., dist. 20 miles. (Ship's head S.E. $\frac{1}{2}$ E.) Deviation as per log. |
| 2  |                           | 10 2              |                           |                    |            |  |
| 3  |                           | 10                |                           |                    |            |  |
| 4  |                           | 10 6              |                           |                    |            |  |
| 5  | S.E. by S.                | 12 4              | S.W. by S.                | $\frac{1}{2}$      | 5° E.      |  |
| 6  |                           | 12 4              |                           |                    |            |  |
| 7  |                           | 12 5              |                           |                    |            |  |
| 8  |                           | 12 5              |                           |                    |            |  |
| 9  | East.                     | 11 2              | N.N.E.                    | $\frac{3}{4}$      | 21° E.     | Variation 22° W.   |
| 10 |                           | 10 6              |                           |                    |            |  |
| 11 |                           | 10 5              |                           |                    |            |  |
| 12 |                           | 10 3              |                           |                    |            |  |
| 1  | S.E. $\frac{1}{2}$ S.     | 8 5               | S.S.W. $\frac{1}{2}$ W.   | 1                  | 7° E.      |  |
| 2  |                           | 8                 |                           |                    |            |  |
| 3  |                           | 8 2               |                           |                    |            |  |
| 4  |                           | 8                 |                           |                    |            |  |
| 5  | S. by E. $\frac{1}{2}$ E. | 7 8               | S.W. $\frac{1}{2}$ W.     | $1\frac{1}{4}$     | 32° E.     | A current set the ship (correct magnetic) E. by S. $\frac{1}{2}$ S., 32 miles, from the time the departure was taken to the end of the day.                |
| 6  |                           | 6 6               |                           |                    |            |  |
| 7  |                           | 6 6               |                           |                    |            |  |
| 8  |                           | 6 3               |                           |                    |            |  |
| 9  | S.E. by E.                | 8 6               | N.E. by E.                | 1                  | 17° E.     |  |
| 10 |                           | 9 2               |                           |                    |            |  |
| 11 |                           | 9                 |                           |                    |            |  |
| 12 |                           | 9 3               |                           |                    |            |  |

4. 1876, Sept. 22nd, in longitude 123° 45' W., observed meridian altitude of sun's L.L. bearing North, was 89° 49' 50", index error + 52', height of eye 26 feet: required the latitude.

5. In latitude 20° 15' S., the departure made good was 352 miles W.: required the difference of longitude by parallel sailing.

6. Required the course and distance from A to B, by Mercator's Sailing.

|            |            |             |            |
|------------|------------|-------------|------------|
| Latitude A | 25° 39' N. | Longitude A | 48° 19' W. |
| Latitude B | 34 28 S.   | Longitude B | 18 28 E.   |

#### ADDITIONAL FOR ONLY MATE.

7. 1875, Sept. 11th: find A.M. and P.M. tides at Alderney, Malacca Fort, long. 102° E., and Madras, long. 80° E.

8. 1876, Sept. 30th, at 5<sup>h</sup> 45<sup>m</sup> P.M., apparent time at ship, latitude 52° 30' N., longitude 12° 10' W., sun's magnetic amplitude N.W.  $\frac{3}{4}$  W.: required error of compass; and supposing the variation to be 30° 28' E., required the deviation of the compass for the position of the ship's head at the time of observation.

9. 1876, Sept. 1st, P.M. at ship, latitude  $9^{\circ} 9' N.$ , observed altitude sun's L.L.  $62^{\circ} 13' 14''$ , index correction  $+ 15''$ , height of eye 16 feet, time by chronometer August  $31^d 15^h 34^m 28^s$ , which was  $2^m 10^s$  slow for mean noon at Greenwich, July 28th, and on August 12th was  $1^m 31^s$  slow on mean noon at Greenwich: required the longitude.

#### ADDITIONAL FOR FIRST MATE.

10. 1876, Sept. 16th, mean time at ship  $8^h 3^m 18^s$  A.M., latitude  $4^{\circ} 22' N.$ , longitude  $81^{\circ} 39' W.$ , sun's bearing by compass N.  $93^{\circ} 20' E.$ , observed altitude sun's L.L.  $29^{\circ} 30' 30''$ , index correction  $+ 1' 22''$ , height of eye 20 feet: required the true azimuth and error of compass; and supposing the variation is  $8^{\circ} 20' E.$ : required the deviation for the position of the ship's head at the time of observation.

11. 1876, Sept. 23rd, A.M. at ship, latitude acct.  $27^{\circ} 32' S.$ , longitude  $168^{\circ} 51' E.$ , observed altitude sun's L.L. North of observer was  $61^{\circ} 59' 40''$ , index correction  $- 1' 50''$ , height of eye 18 feet, time by watch  $11^h 10^m 10^s$  (or  $22^d 23^h 10^m 10^s$ ), which had been found to be  $31^m 31^s$  slow on apparent time at ship, the difference of longitude made to the *East* was  $24' 4''$ , after the error on apparent time was determined: required the latitude.

#### ADDITIONAL FOR MASTER ORDINARY.

12. 1876, Sept. 7th, the observed meridian altitude of star Arcturus was  $86^{\circ} 35' 50''$ , bearing North, index correction  $- 1' 10''$ , height of eye 12 feet: required the latitude.

In the following table give the correct magnetic bearing of the distant object, and thence the deviation:—

Correct magnetic bearing.

| Ship Head<br>by Standard<br>Compass. | Bearing of<br>Distant Object<br>by Standard<br>Compass. | Deviation<br>Required. | Ship's Head<br>by Standard<br>Compass. | Bearing of<br>Distant Object<br>by Standard<br>Compass. | Deviation<br>Required. |
|--------------------------------------|---|------------------------|--|---|------------------------|
| North. ....                          | S. $86^{\circ} W.$                                      |                        | South ....                             | N. $88^{\circ} W.$                                      |                        |
| N.E. ....                            | S. $68^{\circ} W.$                                      |                        | S.W. ....                              | N. $80^{\circ} W.$                                      |                        |
| East. ....                           | S. $66^{\circ} W.$                                      |                        | West ....                              | N. $72^{\circ} W.$                                      |                        |
| S.E. ....                            | S. $79^{\circ} W.$                                      |                        | N.W. ....                              | N. $75^{\circ} W.$                                      |                        |

With the deviation as above, give the courses you would steer by the Standard Compass to make the following courses correct magnetic.

Correct magnetic courses:—W. by S.  $\frac{3}{4} S.$ ; N.  $\frac{1}{2} E.$ ; E.  $\frac{3}{4} N.$ ; S.E.  $\frac{1}{4} E.$

Compass courses:—

Supposing you have steered the following courses by the Standard Compass, find the correct magnetic courses made from the above deviation table.

Compass Courses:—North; S.S.W.  $\frac{1}{4} W.$ ; E. by S.  $\frac{1}{4} S.$ ; N.E.  $\frac{1}{2} E.$

Correct magnetic courses:—

You have taken the following bearing of two distant objects by your Standard Compass as above, with the ship's head at N.N.E.  $\frac{3}{4} E.$ , find the bearings, correct magnetic.

Compass bearings:—N.  $79^{\circ} E.$  and W.  $\frac{1}{4} S.$

Bearings, magnetic:—

#### EXAMINATION PAPER.—No. X.

##### FOR SECOND MATE.

1. Multiply 560072 by 50, by common logarithms.
2. Divide 84919 by 984, by common logarithms.

3.—

| H. | COURSES.            | K. | $\frac{1}{10}$ | WINDS.                  | LEE-WAY.              | DEVIATION. | REMARKS, &c.   |
|----|---------------------|----|----------------|-------------------------|-----------------------|------------|--|
| 1  | W.S.W.              | 11 |                | South.                  | pts.<br>$\frac{1}{2}$ | 11° W.     | A point, Cape Farewell, in lat. 59° 49' N., long. 43° 54' W., bearing by compass N. $\frac{1}{2}$ E. dist. 36 miles. (Ship's head W.S.W.) Dev. as per log. |
| 2  |                     | 11 |                |                         |                       |            |  |
| 3  |                     | 10 | 4              |                         |                       |            |  |
| 4  |                     | 10 | 6              |                         |                       |            |  |
| 5  | West.               | 5  |                | S.S.W.                  | 1                     | 16° W.     |  |
| 6  |                     | 5  |                |                         |                       |            |  |
| 7  |                     | 4  | 5              |                         |                       |            |  |
| 8  |                     | 4  | 5              |                         |                       |            |  |
| 9  | S.E.                | 13 |                | S.S.W.                  | $\frac{1}{2}$         | 10° E.     |  |
| 10 |                     | 12 | 2              |                         |                       |            |  |
| 11 |                     | 12 | 4              |                         |                       |            |  |
| 12 |                     | 12 | 4              |                         |                       |            |  |
| 1  | S. by E.            | 6  |                | S.W. by W.              | 2 $\frac{1}{4}$       | 4° E.      | Variation 70° West.  |
| 2  |                     | 5  | 5              |                         |                       |            |  |
| 3  |                     | 5  |                |                         |                       |            |  |
| 4  |                     | 4  | 5              |                         |                       |            |  |
| 5  | S.W. by S.          | 1  | 5              | S.E. by S.              | 3 $\frac{1}{4}$       | 5° W.      |  |
| 6  |                     | 1  | 5              |                         |                       |            |  |
| 7  | Calm.               | .. | ..             | Calm.                   |                       |            |  |
| 8  |                     | .. | ..             |                         |                       |            |  |
| 9  | W. $\frac{1}{2}$ N. | 3  |                | S.S.W. $\frac{1}{2}$ W. | 2 $\frac{1}{2}$       | 16° W.     | A current set (correct magnetic) S.S.E., 48 miles during the 24 hours.   |
| 10 | S.W.                | 7  | 6              | W.N.W.                  | 1 $\frac{1}{2}$       | 6° W.      |  |
| 11 |                     | 7  | +              |                         |                       |            |  |
| 12 |                     | 7  |                |                         |                       |            |  |

4. 1876, October 20th, in longitude 150° 25' W., observed meridian altitude of sun's L.L. bearing North, was 49° 58' 50", index correction + 1' 10", height of eye 19 feet: required the latitude.

5. In latitude 59° 36' N., the departure made good was 52.9 miles East: required the difference of longitude by parallel sailing.

6. Required the course and distance from A to B, by Mercator's Sailing.

Latitude of A 9° 36' S.

Longitude of A 2° 10' W.

Latitude of B 7 16 S.

Longitude of B 1 24 E.

#### ADDITIONAL FOR ONLY MATE.

7. 1875, October 10th: find A.M. and P.M. times of high water at Calcutta, longitude 88° E., Falmouth, and Scarborough.

8. 1876, October 9th, at 5<sup>h</sup> 51<sup>m</sup> A.M. apparent time at ship, latitude 18° 45' S., longitude 99° 18' E., sun's magnetic amplitude E.  $\frac{1}{4}$  N.: required the error of compass; and supposing the variation to be 1° 50' W.: required the deviation of the compass for the position of the ship's head at the time of observation.

9. 1876, October 30th, P.M. at ship, latitude 32° 45' N., observed altitude sun's L.L. 28° 30', index correction + 2' 30", eye 18 feet, time by chronometer, October 30<sup>d</sup> 11<sup>h</sup> 56<sup>m</sup> 43<sup>s</sup>, which was 2<sup>m</sup> 28<sup>s</sup> slow for Greenwich mean noon, October 1st, and on October 8th, was 2<sup>m</sup> 44<sup>s</sup> 8 slow for mean time at Greenwich: required the longitude.

#### ADDITIONAL FOR FIRST MATE.

10. 1876, October 1st, mean time at ship 4<sup>h</sup> 54<sup>m</sup> P.M., latitude 17° 8' S., longitude 152° 33' E., sun's bearing by compass W.  $\frac{1}{2}$  N., observed altitude sun's L.L. 13° 59', index corr. — 22", eye 17 feet: required the error of compass; and supposing the variation to be 7° 40' E.: required the deviation for the position of the ship's head at the time of observation.

11. 1876, October 2nd, A.M. at ship, latitude account 38° 12' N., longitude 23° 34' W., observed altitude sun's L.L., South of observer, 47° 30', index correction — 1' 38", eye 17 feet, time by watch 1<sup>h</sup> 50<sup>m</sup>, (or 2<sup>d</sup> 1<sup>h</sup> 50<sup>m</sup>), which had been found to be 2<sup>h</sup> 10<sup>m</sup> fast on apparent time at ship, the difference of longitude made to East was 43 miles: required the latitude.

## ADDITIONAL FOR MASTER ORDINARY.

12. 1876, October 7th, the observed meridian altitude of the star *a Pegasi (Markab)* was  $54^{\circ} 10' 15''$ , bearing South, height of eye 13 feet: required the latitude.

In the following table give the correct magnetic bearing of the distant object, and thence the deviation:—

Correct magnetic bearing.

| Ship Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. |
|--------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North. ....                    | S. $37^{\circ}$ W.                             |                     | South ....                       | S. $41^{\circ}$ W.                             |                     |
| N.E. ....                      | S. $55^{\circ}$ W.                             |                     | S.W. ....                        | S. $20^{\circ}$ W.                             |                     |
| East. ....                     | S. $60^{\circ}$ W.                             |                     | West ....                        | S. $14^{\circ}$ W.                             |                     |
| S.E. ....                      | S. $57^{\circ}$ W.                             |                     | N.W. ....                        | S. $19^{\circ}$ W.                             |                     |

With the deviation as above, give the courses you would steer by the Standard Compass to make the following courses correct magnetic.

Correct magnetic courses:—S.E.; N.E.  $\frac{1}{4}$  E.; S.  $10^{\circ}$  W.; E.  $\frac{1}{4}$  N.

Compass courses:—

Supposing you have steered the following courses by the Standard Compass, find the correct magnetic courses made from the above deviation table.

Compass Courses:—S.S.E.  $\frac{1}{4}$  E.; S.  $\frac{3}{4}$  W.; E. by N.  $\frac{3}{4}$  N.; N.  $\frac{1}{4}$  W.

Correct magnetic courses:—

You have taken the following bearing of two distant objects by your Standard Compass as above, with the ship's head at S.E. by E.  $\frac{1}{2}$  E., find the bearings, correct magnetic.

Compass bearings:—E. by S.  $\frac{1}{2}$  S. and W.N.W.

Bearings, magnetic:—

## EXAMINATION PAPER.—No. XI.

## FOR SECOND MATE.

1. Multiply  $45.3$  by  $9.76$ , by common logarithms.
2. Divide  $100.002$  by  $1.0012$ , by common logarithms.
- 3.—

| H. | COURSES.              | K. | $\frac{1}{10}$ | WINDS.     | LEE-WAY.            | DEVIATION.      | REMARKS, &c.   |
|----|-----------------------|----|----------------|------------|---------------------|-----------------|--|
| 1  | N. by E.              | 4  | 2              | E. by N.   | pts. $2\frac{1}{4}$ | $3^{\circ}$ E.  | A point of land in lat. $52^{\circ}$ N., long. $120^{\circ}$ E. bearing by compass N. by E. $\frac{1}{4}$ E., dist. 16 miles. (Ship's head N. by E.) Deviation as per log. |
| 2  |                       | 3  | 8              |            |                     |                 |  |
| 3  |                       | 4  | 5              |            |                     |                 |  |
| 4  | N.E. $\frac{3}{4}$ E. | 4  | 5              | N. by W.   | $3\frac{1}{2}$      | $17^{\circ}$ E. |  |
| 5  |                       | 4  | 5              |            |                     |                 |  |
| 6  |                       | 5  | 5              |            |                     |                 |  |
| 7  |                       | 5  | 5              |            |                     |                 |  |
| 8  |                       | 4  | 5              |            |                     |                 |  |
| 9  | W. $\frac{3}{4}$ N.   | 5  | 6              | N. by W.   | $1\frac{3}{4}$      | $17^{\circ}$ W. | Variation $25^{\circ}$ East.   |
| 10 |                       | 6  | 2              |            |                     |                 |  |
| 11 |                       | 6  | 3              |            |                     |                 |  |
| 12 |                       | 6  | 4              |            |                     |                 |  |
| 1  | E.S.E.                | 6  | 5              | South.     | 3                   | $13^{\circ}$ E. |  |
| 2  |                       | 5  | 5              |            |                     |                 |  |
| 3  |                       | 5  | 8              |            |                     |                 |  |
| 4  | S.E. $\frac{1}{2}$ S. | 5  | 7              | N. by E.   | 0                   | $9^{\circ}$ E.  |  |
| 5  |                       | 4  | 6              |            |                     |                 |  |
| 6  |                       | 4  | 5              |            |                     |                 | A current set (correct magnetic) E.N.E., 22 miles, from the time the departure was taken to the end of the day.  |
| 7  |                       | 4  | 8              |            |                     |                 |  |
| 8  |                       | 4  | 1              |            |                     |                 |  |
| 9  | W. $\frac{3}{4}$ S.   | 6  | 6              | N.W. by N. | $3\frac{1}{4}$      | $14^{\circ}$ W. |  |
| 10 |                       | 6  | 3              |            |                     |                 |  |
| 11 |                       | 6  | 4              |            |                     |                 |  |
| 12 |                       | 6  | 3              |            |                     |                 |  |

4. 1876, November 15th, longitude  $80^{\circ} 11' E.$ , the observed meridian altitude of the sun's L.L., bearing North, was  $67^{\circ} 44'$ , index error  $- 1' 38''$ , height of eye 15 feet: required the latitude.

5. In latitude  $40^{\circ} 50' S.$ , the departure made good was 149 miles East: required the difference of longitude by parallel sailing.

6. Required the course and distance from the ship's position to the Lizard, by calculation on Mercator's principle.

Latitude of position  $17^{\circ} 50' N.$

Longitude of position  $76^{\circ} 42' W.$

Latitude of Lizard  $49^{\circ} 58' N.$

Longitude of Lizard  $5^{\circ} 12' W.$

#### ADDITIONAL FOR ONLY MATE.

7. 1875, November 12th: find A.M. and P.M. times of high water at Bombay, longitude  $73^{\circ} E.$ , Newhaven, and Torbay.

8. 1876, November 10th, at  $4^h 3^m 52^s$  A.M. apparent time at ship, latitude  $58^{\circ} 13' S.$ , longitude  $55^{\circ} 47' E.$ , the sun's magnetic amplitude S. by E.  $\frac{1}{4} E.$ : required the error of the compass; and supposing the variation to be  $16^{\circ} 30' E.$ : required the deviation of the compass for the position of the ship's head when the observation was taken.

9. 1876, November 30th, A.M. at ship, latitude  $40^{\circ} 40' S.$ , observed altitude sun's L.L.  $39^{\circ} 30'$ , index error  $+ 6' 24''$ , eye 22 feet, time by chronometer, November  $30^d 2^h 58^m 45^s$ , which was *fast*  $10^m 50^s$  for Greenwich mean noon, October 13th, and on October 25th was  $10^m 36^s$  *fast* for Greenwich mean time: required the longitude.

#### ADDITIONAL FOR FIRST MATE.

10. 1876, November 15th, mean time at ship,  $2^h 46^m 43^s$  P.M., latitude  $45^{\circ} 31' S.$ , longitude  $119^{\circ} 56' W.$ , sun's bearing by compass S.  $98\frac{1}{2}^{\circ} W.$ , observed altitude sun's L.L.  $43^{\circ} 45'$ , index error  $- 56''$ , eye 20 feet: required the error of the compass; and supposing the variation be  $7^{\circ} 50' W.$ : required the deviation of the compass for the position of the ship's head when the observation was taken.

11. 1876, November 13th, A.M. at ship, latitude by acct.  $50^{\circ} 52' S.$ , longitude  $48^{\circ} 52' W.$ , observed altitude sun's L.L. was  $56^{\circ} 0' N.$ , index error  $+ 23'$ , height of eye 19 feet, time by watch  $4^m 34^s$  (or  $13^d 0^h 4^m 34^s$ ), which had been found to be  $43^m 24^s$  *fast* on apparent time at ship, the difference of longitude made to *West* was 9 miles after the error on apparent time was determined: required the latitude by reduction to meridian.

#### ADDITIONAL FOR MASTER ORDINARY.

12. 1876, November 7th, the observed meridian altitude of the star  $\alpha$  Piscis Australis (*Fomalhaut*), bearing North, was  $59^{\circ} 40'$ , index correction  $+ 1' 12''$ , height of eye 23 feet: required the latitude.

In the following table give the correct magnetic bearing of the distant object, and thence the deviation:—

Correct magnetic bearing.

| Ship's head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation required. | Ship's head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North ....                       | S. $88^{\circ} W.$                             |                     | South. ....                      | N. $88^{\circ} W.$                             |                     |
| N.E. ....                        | S. $70^{\circ} W.$                             |                     | S.W. ....                        | N. $80^{\circ} W.$                             |                     |
| East. ....                       | S. $68^{\circ} W.$                             |                     | West. ....                       | N. $72^{\circ} W.$                             |                     |
| S.E. ....                        | S. $80^{\circ} W.$                             |                     | N.W. ....                        | N. $75^{\circ} W.$                             |                     |

With the deviation as above, give the courses you would steer by the Standard Compass to make the following courses correct magnetic.

Correct magnetic courses:—W. by S.  $\frac{1}{4} S.$ ; N.W. by W.  $\frac{1}{2} W.$ ; E. by S.  $\frac{1}{2} S.$ ; S.  $\frac{1}{4} E.$

Compass courses:—

Supposing you have steered the following courses by the Standard Compass, find the correct magnetic courses made, from the above deviation table.

Compass courses:—W.  $\frac{1}{2}$  N.; N.  $42^\circ$  W.; S.  $64^\circ$  E.; N.E.  $\frac{1}{2}$  N.

Magnetic courses:—

You have taken the following bearings of two distant objects by your Standard Compass as above; with the ship's head at W. by N.  $\frac{1}{2}$  N., find the bearings, correct magnetic.

Compass bearings:—W.  $\frac{1}{2}$  N. and S.  $36^\circ$  E.

Bearings, magnetic:—

## EXAMINATION PAPER.—No. XII.

### FOR SECOND MATE.

1. Multiply 0.00694 by 0.33318 by common logarithms.

2. Divide 999.43 by 67.832, by common logarithms.

3.—

| H. | COURSES.                  | K. $\frac{1}{10}$ | WINDS.                    | LEE-WAY.       | DEVIATION.    | REMARKS, &c.   |
|----|---------------------------|-------------------|---------------------------|----------------|---------------|--|
| 1  | E. by N. $\frac{1}{4}$ N. | 3 5               | N. $\frac{1}{2}$ E.       | pts.<br>2      | $11^\circ$ E. | A point, lat. $50^\circ 0'$ N.<br>long. $40^\circ 0'$ W., bearing by compass<br>E.N.E. $\frac{1}{4}$ E.,<br>dist. 16 miles. (Ship's head E. by N. $\frac{1}{4}$ N.)<br>Deviation as per log. |
| 2  |                           | 3 3               |                           |                |               |  |
| 3  |                           | 4                 |                           |                |               |  |
| 4  |                           | 4 2               |                           |                |               |  |
| 5  | W.N.W.                    | 6 5               | North.                    | $1\frac{1}{2}$ | $10^\circ$ W. |  |
| 6  |                           | 6 2               |                           |                |               |  |
| 7  |                           | 5 6               |                           |                |               |  |
| 8  |                           | 4 7               |                           |                |               |  |
| 9  | S.S.W. $\frac{1}{4}$ W.   | 4 2               | West.                     | $2\frac{1}{2}$ | $4^\circ$ W.  |  |
| 10 |                           | 4                 |                           |                |               |  |
| 11 |                           | 3 6               |                           |                |               |  |
| 12 |                           | 3 2               |                           |                |               |  |
| 1  | N.N.W. $\frac{1}{4}$ W.   | 5 6               | West.                     | $1\frac{3}{4}$ | $5^\circ$ W.  | Variation $36\frac{1}{2}^\circ$ West.  |
| 2  |                           | 5 6               |                           |                |               |  |
| 3  |                           | 6 4               |                           |                |               |  |
| 4  |                           | 6 4               |                           |                |               |  |
| 5  | S.E. $\frac{3}{4}$ E.     | 6 2               | S.S.W.                    | $1\frac{1}{2}$ | $7^\circ$ E.  | A current set (correct mag.) S.S.W., 6 miles, from the time the departure was taken to the end of the day.   |
| 6  |                           | 5 6               |                           |                |               |  |
| 7  |                           | 5 2               |                           |                |               |  |
| 8  |                           | 5                 |                           |                |               |  |
| 9  | S.W. $\frac{3}{4}$ W.     | 2 5               | S. by E. $\frac{1}{4}$ E. | $3\frac{1}{4}$ | $6^\circ$ W.  |  |
| 10 |                           | 3 $2\frac{1}{2}$  |                           |                |               |  |
| 11 |                           | 3                 |                           |                |               |  |
| 12 |                           | 3 3               |                           |                |               |  |

4. 1876, Dec. 31st, in longitude  $123^\circ 45'$  W., observed meridian altitude of sun's L.L. bearing South, was  $67^\circ 8' 10''$ , index correction  $+9''$ , height of eye 13 feet: required the latitude.

5. In latitude  $60^\circ$  N., the departure made good was 111 miles East: required the difference of longitude by parallel sailing.

6. Required the course and distance from Port San Francisco to Cape Palliser, by Mercator's Sailing.

Lat. Port San Francisco  $37^\circ 48'$  N.

Long. Port San Francisco  $122^\circ 24'$  W.

Lat. Cape Palliser  $41^\circ 38'$  S.

Long. Cape Palliser  $175^\circ 21'$  E.

### ADDITIONAL FOR ONLY MATE.

7. 1875, December 28th: find A.M. and P.M. tides at Batavia, long.  $107^\circ$  E., Valentia Harbour, and Kilrush.



8. 1876, December 28th, at 4<sup>h</sup> 11<sup>m</sup> 13<sup>s</sup> A.M., apparent time at ship, latitude 46° 47' S., longitude 179° 54' W., sun's magnetic amplitude S.E. by E.  $\frac{3}{4}$  E.: required error of compass; and supposing the variation to be 15° 30' E., required the deviation of the compass for the position of the ship's head at the time of observation.

9. 1876, December 24th, A.M. at ship, latitude 33° 33' S., observed altitude sun's L.L. 40° 40' 40"; index correction + 2' 20", height of eye 19 feet, time by chronometer 8<sup>h</sup> 7<sup>m</sup> 37<sup>s</sup> P.M., which was 6<sup>m</sup> 8<sup>s</sup> slow for Greenwich mean noon, October 31st, and on November 12th was 7<sup>m</sup> 16<sup>s</sup> 2 slow for Greenwich mean time: required the longitude by chronometer.

#### ADDITIONAL FOR FIRST MATE.

10. 1876, December 27th, mean time at ship 8<sup>h</sup> 0<sup>m</sup> 10<sup>s</sup> A.M., latitude 15° 12' N., longitude 130° W., sun's bearing by compass E. by S.  $\frac{3}{4}$  S., observed altitude sun's L.L. 20° 15', index correction + 2' 5", height of eye 16 feet: required the error of compass; and supposing the variation is 7° 20' E.: required the deviation for the position of the ship's head at the time of observation.

11. 1876, Dec. 4th, A.M. at ship, latitude acct. 51° 54' S., longitude 30° 10' W., observed altitude sun's L.L., North of observer, was 59° 59', index correction — 3' 12", height of eye 20 feet, time by watch 12<sup>m</sup> 10<sup>s</sup> (or 4<sup>d</sup> 0<sup>h</sup> 12<sup>m</sup> 10<sup>s</sup>), which had been found to be 42<sup>m</sup> 10<sup>s</sup> fast on apparent time at ship, the difference of longitude made to the *West* was 10 miles after the error on apparent time was determined: required the latitude.

#### ADDITIONAL FOR MASTER ORDINARY.

12. 1876, Dec. 21st, the observed meridian altitude of star *a* Canis Minoris (*Procyon*) was 52° 51' 50", bearing North, index correction — 49", height of eye 21 feet: required the latitude.

In the following table give the correct magnetic bearing of the distant object, and thence the deviation.

Correct magnetic bearing.

| Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North ....                       | S. 2° W.                                       |                     | South ....                       | S. 5° E.                                       |                     |
| N.E. ....                        | S. 4 W.  |                     | S.W. ....                        | S. 24 E.                                       |                     |
| East .....                       | S. 10 W.                                       |                     | West ....                        | S. 16 E.                                       |                     |
| S.E. ....                        | S. 16 W.                                       |                     | N.W. ....                        | S. 3 E.  |                     |

With the deviation as above, give the courses you would steer by the Standard Compass, to make the following courses correct magnetic.

Correct magnetic courses:—N. 78° E.; E.S.E.; S.W. by W.  $\frac{1}{2}$  W; N.  $\frac{3}{4}$  W.

Compass courses:—

Supposing you have steered the following courses by the Standard Compass, find the correct magnetic courses made from the above deviation table.

Compass courses:—S.S.E.; W. by S.  $\frac{1}{2}$  S.; S. by W.  $\frac{1}{2}$  W.; S.E.  $\frac{1}{2}$  S.

Magnetic courses:—

You have taken the following bearings of two distant objects by your Standard Compass as above, with the ship's head at S.W. by S., find the bearings, correct magnetic.

Compass bearings:—W. by S.  $\frac{1}{2}$  S. and N.N.W.

Bearings, magnetic:—

#### EXAMINATION PAPER—No. XIII.

##### FOR SECOND MATE.

1. Multiply 448000 by '0000448, by common logarithms.
2. Divide '085375 by '07425, by common logarithms.

3.—

| II. | COURSES.                | K. | $\frac{1}{10}$ | WINDS.   | LEE-WAY.           | DEVIATION. | REMARKS, &c.  |
|-----|-------------------------|----|----------------|----------|--------------------|------------|---|
| 1   | S.S.W. $\frac{1}{4}$ W. | 12 | 2              | West.    | pts. $\frac{1}{4}$ | 42° W.     | A point, lat. 62° 18' N. long. 83° 17' E., bear. by compass N. $\frac{1}{2}$ E. $\frac{1}{4}$ E. dist. 23 miles. (Ship's head S.S.W.) Deviation as per log. |
| 2   |                         | 12 | 9              |          |                    |            |   |
| 3   |                         | 12 | 5              |          |                    |            |   |
| 4   | S.W. $\frac{3}{4}$ W.   | 13 | 0              | S. by E. | $\frac{1}{2}$      | 8° W.      |   |
| 5   |                         | 11 | 5              |          |                    |            |   |
| 6   |                         | 11 | 4              |          |                    |            |   |
| 7   |                         | 11 | 2              |          |                    |            |   |
| 8   | E. $\frac{3}{4}$ S.     | 11 | 3              | S. by E. | $1\frac{3}{4}$     | 15° E.     |   |
| 9   |                         | 5  | 4              |          |                    |            |   |
| 10  |                         | 5  | 6              |          |                    |            |   |
| 11  |                         | 5  | 4              |          |                    |            |   |
| 12  |                         | 5  | 3              |          |                    |            |   |
| 1   | W.N.W.                  | 4  | 4              | North.   | 3                  | 19° W.     | Variation 42° E.  |
| 2   |                         | 4  | 2              |          |                    |            |   |
| 3   |                         | 4  | 2              |          |                    |            |   |
| 4   |                         | 5  | 0              |          |                    |            |   |
| 5   | N.W. $\frac{1}{2}$ N.   | 10 | 7              | S. by W. | 0                  | 16° 30' W. |   |
| 6   |                         | 10 | 2              |          |                    |            |   |
| 7   |                         | 11 | 4              |          |                    |            |   |
| 8   |                         | 11 | 8              |          |                    |            |   |
| 9   | E. $\frac{3}{4}$ N.     | 3  | 4              | N. by E. | $3\frac{1}{4}$     | 17° 14' E. | A current set the ship S.W. $\frac{1}{4}$ W. (correct magnetic) 52 miles.   |
| 10  |                         | 3  | 2              |          |                    |            |   |
| 11  |                         | 3  | 0              |          |                    |            |   |
| 12  |                         | 2  | 8              |          |                    |            |   |

4. 1876, August 11th, in longitude 92° 12' E., the observed meridian altitude of sun's L.L. was 42° 42' 10", zenith South of sun, index correction — 2' 50", height of eye 17 feet: required the latitude.

5. In latitude 80° the departure made good was 80 miles: required the difference of longitude by parallel sailing.

6. Required the course and distance from A to B, by Mercator's Sailing.

Latitude of A 51° 30' N.

Longitude of A 3° 30' 30" W.

Latitude of B 20° 0' N.

Longitude of B 33° 4' 56" W.

#### ADDITIONAL FOR ONLY MATE.

7. 1875, July 24th: find A.M. and P.M. tides at Point de Galle, long. 80° E., St. Nazaire, and Jersey.

8. 1876, October 28th, at 8<sup>h</sup> 30<sup>m</sup> A.M. apparent time at ship, latitude 49° 40' N., longitude 116° 12' W., sun's bearing by compass E. 10° 40' N.: required the true amplitude and error of compass: and supposing the variation to be 23° 50' E.: required the deviation for the position of the ship's head at the time of observation.

9. 1876, April 18th, A.M. at ship, latitude 50° 48' N., observed altitude sun's L.L. 38° 10' 50", index correction + 45", height of eye 16 feet, time by chronometer 9<sup>h</sup> 27<sup>m</sup> 28<sup>s</sup>, A.M. at Greenwich, which was 0<sup>m</sup> 49<sup>s</sup>·3 *slow* for mean noon at Greenwich, March 17th, and on April 1st was 1<sup>m</sup> 58<sup>s</sup>·7 *fast* for mean time at Greenwich: required the longitude.

#### ADDITIONAL FOR FIRST MATE.

10. 1876, March 9th, mean time at ship 8<sup>h</sup> 11<sup>m</sup> 42<sup>s</sup> A.M., latitude 29° 58' S., longitude 57° 24' E., observed altitude sun's L.L. 28° 23' 15", height of eye 16 feet, sun's azimuth E. 9° 40' S.: required the error of compass; and supposing the variation to be 17° 10' W.: required the deviation for the position of the ship's head at the time of observation.

11. 1876, July 28th, A.M. at ship, latitude account 38° 54' N., longitude 39° W., observed altitude sun's L.L. 69° 10' S., index corr. + 1' 27", height of eye 23 feet, time by watch 11<sup>h</sup> 3<sup>m</sup> 15<sup>s</sup>, *slow* on apparent time at ship 28<sup>m</sup> 45<sup>s</sup>, the difference of longitude made to *East* was 32 miles after the error on apparent time was determined: required the latitude by reduction to meridian.

ADDITIONAL FOR MASTER ORDINARY.

12. 1876, October 8th, the observed meridian altitude of  $\alpha$  Gruis was  $50^{\circ} 0' S.$ , index correction —  $1' 12''$ , height of eye 17 feet: required the latitude.

In the following table give the correct magnetic bearing of the distant object and thence the deviation.

Correct magnetic bearing.

| Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North ....                       | S. $25^{\circ}$ W.                             |                     | South ....                       | S. $1^{\circ}$ W.                              |                     |
| N.E. ....                        | S. $21^{\circ}$ W.                             |                     | S.W. ....                        | S. $7^{\circ}$ E.                              |                     |
| East ....                        | S. $21^{\circ}$ W.                             |                     | West ....                        | S. $6^{\circ}$ W.                              |                     |
| S.E. ....                        | S. $16^{\circ}$ W.                             |                     | N.W. ....                        | S. $21^{\circ}$ W.                             |                     |

With the deviation as above, give the courses you would steer by the Standard Compass to make the following courses correct magnetic.

Correct magnetic courses:—S.W. by W.; E.N.E.; S. by W.  $\frac{1}{2}$  W.; N.N.E.

Compass courses:—

Supposing you have steered the following courses by the Standard Compass, find the correct magnetic courses made from the above deviation table.

Compass courses:—N.E. by E.; N.W.  $\frac{1}{2}$  N.; N.  $\frac{1}{2}$  E.; S. by E.

Correct magnetic courses:—

You have taken the following bearings of two distant objects by your Standard Compass as above; with the ship's head at S.S.W.  $\frac{1}{2}$  W., find the bearings, correct magnetic.

Compass bearings:—N.E. by E. and S.W. by W.

Bearings, magnetic:—

EXAMINATION PAPER.—No. XIV.

FOR SECOND MATE.

1. Multiply 100001 by 8, by common logarithms.

2. Divide  $37^{\circ} 149$  by  $523^{\circ} 76$ , by common logarithms.

3.—

| H. | COURSES.                             | K. | $\frac{1}{10}$ | WINDS.                | LEE-WAY.            | DEVIATION.      | REMARKS, &c.   |
|----|--------------------------------------|----|----------------|-----------------------|---------------------|-----------------|--|
| 1  | S. by E. $\frac{1}{2}$ E.            | 3  | 3              | S.W. $\frac{1}{2}$ W. | pts. $2\frac{1}{2}$ | $5^{\circ}$ E.  | A point, Cape of Good Hope, in latitude $34^{\circ} 28' S.$ , longitude $18^{\circ} 28' E.$ , bearing by compass N. $6^{\circ}$ W. $\frac{3}{4}$ W., dist. 21 miles. (Ship's head S. by E. $\frac{1}{2}$ E.) Deviation as per log. |
| 2  |                                      | 3  | 4              |                       |                     |                 |  |
| 3  |                                      | 3  | 6              |                       |                     |                 |  |
| 4  |                                      | 3  | 7              |                       |                     |                 |  |
| 5  | N.W. $\frac{1}{2}$ W.                | 2  | 4              | S.W. by W.            | $3\frac{1}{2}$      | $18^{\circ}$ W. |  |
| 6  |                                      | 2  | 3              |                       |                     |                 |  |
| 7  |                                      | 2  | 3              |                       |                     |                 |  |
| 8  |                                      | 2  | 2              |                       |                     |                 |  |
| 9  | N. by E. $\frac{1}{2}$ E.            | 4  | 6              | N.W. $\frac{1}{2}$ W. | $2\frac{1}{4}$      | $6^{\circ}$ E.  |  |
| 10 |                                      | 4  | 4              |                       |                     |                 |  |
| 11 |                                      | 4  | 7              |                       |                     |                 |  |
| 12 |                                      | 4  | 3              |                       |                     |                 |  |
| 1  | S.W. $6^{\circ}$ W. $\frac{1}{2}$ W. | 5  | 6              | N.W. $\frac{1}{2}$ W. | $1\frac{3}{4}$      | $7^{\circ}$ W.  | Variation $25^{\circ}$ W.<br><br>A current set (correct magnetic) E. by S. $\frac{1}{4}$ S., 14 miles, from the time the departure was taken to the end of day.  |
| 2  |                                      | 5  | 7              |                       |                     |                 |  |
| 3  |                                      | 5  | 4              |                       |                     |                 |  |
| 4  |                                      | 5  | 3              |                       |                     |                 |  |
| 5  | W. by N. $\frac{1}{2}$ N.            | 7  | 5              | N. $\frac{1}{2}$ W.   | $\frac{1}{2}$       | $16^{\circ}$ W. |  |
| 6  |                                      | 7  | 6              |                       |                     |                 |  |
| 7  |                                      | 7  | 2              |                       |                     |                 |  |
| 8  |                                      | 6  | 7              |                       |                     |                 |  |
| 9  | N.E. $\frac{1}{4}$ E.                | 5  | 3              | E.S.E.                | 2                   | $16^{\circ}$ E. |  |
| 10 |                                      | 4  | 4              |                       |                     |                 |  |
| 11 |                                      | 5  | 5              |                       |                     |                 |  |
| 12 |                                      | 5  | 4              |                       |                     |                 |  |

4. 1876, Feb. 11th, in longitude  $32^{\circ} 20' E.$ , the observed meridian altitude of the sun's L.L. was  $30^{\circ} 25' 10''$ , observer North of sun, index correction  $-3' 15''$ , height of eye 12 feet: required the latitude.

5. In latitude  $51^{\circ} 10'$  the departure made good was 64.3 miles: required the difference of longitude by parallel sailing.

6. Required the course and distance from A to B, by Mercator's sailing.

Latitude A  $43^{\circ} 24' S.$  Longitude A  $65^{\circ} 39' W.$

Latitude B  $26^{\circ} 38' N.$  Longitude B  $15^{\circ} 8' E.$

#### ADDITIONAL FOR ONLY MATE.

7. 1875, April 2nd: find times of high water at Cape Virgin, longitude  $68^{\circ} W.$ , Waterford Harbour, and Banff.

8. 1876, March 31st, at  $6^h 1^m 48^s A.M.$ , apparent time at ship, in latitude  $6^{\circ} 31' N.$ , longitude  $155^{\circ} 10' E.$ , the sun's magnetic amplitude was  $E. 3^{\circ} 51' S.$ : required the error of compass; and supposing the variation to be  $6^{\circ} E.$ : required the deviation for the position of the ship's head at the time of observation.

9. 1876, May 27th, A.M. at ship, latitude  $55^{\circ} N.$ , observed altitude sun's L.L.  $43^{\circ} 9' 5''$ , index correction  $-14''$ , height of eye 14 feet, time by chronometer  $9^h 13^m 12^s A.M.$ , which was *slow*  $48^s.5$  for mean noon at Greenwich, April 9th, and on April 24th was *fast*  $0^m 25^s$ : required the longitude.

#### ADDITIONAL FOR FIRST MATE.

10. 1876, July 10th,  $9^h 44^m A.M.$ , mean time at ship, latitude  $59^{\circ} 56' N.$ , longitude  $40^{\circ} 20' W.$ , observed altitude sun's L.L.  $44^{\circ} 49'$ , sun's magnetic azimuth  $S. \frac{1}{2} W.$ , height of eye 20 feet: required the error of the compass: and supposing the variation be  $51^{\circ} W.$ : required the deviation for the position of the ship's head at the time of observation.

11. 1876, November 8th, P.M. at ship, latitude by account  $33^{\circ} 9' N.$ , longitude  $89^{\circ} 42' E.$ , observed altitude sun's L.L.  $40^{\circ} 0'$ , South of observer, index corr.  $-6' 12''$ , height of eye 19 feet, time by watch  $8^h 20^m 20^s$ , (or  $7^h 20^m 20^s$ ), *slow* on apparent time at ship, the difference of longitude made to the *East* was 32.3 miles: required the latitude by reduction to meridian.

#### ADDITIONAL FOR MASTER ORDINARY.

12. 1876, July 19th, the observed meridian altitude of  $\alpha$  Pavonis  $32^{\circ} 50' 15''$ , bearing South, index correction  $+4' 48''$ , height of eye 23 feet: required the latitude.

In the following table give the correct magnetic bearing of the distant object, and thence the deviation:—

Correct magnetic bearing.

| Ship's Head<br>by Standard<br>Compass. | Bearing of<br>Distant Object<br>by Standard<br>Compass. | Deviation<br>Required. | Ship's Head<br>by Standard<br>Compass. | Bearing of<br>Distant Object<br>by Standard<br>Compass. | Deviation<br>Required. |
|--|---|------------------------|--|---|------------------------|
| North .....                            | S. $44^{\circ} E.$                                      |                        | South .....                            | S. $11^{\circ} W.$                                      |                        |
| N.E. ....                              | S. $56^{\circ} E.$                                      |                        | S.W. ....                              | S. $13^{\circ} W.$                                      |                        |
| East .....                             | S. $39^{\circ} E.$                                      |                        | West .....                             | S. $4^{\circ} W.$                                       |                        |
| S.E. ....                              | S. $12^{\circ} E.$                                      |                        | N.W. ....                              | S. $12^{\circ} E.$                                      |                        |

With the deviation as above, give the courses you would steer by the Standard Compass to make the following courses correct magnetic.

Correct magnetic courses:—N.N.W.; W.N.W.; S.W. by W.; W.S.W.

Compass courses:—

Supposing you have steered the following courses by the Standard Compass, find the correct magnetic courses made from the above deviation table.

Compass courses:—E.N.E.; S.S.E.; N.W. by W.; N.E. by E.

Magnetic courses:—

You have taken the following bearings of two distant objects by your Standard Compass as above, with the ship's head at N.E.  $\frac{1}{2} E.$ , find the bearings, correct magnetic.

Compass bearings:—N. by W., and E. by N.

Bearings, magnetic:—

EXAMINATION PAPER.—No. XV.

FOR SECOND MATE.

1. Multiply 53.62 by 0.4188, by common logarithms.

2. Divide 5.6949 by 53.058, by common logarithms.

3.—

| II. | COURSES. | K. | $\frac{1}{10}$ | WINDS. | LEE-WAY.           | DEVIATION.           | REMARKS, &c.  |
|-----|----------|----|----------------|--------|--------------------|----------------------|---|
| 1   | N.E.     | 9  |                | N.N.W. | pts. $\frac{3}{4}$ | 6 $\frac{1}{2}$ ° E. | A point lat. 37° 37' N.<br>long. 0° 41' W. bearing by compass<br>N.W. by W. $\frac{1}{4}$ W.<br>dist. 25 miles.<br>(Ship's head N.E.)<br>Dev. as per log. |
| 2   |          | 8  | 6              |        |                    |                      |   |
| 3   |          | 9  | 2              |        |                    |                      |   |
| 4   | E.N.E.   | 8  | 6              | North. | $\frac{1}{4}$      | 11° E.               |   |
| 5   |          | 12 | 3              |        |                    |                      |   |
| 6   |          | 12 | 3              |        |                    |                      |   |
| 7   |          | 11 | 4              |        |                    |                      |   |
| 8   |          | 12 |                |        |                    |                      |   |
| 9   | N.N.W.   | 10 | 5              | N.E.   | $\frac{1}{2}$      | 6° W.                | Variation 19° W.  |
| 10  |          | 11 | 1              |        |                    |                      |   |
| 11  |          | 10 | 6              |        |                    |                      |   |
| 12  |          | 10 | 8              |        |                    |                      |   |
| 1   | E.S.E.   | 6  | 6              | N.E.   | 1 $\frac{1}{2}$    | 9 $\frac{1}{2}$ ° E. |   |
| 2   |          | 6  | 4              |        |                    |                      |   |
| 3   |          | 6  | 5              |        |                    |                      |   |
| 4   |          | 6  | 5              |        |                    |                      |   |
| 5   | N.N.E.   | 4  | 3              | East.  | 2 $\frac{1}{4}$    | 4° E.                | A current set by compass E. by S., 36 miles from the time the departure was taken to the end of the day.  |
| 6   |          | 4  | 8              |        |                    |                      |   |
| 7   |          | 4  | 5              |        |                    |                      |   |
| 8   |          | 4  | 4              |        |                    |                      |   |
| 9   | S.E.     | 8  | 5              | E.N.E. | 1 $\frac{1}{4}$    | 4° E.                |   |
| 10  |          | 8  | 7              |        |                    |                      |   |
| 11  |          | 7  | 4              |        |                    |                      |   |
| 12  |          | 7  | 4              |        |                    |                      |   |

4. 1876, November 21st, in longitude 70° 20' E., observed meridian altitude of the sun's L.L. was 80° 20', bearing North, index correction — 2' 50", height of eye 20 feet: required the latitude.

5. In latitude 35° 39', the departure made good 66 miles.

6. Required the course and distance from A to B, by Mercator's sailing.

Latitude A 6° 1' N.

Longitude A 60° 14' E.

Latitude B 6 10 S.

Longitude B 39 15 E.

ADDITIONAL FOR ONLY MATE.

7. 1875, September 1st: find the times of high water, A.M. and P.M., at Victoria River, longitude 130° E., and also at Beachy Head and Antwerp.

8. 1876, January 16th, at 7<sup>h</sup> 22<sup>m</sup> P.M., apparent time at ship, latitude 43° 4' S., longitude 10° 6' W., sun's magnetic amplitude W. 15° 56' S.: required the error of compass; and supposing the variation to be 23° 20' W.: required the deviation of the compass for the position of the ship's head at the time of observation.

9. 1876, June 5th, A.M. at ship, latitude 2° 5' S., observed altitude sun's L.L. 28° 4', index correction + 4' 25", eye 15 feet, time by chronometer, June 4<sup>h</sup> 12<sup>h</sup> 28<sup>m</sup> 42<sup>s</sup>, which was 1<sup>m</sup> 4<sup>s</sup> fast for mean noon at Greenwich, March 6th, and on March 24th was 0<sup>m</sup> 8<sup>s</sup> slow on mean time at Greenwich: required the longitude.

## ADDITIONAL FOR FIRST MATE.

10. 1876, November 10th, 8<sup>h</sup> 45<sup>m</sup> 38<sup>s</sup> A.M., mean time at ship, latitude 50° 30' N., longitude 86° 43' E., observed altitude sun's L.L. 6° 7' 10", height of eye 15 feet, sun's magnetic azimuth S. 49° 50' E.: required the error of compass; and supposing the variation to be 7° 20' E.: required the deviation of the compass for the position of the ship's head at the time of observation.

11. 1876, January 8th, A.M. at ship, latitude account 35° 10' S., longitude 55° 12' W., observed altitude of sun's L.L. 76° 44', N., index correction + 1' 18", height of eye 14 feet, time by watch 39<sup>m</sup> 34<sup>s</sup>, (or 8<sup>d</sup> 0<sup>h</sup> 39<sup>m</sup> 34<sup>s</sup>), which was 50<sup>m</sup> 3<sup>s</sup> fast on apparent time at ship, the difference of longitude made to the East 21', after the error on apparent time was determined: required the latitude.

## ADDITIONAL FOR MASTER ORDINARY.

12. 1876, February 1st, longitude 50° W., observed meridian altitude of the star  $\alpha$  Canis Majoris (*Sirius*) 37° 50' 20" S., height of eye 19 feet, index correction + 1' 4": required the latitude.

In the following table give the correct magnetic bearing of the distant object, and thence the deviation:—

Correct magnetic bearing.

| Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North ....                       | North.   |                     | South ....                       | N. 24° E.                                      |                     |
| N.E. ....                        | N. 12° E.                                      |                     | S.W. ....                        | N. 5° E.                                       |                     |
| East .....                       | N. 29° E.                                      |                     | West ....                        | N. 5° W.                                       |                     |
| S.E. ....                        | N. 36° E.                                      |                     | N.W. ....                        | N. 5° W.                                       |                     |

With the deviation as above, give the courses you would steer by the Standard Compass to make the following courses correct magnetic.

Correct magnetic courses:—W.N.W.; W.S.W.; S.E. by E.; S.S.E.

Compass courses:—

Supposing you have steered the following courses by the Standard Compass, find the correct magnetic courses made from the above deviation table.

Compass courses:—E. by S.  $\frac{1}{2}$  S.; S. by E.  $\frac{1}{2}$  E.; N.W. by W.; W.  $\frac{1}{2}$  S.

Magnetic courses:—

You have taken the following bearings of two distant objects by your Standard Compass as above, with the ship's head at E. by S.  $\frac{1}{2}$  S. find the bearings, correct magnetic.

Compass bearings:—N. W. by W.  $\frac{1}{2}$  W., and S. by E.  $\frac{1}{2}$  E.

Bearings, magnetic:—

## EXAMINATION PAPER—No. XVI.

## FOR SECOND MATE.

1. Multiply 5940 by 530, and .00087214 by .001963, by common logarithms.
2. Divide 9504000 by 98, and .9649 by 35°0583, by common logarithms.

3.—

| H. | COURSES.                  | K. | $\frac{1}{10}$ | WINDS.                    | LEE-WAY.              | DEVIATION: | REMARKS, &c.   |
|----|---------------------------|----|----------------|---------------------------|-----------------------|------------|--|
| 1  | W.N.W.                    | 12 | 6              | North.                    | pts.<br>$\frac{1}{4}$ | 10° W.     | A point, lat. 36° 27' S.,<br>long. 68° 37' W., bearing<br>by compass E. $\frac{3}{4}$ S.<br>dist. 25 miles. (Ship's<br>head W.N.W.) De-<br>viation as per log. |
| 2  |                           | 12 | 6              |                           |                       |            |  |
| 3  |                           | 12 | 8              |                           |                       |            |  |
| 4  |                           | 13 |                |                           |                       |            |  |
| 5  | S.W. by W.                | 10 | 6              | N.W. by W.                | $\frac{3}{4}$         | 7° W.      |  |
| 6  |                           | 10 | 4              |                           |                       |            |  |
| 7  |                           | 10 | 4              |                           |                       |            |  |
| 8  |                           | 10 | 6              |                           |                       |            |  |
| 9  | N. by E. $\frac{1}{2}$ E. | 7  | 3              | N.W. $\frac{1}{2}$ W.     | $1\frac{1}{4}$        | 2½° W.     |  |
| 10 |                           | 7  | 6              |                           |                       |            |  |
| 11 |                           | 7  | 8              |                           |                       |            |  |
| 12 |                           | 7  | 3              |                           |                       |            |  |
| 1  | N.W.                      | 11 | 4              | N.N.E.                    | $\frac{1}{2}$         | 8° W.      | Variation 22½° East.   |
| 2  |                           | 11 | 4              |                           |                       |            |  |
| 3  |                           | 11 | 8              |                           |                       |            |  |
| 4  |                           | 11 | 4              |                           |                       |            |  |
| 5  | S.W. $\frac{1}{4}$ W.     | 3  | 3              | W.N.W.                    | $3\frac{1}{4}$        | 7° W.      |  |
| 6  |                           | 2  | 8              |                           |                       |            |  |
| 7  |                           | 2  | 6              |                           |                       |            |  |
| 8  |                           | 2  | 3              |                           |                       |            |  |
| 9  | N.E. $\frac{1}{2}$ E.     | 4  | 7              | N. by W. $\frac{1}{2}$ W. | $2\frac{3}{4}$        | 8° E.      | A current set (correct<br>magnetic) S.S.W. $\frac{1}{2}$ W.<br>32 miles, from the time<br>the departure was<br>taken to the end of the<br>day.                 |
| 10 |                           | 4  | 4              |                           |                       |            |  |
| 11 |                           | 3  | 6              |                           |                       |            |  |
| 12 |                           | 3  | 3              |                           |                       |            |  |

4. 1877, January 1st, in longitude 167° 54' E., the observed meridian altitude of sun's L.L., 83° 40', zenith North of sun, index correction + 47", height of eye 23 feet: required the latitude.

5. In latitude 60° 5' S., longitude 179° 17' W., a ship sails due West 96 miles: find the longitude in.

6. Required the course and distance from A to B, by Mercator's Sailing.

Latitude of A 8° 57' N.

Longitude of A 79° 31' W.

Latitude of B 36 50 S.

Longitude of B 174 49 E.

# ADDITIONAL FOR ONLY MATE.

7. 1875, March 28th: find the times of high water at Gibraltar, Port Louis (Mauritius), long. 57½° E., and Halifax, long. 64° W.

8. 1876, November 4th, at 4<sup>h</sup> 52<sup>m</sup> 42<sup>s</sup> A.M., apparent time at ship, latitude 46° 40' S., longitude 8° 57' W., sun's magnetic amplitude S.E.  $\frac{1}{2}$  S.: required the error of compass; and supposing the variation to be 16° 30' W.: required the deviation of the compass for the position of the ship's head at the time of observation.

9. 1876, Sept. 1st, A.M. at ship, latitude 15° 31' S., observed altitude sun's L.L. was 15° 18' 20", index correction — 20", height of eye 26 feet, time by chronometer, August 31<sup>d</sup> 20<sup>h</sup> 12<sup>m</sup> 40<sup>s</sup>, slow 1<sup>m</sup> 30<sup>s</sup> on April 15th, and on April 29th was 0<sup>m</sup> 29<sup>s</sup> fast on Greenwich mean time: required the longitude.

## ADDITIONAL FOR FIRST MATE.

10. 1876, June 1st, 8<sup>h</sup> 19<sup>m</sup> A.M., mean time at ship, latitude  $21^{\circ} 10' N.$ , longitude  $61^{\circ} 30' E.$ , observed altitude sun's L.L.  $39^{\circ} 10'$ , index correction  $- 15''$ , height of eye 18 feet, sun's magnetic azimuth  $E. \frac{3}{4} N.$ : required the error of compass; and supposing the variation to be  $0^{\circ} 50' E.$ : required the deviation of the compass for the position of the ship's head at the time of observation.

11. 1876, April 13th, A.M. at ship, latitude account  $0^{\circ}$ , longitude  $147^{\circ} 10' E.$ , observed altitude of sun's L.L.  $80^{\circ} 30'$ , North of observer, index correction  $+ 1' 10''$ , height of eye 16 feet, time by watch  $0^h 0^m 12^s$  which had been found to be  $11^m 1^s$  fast on apparent time at ship, the difference of longitude made to the East was  $8\frac{1}{2}$  miles, after the error on apparent time was determined.

## ADDITIONAL FOR MASTER ORDINARY.

12. 1876, May 10th, the observed meridian altitude of  $\alpha^2$  Centuri was  $10^{\circ} 4' 15''$ , (zenith North), index correction  $- 2' 10''$ , height of eye 20 feet: required the latitude.

13. At what time will the star  $\alpha$  Aquilæ (*Altair*) pass the meridian of the Land's End, on December 8th, 1876, and how far North or South of the Zenith.

14. 1876, January 8th, at  $2^h 18^m$ , what stars will be near the meridian of a place in long.  $45^{\circ} 20' E.$

In the following table give the correct magnetic bearing of the distant object and thence the deviation.

## Correct magnetic bearing.

| Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North ....                       | S. $34^{\circ}$ W.                             |                     | South ....                       | S. $6^{\circ}$ E.                              |                     |
| N.E. ....                        | S. $30^{\circ}$ W.                             |                     | S.W. ....                        | South.   |                     |
| East .....                       | S. $18^{\circ}$ W.                             |                     | West ....                        | S. $13^{\circ}$ W.                             |                     |
| S.E. ....                        | S. $2^{\circ}$ E.                              |                     | N.W. ....                        | S. $25^{\circ}$ W.                             |                     |

With the deviation as above, give the courses you would steer by the Standard Compass to make the following courses correct magnetic.

Correct magnetic courses:—S. by W.  $\frac{1}{2}$  W.; E.  $\frac{1}{4}$  N.; N. by E.  $\frac{1}{2}$  E.; N.  $\frac{1}{2}$  W.

Compass courses:—

Supposing you have steered the following courses by the Standard Compass, find the correct magnetic courses made from the above deviation table.

Compass courses:—S. by E.  $\frac{1}{4}$  E.; E.  $\frac{1}{4}$  S.; S.W. by S.; N.  $\frac{1}{2}$  E.

Correct magnetic courses:—

You have taken the following bearings of two distant objects by your Standard Compass as above; with the ship's head at S. by W.  $\frac{1}{2}$  W., find the bearings, correct magnetic.

Compass bearings:—W.  $\frac{3}{4}$  S. and E. by N.  $\frac{1}{4}$  N.

Bearings, magnetic:—



EXAMINATION PAPER.—No. XVII.

FOR SECOND MATE.

1. Multiply  $30^{\circ}24$  by  $12.5$ , and  $034632$  by  $.397302$ , by common logarithms.
2. Divide  $8100900$  by  $900$ , and  $.00005$  by  $2.5$ , by  $25$ , and by  $.0000025$  by common logs.

3.—

| H. | COURSES.                  | K. | $\frac{1}{10}$ | WINDS.                    | LEE-WAY.           | DEVIATION.          | REMARKS, &c.   |
|----|---------------------------|----|----------------|---------------------------|--------------------|---------------------|--|
| 1  | N.E. $\frac{1}{2}$ E.     | 13 | 2              | N. by W. $\frac{1}{2}$ W. | pts. $\frac{1}{4}$ | 4° E.               | A point of land in lat. $50^{\circ}25'$ S., long. $179^{\circ}40'$ E. bearing by compass N. by W. $\frac{1}{4}$ W. dist. 16 miles. (Ship's head N.E. $\frac{1}{2}$ E.) Deviation as per log. |
| 2  |                           | 12 | 9              |                           |                    |                     |  |
| 3  |                           | 13 | 5              |                           |                    |                     |  |
| 4  |                           | 13 | 4              |                           |                    |                     |  |
| 5  | W.S.W.                    | 3  | 5              | N.W.                      | $2\frac{1}{4}$     | $9\frac{1}{2}$ ° W. |  |
| 6  |                           | 4  | 0              |                           |                    |                     |  |
| 7  |                           | 4  | 1              |                           |                    |                     |  |
| 8  |                           | 3  | 8              |                           |                    |                     |  |
| 9  | E. by N.                  | 12 | 2              | N. by E.                  | $\frac{1}{2}$      | 11° E.              |  |
| 10 |                           | 12 | 4              |                           |                    |                     |  |
| 11 |                           | 12 | 6              |                           |                    |                     |  |
| 12 |                           | 12 | 8              |                           |                    |                     |  |
| 1  | N. by W. $\frac{1}{2}$ W. | 2  | 4              | N.E. $\frac{1}{2}$ E.     | 3                  | 4° W.               | Variation 14° East.  |
| 2  |                           | 2  | 3              |                           |                    |                     |  |
| 3  |                           | 2  | 3              |                           |                    |                     |  |
| 4  |                           | 2  | 0              |                           |                    |                     |  |
| 5  | S. $\frac{3}{4}$ W.       | 6  | 9              | W. by S.                  | $\frac{1}{4}$      | 2° W.               | A current set by compass E.N.E., 42 miles, from the time the departure was taken to the end of the day.  |
| 6  |                           | 6  | 8              |                           |                    |                     |  |
| 7  |                           | 6  | 8              |                           |                    |                     |  |
| 8  |                           | 7  | 5              |                           |                    |                     |  |
| 9  | E. by N. $\frac{1}{2}$ N. | 11 | 5              | N. by E. $\frac{1}{2}$ E. | $\frac{3}{4}$      | 8° E.               |  |
| 10 |                           | 12 | 2              |                           |                    |                     |  |
| 11 |                           | 11 | 6              |                           |                    |                     |  |
| 12 |                           | 11 | 7              |                           |                    |                     |  |

4. 1876, September 23rd, in longitude  $57^{\circ}45'$  E., observed meridian altitude of sun's L.L.,  $84^{\circ}10'50''$ , bearing North, index correction —  $1'36''$ , height of eye 16 feet: required the latitude.

5. In latitude  $52^{\circ}$  S., longitude  $0^{\circ}40'$  W., a ship sails 136 miles due East: required the longitude in.

6. Required the course and distance from A to B.

Latitude of A  $5^{\circ}21'$  N.

Longitude of A  $163^{\circ}1'$  E.

Latitude of B  $36^{\circ}50'$  S.

Longitude of B  $73^{\circ}6'$  W.

ADDITIONAL FOR ONLY MATE.

7. 1875, December 12th: find A.M. and P.M. tides at Aberdeen Bar, Penzance, King's Road (Bristol Channel), and Southampton.

8. 1876, November 5th, at  $5^h10^m$  P.M. apparent time at ship, in latitude  $20^{\circ}45'$  N., longitude  $116^{\circ}45'$  E., sun's magnetic amplitude was S.W.  $\frac{3}{4}$  W.: required the error of compass; and supposing the variation to be  $1^{\circ}$  E.: required the deviation of the compass for the position of the ship's head at the time of observation.

9. 1876, August 5th, A.M. at ship, latitude at noon  $30^{\circ}30'$  N., observed altitude sun's L.L.  $35^{\circ}6'$ , height of eye 16 feet, time by chron.  $8^h39^m22^s$  P.M., which was *fast*  $29^m32^s.4$  on Greenwich mean noon, July 8th, and on July 20th, was *fast*  $30^m0^s$  on Greenwich mean noon; course till noon West (true) 48 miles: required the longitude in at noon.

## ADDITIONAL FOR FIRST MATE.

10. 1876, August 13th, mean time at ship 9<sup>h</sup> 5<sup>m</sup> 20<sup>s</sup> A.M., latitude 30° 46' S., longitude 78° 50' W., sun's bearing by compass N. 25° E., observed altitude sun's L.L. 27° 12', index correction + 1' 45", height of eye 21 feet: required the true azimuth and error of compass; and supposing the variation to be 16° 20' E.: required the deviation of the compass for the position of the ship's head at the time of observation.

11. 1876, June 12th, P.M. at ship, latitude account 15° 50' S., longitude 72° 12' E., observed altitude of sun's L.L., 50° 10' 10", zenith South of observer, index correction — 5' 40", height of eye 26 feet, time by watch 28<sup>m</sup> 40<sup>s</sup> (or 12<sup>d</sup> 0<sup>h</sup> 28<sup>m</sup> 40<sup>s</sup>), which had been found to be slow 4<sup>m</sup> 44<sup>s</sup> on apparent time at ship, the difference of longitude made to West was 16½', after the error on apparent time was determined: required the latitude.

## ADDITIONAL FOR MASTER ORDINARY.

12. 1876, December 7th, the observed meridian altitude of the star  $\alpha$  Arietis was 60° 29' 50", zenith North of star, index correction — 2' 10", height of eye 18 feet: required the latitude.

In the following table give the correct magnetic bearing of the distant object, and thence the deviation.

Correct magnetic bearing.

| Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. |
|----------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North ....                       | S. 2° W.                                       |                     | South ....                       | S. 35° E.                                      |                     |
| N.E. ....                        | S. 10° E.                                      |                     | S.W. ....                        | S. 30° E.                                      |                     |
| East .....                       | S. 23° E.                                      |                     | West ....                        | S. 20° E.                                      |                     |
| S.E. ....                        | S. 34° E.                                      |                     | N.W. ....                        | S. 10° E.                                      |                     |

With the deviation as above, give the courses you would steer by the Standard Compass, to make the following courses correct magnetic.

Correct magnetic courses:—N.W. ½ N.; S.W. by S. ½ S.; N.N.E.; N. ½ W.

Compass courses:—

Supposing you have steered the following courses by the Standard Compass, find the correct magnetic courses made from the above deviation table.

Compass courses:—S. ¾ W.; S.E. ¾ E.; W.S.W.; S. by E. ½ E.

Magnetic courses:—

You have taken the following bearings of two distant objects by your Standard Compass as above, with the ship's head at N. ½ E., find the bearings, correct magnetic.

Compass bearings:—W. by N. and N.W. ¼ W.

Bearings, magnetic:—

## EXAMINATION PAPER—No. XVIII.

## FOR SECOND MATE.

1. Multiply 7642 by 74295, and 0.00064 by 10.0004, by common logarithms.
2. Divide .39765 by 25, and 1000000 by .0000001, by common logarithms.

3.—

| H. | COURSES.                | K. | $\frac{1}{10}$ | WINDS.                | LEE-WAY.               | DEVIATION.                 | REMARKS, &c.  |
|----|-------------------------|----|----------------|-----------------------|------------------------|----------------------------|---|
| 1  | N. by W.                | 6  | 4              | W. by N.              | pts.<br>$1\frac{1}{2}$ | $8^{\circ}$ W.             | A point, lat. $57^{\circ} 0'$ N. long. $40^{\circ} 0'$ W., bearing by compass N.E. by E. $\frac{1}{4}$ E. dist. 19 miles. (Ship's head N. 6 W.) Deviation as per log. |
| 2  |                         | 6  | 3              |                       |                        |                            |   |
| 3  |                         | 5  | 6              |                       |                        |                            |   |
| 4  |                         | 5  | 4              |                       |                        |                            |   |
| 5  | S.S.W. $\frac{3}{4}$ W. | 4  | 8              | W. $\frac{1}{2}$ N.   | $2\frac{1}{4}$         | $5^{\circ}$ W.             |   |
| 6  |                         | 4  | 2              |                       |                        |                            |   |
| 7  |                         | 3  | 7              |                       |                        |                            |   |
| 8  |                         | 3  | 6              |                       |                        |                            |   |
| 9  | N.N.E. $\frac{3}{4}$ E. | 4  | 2              | N.W. $\frac{3}{4}$ N. | 2                      | $13^{\circ}$ E.            | Variation $48^{\circ}$ W.   |
| 10 |                         | 4  | 4              |                       |                        |                            |   |
| 11 |                         | 4  | 5              |                       |                        |                            |   |
| 12 |                         | 4  | 5              |                       |                        |                            |   |
| 1  | W. by N.                | 3  | 4              | N. by W.              | $2\frac{1}{2}$         | $17\frac{1}{2}^{\circ}$ W. |   |
| 2  |                         | 3  | 4              |                       |                        |                            |   |
| 3  |                         | 3  | 6              |                       |                        |                            |   |
| 4  |                         | 3  | 7              |                       |                        |                            |   |
| 5  | S.E. $\frac{3}{4}$ E.   | 9  | 8              | S.S.W.                | $\frac{1}{4}$          | $11^{\circ}$ E.            | A current set correct magnetic W.N.W. for the last 5 hours, 3 miles an hour.  |
| 6  |                         | 10 | 5              |                       |                        |                            |   |
| 7  |                         | 11 | 2              |                       |                        |                            |   |
| 8  |                         | 10 | 8              |                       |                        |                            |   |
| 9  | S. $\frac{1}{2}$ W.     | 3  | 2              | W.S.W.                | $2\frac{3}{4}$         | $2^{\circ}$ W.             |   |
| 10 |                         | 3  | 3              |                       |                        |                            |   |
| 11 |                         | 2  | 8              |                       |                        |                            |   |
| 12 |                         | 2  | 7              |                       |                        |                            |   |

4. 1876, June 25th, in longitude  $59^{\circ} 15'$  E., the observed meridian altitude of sun's u.l. bearing North, was  $60^{\circ} 23' 15''$ , index correction  $+ 2' 21''$ , height of eye 30 feet: required the latitude.

5. A ship sailed due West 120 miles from Cape Roca, in latitude  $38^{\circ} 46'$  N., and longitude  $9^{\circ} 30'$  W.: required the longitude of the ship.

6. Required the compass course and distance from Cape East, New Zealand, to San Francisco. Variation  $14^{\circ} 20'$  E., and deviation  $5^{\circ} 40'$  E.

Latitude Cape East  $37^{\circ} 40'$  S. Longitude Cape East  $178^{\circ} 36'$  E.

Latitude San Francisco  $37^{\circ} 48.5'$  N. Longitude San Francisco  $122^{\circ} 24'$  W.

# ADDITIONAL FOR ONLY MATE.

7. 1875, August 7th: find times of high water A.M. and P.M. at Hong Kong, long.  $114^{\circ}$  E., New York (Sandy Hook), long.  $74^{\circ}$  W., and Skull.

8. 1876, June 24th, at 6<sup>h</sup> A.M. apparent time at ship, latitude  $0^{\circ}$  N., longitude  $120^{\circ} 3'$  W., sun at setting bore by compass S.E. by E.  $\frac{1}{4}$  E., variation by chart was  $21^{\circ} 40'$  W.: required the error of compass and the deviation.

9. 1876, September 22nd, A.M. at ship, on the Equator, observed altitude sun's u.l.  $17^{\circ} 20' 40''$ , index correction  $- 1' 18''$ , height of eye 20 feet, time by chronometer September 22<sup>d</sup> 4<sup>h</sup> 59<sup>m</sup> 16<sup>s</sup>, which was *slow*  $15^s$  for Greenwich mean noon, April 30th, and on June 1st was *fast*  $10^m 6^s$  for mean time at Greenwich: required the longitude.

## ADDITIONAL FOR FIRST MATE.

10. 1876, March 21st, mean time at ship 3<sup>h</sup> 15<sup>m</sup> P.M., latitude 9° 7' S., longitude 159° 4' W., sun's bearing by compass W.  $\frac{1}{2}$  S., the observed altitude sun's L.L. 42° 49' 45", index correction — 3' 14", height of eye 21 feet, variation by chart 7° 50' E.: required the error of the compass and deviation.

11. 1876, October 4th, A.M. at ship, latitude account 30° 24' S., longitude 140° 30' E., observed altitude sun's L.L. North of observer was 63° 37' 10", index corr. — 1' 15", height of eye 21 feet, time by watch October 3<sup>d</sup> 22<sup>h</sup> 37<sup>m</sup> 15<sup>s</sup>, which had been found to be 1<sup>h</sup> 10<sup>m</sup> 20<sup>s</sup> slow on apparent time at ship, the difference of longitude made to East was 23 $\frac{1}{2}$  miles after the error on apparent time was determined: required the latitude.

## ADDITIONAL FOR MASTER ORDINARY.

12. 1876, June 10th, longitude 25° W., the observed meridian altitude of the star  $\alpha$  Cassiopeæ, bearing South, was 85° 0' 20", index correction + 34", height of eye 18 feet: required the latitude.

In the following table give the correct magnetic bearing of the distant object, and thence the deviation:—

Correct magnetic bearing.

| Ship Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. | Ship's Head by Standard Compass. | Bearing of Distant Object by Standard Compass. | Deviation Required. |
|--------------------------------|--|---------------------|----------------------------------|--|---------------------|
| North. ....                    | N. 18° W.                                      |                     | South ....                       | N. 2° W.                                       |                     |
| N.E. ....                      | N. 17 W.                                       |                     | S.W. ....                        | N. 1 E.  |                     |
| East. ....                     | N. 13 W.                                       |                     | West ....                        | N. 1 W.  |                     |
| S.E. ....                      | N. 8 W.  |                     | N.W. ....                        | N. 6 W.  |                     |

With the deviation as above, give the courses you would steer by the Standard Compass to make the following courses correct magnetic.

Correct magnetic courses:—W.S.W.; N.E. by E.; S. by E.; W.  $\frac{1}{2}$  S.

Compass courses:—

Supposing you have steered the following courses by the Standard Compass, find the correct magnetic courses made from the above deviation table.

Compass Courses:—S.W.  $\frac{1}{2}$  W.; S.  $\frac{1}{2}$  W.; E.  $\frac{1}{4}$  N.; E.S.E.

Correct magnetic courses:—

You have taken the following bearing of two distant objects by your Standard Compass as above, with the ship's head at N.E.  $\frac{1}{2}$  E., find the bearings, correct magnetic.

Compass bearings:—W.  $\frac{1}{4}$  S. and N.E. by E.

Bearings, magnetic:—

## EXAMINATION PAPER.—No. XIX.

## FOR SECOND MATE.

1. Multiply 6054 by 912, and 2070.5 by 62.0898, by common logarithms.
2. Divide 117.658 by 146.932, and 167342 by .002, by common logarithms.

3.—

| H. | COURSES.              | K. | $\frac{1}{10}$ | WINDS.   | LEE-WAY.               | DEVIATION. | REMARKS, &c.  |
|----|-----------------------|----|----------------|----------|------------------------|------------|---|
| 1  | S. $\frac{1}{2}$ W.   | 4  | 5              | W. by S. | pts.<br>$2\frac{1}{4}$ | 5° E.      | A point, lat. 62° 20' N.<br>long. 64° 40' W., bearing by compass<br>W. by N. $\frac{1}{2}$ N.,<br>dist. 21 miles. (Ship's head S. $\frac{1}{2}$ W.) Deviation as per log. |
| 2  |                       | 4  | 2              |          |                        |            |   |
| 3  |                       | 4  |                |          |                        |            |   |
| 4  |                       | 3  | 9              |          |                        |            |   |
| 5  | S.W. $\frac{3}{4}$ W. | 3  | 5              | S. by E. | $3\frac{1}{2}$         | 9° W.      |   |
| 6  |                       | 3  | 4              |          |                        |            |   |
| 7  |                       | 3  | 2              |          |                        |            |   |
| 8  |                       | 3  | 3              |          |                        |            |   |
| 9  | E. $\frac{3}{4}$ S.   | 5  | 4              | S. by E. | $1\frac{3}{4}$         | 15° E.     |   |
| 10 |                       | 5  | 3              |          |                        |            |   |
| 11 |                       | 4  | 4              |          |                        |            |   |
| 12 |                       | 4  | 2              |          |                        |            |   |
| 1  | W.N.W.                | 3  | 6              | North.   | 3                      | 19° W.     | Variation 59° West.   |
| 2  |                       | 4  | 5              |          |                        |            |   |
| 3  |                       | 5  | 3              |          |                        |            |   |
| 4  |                       | 5  | 7              |          |                        |            |   |
| 5  | N.W. $\frac{1}{2}$ N. | 10 | 2              | E.N.E.   | 0                      | 17° W.     |   |
| 6  |                       | 11 | 4              |          |                        |            |   |
| 7  |                       | 12 | 6              |          |                        |            |   |
| 8  |                       | 13 | 4              |          |                        |            |   |
| 9  | E. $\frac{3}{4}$ N.   | 5  | 5              | N. by E. | $3\frac{1}{4}$         | 18° E.     |   |
| 10 |                       | 5  | 4              |          |                        |            |   |
| 11 |                       | 5  | 4              |          |                        |            |   |
| 12 |                       | 5  |                |          |                        |            |   |

4. 1876, June 1st, in longitude 44° 40' E., observed meridian altitude of sun's L.L. was 72° 14' 10", zenith North of sun, index correction + 3' 45", height of eye 22 feet: required the latitude.

5. In latitude 32° 3' S., longitude 179° 45' W., a ship makes 54 miles West, then 80 miles North: what is the longitude in, also find the compass course and distance; variation 18° E.; 1st deviation 4° 5' E.; 2nd deviation 3° 10' W.

6. Required the course and distance from Cape Lopatka to Callao.

Lat. Cape Lopatka 50° 33' N.

Long. Cape Lopatka 156° 46' E.

Lat. Callao 12 4 S.

Long. Callao 77 14 W.

# ADDITIONAL FOR ONLY MATE.

7. 1875, May 4th: find the A.M. and P.M. tides at Aberdeen, Wick, Fécamp.

8. 1876, December 28th, at 4<sup>h</sup> 35<sup>m</sup> A.M., apparent time at ship, latitude 40° 10' S., longitude 75° E., sun rose by compass South: required error of the compass; and supposing the variation to be 19° 10' W.: required the deviation of the compass for the position of the ship's head when the observation was taken.

9. 1876, January 29th, P.M. at ship, latitude at noon 28° 45' N., observed altitude sun's L.L. 17° 46' 30", index correction — 3' 25", height of eye 16 feet, time by a chronometer, Jan. 28<sup>d</sup> 16<sup>h</sup> 31<sup>m</sup> 30", which was 1<sup>m</sup> 16<sup>s</sup> 5 fast for mean time at Greenwich, December 17th, 1875, and on January 1st, 1876, was 1<sup>m</sup> 3<sup>s</sup> slow for mean time at Greenwich; course since noon N.W. by W. (true), distance 20 miles: required the longitude at the time of observation, and also at noon.

## ADDITIONAL FOR FIRST MATE.

10. 1876, July 10th, mean time at ship  $3^h 14^m 2^s$  P.M., latitude  $38^\circ 2' S.$ , longitude  $140^\circ 58' E.$ , sun's bearing by compass  $N. 2^\circ 15' E.$ , observed altitude sun's  $U.L. 14^\circ 56' 30''$ , index correction  $+ 3' 30''$ , height of eye 19 feet, variation by chart  $6^\circ 45' E.$ : required the deviation of the compass for the position of the ship's head.

11. 1876, November 29th, P.M. at ship, latitude account  $6^\circ 20' S.$ , longitude  $123^\circ 25' E.$ , observed altitude of sun's  $L.L. 74^\circ$ , index correction  $+ 4' 0''$ , eye 19 feet, time by watch November  $28^d 22^h 46^m$ , which had been found to be  $1^h 27^m$  slow on apparent time at ship, the difference of longitude made to the *West* was 12.3 miles after the error on apparent time was determined: required the latitude.

## ADDITIONAL FOR MASTER ORDINARY.

12. 1876, May 15th, the observed meridian altitude of star  $\beta$  Orionis  $52^\circ 20' 30''$ , zenith North of star, index correction  $- 4' 10''$ , height of eye 15 feet: required the latitude.

13. 1876, September 4th, what bright stars in the *Nautical Almanac* will pass the meridian of a place in longitude  $54^\circ 40' E.$ , between the hours of seven and ten.

14. 1876, June 15th, observed meridian altitude of  $\eta$  Argus, under the South pole, was  $47^\circ 50' 30''$ , index correction  $+ 3' 20''$ , height of eye 20 feet: required the latitude.

In the following table give the correct magnetic bearing of the distant object, and thence the deviation:—

Correct magnetic bearing.

| Ship's head<br>by Standard<br>Compass. | Bearing of<br>Distant Object<br>by Standard<br>Compass. | Deviation<br>required. | Ship's head<br>by Standard<br>Compass. | Bearing of<br>Distant Object<br>by Standard<br>Compass. | Deviation<br>required. |
|--|---|------------------------|--|---|------------------------|
| North .....                            | S. $23^\circ$ E.  |                        | South. ....                            | S. $6^\circ$ W.   |                        |
| N.E. ....                              | S. $11^\circ$ E.  |                        | S.W. ....                              | S. $18^\circ$ E.  |                        |
| East. ....                             | S. $5^\circ$ W.   |                        | West. ....                             | S. $21^\circ$ E.  |                        |
| S.E. ....                              | S. $20^\circ$ W.  |                        | N.W. ....                              | S. $22^\circ$ E.  |                        |

With the deviation as above, give the courses you would steer by the Standard Compass to make the following courses correct magnetic.

Correct magnetic courses:—S.  $\frac{1}{2}$  W.; E. by N.; S.E. by S.; W. by N.

Compass courses:—

Supposing you have steered the following courses by the Standard Compass, find the correct magnetic courses made, from the above deviation table.

Compass courses:—N.W. by N.; W.N.W.; S.E. by E.; N.N.E.

Magnetic courses:—

You have taken the following bearings of two distant objects by your Standard Compass as above; with the ship's head at S.E. by S., find the bearings, correct magnetic.

Compass bearings:—N.  $84^\circ$  W. and N.W. by W.  $\frac{1}{2}$  W.

Bearings, magnetic:—

## EXAMINATION PAPER.—No. XX.

## FOR SECOND MATE.

1. Multiply 6893 by 11300, and .0001468 by .000395, by common logarithms.
2. Divide 7122 by 8.9596, and 268430 by .003010, by common logarithms.

3.—

| H. | COURSES.                  | K. | $\frac{1}{10}$ | WINDS.                      | LEE-WAY.           | DEVIATION.           | REMARKS, &c.   |
|----|---------------------------|----|----------------|-----------------------------|--------------------|----------------------|--|
| 1  | S.E. $\frac{1}{4}$ E.     | 13 | 7              | N.E. by E. $\frac{1}{2}$ E. | pts. $\frac{1}{4}$ | 11° E.               | A point, lat. 59° 49' N. long. 44° 10' W., bearing by compass N.W. $\frac{1}{4}$ W., dist. 30 miles. (Ship's head S.E. $\frac{1}{4}$ E.) Deviation as per log. |
| 2  |                           | 14 |                |                             |                    |                      |  |
| 3  |                           | 13 | 2              |                             |                    |                      |  |
| 4  | E. $\frac{1}{2}$ S.       | 13 | 3              | S. by E. $\frac{1}{2}$ E.   | $\frac{3}{4}$      | 14° E.               |  |
| 5  |                           | 10 | 4              |                             |                    |                      |  |
| 6  |                           | 10 | 4              |                             |                    |                      |  |
| 7  |                           | 10 | 5              |                             |                    |                      |  |
| 8  |                           | 10 | 3              |                             |                    |                      |  |
| 9  | N. by W. $\frac{1}{2}$ W. | 4  | 6              | N.E. $\frac{1}{2}$ E.       | 2 $\frac{1}{4}$    | 8 $\frac{1}{2}$ ° W. |  |
| 10 |                           | 3  | 4              |                             |                    |                      | Variation 53 $\frac{1}{2}$ ° W.  |
| 11 |                           | 3  | 4              |                             |                    |                      |  |
| 12 | S.S.W. $\frac{1}{2}$ W.   | 3  | 6              | S.E. $\frac{1}{2}$ S.       | $\frac{1}{2}$      | 2 $\frac{1}{2}$ ° W. |  |
| 1  |                           | 11 | 7              |                             |                    |                      |  |
| 2  |                           | 11 | 8              |                             |                    |                      |  |
| 3  |                           | 11 | 8              |                             |                    |                      |  |
| 4  | N.E. $\frac{1}{4}$ N.     | 11 | 4              | E. by S. $\frac{1}{2}$ S.   | 1                  | 14° E.               |  |
| 5  |                           | 7  | 2              |                             |                    |                      |  |
| 6  |                           | 7  | 3              |                             |                    |                      | A current set by compass S.E. $\frac{1}{4}$ E. 1.7 knots per hour from the time the departure was taken to the end of day.                                     |
| 7  |                           | 7  | 4              |                             |                    |                      |  |
| 8  |                           | 7  | 2              |                             |                    |                      |  |
| 9  | S. $\frac{1}{4}$ E.       | 12 | 5              | E.S.E.                      | $\frac{1}{4}$      | 3° E.                |  |
| 10 |                           | 12 |                |                             |                    |                      |  |
| 11 |                           | 12 | 3              |                             |                    |                      |  |
| 12 |                           | 12 | 4              |                             |                    |                      |  |

4. 1876, October 1st, longitude 84° 40' E., the observed meridian altitude of sun's u.L., zenith North, was 57° 20' 30", index correction — 3' 36", height of eye 17 feet: required the latitude.

4.\* 1876, July 2nd, in longitude 45° 15' E., observed meridian altitude of the sun's L.L., below the pole, was 10° 19' 45", index correction — 1' 15", height of eye 12 feet: required the latitude.

5. A ship from latitude 35° 30' S., longitude 27° 28' W., sailing due East (true) 301 miles: required the compass course steered, and what will be the longitude in, variation 1  $\frac{3}{4}$  point E., and deviation 8° 50' E.

6. Required the course and distance from A to B.

Latitude of A 10° 8' S. Longitude of A 175° 18' E.

Latitude of B 23 12 N. Longitude of B 141 15 E.

Variation  $\frac{1}{2}$  point West, and deviation 7° 15' West.

# ADDITIONAL FOR ONLY MATE.

7. 1875, March 18th: find the times of high water, A.M. and P.M., at Cadiz, Southampton, Angra l'equena (S.W. coast of Africa), longitude 15° E.

8. 1876, April 25th, at 7<sup>h</sup> 22<sup>m</sup> 8<sup>s</sup> P.M. apparent time at ship, latitude 57° 18' S., longitude 101° 50' E., sun's setting by compass N.  $\frac{1}{4}$  E., variation by chart 35° 50' W.: required the error of the compass and deviation.

9. 1876, August 24th, A.M. at ship, latitude at noon 37° 59' N., observed altitude sun's L.L. 37° 13' 30", index corr. + 2' 40", eye 18 feet, time by chronometer, August 24<sup>d</sup> 6<sup>h</sup> 13<sup>m</sup> 24<sup>s</sup>, A.M. at Greenwich, which was 1<sup>m</sup> 5<sup>s</sup> fast for mean noon at Greenwich, August 1st, and on August 10th was 0<sup>m</sup> 42<sup>s</sup> slow for mean time at Greenwich, course since observation N.N.W., 22° 4' (true): required the longitude at noon.

## ADDITIONAL FOR FIRST MATE.

10. 1876, November 1st, mean time at ship, 8<sup>h</sup> 40<sup>m</sup> A.M., latitude 50° 21' N., longitude 23° 56' W., sun's bearing by compass S.  $\frac{1}{4}$  W., observed altitude sun's L.L. 12° 19', index corr. — 3' 20", eye 21 feet: required the error of the compass; and supposing the variation to be 33° 20' W.: required the deviation for the position of the ship's head at the time of observation.

11. 1876, May 29th, A.M. at ship, latitude account 0° 31' S., longitude 150° 40' W., observed altitude sun's L.L. 67° 41' N., index correction + 1', height of eye 20 feet, time by watch May 29<sup>d</sup> 3<sup>h</sup> 32<sup>m</sup>, *fast* on apparent time at ship 3<sup>h</sup> 38<sup>m</sup>, the difference of longitude made to *East* was 26.9 miles, after the error on apparent time was determined: required the latitude by reduction to meridian.

## ADDITIONAL FOR MASTER ORDINARY.

12. 1876, June 17th, the longitude 98° W., observed meridian altitude of  $\alpha$  Serpentis, zenith South of object, was 29° 0' 40", index correction + 4' 20", height of eye 24 feet: required the latitude.

13. 1876, June 15th, at what time will  $\alpha$  Serpentis pass the meridian of a place in latitude 37° N. and longitude 15° 30' E.; what distance N. or S. of the Zenith?

14. 1876, May 18th, observed meridian altitude of  $\eta$  Draconis under the North Pole was 34° 56' 15", index correction — 5' 45", height of eye 22 feet: required the latitude.

15. At the Cape of Good Hope the variation is about 28° W., if the sun at noon bears due North by compass, what is the deviation?

In the following table give the correct magnetic bearing of the distant object and thence the deviation.

Correct magnetic bearing.

| Ship's Head<br>by Standard<br>Compass. | Bearing of<br>Distant Object<br>by Standard<br>Compass. | Deviation<br>Required. | Ship's Head<br>by Standard<br>Compass. | Bearing of<br>Distant Object<br>by Standard<br>Compass. | Deviation<br>Required. |
|--|---|------------------------|--|---|------------------------|
| North ....                             | S. 29° E.   |                        | South ....                             | S. 69° E.   |                        |
| N.E. ....                              | S. 33 E.  |                        | S.W. ....                              | S. 64 E.  |                        |
| East .....                             | S. 47 E.  |                        | West ....                              | S. 48 E.  |                        |
| S.E. ....                              | S. 63 E.  |                        | N.W. ....                              | S. 38 E.  |                        |

With the deviation as above, give the courses you would steer by the Standard Compass to make the following courses correct magnetic.

Correct magnetic courses:—S.W.  $\frac{1}{2}$  W.; S.S.E.  $\frac{1}{2}$  E.; W. by N.  $\frac{1}{4}$  N.; N.  $\frac{1}{2}$  E.

Compass courses:—

Supposing you have steered the following courses by the Standard Compass, find the correct magnetic courses made from the above deviation table.

Compass courses:—N.E. by N.  $\frac{1}{2}$  N.; S.W. by W.  $\frac{3}{4}$  W.; S.  $\frac{1}{4}$  E.; S.W.

Correct magnetic courses:—

You have taken the following bearings of two distant objects by your Standard Compass as above; with the ship's head at N.N.E., find the bearings, correct magnetic.

Compass bearings:—S. by W. and W. by N.  $\frac{1}{2}$  N.

Bearings, magnetic:—



## QUADRANT AND SEXTANT.

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307. The **Quadrant** and **Sextant**\* are reflecting astronomical instruments for measuring angles, and are the instruments chiefly in use for taking the observations required for the solution of a number of the most useful problems in navigation, such as to find the time, the latitude and longitude of a place. The **Quadrant** contains an arc of  $45^\circ$  in real extent, and measures a few degrees more than  $90^\circ$ ;† it is usually of wood, and the graduated arc, which is ivory, reads to minutes, and sometimes to  $30''$ . The **Sextant** is constructed on the same principles as the Quadrant; has a graduated limb of more than  $60^\circ$  in real extent; and furnishes the means of measuring the angle between two objects in whatever direction they may be placed, so that the angle does not exceed  $140^\circ$ . The quadrant serves for common purposes at sea; but the sextant is used when considerable precision is required, as, for instance, in taking a lunar observation.

308. The form of a sextant, as at present in common use, consists of a single frame of brass, so constructed as to combine strength with lightness; and in others a double frame connected by pillars; the graduated arc, inlaid in the brass, is usually of silver, sometimes of gold, or platinum. The explanation of the parts of a sextant, and of the adjustments of that instrument, will answer for the quadrant, since the parts and appendages are common to both.

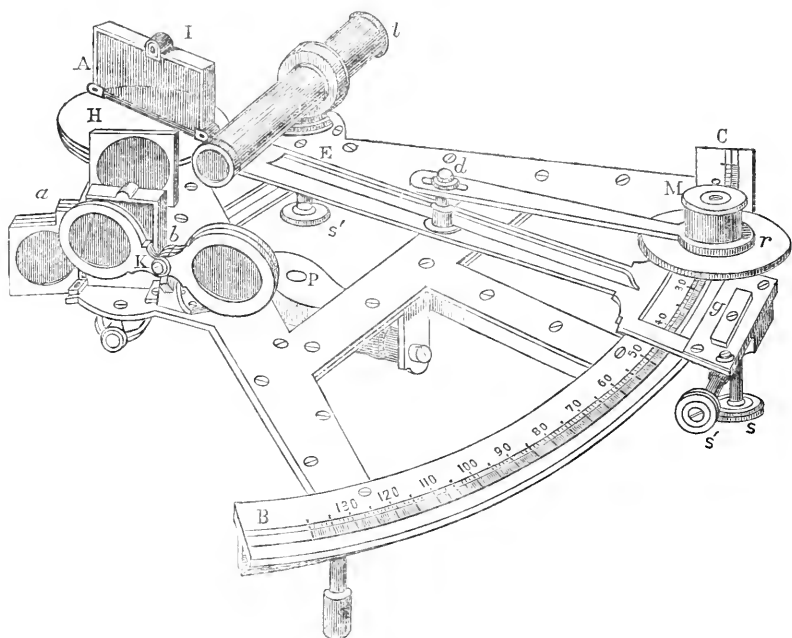
309. The flat surface of the sextant is called the *plane of the sextant*; the circular part B C is the arc or limb, which is graduated from the zero point  $0^\circ$  to about  $140^\circ$ , and each degree in the best instruments is again sub-divided into six equal parts of  $10'$  each, while the vernier *g* used in estimating the sub-divisions of the arc shows  $10''$ . The divisions are also continued a short distance in the opposite direction on the other side of zero ( $0$ ), towards C, forming what is termed the *arc of excess*, for the purpose of determining the index error in the manner that will be subsequently explained. The microscope M, and its reflector *r* secured at the point *d* by a moveable arm *dr* to the index bar A E, may be adjusted to read off the divisions on the graduated limb and the vernier *g*. The index bar A E is secured to the arc B C by the intervention of a mill-headed clamp screw *s* at its back, which must be loosened when the index has to be moved any considerable distance, and when

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\* The first *inventor* of the sextant (or quadrant) was NEWTON, among whose papers a description of such an instrument was found after his death; not, however, until after its re-invention by THOMAS GODFRAY of Philadelphia, in 1730, and, perhaps, by HADLEY, in 1731.

† This depends on the properties of light, which we cannot consider here.

the contact nearly has been made by hand, the screw is again to be fixed, and a tangent screw  $s'$  enables the index bar and the vernier\* upon it to be moved by a small quantity along the limb, so as to render the contact of the objects observed more perfect than could be effected by moving the index solely by hand; the other extremity of the index bar has a silvered glass or reflector  $I$  fixed perpendicular to the plane of the instrument and directly over the centre;



another glass  $b$  is fixed perpendicular to the plane of the instrument frame  $H$ , of which the lower half only is silvered and the upper transparent; it is usually provided with screws, by which its position with respect to the plane of the sextant may be rectified; the plane of this glass, usually termed the horizon-glass, is made parallel to the plane of index glass  $I$ , when the vernier  $g$  is adjusted to zero on the divided arc  $B C$ , or if not so made, the want of parallelism constitutes what is termed the index error of the instrument. The telescope  $t$  is carried by a ring fastened to a stem  $E$ , which can be raised or lowered by a mill-headed screw  $s''$  at the back of the frame, for the purpose of so placing the field of the telescope that it may be bisected by the line on the horizon-glass, separating the silvered from the unsilvered part, whereby the brightness of the reflected object and that seen by direct vision may be made equal, and the quality of the observations improved; the ring and its elevating apparatus are technically known as an "up-and-down piece." It is usual to supply a direct and inverting telescope, of which the latter is to

\* **VERNIER**—so called after its inventor, PETER VERNIER, of France, who lived about 1630. By some it is called a *nonius*, after the Portuguese, NUNEN or NONIUS; but the invention of the latter (who died in 1577) was quite different.

be preferred, as possessing greater magnifying power, and thus showing a better contact of the images of the objects. Two wires parallel to each other, and to the plane of the instrument, are placed in the inverting telescope, within which limit the observation should be made. In the quadrant the telescope is omitted, and the eye is applied to a small circular orifice in a piece of brass, placed in the same position as the telescope in the drawing.

Dark glasses of different colours and shades are a necessary accompaniment to the sextant to enable the sun to be observed, and they are usually attached to a hinged joint at K. Four of these glasses or shades are placed at *a*, between the index and horizon-glasses, so as to admit of one or more of them being interposed between the index and horizon-glass, to moderate the light of any brilliant object seen by reflection. Three more such glasses, sometimes called back shades, are placed behind the horizon-glass at K, any one or more of which can also be turned down to moderate the intensity of the light before meeting the eye, when observing a bright object, such as the sun. There is also a dark glass which can be placed at the eye-end *t* of the telescope, which method is preferable to the other, as no error in this is liable to be introduced in the passage of the rays from the index to the horizon-glass.\*

When observing, the instrument is to be held with one hand by the handle P placed at the back of the frame, while the other hand moves the index.

310. **Reading off the Angle.**—The following brief directions for reading off will be more readily understood by the learner, if he place a sextant before him for reference and examination.

It will be seen that the arc is divided into degrees from  $0^{\circ}$  to about  $140^{\circ}$ ; every 10th degree is numbered from 0 to  $140^{\circ}$ ; the space between every  $10^{\circ}$  is divided into 10 equal parts by straight lines; consequently, every part is  $1^{\circ}$ ; every fifth line is made a little longer than the others, to represent every fifth degree; and (in the best instruments) every degree is sub-divided into six equal parts by lines shorter than those which represent the degrees; those short lines divide every degree into sixths of a degree, or  $10'$ . We will suppose it is an instrument of this kind before the learner. The *index*, up to which an arc is read off, is a line cut in a plate at the end of the moveable radius, and is generally distinguished from the other line on the plate by a diamond-shaped mark, resembling a spear-head. Supposing this index to stand exactly at any of the lines on the arc, that is, so that the two lines are in the same direction; in such a case the reading off is easily known, for it must be a certain number of divisions and sub-divisions, of which the value is seen at once. Thus, if it coincide, for example, with the second line to the left of  $40^{\circ}$ , then the reading off will be  $40^{\circ} 20'$ , since each line on the arc represents  $10'$ .

\* With respect to the dark glasses, when it is possible (as in observing altitudes of the sun in the mercurial horizon, &c.) to make the observation with a single dark glass on the eye-end of the telescope, without using any shade, this should always be done, for the error of this dark glass does not affect the contact at all, and the distortion caused by it is not magnified, whereas any fault in the dark shade between the index and horizon-glasses produces actual error in the observation, and the distortion is magnified subsequently by the telescope.

But suppose the index not to stand exactly at any line whatever on the arc, but somewhere between two, as in the above example, between the second and third line from  $40^\circ$ , suppose it appeared to be about half-way between the second and third lines (the learner may place it in that position). But as this is a rough and imperfect way of estimating the additional minutes and seconds beyond the second division from  $40^\circ$ , the exact value of this small space is known by means of a few divisions on the index plate to the left of the index, and called the *vernier*. These divisions are made less than the arc divisions, so that the line on the plate immediately to the left of the index is somewhat nearer to the corresponding one on the arc than the small space to be determined. It is nearer thereto, as is manifest by difference of a division on the arc and one on the index plate. In like manner the second line, reckoning from the index, must be nearer to the corresponding line by two differences, the third by three, and so on. At length, therefore, there must be a coincidence of two lines, or nearly so, that is, they must appear to an eye placed directly over them to lie in the same direction, or nearly so. And since, upon the whole, the lines on the vernier have approached those upon the arc through the small part the index is in advance of  $20'$ , this excess must be equal to as many times the difference of two divisions, as there are lines, reckoning from the index, before this coincidence takes place. Hence, if we know the value of a difference, we shall know the value of the small arc to be measured.

This difference is known as follows: By examining the arc of the sextant before us, it will be seen that 60 divisions of the vernier just cover or coincide with 59 divisions on the arc, or the difference between a division on the arc and one on the vernier is  $\frac{1}{60}$  of a division of the arc; if therefore a division on the arc is  $10'$ , the difference will be  $\frac{1}{60}$  of  $10'$  or  $10''$ . Every sixth division of the vernier being distinguished by a figure denoting minutes, and the interval between each of these figures is divided into six parts of  $10''$  each.

311. **To read off on a Sextant.**—First examine the divisions and subdivisions on the arc, up to the line which stands before the index. We then move the microscope on the vernier and examine the numbered lines. If any one of these coincides in direction with the opposite one on the arc, the reading off to be added will be so many minutes; if not, we observe between which numbered lines the coincidence actually takes place, and then reckon the preceding minutes as numbered, and afterwards the subdivisions of the vernier, as so many minutes or seconds. Let us now suppose the index to stand between the second and third divisions from  $40^\circ$ . In reading off, first  $40^\circ 20'$  is noted on the arc, and then running the microscope farther on the arc, it is observed that a line on the vernier and an arc line are in the same direction, between the lines on the vernier marked 5 and 6. The farther reading off is therefore  $5'$  and some seconds. On examining the interval between 5 and 6, which is divided into six equal parts, the fourth line to the left of 5 is found to be in the same direction with the opposite one on the arc. The remaining reading off is therefore  $40''$ . Hence the whole reading off is  $40^\circ 25' 40''$ .

The sextant supposed under examination is marked to read off to the nearest 10"; some instruments are graduated to 15" or 30", &c., but the same method of reading off is to be followed as pointed out above.

312. To read off on the arc of excess —As has been observed before, the graduation of the arc of the sextant is usually continued to the right of 0° or zero, in which case we have to read off an arc divided from left to right by means of an index which is divided from right to left; this, however, is easily done if we remember that the line on the vernier marked 10' must be considered as the commencement of the divisions, 9' must be considered as 1', 8' as 2', 7 as 3', &c.; or else take the difference between the minutes and seconds denoted by the vernier and 10'; thus if the coincidence of lines on the arc and vernier is at 7' 20", we must read this as 2' 40"; if at 5' 40" we must read this as 4' 20", and so on.

#### ADJUSTMENTS OF THE SEXTANT AND QUADRANT.

313. The *adjustments* of the sextant and quadrant are:—(1) *To set the index-glass and* (2) *the horizon-glass perpendicular to the plane of the instrument*; (3) *to adjust the line of collimation of the telescope, i.e., to set the axis of the telescope parallel to the plane of the instrument*; (4) *and to set the horizon-glass parallel with the index-glass, when 0 (zero) on the vernier coincides with 0 (zero) on the arc*; then, if the adjustments cannot be perfected, (5) *to find the index error of the instrument*:—

1st. The index-glass, or central mirror, must be perpendicular to the plane of the instrument.—Place the index to about the middle of the arc. Hold the sextant with its face up, the index-glass being placed near the eye, and the limb turned from the observer. Look obliquely down the glass; then, if the part of the arc to the right, viewed by direct vision, and its image in the mirror, appear as one *continued arc of a circle*, the adjustment is perfect; if the reflection seems to *droop* from the arc itself, the glass leans *back*; if it *rises upward*, the glass leans *forward*. The position is rectified by screws at the back.

2nd. The horizon-glass, or fixed mirror, must be perpendicular to the plane of the instrument.—(a) *By the sea horizon*.—Set 0 on the index to 0 on the arc; hold the instrument with its face up; direct the sight to the horizon-glass, give the instrument a small nodding motion; then if the horizon, as seen through the transparent part of the horizon-glass, and its image, as seen in the silvered part, appear to be in a *continued straight line*, the adjustment is perfect.

For this method of (a) testing there must be no index error, which caution is unnecessary when (b) the sun is used.

(b) *By the sun*.—The instrument being held perpendicular, look at the sun; sweep the index-glass along the limb, and if the reflected image pass exactly over the object itself, appearing neither to the right nor left of the object, then the horizon-glass is perpendicular to the plane of the instrument; if not, turn the adjusting screw, which in some instruments is a mill-headed one at the back of the instrument, while in others it is a small screw behind and near the upper part of the glass itself, which can be turned by placing a capstan-pin into the hole in the head of the screw.

3rd. The axis of the telescope must be parallel to the plane of the instrument.\*—Turn the eye-piece of the telescope till two of the parallel wires in its focus appear parallel to the plane of the instrument; then select two objects, as the sun and moon, whose angular distance must not be *less* than from  $100^{\circ}$  to  $120^{\circ}$ , because an error is more easily discovered when the distance is great; bring the reflected image of the sun exactly in contact with the direct image of the moon, at the wire nearest the plane of the sextant, and fix the index; then, by altering a little the position of the instrument, make the object appear on the other wire; if the contact still remains perfect, no adjustment is required; if they separate, *slacken* the screw *furthest* from the instrument in the ring which holds the telescope, and tighten the other, and *vice versa* if they overlap.

4th. The horizon-glass must be parallel to the index-glass.—Set  $\circ$  on the index to  $\circ$  on the arc; screw the tube or telescope into its socket, and turn the screw at the back of the instrument till the line which separates the transparent and silvered parts of the horizon-glass appears in the middle of the tube or telescope. Hold the sextant vertically—that is, with its arc or limb downwards—and direct the sight through the tube or telescope to the horizon; then if the reflected and true horizons do not coincide, turn the tangent screw at the back of the horizon-glass till they are made to appear in the same straight line. Then will the horizon-glass be truly parallel to the index-glass.†

314. Def.—Index Error of reflecting instruments such as the sextant, is the difference between the zero point of the graduated limb, and where the zero point ought to be as shown by the index when the index-glass is parallel to the horizon-glass.

5th. To find the Index Correction.—The two objects generally used to determine the index error are (a) the sea horizon, and (b) the sun.

(a) *By the horizon.*—Move the index till the horizon, or any distant object, coincides with its image, and the distance of  $\circ$  on the index from  $\circ$  on the limb is the index error; *subtractive* when  $\circ$  on the index is to the *left*, and *additive* when it is to the *right* of  $\circ$  on the limb.

*Example 1.*—The horizon and its image being made to coincide, the reading is  $2'$  on the arc. Then  $2'$  is the *Index Correction* to be *subtracted* from every angle observed.

*Example 2.*—When the horizon and its image were made to coincide, the reading was  $3' 20''$  off the arc; the index correction therefore was  $+ 3' 20''$ .

(2.) Or measure the sun's horizontal diameter, moving the index forward on the divisions until the images of the true and reflected suns touch at the edges; read off the measure which will be on the arc; then cause the images to change sides, by moving the index back; take the measure again and read off; this reading will be *off* the arc; half the difference of the two readings is the index correction.

\* The error caused by the imperfection of this adjustment is called the '*Error of Collimation*' and the observed angle is always too great.

† Some sextants, as Troughton's Pillar Sextants, are not provided with the means for making this adjustment; because it is not absolutely necessary. An allowance, called *Index Error*, being made for the want of parallelism of the two glasses when the zeroes coincide.

When the reading *on* the arc is the *greater*, the correction is *subtractive*; when the *lesser*, *additive*.

## EXAMPLES.

$$\begin{array}{rcl} \text{Ex. 1. On the arc} & - & 33' 10'' \\ \text{Off} & + & 30' 50'' \\ \hline & & 2) 220 \\ \hline \text{INDEX CORR. sub.} & & 110 \end{array}$$

$$\begin{array}{rcl} \text{Ex. 2. On the arc} & - & 30' 20'' \\ \text{Off} & + & 33' 30'' \\ \hline & & 2) 310 \\ \hline \text{INDEX CORR. add} & & 155 \end{array}$$

If both readings are *on* the arc, or both *off* the arc, half their sum is the index correction—*subtractive* when both *on*, *additive* when both *off* the arc.

$$\begin{array}{rcl} \text{Ex. 3. 1st reading on the arc} & - & 65' 30'' \\ \text{2nd do. on the arc} & - & 1' 40'' \\ \hline & & 2) 6710 \\ \hline \text{INDEX CORR. sub.} & & 3335 \end{array}$$

$$\begin{array}{rcl} \text{Ex. 4. 1st reading off the arc} & + & 1' 30'' \\ \text{2nd do. off the arc} & + & 66' 50'' \\ \hline & & 2) 6820 \\ \hline \text{INDEX CORR. add.} & & 3410 \end{array}$$

One-fourth of the sum of the two readings should be equal to the sun's semi-diameter in the *Nautical Almanac* for the day; but if both readings be *on* or both *off* the arc *one-fourth* their *difference* should be the sun's semi-diameter.

Thus, suppose the observations, in Example 1, to be made on September 26th, 1876; here one-fourth of the sum of the two readings is 16' 0", agreeing with the semi-diameter as given in the *Nautical Almanac* for the given day.

This affords a test of the accuracy with which the observation has been made.

In order to obtain the index correction with the greatest precision, the mean of a number of measures of the sun's diameter should be taken.

## EXAMPLES FOR PRACTICE.

Ex. 1. 1876, April 17th, the reading on the arc 29' 40", the reading off the arc 34' 10": required the index correction and semi-diameter.

Ex. 2. 1876, July 4th, the reading on 33' 10", off 29' 50": find index correction and semi-diameter.

Ex. 3. 1876, November 13th, on 4' 40", off 60' 10": find index correction and semi-diameter.

Ex. 4. 1876, July 10th, on 32' 45", off 34' 30": find index correction and semi-diameter.

Ex. 5. 1876, March 21st, off 12' 10' 0", off 6' 40": find index correction and semi-diameter.

Ex. 6. 1876, January 17th, on 67' 40", on 2' 30": find index correction and semi-diameter.

315. **The Prismatic Sextant.**—In the form of instrument just described, and which is all but universally employed, the angle measurable is limited to 140°; but we may perhaps add that Pistor and Martins, of Berlin, have, by an ingenious modification of the horizon-glass (for which they substitute a prism), produced a sextant which will measure any angle up to 180°. This instrument is called **THE PRISMATIC SEXTANT**.

*The following shows the form of Examination Paper on the Adjustment of the Sextant.*

### EXAMINATION PAPER.

Exn. 9a.

*Port of*

Rotation No.

### ADJUSTMENTS OF THE SEXTANT.

*The applicant will answer in writing, on a sheet of paper which will be given him by the examiner, all the following questions, numbering his answers with the numbers corresponding to the questions.*

1.—What is the first adjustment of the sextant?

A.—The index-glass must be perpendicular to the plane of the sextant.

2.—How do you make that adjustment?

A.—Place the index near the middle of the arc, and look into the index-glass so that you can see both the arc and its reflection; if they be in one line, the glass is perpendicular, but if not in one line, they are brought so by gently moving the screws in the frame upon which the glass stands.

3.—What is the second adjustment?

A.—The horizon-glass must be perpendicular to the plane of the sextant.

4.—Describe how you make that adjustment?

A.—Place O of the vernier on O on the arc, hold the instrument obliquely, with its face upwards, and look at the horizon; if the reflected part and the direct portions of the horizon are in one line, this adjustment is perfect, but if not, they must be brought in line by gently moving a screw at the back of the glass.

5.—What is the third adjustment?

A.—The index and horizon-glasses must be parallel when the index is at O.

6.—How would you make the third adjustment?

A.—Place the index at O, and holding the instrument vertically, look at the horizon; if the reflected and direct parts are in one line, this adjustment is perfect, but if they are not in one line, move a screw at the back of the horizon-glass until they are.

7.—In the absence of a screw how would you proceed?

A.—I would find the index correction, or as it is called, the index error.

8.—How would you find the index error by the horizon?

A.—Hold the instrument vertically, and, looking at the horizon, I would move the tangent screw until the horizon in both parts of the horizon-glass form one line; the reading is the index error.

9.—How is it to be applied?

A.—To be added when the reading is off the arc, and to subtract when the reading is on the arc.

10.—Place the index at the error of \_\_\_\_\_ minutes to be added, clamp it, and leave it.

NOTE.—The examiner will see it is correct.

11.—The examiner will then place the zero of the vernier on the arc, not near any of the marked divisions, and the candidate will read it.

NOTE.—In all cases the candidate will name or otherwise point out the screws used in the various adjustments.

NOTE to 10 and 11.—When the examiner is satisfied that the candidate can read the arc of the sextant both on and off the arc, it will be sufficient to place his initials against 10 and 11 on the paper containing the answer.

*The above completes the examination of Second and Only Mates.*



In addition to the above, First Mates and Masters will be required to state in writing :—

12.—How do you find the index error by the sun ?

A.—I would place the index at about 32' on the arc, and, looking at the sun, two suns will be seen ; bring their upper and lower limbs in exact contact, read off and mark down, then place the index at about 32' off the arc, or to the right of O, bring down the upper and lower limbs in contact as before, read off and mark down ; half the difference of these two readings will be the index error.

13.—How is the same applied ?

A.—It is to be added when the greatest reading is off the arc, and subtracted when the greatest reading is on the arc.

14. What proof have you that those measurements or angles have been taken with tolerable accuracy ?

A.—I would add the two readings together, and divide the sum by 4 ; if the measurements are correct, the result should be nearly equal to the semi-diameter for the day, as given in the Nautical Almanac. If they do not so agree, I would repeat my observations until they do.

## ON THE CHART.

316. A CHART is a map or plan of a sea or coast. It is constructed for the purpose of ascertaining the position of the ship with reference to the land, and of shaping a course to any place.

317. The use to be made of the chart in each case determines the method of projection, and the particulars to be inserted. (1) The chart may be required for coasting purposes, for the use of the pilot, &c., and then only a very small portion of the surface of the globe being represented at once, no practical error results from considering that surface a plane, and a "*plane chart*" is constructed in which the different headlands, lighthouses, &c., are laid down according to their bearings. The soundings on these charts are marked with great accuracy ; the rocks, banks, and shoals, the channels, with their buoys, the local currents, and circumstances connected with the tides, are also noted. (2) Again, for long sea passages the seaman requires a chart on which his course may be conveniently laid down. The track of a ship always steering the same course appears as a straight line (and can at once be drawn with a ruler) on the *Mercator's Chart*. Hence the charts used in navigation are *Mercator's charts*. (3) When great circle sailing is practicable, and of advantage, a chart on the "*central projection*," or gnomonic, exhibits the track as a straight line, and is therefore convenient.\*

\* The method lately introduced by HUGH GODFRAY, Esq., M.A., St. John's College, Cambridge, deserves special mention, as its beauty and simplicity will ultimately lead to its general adoption. A chart on the central projection, as stated above, exhibits the great circle as a straight line, and thus it is seen at once, whether the track between two places is a practicable one ; hence, also, we have by inspection the point of highest latitude. An accompanying diagram then gives the different courses, and distances to be run on each, in order to keep within  $\frac{1}{2}$  of a point to the great circle. This chart and diagram is fully described in the *Transactions of the Cambridge Philosophical Society*, vol. X, part II, and is published by J. D. Potter, Poultry.

## ON MERCATOR'S CHARTS.

(See Norie, pages 126—131; or Raper's "Practice of Navigation," pages 120—127, on this subject.)

318. A chart used at sea for marking down a ship's track and for other purposes, exhibits the surface of the globe on a plane on which the meridians are drawn parallel to each other, and therefore the parts, BH, CI, DK, &c. (fig. chap. def. nav.), arcs of parallels of latitude, are increased and become equal to the corresponding parts of the equator UV, VW, &c. Now, in order that every point of this plane may occupy the same relative position with respect to each other that the points corresponding to them do on the surface of the globe, the distance between any points, A and O, and A and F must be increased in the same proportion as the distance FO has been increased. The true difference of latitude, AO, is thus projected on the chart into what is called the *meridional difference* of latitude, and the departure BH + CI + DK, &c., into the difference of longitude, and the representation is called a Mercator's projection. It is evidently a true representation as to *form* of every particular small track, but varies greatly as to point of *scale* in its different regions, each portion being more and more enlarged as it lies farther from the equator, and thus giving an appearance of distortion.\*

(1.) In charts generally, the upper part as the spectator holds it, is the North, the lower part South, and that towards his right hand the East, that towards the left West, as on the compass card.

In a case which sometimes happens when the upper part is not the North, the North part may be known by the North part of the compass.

(2.) On Mercator's chart the parallel lines from North to South (from top to bottom) are termed *meridians*, and they are all perpendicular to the equator; the meridians on the extreme *right* and *left* are the *graduated* meridians

\* It is plain from the principles of Mercator's projection, and from the diagram (page 183) which connects the enlarged meridian with the difference of longitude, that if a ship set out on any point on the globe, and sail on the same oblique rhumb towards the pole, it can reach it only after an infinite number of revolutions round it. For from any point to the pole, the projected meridian is infinite in length, and so, therefore, is the difference of longitude due to this advance in latitude upon an oblique course. Consequently, this latitude can be reached only after the ship has circulated round the pole an infinite number of times.

These endless revolutions, however, are all performed in a finite time, the entire track of the ship being of limited extent. This, however paradoxical it may appear, is necessarily true from the principles of plane sailing, which shows that any finite advance in latitude is always connected with a finite length of track, this length being  $\frac{\text{diff. lat.}}{\cos. \text{course.}}$

The apparent paradox of the infinite number of revolutions about the pole being performed in a finite time, becomes explicable when we consider that, whatever be the progressive rate of the ship along its undeviating course, the times of performing the successive revolutions continually diminish as the ship approaches the pole, both the extent of circuit and the time of tracing it tending to zero, the limit actually attained at the pole itself; hence there must ultimately be an infinite number of such circuits to occupy a finite time.

When the pole is reached the direction all along preserved may still be continued, and a descending path will be described similar to that just considered, and which will conduct the ship to the opposite pole, after an infinite number of revolutions round it, as in the former case. In receding from this pole the track described will at length unite with that at first traced, the point of junction being that from which the ship originally departed. But for the strict mathematical proof of these latter circumstances the student may consult Professor DAVIES' curious and instructive papers on *Spherical Co-ordinates* in the *Edinburgh Transactions*, vol. XII.

—so called from showing the divisions for degrees and minutes. The *latitude* is measured on the graduated meridians, and also the *distance*.

(3.) The parallel lines from West to East (from left to right) are called *parallels*, and they are all parallel to the equator, the parallels at the top and bottom are *graduated* to degrees and minutes—and longitude is measured on the graduated parallels.

(4.) The depth of water is denoted, as also in some places the quality of the bottom. The numerals or figures in harbours, bays, channels, &c., indicate *soundings reduced to low water ordinary spring tides*. The *Roman figures* indicate the time of high water at full and change of the moon. Thus: XI hrs. 34<sup>m</sup> F & C means that the time of high water is thirty-four minutes past eleven on days of full and new moon. The *anchors* on the chart denote anchorage. The small *arrows* show the *direction of the set of the current*, the current going with the arrow.

(5.) Lines called *Compasses*, similar to those on the compass card, are drawn at convenient intervals on the chart. In charts of large seas, as the Atlantic, these compasses are generally drawn so that the line from the North to the South point corresponds with the true meridian; but in coasting charts the same line generally coincides with the magnetic meridian.

(6.) When the *true course* between two places is known, it must be remembered that *Westerly* variation is allowed to the *right*, and *Easterly* to the *left* hand of the true course in order to obtain the *compass course*.

(7.) In "*cross bearings*," both bearings must be corrected for the deviation due to the direction of the ship's head at the instant of making the observations.

(8.) With respect to the method of determining the ship's position by cross bearings, it may be observed that this is the most complete of all methods when the difference of bearings is near 90°; but if the difference is small—as, for example, less than 10° or 20°, or near 180°—the ship's position will be uncertain, because a small error in the bearing will cause a great error in the distance.—(Raper, page 120, No. 367.)

### EXERCISES ON THE CHART.

FOR ONLY MATE, FIRST MATE, AND MASTER.

#### *North Sea.*

|  |   |
|--|---|
| (1.) Latitude 55° 5' N.<br>Longitude 0 5 E.<br>Required the course and distance to<br>Hartlepool.          | (2.) Latitude 57° 30' N.<br>Longitude 0 40 E.<br>Required the course and distance to<br>Tynemouth Light.    |
| (3.) Latitude 53° 35' N.<br>Longitude 0 55 E.<br>Required the course and distance to the<br>Dudgeon Light. | (4.) Latitude 55° 10' N.<br>Longitude 0 35 E.<br>Required the course and distance to<br>Flaumbro' Head.     |
| (5.) Latitude 60° 21' N.<br>Longitude 0 35 E.<br>Required the course and distance to<br>Udsire.            | (6.) Latitude 57° 25' N.<br>Longitude 7 25 E.<br>Required the course and distance to the<br>Naze of Norway. |

- (7.) Latitude  $55^{\circ} 28' N.$   
Longitude  $0^{\circ} 30' W.$

Required the course and distance to Tynemouth Light.

- (9.) Latitude  $55^{\circ} 40' N.$   
Longitude  $0^{\circ} 15' W.$

Required the compass course and the distance to St. Abb's Head Light.

(11.) Required the true and magnetic Bearing and Distance between Whitby and the Naze of Norway.

(13.) A ship from Kinnaird's Head, in Scotland, sailed S.E. by E. (true) 186 miles: required the latitude and longitude she is come to, and the direct course and distance she must sail, in order to arrive at Heligoland.

(14.) A ship from Heligoland sailed on a direct course between the North and West 197 miles, and spoke a ship which had run 170 miles on a direct course from Hartlepool: required the latitude and longitude of the place of meeting; also the course steered by each ship.

- (15.) Sunderland Light, bearing by compass S.W.  $\frac{1}{2}$  S.  
Coquet Island " " N.W.

Required the latitude and longitude of ship; also the course and distance to Hartlepool Light.

- (16.) Buchanness Light, N. by W.  $\frac{1}{2}$  W., by compass.  
Girdleness Light, West.

Required the latitude and longitude of ship; also the course (by compass) and distance to the Staples.

- (17.) The Skerries North by compass.  
Sumburg Head, W.  $\frac{1}{4}$  S. "

Required the latitude and longitude in; also the compass course and distance to Peterhead.

- (18.) Flambro' Head Light, S.W. by S. by compass.  
Whitby Lights, N.W. by W.  $\frac{3}{4}$  W. "

Required the latitude and longitude in; also the compass course and distance to Outer Dowsings.

- (19.) Farn Lights, S.W. by S., by compass.  
Berwick Lights, W. by N. "

Required the latitude and longitude; also the distance from each light.

- (20.) The Dudgeon Light, W. by N. by compass.  
Hasbro' Sand-end Light, S.S.W. "

Required the latitude and longitude of ship; also the compass course and distance to Flambro' Head.

(21.) Scarbro' light was observed to bear S.W. by compass, then sailed E.S.E. 11 miles, and the light then bore West: required the latitude and longitude of the ship at each station, and her distance from the light.

(22.) Coasting along shore, I observed Tynemouth light to bear W. by S. by compass; I then sailed S. by W. 16 miles, and the light bore N.W. by N.: required the latitude and longitude of the ship, and her distance from the light.

*English and Bristol Channels, and South Coast of Ireland.*

- (1.) Latitude  $50^{\circ} 1' N.$   
Longitude  $2^{\circ} 4' W.$

Required the compass course and distance to the Caskets.

- (3.) Latitude  $49^{\circ} 30' N.$   
Longitude  $3^{\circ} 30' W.$

Required the compass course and distance to the Start Point.

- (2.) Latitude  $48^{\circ} 50' N.$   
Longitude  $5^{\circ} 50' W.$

Required the compass course and distance to Ushant.

- (4.) Latitude  $50^{\circ} 10' N.$   
Longitude  $1^{\circ} 10' W.$

Required the compass course and distance to St. Catherine's Light.

(5.) Latitude  $50^{\circ} 30' N.$   
Longitude  $0^{\circ} 55' E.$   
Required the compass course and distance to Dungeness.

(7.) Latitude  $50^{\circ} 10' N.$   
Longitude  $3^{\circ} 10' W.$   
Required the compass course and distance to Portland.

(9.) Latitude  $50^{\circ} 50' N.$   
Longitude  $10^{\circ} 35' W.$   
Required the compass course and distance to the Fastnet Rock.

(11.) Latitude  $50^{\circ} 18' N.$   
Longitude  $0^{\circ} 10' E.$   
Required the compass course and the distance to Beachy Head.

(13.) Latitude  $51^{\circ} 6' N.$   
Longitude  $6^{\circ} 12' W.$   
Required the compass course and the distance to St. Anne's Head Light.

(15.) Latitude  $50^{\circ} 50' N.$   
Longitude  $7^{\circ} 20' W.$   
Required the compass course and distance to Old Head of Kinsale.

(17.) Latitude  $50^{\circ} 40' N.$   
Longitude  $6^{\circ} 30' W.$   
Required the compass course and distance to Lundy Island.

(19.) Longships Light, bearing by compass E.N.E.  
St. Agnes' Light, " " N.N.W.  $\frac{1}{2}$  W.

Required the latitude and longitude in; also the compass course and distance to the Lizard.

(20.) Cape Barfleur, bearing by compass N.W.  
St. Marcouf, " " S.W.

Required the latitude and longitude of ship; also the compass course and distance to Cape de la Heve.

(21.) Berry Head, bearing by compass N.  $\frac{1}{2}$  E.  
Start Point, " " W. by N.  $\frac{1}{2}$  N.

Required the compass course and the distance to Portland.

(22.) Bill of Portland, bearing by compass N.W. by W.  
St. Alban's Head " " N.E.  $\frac{1}{2}$  E.

Required the latitude and longitude of ship, and the compass course and the distance to Start Point.

(23.) Longships Light, bearing by compass S.S.E.  
Seven Stones Light " " W. by S.

Required the latitude and longitude of ship; also the compass course and the distance to Roches Point.

(24.) Tuskar Rock N.E. by compass.  
Great Saltees Lightvessel N.W.  $\frac{1}{2}$  W. "

Required the latitude and longitude of ship; also the course (by compass) and distance to the Smalls.

(6.) Latitude  $48^{\circ} 55' N.$   
Longitude  $6^{\circ} 5' W.$   
Required the compass course and distance to the Lizard.

(8.) Latitude  $49^{\circ} 55' N.$   
Longitude  $3^{\circ} 55' W.$   
Required the compass course and distance to the Eddystone.

(10.) Latitude  $50^{\circ} 55' N.$   
Longitude  $6^{\circ} 55' W.$   
Required the compass course and distance to Trevoze Head.

(12.) Latitude  $51^{\circ} 16' N.$   
Longitude  $10^{\circ} 38' W.$   
Required the compass course and the distance to the Fastnet Light.

(14.) Latitude  $51^{\circ} 52' N.$   
Longitude  $6^{\circ} 6' W.$   
Required the compass course and the distance to the Tuskar Light.

(16.) Latitude  $50^{\circ} 30' N.$   
Longitude  $8^{\circ} 30' W.$   
Required the compass course and distance to Cape Clear.

(18.) Latitude  $51^{\circ} 28' N.$   
Longitude  $6^{\circ} 30' W.$   
Required the compass course and distance to Smalls Rock.

- (25.) Shipwash Light bearing by compass W. by N.  
Gallopier " " " S.S.W.

Required the latitude and longitude in; also the compass course and distance to Corton Lightvessel.

- (26.) Bembridge Lightvessel, bearing by compass N.  $\frac{1}{2}$  W.  
Owers Lightvessel, " " East.

Required the latitude and longitude of ship; also the compass course and distance to St. Catherine's Point.

- (27.) Needles Light, bearing by compass N.  $\frac{1}{4}$  E.  
St. Catherine's Light, " " E.  $\frac{1}{4}$  S.

Required the latitude and longitude of ship; also the compass course and distance to St. Alban's Head.

- (28.) Cudly Island Light, bearing by compass E.N.E.  
Lundy Island Light, " " S. by E.

Required the latitude and longitude of ship; also the compass course and distance to the Smalls.

- (29.) Lizard Lights, bearing by compass E.  $\frac{1}{4}$  S.  
Longships, " " N.  $\frac{1}{4}$  W.

Required the latitude and longitude of ship; also the compass course and distance to St. Agnes' Light.

- (30.) Mine Head Light, bearing by compass N.E.  $\frac{1}{4}$  N.  
Ballycotton Light, " " N.W.

Required the latitude and longitude of ship; also the compass course and distance to Old Head of Kinsale.

- (31.) Smalls Light bearing by compass N.  $\frac{1}{2}$  E.  
St. Ann's (Milford Haven) " " E.S.E.

Required the latitude and longitude of ship; also the compass course and distance to Seal Rock (Lundy Island.)

- (32.) Dungeness, bearing by compass N.E. by E.  $\frac{1}{2}$  E.  
Beachy Head, " " N.W.  $\frac{1}{2}$  W.

Required the latitude and longitude of the ship; and her distance from each place.

(33.) A ship is bound to Boulogne, being 18 miles distant, and lying directly to windward, the wind being E. by N. (true). It is intended to reach her port on two boards, the first being on the port tack, and the ship can lie within six points of the wind; required the course and distance upon each tack.

### EXAMINATION PAPER.

Exn. 9b.

*Port of*

|              |
|--------------|
| Rotation No. |
|              |

### EXAMINATION IN CHART.

*The applicant will be required to answer in writing, on a sheet of paper which will be given him by the Examiner, all the following questions according to the grade of Certificate required, numbering his answers with the numbers corresponding with those in the question paper.*

1.—A strange chart being placed before you, what should be your special care to determine, before you answer any questions concerning it, or attempt to make use of it?

A.—Which is the north part of the chart.

2.—How do you ascertain that in our British Charts?

A.—In our British charts there is always at least one compass, the true north point of which is designated by a star or other ornament.

3.—Describe how you would find the course by the chart between any two places, A and B.

A.—I would lay the edge of a parallel ruler over the two given places, A and B, then taking care to preserve the direction, I would move one edge of the ruler until it came over the centre of the nearest compass on the chart, the circumference of the compass cut by the edge of the ruler would show the course according to the direction the one place is from the other.

4.—Supposing there to be        points of        variation at the first named place, what would the course be magnetic? *the true course being*

A.—        points of        variation should be allowed to the  
and the magnetic course would be

5.—How would you measure the distance between those two or any other two places on the chart?

A.—I would measure one-half the distance on the chart by my dividers, then placing one leg of the dividers on the middle latitude, I would measure on each side of the same, and the distance measured between those two extreme points would be the distance.

6.—Why would you measure it in that particular manner?

A.—Because on a Mercator's chart the degrees of latitude increase as you approach the poles.

*The above comprises all the questions on the chart that are put to Mates and only Mates.*

In addition to the above, the Masters are required to answer:

7.—What do you understand those small numbers to indicate that you see placed about the chart?

A.—Depths of water in fathoms.

8.—At what time of the tide?

A.—At low water ordinary springs.

9.—What are the requisites you should know in order that you may compare the depths obtained by your lead-line on board with the depths marked on the chart?

A.—The time of the tide and the "rise and fall," or as it is now called the "mean spring range."

10.—What do the Roman numerals indicate that are occasionally seen near the coast and in harbours?

A.—The time of high water at that place at full and change of the moon.

11.—How would you find the time of high-water at any place, the Admiralty tide tables not being at hand, nor any other special tables available?

A.—To the time of high water at full and change I would add 49 minutes for every day that has elapsed since the full or change of moon, the sum would be the P.M. tide for the given day approximately; or, to the time of the moon's meridian passage, corrected for longitude, add the port establishment, the sum would be the P.M. tide required.

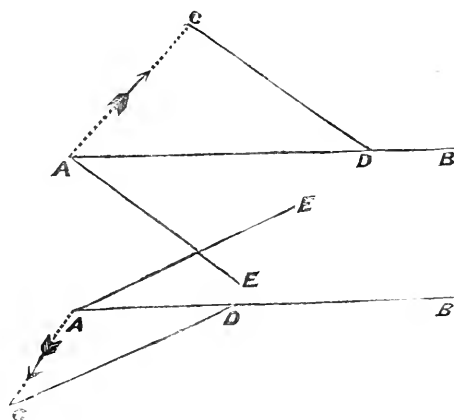
*All the above questions should be answered, but this does not preclude the Examiner from putting any other questions of a practical character, or which the local circumstances of the port may require.*

## TO FIND THE COURSE TO STEER IN ORDER

TO MAKE GOOD ANY COURSE IN A KNOWN CURRENT,  
AND ALSO THE DISTANCE MADE GOOD.

Draw a line on a chart to represent the course to be made good; from the ship's place on the chart lay off a line in the direction of the set of the current, on which mark off from the ship's place the rate of the current per hour;

then take in the compasses the distance the ship sails in an hour by log, and put one foot on the last-named mark, and from the point where the other foot reaches the first line draw a line to the mark on the line representing the direction of the current. The course to be steered is represented by the line last drawn, and the parallel ruler being placed to it, and moved to the centre of the compass on the chart, will give the course of the ship; and that portion of the first line drawn, intersected by the last line drawn, will be the distance the ship will make good per hour.



On a chart, suppose A to be the place of the ship, B the port of destination; also AC the set of the current, the rate per hour being taken from the scale of miles and laid off in the direction of the line. Take the distance sailed by the ship per hour from the scale of miles, and with one foot of the dividers at C, make an arc cutting A at D. Join CD, and move the parallel ruler from CD to A, drawing AE parallel to CD; then AE will be the direction of the ship's head; and the parallel ruler being moved to the centre of the compass on the chart, will give the course of the ship on the chart; and AD will be the distance the ship will make good.

## LOG LINE.

319. The length of the stray-line should be sufficient to allow the log-chip to be clear of the eddies of the vessel's wake.

The distance between the knots should bear the same proportion to the number of seconds run by the glass intended to be used, as the number of feet in a nautical mile bears to the number of seconds in an hour.

The number of feet in a nautical mile is 6080.

The number of seconds in an hour is 3600.



Therefore, to find the length of a knot corresponding to a 28 seconds glass, we proceed as follows:—\*

$$\begin{array}{r}
 3600 : 6080 :: 28 \\
 \hline
 48640 \\
 12160 \\
 \hline
 \text{ft. in.} \\
 360,0)17024,0(47\ 3\frac{1}{2} \\
 1440 \\
 \hline
 2624 \\
 2520 \\
 \hline
 104 \\
 12 \\
 \hline
 360)1248(3\frac{1}{2} \\
 1080 \\
 \hline
 \end{array}$$

We have for glasses running 30 seconds and 32 seconds the following proportions:—

$$\begin{array}{l}
 3600 : 6080 :: 30 : 50 \text{ feet } 8 \text{ inches.} \\
 3600 : 6080 :: 32 : 54 \text{ feet } 0\frac{1}{2} \text{ inch.}
 \end{array}$$

## MARKING THE LEAD LINE.

320. In nautical phrase the **lead line** has “nine marks and eleven deeps.”

At two fathoms, the mark is leather; at three fathoms, leather; at five, white rag; at seven, red rag; at ten, a piece of leather with a hole in it; at thirteen, blue rag; fifteen, white rag; seventeen, the same as at seven; at twenty fathoms, a piece of cord with two knots.

321. **Deep-sea** lead lines are marked the same as far as twenty fathoms; then add a piece of cord with an additional knot for every ten fathoms, and a strip of leather for every five fathoms.

## SOUNDINGS.

322. In the open sea, the tide requires about six hours and a quarter to rise from low to high water, and an equal interval to fall from high to low water. If the rise or fall was an uniform quantity throughout, by simply taking a proportionate part of the rise or fall due to the time of tide, we should at once obtain the quantity required to reduce the soundings to the low water of that day. But the water does not rise in equal proportions, the rise during the first and last hours being very small (about one-sixteenth of the whole range); in the second hour there is a considerable increase of rise;

\* The Rule for Proportion is—Multiply the second and third terms together and divide this product by the first term, the quotient will be the fourth term required.

in the third and fourth hours a still greater increase of rise; and then the rise begins to take off in the same proportion as it increased.\*

The correct amount for every half-hour, and for various ranges, is given in the "Tide Tables for the English and Irish Ports for 1875," (p. 98, Table B), published by the Hydrographic Office, Admiralty.†

323. As the soundings upon the chart are all referred to or measured downwards from the mean level of low water of *ordinary* spring tides,‡ casts of the lead taken at any other time of the tide, or any other day than full and change, will exceed the depth marked on the chart (except when it happens to be low water of *greatest* spring tides). It is necessary for the seaman to be able to calculate the difference between the actual depth obtained by means of his lead, and that marked on his chart, in order to the identification of his ship's place, more especially when the range of the tide is considerable, and the depth not great. Also, when about to enter a port in a vessel whose draught of water is nearly equal to the depth, it is necessary to find the height of the tide as exactly as circumstances will permit.

324. Two classes of questions may be proposed in reference to this subject—*firstly*, to find the depth of water at a given place and time; *secondly*, having obtained the actual depth by a cast of the lead, to find the sounding on the chart corresponding thereto, and thence to identify the ship's place. Both these classes of questions require us to know the *time* of high water and the *range* of the tide on the given day; and for this purpose almanacs are published. The most correct, and by far the most useful of all these, are the "Tide Tables" published by the Admiralty, and to which we have already referred. In this book are given the times of *high water* and the *height of the tide* for every day in the year, at each of the principal ports in Great Britain.

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\* The reader may obtain an idea of this law, sufficiently exact for practical purposes, in the following manner:—Describe a circle, and divide the circumference into six equal parts on each side, corresponding to the hours of the tide; then divide the diameter into proportional parts, corresponding to a given (assumed) range of tide. Connect the segments of the circle by straight lines drawn across the figure, when it will be perceived that they intersect the diameter at certain divisions of the range. These are the correct quantities respectively due to each hour's rise or fall of such a tide from low to high water, and *vice versa*. An examination of these quantities will show, that in the first hour of the tide the rise is equal to one-sixteenth of the whole range; at two hours from low or high water, the tide has risen or fallen *one-fourth* of the whole range; at three hours it has risen just *half* its range; at four hours it has risen *three-fourths* of the whole range; at five hours, to within a *sixteenth* of the whole range. The above method, which is constructed upon principles theoretically correct, will represent with sufficient exactness all that is necessary for practical purposes.

† Table XIX, Raper, which the author, in 1847, computed for Raper's work, also shows the space through which the surface of the water rises and falls at given intervals from high or low water.

‡ On most charts the soundings expressed are reduced to low water of *ordinary spring tides*; but in some charts, however, the soundings are reduced to the low water of *extraordinary* spring tides—such, for example, is the case on the chart of Liverpool, surveyed by Captain Denham, R.N., the soundings on which are reduced to a spring range of thirty feet, while the mean spring range for that place, as deduced from observations made for two years at the Tide Gauge, St. George's Pier, is 26 feet.

325. To find how much we must subtract from east of the lead, in order to a comparison with the soundings marked on the chart, proceed by

### RULE CIII.

1°. Open the Admiralty Tide Tables at the proper month; and in the column under the head of the place near your position, and opposite the day of the month, take out the "time" of high water in the morning or afternoon, as the case requires, and also from the adjoining column, under "height," take out the height of the tide.

2°. Next, underneath the time of high water place the time at ship, and take the difference and call it "time from high water."

3°. From the height of tide subtract the half mean Spring Range, which stands at the foot of the column.

The remainder is the half range of the day.

4°. Enter Table B, page 98, Admiralty Tide Tables, and under the time from high water, and opposite the half range for the given day, take out the correction corresponding thereto, observing whether it is to be added or subtracted.

5°. Add or subtract the correction, as directed, to the mean half Spring Range marked on the chart.

The result is the excess of the sounding observed above the sounding recorded on the chart, or is the height of the tide above zero.

6°. Subtract this last from the sounding shown by the lead, the remainder is the sounding shown by the chart.

NOTE I. When it happens to be an extraordinary low ebb tide, the quantity given in Table B will be greater than the half mean spring range, and will be subtractive. In such cases, subtract the half mean spring range from the correction by Table B, and add the result to the soundings by lead; the sum will be the sounding on the chart.

### EXAMPLES.

Ex. 1. 1875, September 15th, at 9<sup>h</sup> 19<sup>m</sup> P.M., a ship off Liverpool strikes soundings in 8 fathoms: required the corrected soundings to compare with the chart. (The half spring range by Captain Denham's chart is 15 feet.)

|  |                                      |
|--|--------------------------------------|
| Admiralty Tide Tables (page 70); time of high water at Liverpool, September 15th, 1875 .. .. . | 11 <sup>h</sup> 19 <sup>m</sup> P.M. |
| Time of sounding .. .. .   | 9 19                                 |
| Time from high water .. .. .   | 2 0                                  |
|  | ft. in.                              |
| Height at Liverpool .. .. .  | 26 6                                 |
| Half mean spring range .. .. .   | 13 0                                 |
| Half-range of the day .. .. .  | 13 6                                 |
| In Table B, page 98, under 2 <sup>h</sup> , opposite 13½ ft., stands add..                     | 6 9                                  |
| Half spring range by chart .. .. .   | 15 0                                 |
| Correction 3½ fathoms, or .. .. .  | 21 9                                 |
| Depth by lead .. .. .  | 8 fathoms.                           |
| Correction .. .. .   | 3½ "                                 |
| Showing the depth by comparison .. .. .  | 4½ "                                 |

Whence the depth to compare with the chart is only 4½ fathoms instead of 8 fathoms.

Ex. 2. 1875, October 16th, at 7<sup>h</sup> 42<sup>m</sup> A.M., a vessel anchored off Weston-super-mare in 6½ fathoms; at low water the vessel was "high and dry:" required the cause of this. (Half spring range by chart 23 feet.)

|   |                                     |
|---|-------------------------------------|
| By Table: October 16th, the time of high water at Weston-super-mare .. .. . | 7 <sup>h</sup> 18 <sup>m</sup> A.M. |
| Time of anchoring .. .. .   | 7 42                                |
| Time before high water .. .. .  | 0 24                                |
| Height of tide by Tables .. .. .  | 40ft. 0 in.                         |
| Half spring range .. .. .   | 18 7                                |
| Half range .. .. .  | 21 5                                |
| By Table B, 24 <sup>m</sup> and half range 21 feet 5 inches give <i>add</i> | 20 10                               |
| By chart; half spring range .. .. .   | 23 0                                |
| Correction to low water .. .. .   | 43 10                               |
| Sounding 6½ fathoms, or .. .. .   | 39 0                                |
|   | 4 10                                |

Water below the sounding; or, the ship is found to be 4 feet 10 inches dry at low water.

Ex. 3. 1875, March 7th, at 9<sup>h</sup> 1<sup>m</sup> A.M., a vessel has to cross the Victoria Bar, Liverpool: it is required to know what water she will have over the bar. (Depth at low water springs on chart, 11 feet).

|   |                                     |
|---|-------------------------------------|
| By Tables: March 7th, time of high water at Liverpool ..                              | 11 <sup>h</sup> 4 <sup>m</sup> A.M. |
| Time of crossing the bar .. .. .  | 9 1                                 |
| Time from high water .. .. .  | 2 3                                 |
| Height of Tide by Tables .. .. .  | 25ft. 7 in.                         |
| Half spring range .. .. .   | 13 0                                |
| Half range for the day .. .. .  | 12 7                                |
| By Table B: 2 <sup>h</sup> 3 <sup>m</sup> and half range 12ft. 7 in. .. .. <i>add</i> | 6 3                                 |
| Half spring range by chart .. .. .  | 13 0                                |
| Add for Liverpool chart .. .. .   | 2 0                                 |
| Correction .. .. .  | 21 3                                |
| Depth on Bar at 2 <sup>h</sup> 3 <sup>m</sup> from high water, March 7th .. ..        | 11 0                                |
| By Chart: depth on Victoria Bar at low water springs ..                               | 32 3                                |
|   | or 5½ fathoms, nearly.              |

Ex. 4. 1875, September 17th, at 2<sup>h</sup> 34<sup>m</sup> P.M., off Weston-super-mare, sounded in 4½ fathoms: required the soundings on the chart.

|   |                                    |
|---|------------------------------------|
| Time of high water, Weston-super-mare, September 17th ..                            | 8 <sup>h</sup> 6 <sup>m</sup> P.M. |
| Time of Sounding .. .. .  | 2 34                               |
| Time from high water .. .. .  | 5 32                               |
| Height of Tide, Weston-super-mare, September 18th .. ..                             | 39ft. 6 in.                        |
| Half mean spring range .. .. .  | 18 7                               |
| Height above half tide .. .. .  | 20 11                              |
| By Table B: 5 <sup>h</sup> 32 <sup>m</sup> and half range 21 ft. .. .. <i>subt.</i> | 20 3                               |
| Half spring range .. .. .   | 18 7                               |
| Level of tide below zero .. .. .  | 1 8                                |
| Soundings by lead 4½ fathoms, or .. .. .  | 27 0                               |
| Correction .. .. .  | + 1 8                              |
| Soundings on chart .. .. .  | 28 8                               |
|   | Or a little less than 5 fathoms.   |

EXAMPLES FOR PRACTICE.

Ex. 1. 1875, August 18th, at 9<sup>h</sup> 12<sup>m</sup> A.M.: required the depth of water on the "Four-fathom Ledge," off Weston-super-mare.

Ex. 2. 1875, June 18th, at 5<sup>h</sup> 17<sup>m</sup> P.M.; off Brest, the depth of water by the lead was 10 $\frac{3}{4}$  fathoms: required the soundings on the chart.

Ex. 3. 1875, August 16th, at 9<sup>h</sup> 24<sup>m</sup> P.M., sounded in the Victoria Channel, Liverpool, in 5 fathoms: required the soundings on the chart.

Ex. 4. 1875, September 18th, at 8<sup>h</sup> 38<sup>m</sup> A.M., a vessel anchored off Weston-super-mare in 6 fathoms: required the depth at low water.

Ex. 5. 1875, March 9th, at 5<sup>h</sup> 42<sup>m</sup> A.M.: required the height of the tide above mean low water of spring tides at Liverpool.

Ex. 6. 1875, December 25th, at 9<sup>h</sup> 39<sup>m</sup> A.M.: going up the Firth of Forth, the lead showed 12 fathoms: required the soundings on the chart.

326. The following is the form of the Rule as used at the Liverpool Examinations:—

1°. Take the difference between the time of high water, full and change, at Liverpool and full and change at ship, and take this difference from the time of high water on the given day at Liverpool; the result is time of high water at ship.

2°. Next find the time from high water when the "cast" was taken.

3°. Take 13 feet, the half mean spring range from the height of tide on given day at Liverpool.

4°. Apply a correction from Table B to the half mean spring range, as directed at the head of the Table; the result is the Reduction at Liverpool.

Lastly.—Find the Reduction at ship (by proportion) thus:—

|                                  |   |  |
|----------------------------------|---|--|
| As Spring Range at Liverpool     | } | The Reduction or Correction<br>of Soundings<br>is to be taken from the Cast. |
| Is to Spring Range at Ship,      |   |  |
| So is the Reduction at Liverpool |   |  |
| To the Reduction at Ship.        |   |  |

1875, September 19th, at 1<sup>h</sup> 57<sup>m</sup> P.M. at ship, off Holyhead, sounded in 45 fathoms: required the corrected cast to compare with the chart.

|                              |                                 |   |  |
|------------------------------|---------------------------------|---|--|
| Full and change at Liverpool | 11 <sup>h</sup> 23 <sup>m</sup> | { | Page 152 Admiralty Tide<br>Tables, 1875. |
| Full and change at Holyhead  | 10 11                           |   |  |

|  |            |                                |
|--|------------|--------------------------------|
| Difference                             | — 1 12     |                                |
| Time high water, Liverpool, Sept. 19th | 1 9 P.M.,  | and Height of tide 27ft.       |
| Time high water at ship                | 11 57 A.M. | Half mean spring range 13      |
| Time of cast                           | 10 57 P.M. | Half range for day 14          |
| Time of cast from high water           | 2 0 }      | give in Table B correction + 7 |
| Half range                             | 14ft. }    | Half spring range 13           |

|                |     |          |                      |
|----------------|-----|----------|----------------------|
| By Proportion. |     |          |                      |
| ft.            | ft. | ft.      |                      |
| 26             | :   | 20 :: 16 |                      |
| 16             |     |          |                      |
| —              |     |          | fath. ft.            |
| 26             | 320 | (12 feet | = 2 0                |
| 26             |     |          | 45 0 cast taken.     |
| —              |     |          |                      |
| 60             |     |          | 43 0 cast corrected. |
| —              |     |          |                      |
| 52             |     |          |                      |
| —              |     |          |                      |
| 8              |     |          |                      |

NOTE.—In the above proportion, 26 is the spring range at Liverpool, 16 the spring range at ship, and 20 the reduction at Liverpool.

## ANSWERS.

### NOTATION, page 16.

1. 63; 81; 99; 40; 13.
2. 200; 303; 598; 888.
3. 4000; 1783; 6083; 7930; 9009.
4. 27504; 89064; 33000.
5. 100000; 676050; 603240.
6. 20600; 90092; 204641; 800800.
7. 3006004; 5030040; 7700006; 10010010.
8. 7003000; 11108106; 54054088; 613020303.
9. 70704032; 45387025; 349004065; 100010001.
10. 842248484; 909009099; 222000040; 305040008.
11. 700700700; 202202200; 900000900; 100010001.

### NUMERATION, page 17.

1. Forty-three. 2. Sixty. 3. Eighty-eight. 4. Ninety-seven. 5. Fifty-nine.
6. Twelve. 7. Twenty-one. 8. Nineteen. 9. One hundred and twenty-three.
10. Four hundred and seven. 11. Five hundred. 12. Nine hundred and ninety-nine.
13. Seven hundred and thirty-eight. 14. Eight hundred and thirty-seven. 15. Two thousand seven hundred and sixty. 16. Five thousand and eighty. 17. Seven thousand and thirty-six. 18. Two thousand. 19. Three thousand and three. 20. Five thousand five hundred and five. 21. Thirty-seven thousand six hundred and fifty-four. 22. Eighty-seven thousand and seventy-eight. 23. Thirty-seven thousand and three. 24. Sixty-three thousand and ninety. 25. Six hundred and ninety thousand and six. 26. Eight million, forty-seven thousand three hundred and twenty-eight. 27. Four million, ninety thousand and three hundred. 28. Five million, two hundred and ten thousand and seven. 29. Six million, thirty thousand four hundred and five. 30. Five hundred and sixty thousand and seventy-five. 31. Three million and six. 32. One million, three hundred and ninety-seven thousand four hundred and seventy-five. 33. Twenty million, eighty-four thousand two hundred and sixteen. 34. Five million, one thousand eight hundred and sixty. 35. Eight million, eighty thousand eight hundred and eight. 36. Fifty-five million, seven hundred thousand and five. 37. Seventy-six million, fourteen thousand and fifty-nine. 38. Six million, six thousand six hundred and six. 39. Fifty-six million, seven hundred thousand five hundred and five. 40. One hundred and twenty million, fifteen thousand and fifteen. 41. Two hundred and two million, two hundred and two thousand two hundred. 42. One hundred million, one hundred thousand one hundred and one. 43. Two hundred and seventy-five million, eight thousand and five. 44. Twenty million, eighty-four thousand two hundred and sixteen. 45. Seventy-nine million, thirty thousand one hundred and eighty-four. 46. Four hundred and eight million, seventy-six thousand and thirty-two. 47. Four hundred and one million, four hundred thousand and fifty-six. 48. Nine hundred and eight million, five hundred thousand and sixty.

### SIMPLE ADDITION, pages 18—19.

- |                  |              |               |                 |              |
|------------------|--------------|---------------|-----------------|--------------|
| 1. 1274170       | 2. 1634607   | 3. 1659291    | 4. 2333431      | 5. 3005313   |
| 6. 1536206       | 7. 1648127   | 8. 2067690    | 9. 3329175      | 10. 3724599  |
| 11. 4483647      | 12. 4105670  | 13. 3312667   | 14. 3018498     | 15. 2797285  |
| 16. 3519772      | 17. 9185198  | 18. 7485613   | 19. 8518439     | 20. 7498159  |
| 21. 9560155      | 22. 5621434  | 23. 6524956   | 24. 8238336     |              |
| 25. (1) 13788543 | (2) 12844819 | (3) 14661377  | (4) 13937260    | (5) 15878135 |
|                  | (7) 10970368 | (8) 13825798. | 26. 20566726566 | (6) 10176138 |

## SIMPLE SUBTRACTION, page 20.

- |                  |                    |                    |                   |
|------------------|--------------------|--------------------|-------------------|
| 1. 621511        | 2. 539540          | 3. 1               | 4. 9              |
| 5. 676001        | 6. 554999          | 7. 480895          | 8. 590998         |
| 9. 681179        | 10. 507871         | 11. 376999         | 12. 174386        |
| 13. 107500       | 14. 222419         | 15. 157406         | 16. 58024         |
| 17. 8261243256   | 18. 2358235814     | 19. 2006289547     | 20. 763595488     |
| 21. 6009085424   | 22. 9957614250     | 23. 78098951912    | 24. 7501213600    |
| 25. 91089009099  | 26. 238036793034   | 27. 43437255048818 | 28. 9088910990901 |
| 29. 353532599691 | 30. 73708072035222 | 31. 5540058        | 32. 5866974       |
| 33. 6521913      | 34. 4244103        | 35. 5160813        | 36. 8026758       |
| 37. 8087; 4936   | 38. 207786         | 39. 55599          | 40. 999882        |
| 41. 30094003     | 42. 30449329       |                    |                   |

## SIMPLE MULTIPLICATION, page 25.

- |                                |                              |                              |                 |
|--------------------------------|------------------------------|------------------------------|-----------------|
| 1. 685295792                   | 2. 1962965961                | 3. 1506172792                | 4. 1899328910   |
| 5. 550942443156                | 6. 45652143474               | 7. 3886950304                | 8. 5159176101   |
| 9. 9876543210                  | 10. 9803614194               | 11. 7774239492               | 12. 11019283848 |
| 13. 1350705843                 | 14. 2684444024               | 15. 5629618680               | 16. 8918232255  |
| 17. 27349835014665             | 18. 22591055500000           | 19. 770930181732             |                 |
| 20. 199999929143681            | 21. 10285980                 | 22. 16261578                 |                 |
| 23. 12838608                   | 24. 40261296                 | 25. 13503780000              |                 |
| 26. 55275801000                | 27. 35205962324              | 28. 61286228934              |                 |
| 29. 15993780666                | 30. 490360 9193              | 31. 2243503727343888         |                 |
| 32. 5750745672129              | 33. 531954730112             | 34. 32228449759163           |                 |
| 35. 2997332184                 | 36. 2466490572               | 37. 38114062                 |                 |
| 38. 24335360                   | 39. 47094144                 | 40. 20146968                 |                 |
| 41. 28894158                   | 42. 78522048                 | 43. 3951312893090991         |                 |
| 44. 6680943744279021           | 45. 8312372968202684         | 46. 121932631112635269       |                 |
| 47. 2872556494008787           | 48. 6324602392508400         | 49. 35333670133890810        |                 |
| 50. 2054793040961760           | 51. 47287079491501550        | 52. 12003400820050006000000  |                 |
| 53. 1944460921158              | 54. 5060344127169150         | 55. 296229611814587191480656 |                 |
| 56. 10203029078666688093030201 | 57. 99999995000000040000     |                              |                 |
| 58. 999400149980001499940001   | 59. 999400149980001499940001 | 60. 45673337928960           |                 |

## SIMPLE DIVISION, page 30.

- |                           |                 |                          |                  |
|---------------------------|-----------------|--------------------------|------------------|
| 1. 67896347-1             | 2. 194899128-2  | 3. 99836471              | 4. 59648952      |
| 5. 66779748-5             | 6. 39512348-1   | 7. 868427625-6           | 8. 274473675     |
| 9. 25409614-6             | 10. 100107478-9 | 11. 91261430-10          | 12. 4953087942-8 |
| 13. 463519673763533-5     |                 | 14. 27201490438560034-10 |                  |
| 15. 1582874324701-32      |                 | 16. 187157296759729-46   |                  |
| 17. 95022741046776-8      |                 | 18. 14964459409277-63    |                  |
| 19. 133683783399807-6     |                 | 20. 4031632208110056-69  |                  |
| 21. 27206980239559-123    |                 | 22. 34045491087172-1     |                  |
| 23. 329218107-670         |                 | 24. 6897234900           |                  |
| 25. 8607936214-143        |                 | 26. 740630987644-3; 203  |                  |
| 27. 241993504-518790      |                 | 28. 4843530-477265       |                  |
| 29. 48481368-72           |                 | 30. 90000900009-1        |                  |
| 31. 862152-1422           |                 | 32. 1654772              |                  |
| 33. 4713708               |                 | 34. 139066-29316950      |                  |
| 35. 14278693864-88877     |                 | 36. 8485852-43614        |                  |
| 37. 1068392-117002        |                 | 38. 4144081-7839494      |                  |
| 39. 3183098861-2599872450 |                 |                          |                  |





16. One, and one millionth; One million and one ten millionth; One hundred millionths; One, and thirteen thousand and four hundred thousandths; Nine, and two hundred and three thousand one hundred and sixty-seven millionths; Four, and three million eight thousand and four ten millionths; Twenty-seven, and four million six hundred and twenty-seven thousand three hundred and fifty ten millionths.

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ADDITION OF DECIMALS, *page 35.*

- |                           |                         |
|---------------------------|-------------------------|
| 1. 745'0261; 2'919563.    | 7. 53'6769; 127'050340. |
| 2. 886'9326; 1681'679.    | 8. 1'1111; 42'7162.     |
| 3. 1437'4179; 330'875521. | 9. 1'2345; 945'5993.    |
| 4. 4009'0; 501'15998.     | 10. 2'9291474.          |
| 5. 538'6422021.           | 11. 2'471092.           |
| 6. 140'1996; 1408'25559.  | 12. 0'1627165.          |
- 

SUBTRACTION OF DECIMALS, *page 37.*

1. 3'431; 8'20001; '0011; 8'000001.
  2. 39'8479194; 31'99968; 7'336606; 91'7423.
  3. '01; 98'9999901; 9'999999; 995'710; 541'787.
  4. 64'0317753; 8'20001; 72'5193401.
  5. '000099; '000396; 31'99968; 24680'12377.
  6. 699'930; '0000999.
  7. '0378; '062156; '00510; 28999'908.
- 

MULTIPLICATION OF DECIMALS, *page 38.*

1. 10'0; 10'0; 1190'0; 11'9; '0119; '00119.
  2. '000000202; 3'06034; '000000112; '00210175.
  3. '0360963; 26'5344; '000604476; 2'02100.
  4. '075460; 1'8019; 74'9265; '00104886933696.
  5. '0108575; '032016; '000000072; '26439622160671.
  6. '0306002448; 470116914'4360; 536'660075952.
  7. '00164389993; 160'86701632806; '06288405909156.
  8. 2'5067823; '000011826009; '00000006676542672.
  9. 47'83; 500'0; 75000'0.
  10. '001301400; 1'5; '000000072.
  11. 5'314410; 4'096; '032016
  12. '0001234321; '000444080; 6138'36.
- 

DIVISION OF DECIMALS, *page 40.*

1. 19'82421; 14'16015; 11'01345; 2'7533625; 1'12637557.
2. 1'66704; 1'11136; 0'83352; '2667264; '01058438.
3. '2017386; '1008693; '0672462; '025217325; '0009456496.
4. 311'487360333; 66'6188183; 2'2258942.
5. 134'88057; 790'9882353; 59'406396; 24'82661.
6. 14'789983; 255'121; 1210'234426; '02.
7. '8810891; 908'83768; '1108754; '0174532922.
8. 711'855; 2280'28; 234508.

9. '03; 74 84; 43206'7; '000007375; 83671000; '000000000003; '061096.
10. 2681'081081; '0000360074; '0001; 6'578947; 'c0862.
11. 15000 0; 5060000'0; '008; '0375313.
12. '013; 4'57; '008; 73939 39.
13. '050005; 1250'0; '0125; 60'2589.
14. '0000000125; 125'0; 125'0; '00004
15. '00000125; '00001; 20200; 77485'93.
16. 11900000; '163.
17. '10; 10'0; '001; '001; '1000; 10000; '00001.
18. '0093536; 7393'939; 39723'66; 241'6292; 200'0; '60000000; 4000000; '000006;
- 32000000.
19. '0036; '93; '52306; '0008; '0000020076364.
20. '0882352941; '017256637168; '0000999000999000999000999.
21. '0000000900090009000900090; '000000123456790; '00000618.

### REDUCTION OF DECIMALS, page 43.

1. '4375; '73; '2142857; '34375; '1875; '076923; '0112; '275.
2. '5384615; '6470588; '6315789; '185; '7167235; '3183098; '4683544; '0104895.

### page 45.

1. '2833; '4833; '7; '4166; '8; '9666.
2. '788260449735.
3. 29'530588194.
4. 12'175 hours; '0013.
5. 1 N.M. = 1'15202 I.M.; 1 I.M. = '86804 N.M., 1'1515, '868421.
6. '997269560 day.
7. 12<sup>h</sup> 59'25; 29<sup>h</sup> 7'16493055; 15<sup>d</sup> 74229'166; 119<sup>d</sup> 221701388.
8. 8° 18'75; 19° 6'7916; 104° 26'875; 82° 32'5.
9. 37° 30'5; sum 78° 75'5 or 78° 45' 18".
10. 1 Kilometre = '621382 miles; 1 mile = 1'609315 kilometres.

### page 46.

- |                              |                        |   |
|------------------------------|------------------------|---|
| 1. 15 cwt. 2 qrs. 4 lbs. 032 | 2. 7° 51' 15" 3        | 3. 64° 22' 57"  |
| 4. 4 cwt. 2 qrs.             | 5. 7 cwt. 1 qr.        | 6. 10° 52' 21"  |
| 7. 0° 17' 44" 8062           | 8. 3 cwt. 1 qr. 7 lbs. | 9. 12 <sup>h</sup> 44 <sup>m</sup> 21 <sup>s</sup> 86 |

### CHARACTERISTICS OF LOGARITHMS, page 49.

|      |       |       |       |
|------|-------|-------|-------|
| 1. 2 | 6. 4  | 11. 5 | 16. 2 |
| 2. 0 | 7. 2  | 12. 3 | 17. 7 |
| 3. 2 | 8. 3  | 13. 0 | 18. 4 |
| 4. 1 | 9. 2  | 14. 0 | 19. 0 |
| 5. 0 | 10. 0 | 15. 1 | 20. 1 |

### CHARACTERISTICS OF LOGARITHMS, page 51.

|           |            |            |             |
|-----------|------------|------------|-------------|
| 1. 2 or 8 | 6. 7 or 3  | 11. 1 or 9 | 16. 2 or 8  |
| 2. 1 or 9 | 7. 2 or 8  | 12. 3 or 7 | 17. 7 or 3  |
| 3. 4 or 6 | 8. 4 or 6  | 13. 7 or 3 | 18. 7 or 3  |
| 4. 1 or 9 | 9. 2 or 8  | 14. 5 or 5 | 19. 1 or 9  |
| 5. 3 or 7 | 10. 1 or 9 | 15. 4 or 6 | 20. 11 or 9 |

LOGARITHMS OF NATURAL NUMBERS, *pages 53—55.*

|                             |                             |                             |                             |
|-----------------------------|-----------------------------|-----------------------------|-----------------------------|
| 1. 0°698970                 | 2. 0°954243                 | 3. 3°954243<br>or 7°954243  | 4. 2°000000<br>or 8°000000  |
| 5. 4°000000<br>or 6°000000  | 6. 1°146128                 | 7. 1°612784                 | 8. 3°602060<br>or 7°602060  |
| 9. 0°380211                 | 10. 1°380211                | 11. 1°380211<br>or 9°380211 | 12. 3°322219<br>or 7°322219 |
| 13. 1°973128                | 14. 1°698970<br>or 9°698970 | 15. 1°875061<br>or 9°875061 | 16. 0°397940                |
| 17. 1°397940<br>or 9°397940 | 18. 2°954243<br>or 8°954243 | 19. 3°954041<br>or 7°954041 | 20. 1°397940                |
| 21. 2°380211<br>or 8°380211 | 22. 5°544068<br>or 5°544068 | 23. 5°755875<br>or 5°755875 | 24. 4°698970<br>or 6°698970 |

|                             |                             |                             |              |                             |
|-----------------------------|-----------------------------|-----------------------------|--------------|-----------------------------|
| 1. 2°000000                 | 2. 2°161368                 | 3. 0°468347                 | 4. 2°557507  | 5. 2°828015                 |
| 6. 2°899820                 | 7. 2°992111                 | 8. 0°681241                 | 9. 0°952308  | 10. 0°167317                |
| 11. 1°167317<br>or 9°167317 | 12. 1°954725<br>or 9°954725 | 13. 2°167317<br>or 8°167317 | 14. 2°627366 | 15. 3°651278<br>or 5°651278 |
| 16. 5°651278                |                             |                             |              |                             |

|             |              |                             |                             |
|-------------|--------------|-----------------------------|-----------------------------|
| 1. 3°000000 | 2. 3°091315  | 3. 1°409087                 | 4. 3°734960                 |
| 5. 1°415974 | 6. 0°415974  | 7. 2°005180<br>or 8°005180  | 8. 1°977129                 |
| 9. 0°890812 | 10. 2°994581 | 11. 2°835247<br>or 8°835247 | 12. 3°444669<br>or 7°444669 |

|             |                             |                             |              |
|-------------|-----------------------------|-----------------------------|--------------|
| 1. 4°585178 | 7. 2°639088                 | 13. 5°301030                | 19. 5°562474 |
| 2. 2°585178 | 8. 1°895445                 | 14. 2°749845<br>or 8°749845 | 20. 2°998755 |
| 3. 4°091491 | 9. 0°343507                 | 15. 3°993714<br>or 7°993714 | 21. 1°507732 |
| 4. 2°734968 | 10. 1°894105<br>or 9°894105 | 16. 5°808742                | 22. 0°014001 |
| 5. 4°823904 | 11. 4°000000                | 17. 3°052717                | 23. 3°000003 |
| 6. 3°965898 | 12. 4°903120<br>or 6°903120 | 18. 1°999172<br>or 9°999172 | 24. 2°775555 |

NATURAL NUMBERS OF LOGARITHMS, *pages 58—59.*

|              |                |               |                   |
|--------------|----------------|---------------|-------------------|
| 1. 3         | 11. 1234       | 21. 978°5     | 31. °0000009797   |
| 2. 8         | 12. 7916       | 22. 34800     | 32. 80080000      |
| 3. 1°1       | 13. 345°6      | 23. 52790     | 33. °04183        |
| 4. 2         | 14. 24°83      | 24. °5547     | 34. °000000007968 |
| 5. 9°4       | 15. 7000       | 25. °3171     | 35. °0046         |
| 6. 14°5      | 16. 10000000   | 26. °00000075 | 36. °00071        |
| 7. 6°49      | 17. 669000     | 27. 4000000   | 37. °000006       |
| 8. 586       | 18. 400000     | 28. °00000007 | 38. 8199000       |
| 9. 2°48      | 19. 50000      | 29. 4029      | 39. 1°010         |
| 10. 30°09    | 20. 100000     | 30. 2784      | 40. 738800        |
| 1. 853°52167 | 8. 543210      | 15. 678945°3  | 22. °000290888    |
| 2. 4220°3    | 9. 666660      | 16. 260418    | 23. °0174533      |
| 3. 71105°9   | 10. 98765      | 17. 69500°645 | 24. 2349632°4     |
| 4. 23000°1   | 11. 84321      | 18. 12375°426 | 25. °0000017645   |
| 5. 53°133    | 12. 123456     | 19. 1°7       | 26. °99727        |
| 6. 93°8689   | 13. 342°945    | 20. 165°374   | 27. °7854         |
| 7. 456780    | 14. 5555°54    | 21. °0096532  | 28. °000856735    |
|              | 29. °000036808 |               |                   |

## LOGARITHMS OF NATURAL NUMBERS, page 60.

|              |              |              |              |              |
|--------------|--------------|--------------|--------------|--------------|
| 1. 0.903090  | 11. 1.802774 | 21. 2.926548 | 31. 1.972043 | 41. 7.000000 |
| 2. 1.000000  | 12. 3.805501 | 22. 1.964240 | 32. 4.722552 | 42. 2.792392 |
| 3. 0.690196  | 13. 1.165244 | 23. 2.953760 | 33. 4.698970 | 43. 4.477134 |
| 4. 1.579784  | 14. 0.588160 | 24. 4.000000 | 34. 5.845154 | 44. 4.000039 |
| 5. 2.579784  | 15. 3.829561 | 25. 4.681241 | 35. 5.421604 | 45. 5.774152 |
| 6. 2.000000  | 16. 2.942504 | 26. 3.958124 | 36. 5.606388 | 46. 7.947385 |
| 7. 6.000000  | 17. 1.539954 | 27. 4.763428 | 37. 5.699759 | 47. 2.458852 |
| 8. 1.390935  | 18. 0.034628 | 28. 2.554755 | 38. 1.686877 | 48. 3.551938 |
| 9. 0.588832  | 19. 1.069610 | 29. 4.651278 | 39. 1.970876 | 49. 4.932847 |
| 10. 2.954243 | 20. 3.954243 | 30. 7.651278 | 40. 2.515397 | 50. 7.816109 |

## NATURAL NUMBERS OF LOGARITHMS, page 60.

|            |             |             |               |                |
|------------|-------------|-------------|---------------|----------------|
| 1. 204     | 10. 3.673   | 19. .09     | 28. 404007    | 37. .763888    |
| 2. 4753    | 11. 6.004   | 20. .0091   | 29. 100000    | 38. 4220.3     |
| 3. 9       | 12. 588.172 | 21. 50800   | 30. .0762     | 39. 53.1329    |
| 4. 50      | 13. 594500  | 22. 2.606   | 31. .147      | 40. .042404    |
| 5. 1       | 14. 264000  | 23. .1      | 32. .00000075 | 41. .0048553   |
| 6. 100     | 15. 1000    | 24. .009    | 33. 1.00043   | 42. 2.5152     |
| 7. 366.855 | 16. 2480000 | 25. .052    | 34. 8859000   | 43. 100591     |
| 8. 3659    | 17. 26.042  | 26. 451070  | 35. .0918504  | 44. .000209675 |
| 9. 418.557 | 18. 15.438  | 27. 2.71828 | 36. 5.80693   | 45. 7.5        |

## MULTIPLICATION BY LOGARITHMS, page 63.

1.  $3.774517 = 5950$ ;  $3.022429 = 1053$ ;  $3.000000 = 1000$ ;  $3.521269 = 3321$ .
2.  $2.971331 = 936.12$ ;  $4.034147 = 10818$ ;  $3.494850 = 3125$ ;  $4.443232 = 27748$ .
3.  $1.009026 = 10.21$ ;  $0.436878 = 2.7345$ ;  $1.818753 = .6588$ ;  $1.575742 = 37.648$ .
4.  $5.425758 = 266537$ ;  $4.532375 = 34070.2$ ;  $2.639870 = 436.385$ ;  $1.292881 = 19.62826$ .  
 $6783260 = 6071000$ .
5.  $4.586678 = 38608$ ;  $4.677607 = 47600$ ;  $2.680225 = 478.878$ ;  $5.237543 = 172800$ ;  
 $5.786113 = 611101$ .
6.  $3.971387 = 9362.39$ ;  $2.993736 = 985.68$ ;  $4.659678 = 45675$ ;  $5.749272 = 561400$ ;  
 $3.723999 = 5296.6$ .
7.  $7.146212 = 14002718$ ;  $6.445142 = 2787032$ ;  $6.919110 = 8300615$ ;  $7.498480 =$   
 $31512319$ .
8.  $3.100249 = 1259.64$ ;  $2.511391 = 324.632$ ;  $5.000000 = 100000$ ;  $8.696466 =$   
 $.0497125$ .
9.  $7.499467 = 31583985.5$ ;  $3.782115 = 6055$ ;  $3.842614 = 6960.08$ ;  $4.327379 =$   
 $21250.98$ .
10.  $5.599311 = 397476.1$ ;  $3.590806 = 3897.68$ ;  $5.477728 = 300419.31$ ;  $7.623683 =$   
 $42041942$ .
11.  $6.314887 = 2064842.8$ ;  $4.808914 = 64404.2$ ;  $2.552762 = 357.077$ ;  $3.983651 =$   
 $9630.555$ .
12.  $3.394677 = 2481.28$ ;  $4.312842 = 20551.4$ ;  $0.123363 = 1.32850$ ;  $3.519872 = 3310.34$ .
13.  $8.763323 = .00000057986$ ;  $3.778168 = .006000236$ ;  $7.740796 = .00000055055$ ;  
 $1.233799 = .171317$ .
14.  $5.755418 = .00003694$ ;  $0.622110 = 4.189$ ;  $3.473368 = .00297418$ ;  $4.147399 =$   
 $14041.03$ .
15.  $2.951043 = 893.394$ ;  $3.524617 = 3346.7$ ;  $3.398070 = .00250075$ ;  $4.783612 =$   
 $.000607593$ .
16.  $2.000000 = .01$ ;  $1.000000 = .000000001$ ;  $3.050035 = .0000112211$ ;  $5.000000 =$   
 $100000$ .

## DIVISION BY LOGARITHMS, pages 66—67.

1.  $1.919078 = 83$ ;  $2.778875 = 601$ ;  $1.924279 = 84$ ;  $2.096910 = 125$ .
2.  $2.986680 = 969.8$ ;  $3.698970 = 5000$ ;  $5.830170 = 758875.4$ ;  $2.775257 = 596.015$ .
3.  $1.809855 = .64544$ ;  $3.644712 = 4412.78$ ;  $3.477122 = 3000$ ;  $1.822584 = 66.4637$ .
4.  $0.494768 = 3.1244$ ;  $1.614317 = 41.145$ ;  $1.428589 = 26.828$ ;  $0.139814 = 1.3798$ .
5.  $0.472427 = 2.967762$ ;  $2.785908 = .06108$ ;  $2.385683 = .0243043$ ;  $2.571411 = .037274$ ;  $5.301030 = .000002$ ;  $4.301030 = .000002$ ;  $1.301030 = 20$ .
6.  $3.886534 = 7700.76 +$ ;  $1.999234 = .998236$ ;  $1.999489 = 99.8825$ ;  $3.763429 = 5800$ .
7.  $1.569001 = 37.0684$ ;  $1.425115 = .266143$ ;  $4.376859 = 23815.5$ ;  $1.378403 = 23.9003$ .
8.  $1.995636 = 99$ ;  $1.319142 = 20.8517$ ;  $1.854294 = 71.498$ ;  $0.793259 = 6.2124$ .
9.  $4.699490 = 5006$ ;  $4.514747 = 32715$ ;  $4.317415 = 20769$ ;  $2.096910 = 125$ .
10.  $0.942505 = 8.76$ ;  $2.525020 = 334.98$ ;  $5.291146 = 195500$ ;  $1.004364 = 10.1010$ .
11.  $1.832752 = .68038$ ;  $4.903504 = .000800763$ ;  $1.030734 = .107333$ ;  $2.509203 = 323$ ;  $5.778151 = 600000$ .
12.  $2.735031 = 543.288$ ;  $1.602689 = 40.058$ ;  $2.264818 = 18.4$ ;  $3.946651 = 8844.04$ .
13.  $1.940506 = 87.1978$ ;  $2.297735 = .0198488$ ;  $1.278331 = .189815$ ;  $0.833525 = 6.81592$ .
14.  $1.421422 = .265388$ ;  $1.421422 = .265388$ ;  $1.421422 = .265388$ ;  $3.421422 = 2653.88$ ;  $7.301030 = 20000000$ ;  $7.477122 = 30000000$ .
15.  $1.057101 = .11405$ ;  $2.537395 = 344.663$ ;  $5.003528 = .0000100816$ ;  $0.833525 = 6.816$ .
16.  $2.339894 = 218.723$ ;  $2.934196 = 859.4$ ;  $1.004751 = .1011$ ;  $7.505150 = 32000000$ ;  $5.028878 = .0000106875$ .
17.  $0 = 1$ ;  $13 = 10000000000000$ ;  $1 = .1$ ;  $2 = .01$ ;  $4 = 10000$ .

## NATURAL SINES AND COSINES, page 70.

## Natural Sines.

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| 1. 570774 | 3. 947463 | 5. 723895 | 7. 800000 |
| 2. 867085 | 4. 370352 | 6. 974228 | 8. 997630 |

## Natural Cosines, page 70.

|           |           |           |           |
|-----------|-----------|-----------|-----------|
| 1. 969227 | 3. 167237 | 5. 688000 | 7. 782397 |
| 2. 328958 | 4. 995612 | 6. 868805 | 8. 989472 |

## Arcs of Natural Sines, page 71.

|                          |                          |                          |                          |                           |
|--------------------------|--------------------------|--------------------------|--------------------------|---------------------------|
| 1. $63^{\circ} 53' 47''$ | 3. $53^{\circ} 7' 49''$  | 5. $26^{\circ} 21' 34''$ | 7. $47^{\circ} 48' 33''$ | 9. $48^{\circ} 46' 34''$  |
| 2. $21^{\circ} 44' 21''$ | 4. $66^{\circ} 59' 10''$ | 6. $11^{\circ} 45' 52''$ | 8. $31^{\circ} 57' 10''$ | 10. $73^{\circ} 44' 23''$ |

## Arcs of Natural Cosines, page 71.

|                          |                          |                         |                           |
|--------------------------|--------------------------|-------------------------|---------------------------|
| 1. $63^{\circ} 19' 58''$ | 4. $45^{\circ} 24' 39''$ | 7. $39^{\circ} 42' 4''$ | 10. $77^{\circ} 33' 15''$ |
| 2. $18^{\circ} 29' 12''$ | 5. $59^{\circ} 0' 47''$  | 8. $12^{\circ} 53' 4''$ | 11. $2^{\circ} 33' 48''$  |
| 3. $43^{\circ} 21' 52''$ | 6. $23^{\circ} 54' 9''$  | 9. $35^{\circ} 8' 32''$ | 12. $53^{\circ} 7' 48''$  |

## LOG. SINES, TANGENTS, SECANTS, ETC., page 74.

|                |                |                |                 |
|----------------|----------------|----------------|-----------------|
| 1. $9.202234$  | 4. $9.883934$  | 7. $9.774729$  | 10. $9.275658$  |
| 2. $10.185981$ | 5. $10.829843$ | 8. $9.895443$  | 11. $10.144904$ |
| 3. $9.989071$  | 6. $10.135990$ | 9. $10.308556$ | 12. $9.907590$  |

B B B

## LOG. SINES, TANGENTS, SECANTS, ETC., page 78.

| NO. | SINE.    | TANGENT.      | SECANT.       | COSINE.      | COTANGENT.    | COSECANT. |
|-----|----------|---------------|---------------|--------------|---------------|-----------|
| 1.  | 9°079607 | 9°082763      | 10°003156     | 9°996844     | 10°917237     | 10°920393 |
| 2.  | 9°611999 | 9°651805      | 10°039806     | 9°960194     | 10°348195     | 10°388001 |
| 3.  | 9°787595 | 9°890004      | 10°102409     | 9°897591     | 10°109996     | 10°212405 |
| 4.  | 9°923122 | 10°185903     | 10°262781     | 9°737219     | 9°814097      | 10°076878 |
| 5.  | 9°246845 | 9°253720      | 10°006876     | 9°993124     | 10°746280     | 10°753155 |
| 6.  | 9°975130 | 10°457990     | 10°482859     | 9°517141     | 9°542010      | 10°024870 |
| 7.  | 8°504189 | 8°504410      | 0°000221      | 9°999779     | 11°435590     | 1°495811  |
| 8.  | 9°999580 | 11°356298     | 1°356719      | 8°643281     | 8°643702      | 0°000421  |
| 9.  | 8°246654 | 8°246721      | 0°000068      | 9°999932     | 11°753279     | 1°753346  |
| 10. | 9°955206 | 10°319983     | 0°364777      | 9°635223     | 9°680017      | 0°044794  |
| 11. | 9°938922 | 0°244180      | 0°305259      | 9°694741     | 9°755820      | 0°061078  |
| 12. | 9°990926 | 10°684913     | 0°693987      | 9°306013     | 9°315087      | 0°009074  |
| 13. | 8°668140 | 17. 8°361681  | 21. 10°348195 | 25. 8°024643 | 29. 10°714159 |           |
| 14. | 9°217118 | 18. 9°505271  | 22. 10°100598 | 26. 8°658227 | 30. 9°972464  |           |
| 15. | 8°504188 | 19. 8°297036  | 23. 10°203779 | 27. 8°305785 |               |           |
| 16. | 6°297326 | 20. 11°263695 | 24. 8°546002  | 28. 8°258261 |               |           |

## ARCS OF LOG. SINES, page 80.

|    |             |    |           |    |            |     |           |     |             |
|----|-------------|----|-----------|----|------------|-----|-----------|-----|-------------|
| 1. | 33° 26' 48" | 4. | 2° 17' 7" | 7. | 18° 26' 6" | 10. | 0° 9' 50" | 13. | 52° 35' 30" |
| 2. | 57 30 53    | 5. | 19 15 35  | 8. | 39 7 15    | 11. | 37 38 20  | 14. | 4 1 28      |
| 3. | 2 55 26     | 6. | 58 15 30  | 9. | 54 13 20   | 12. | 70 34 18  | 15. | 1 39 39     |

## ARCS OF LOG. COSINES, page 80.

|    |             |    |           |    |             |     |            |     |             |
|----|-------------|----|-----------|----|-------------|-----|------------|-----|-------------|
| 1. | 52° 13' 35" | 4. | 8° 6' 31" | 7. | 70° 47' 25" | 10. | 31° 9' 33" | 13. | 89° 38' 20" |
| 2. | 55 45 8     | 5. | 81 18 0   | 8. | 80 37 20    | 11. | 3 56 40    | 14. | 84 15 39    |
| 3. | 89 13 8     | 6. | 79 11 16  | 9. | 88 40 54    | 12. | 88 54 16   | 15. | 84 4 38     |

## ARCS OF LOG. SECANTS, page 80.

|    |             |    |           |    |             |    |             |     |            |
|----|-------------|----|-----------|----|-------------|----|-------------|-----|------------|
| 1. | 14° 23' 15" | 3. | 3° 24' 0" | 5. | 79° 39' 51" | 7. | 18° 22' 17" | 9.  | 61° 4' 15" |
| 2. | 51 28 50    | 4. | 26 33 0   | 6. | 84 19 47    | 8. | 88 41 42    | 10. | 86 22 57   |

## ARCS OF LOG. COSECANTS, page 80.

|    |            |    |           |    |            |     |             |     |             |
|----|------------|----|-----------|----|------------|-----|-------------|-----|-------------|
| 1. | 26° 43' 0" | 4. | 6° 5' 13" | 7. | 5° 43' 39" | 10. | 58° 15' 30" | 13. | 78° 22' 32" |
| 2. | 34 1 14    | 5. | 49 11 9   | 8. | 1 57 4     | 11. | 7 13 56     | 14. | 60 13 52    |
| 3. | 5 40 16    | 6. | 2 4 7     | 9. | 3 54 45    | 12. | 4 46 56     | 15. | 2 56 20     |

## ARCS OF LOG. TANGENT, page 80.

|    |            |    |             |    |             |     |             |     |             |
|----|------------|----|-------------|----|-------------|-----|-------------|-----|-------------|
| 1. | 77° 0' 23" | 4. | 81° 31' 58" | 7. | 86° 58' 16' | 10. | 23° 43' 17" | 13. | 48° 58' 24" |
| 2. | 45 0 24    | 5. | 54 43 26    | 8. | 1 8 7       | 11. | 35 3 32     | 14. | 2 40 10     |
| 3. | 62 42 21   | 6. | 5 13 23     | 9. | 27 28 54    | 12. | 87 0 46     | 15. | 1 2 18      |

## ARCS OF LOG. COTANGENTS, page 80.

|    |            |    |            |    |             |     |             |     |             |
|----|------------|----|------------|----|-------------|-----|-------------|-----|-------------|
| 1. | 61° 2' 39" | 4. | 41° 1' 35" | 7. | 88° 46' 54" | 10. | 82° 49' 23" | 13. | 88° 20' 53" |
| 2. | 7 34 16    | 5. | 11 0 41    | 8. | 44 20 2     | 11. | 8 30 34     | 14. | 76 40 15    |
| 3. | 27 16 43   | 6. | 3 37 50    | 9. | 86 32 24    | 12. | 88 55 35    | 15. | 0 29 16     |

## MISCELLANEOUS EXAMPLES.

For practice in natural and logarithmic Sines, Tangents, and Secants, *page 80.*

- (1.) Nat. sine  $\cdot 432651$ , its common log. is  $9\ 636138$ , which is the log. sine required.
- (2.) Nat. tang.  $3$ , its common log. is  $10\ 477121$ , which is the log. tang. required.
- (3.) Log.  $9\ 236713$ , its corresponding nat. no. is  $\cdot 172470$ , the nat. cos. required.
- (4.) The given log. tang.  $9\ 850593$ , being subtracted from  $20$ , gives  $10\ 149407$ , the log. cotang.
- (5.) The nat. sine of  $68^{\circ} 45' 24''$  is  $\cdot 932050$ , the log. of which, or  $9\ 969439$ , is its log. sine, which, being subtracted from  $20$ , leaves  $10\ 030561$  for the log. cosec.
- (6.) The log. sec.  $11\ 024680$  subtracted from  $20$ , leaves  $8\ 975320$ , the log. cosine, the nat. no. corresponding to which, or  $\cdot 094476$ , is the nat. cosine sought.
- (7.) 1. The quantity  $9\ 450981$  is found in the tables to be the log. cosine of the arc  $73^{\circ} 35' 31''$ . 2. The nat. no. corresponding to the given log. is  $\cdot 282476$ , which is the nat. cos. of  $73^{\circ} 35' 31''$ , the arc  $A$  sought.
- (8.) 1. The square of radius, or  $1$ , divided by the nat. sec.  $2\ 005263$ , gives  $\cdot 498688$ , the nat. cosine of  $A$ , which is found in the tables of nat. cosines, to correspond to  $60^{\circ} 5' 12''$  the value  $A$ . 2. The common log. of the nat. sec.  $2\ 005263$  is  $0\ 302171$ , which is found to be the log. sec. of  $60^{\circ} 5' 12''$ , the arc  $A$  sought.

DIFFERENCE OF LATITUDE, *page 92.*

- |              |              |              |              |             |
|--------------|--------------|--------------|--------------|-------------|
| 1. $203' N.$ | 3. $293' S.$ | 5. $795' N.$ | 7. $610' S.$ | 9. $94' N.$ |
| 2. $470 S.$  | 4. $330 N.$  | 6. $157 S.$  | 8. $459 N.$  |             |

MERIDIONAL DIFFERENCE OF LATITUDE, *page 92.*

- |         |           |          |           |          |          |
|---------|-----------|----------|-----------|----------|----------|
| 1. $97$ | 2. $2426$ | 3. $345$ | 4. $1216$ | 5. $932$ | 6. $260$ |
|---------|-----------|----------|-----------|----------|----------|

LATITUDE IN, *page 93.*

- |                       |                      |                       |                       |                         |
|-----------------------|----------------------|-----------------------|-----------------------|-------------------------|
| 1. $34^{\circ} 2' N.$ | 3. $0^{\circ} 8' N.$ | 5. $2^{\circ} 48' S.$ | 7. $0^{\circ} 20' S.$ | 9. Equator.             |
| 2. $27\ 54 N.$        | 4. $3\ 1 N.$         | 6. $2\ 54 S.$         | 8. Equator.           | 10. $39^{\circ} 14' S.$ |

MIDDLE LATITUDE, *page 94.*

- |                     |                               |                     |                                |                                |                     |
|---------------------|-------------------------------|---------------------|--------------------------------|--------------------------------|---------------------|
| 1. $17^{\circ} 19'$ | 2. $2^{\circ} 10\frac{1}{2}'$ | 3. $35^{\circ} 37'$ | 4. $61^{\circ} 31\frac{1}{2}'$ | 5. $53^{\circ} 12\frac{1}{2}'$ | 6. $64^{\circ} 31'$ |
|---------------------|-------------------------------|---------------------|--------------------------------|--------------------------------|---------------------|

DIFFERENCE OF LONGITUDE, *page 95.*

- |              |              |              |              |              |                |
|--------------|--------------|--------------|--------------|--------------|----------------|
| 1. $300' E.$ | 3. $716' W.$ | 5. $270' E.$ | 7. $368' E.$ | 9. $180' W.$ | 11. $2835' E.$ |
| 2. $507 E.$  | 4. $260 W.$  | 6. $422 W.$  | 8. $420 W.$  | 10. $412 E.$ | 12. $1200 W.$  |

LONGITUDE IN, *page 96.*

- |                       |                       |                       |                       |
|-----------------------|-----------------------|-----------------------|-----------------------|
| 1. $7^{\circ} 38' W.$ | 2. $1^{\circ} 18' E.$ | 3. $31^{\circ} 4' E.$ | 4. $0^{\circ} 30' W.$ |
| 5. $1\ 15 E.$         | 6. $0\ 45 W.$         | 7. $39\ 10 W.$        | 8. $92\ 9 E.$         |
| 9. $103\ 56 E.$       | 10. $178\ 26 W.$      | 11. $178\ 57 E.$      | 12. $179\ 59 E.$      |

LEEWAY--CORRECTED COURSES, *page 105.*

- |                                   |                                     |                                      |   |
|-----------------------------------|-------------------------------------|--------------------------------------|---|
| $\times$ 1. S.W. $\frac{1}{2} S.$ | $\nabla$ 2. S.S.W. $\frac{1}{4} W.$ | $\downarrow$ 3. N. $\frac{1}{4} E.$  | $\nearrow$ 4. N.E. $\frac{1}{2} E.$       |
| $\perp$ 5. E. by S.               | $\nwarrow$ 6. N.W. by W.            | $\rightarrow$ 7. W. $\frac{1}{4} S.$ | $\searrow$ 8. N.E. by E. $\frac{3}{4} E.$ |

### VARIATION—TRUE COURSES, page 110.

|                                 |                               |                                |
|---------------------------------|-------------------------------|--------------------------------|
| 1. N.E.                         | 2. S.S.E.                     | 3. W.S.W.                      |
| 4. N.W.                         | 5. N.N.E.                     | 6. S.E.                        |
| 7. S.S.W.                       | 8. N.W. by W.                 | 9. S.E. by E. $\frac{1}{2}$ E. |
| 10. N. $\frac{3}{4}$ E.         | 11. S. $\frac{3}{4}$ E.       | 12. N. $\frac{1}{4}$ W.        |
| 13. S.W. by W. $\frac{1}{2}$ W. | 14. E. by S. $\frac{1}{2}$ S. | 15. E.N.E.                     |
| 16. W. by S. $\frac{1}{2}$ S.   |                               |                                |

### DEVIATION—TRUE COURSES, page 137.

|                                     |                                      |                                      |                                      |
|-------------------------------------|--------------------------------------|--------------------------------------|--------------------------------------|
| 1. N. $38^{\circ}59'$ E.            | 8. S. $48^{\circ}55'$ E.             | 15. S. $28^{\circ}57'$ W.            | 22. S. $78^{\circ}10'$ W.            |
| 2. N. $0^{\circ}22'$ W.             | 9. N. $19^{\circ}25\frac{1}{2}'$ E.  | 16. S. $4^{\circ}38\frac{1}{2}'$ E.  | 23. S. $56^{\circ}2\frac{1}{2}'$ W.  |
| 3. N. $20^{\circ}58\frac{1}{2}'$ W. | 10. S. $0^{\circ}16'$ W.             | 17. S. $73^{\circ}10\frac{1}{2}'$ W. | 24. S. $4^{\circ}34\frac{1}{2}'$ W.  |
| 4. S. $43^{\circ}39\frac{1}{2}'$ W. | 11. S. $84^{\circ}7\frac{1}{2}'$ W.  | 18. N. $32^{\circ}24\frac{1}{2}'$ E. | 25. S. $63^{\circ}11\frac{1}{2}'$ W. |
| 5. S. $84^{\circ}7\frac{1}{2}'$ W.  | 12. S. $36^{\circ}12\frac{1}{2}'$ E. | 19. N. $3^{\circ}0'$ E.              | 26. S. $74^{\circ}3\frac{1}{2}'$ E.  |
| 6. S. $24^{\circ}5\frac{1}{2}'$ W.  | 13. S. $87^{\circ}0'$ E.             | 20. N. $89^{\circ}55'$ W.            | 27. S. $79^{\circ}16'$ E.            |
| 7. S. $89^{\circ}35'$ E.            | 14. N. $59^{\circ}12\frac{1}{2}'$ W. | 21. S. $9^{\circ}33'$ E.             | 28. N. $77^{\circ}46'$ W.            |

### MAGNETIC BEARINGS OF OBJECTS, page 140.

|                          |                          |                           |
|--------------------------|--------------------------|---------------------------|
| 1. N. $78^{\circ}10'$ E. | 5. N. $84^{\circ}54'$ E. | 9. S. $86^{\circ}2'$ W.   |
| 2. S. $72^{\circ}32'$ E. | 6. S. $11^{\circ}53'$ W. | 10. S. $2^{\circ}39'$ E.  |
| 3. N. $5^{\circ}14'$ E.  | 7. N. $8^{\circ}37'$ E.  | 11. N. $72^{\circ}33'$ W. |
| 4. S. $10^{\circ}16'$ E. | 8. S. $89^{\circ}13'$ W. | 12. N. $3^{\circ}6'$ W.   |

### LEEWAY, VARIATION, and DEVIATION—TRUE COURSES page 143.

|                                 |                                   |                                   |
|---------------------------------|-----------------------------------|-----------------------------------|
| 1. E. by S. $\frac{1}{4}$ S.    | 13. N. $64^{\circ}$ E.            | 25. S. $36^{\circ}$ E.            |
| 2. N.W. by N.                   | 14. N. $78^{\circ}$ W.            | 26. S. $9^{\circ}$ E.             |
| 3. N. by W.                     | 15. S. $85^{\circ}$ E.            | 27. N. $59^{\circ}$ E.            |
| 4. N.N.W.                       | 16. S. $79^{\circ}$ W.            | 28. N. $89^{\circ}$ E.            |
| 5. S.E. by E.                   | 17. S. $6^{\circ}$ E.             | 29. S. $60^{\circ}$ W.            |
| 6. S.E.                         | 18. S. $73^{\circ}$ W.            | 30. N. $10^{\circ}$ E.            |
| 7. N.W. $\frac{1}{2}$ N.        | 19. S. $37^{\circ}$ W.            | 31. S. $60\frac{1}{2}^{\circ}$ E. |
| 8. South                        | 20. S. $57\frac{1}{2}^{\circ}$ W. | 32. S. $77^{\circ}$ E.            |
| 9. S. by W. $\frac{1}{4}$ W.    | 21. S. $77^{\circ}$ E.            | 33. S. $76^{\circ}$ W.            |
| 10. S.E. by E. $\frac{3}{4}$ E. | 22. N. $84^{\circ}$ W.            | 34. N.E. $\frac{1}{2}$ E.         |
| 11. W. $\frac{1}{2}$ N.         | 23. S. $81^{\circ}$ E.            | 35. N. $\frac{3}{4}$ W.           |
| 12. S. $44^{\circ}$ E.          | 24. S. $32^{\circ}$ W.            | 36. W. $\frac{1}{4}$ N.           |

### NAPIER'S DIAGRAM.

#### Deviations, page 148.

(a) CURVE A.— $10^{\circ}$  E.;  $19^{\circ}$  E.;  $24^{\circ}$  W.;  $18\frac{1}{2}^{\circ}$  W.;  $25^{\circ}$  W.;  $2^{\circ}$  E.;  $23\frac{1}{2}^{\circ}$  E.;  $17^{\circ}$  W.;  $24\frac{1}{2}^{\circ}$  E.;  $24^{\circ}$  W.;  $15^{\circ}$  E.

(b) CURVE B.— $3^{\circ}$  E.;  $5\frac{1}{2}^{\circ}$  E.;  $5^{\circ}$  W.;  $8\frac{1}{2}^{\circ}$  W.;  $10\frac{1}{2}^{\circ}$  W.;  $0^{\circ}$ ;  $8^{\circ}$  E.;  $7\frac{1}{2}^{\circ}$  W.;  $10^{\circ}$  E.;  $6^{\circ}$  W.;  $5\frac{1}{2}^{\circ}$  E.

(c) CURVE C.— $15^{\circ}$  W.;  $11\frac{1}{2}^{\circ}$  W.;  $0\frac{1}{2}^{\circ}$  W.;  $28\frac{1}{2}^{\circ}$  E.;  $10\frac{1}{2}^{\circ}$  E.;  $6^{\circ}$  E.;  $14\frac{1}{2}^{\circ}$  W.;  $28\frac{1}{2}^{\circ}$  E.;  $24\frac{1}{2}^{\circ}$  W.;  $2^{\circ}$  E.

#### Correct Magnetic Courses, page 150.

CURVE A.—N.  $66^{\circ}$  W.; S.  $87^{\circ}$  E.; S.  $23^{\circ}$  E.; S.  $54^{\circ}$  W.; S.  $63\frac{1}{2}^{\circ}$  W.; N.  $68^{\circ}$  E.; S.  $31\frac{1}{2}^{\circ}$  E.; S.  $63^{\circ}$  W.; N.  $41\frac{1}{2}^{\circ}$  W.; S.  $16^{\circ}$  W.

CURVE B.—N.  $56^{\circ}$  W.; N.  $86^{\circ}$  E.; S.  $22\frac{1}{2}^{\circ}$  E.; S.  $58\frac{1}{2}^{\circ}$  W.; S.  $67^{\circ}$  W.; N.  $61^{\circ}$  E.; S.  $37^{\circ}$  E.; S.  $67^{\circ}$  W.; N.  $31\frac{1}{2}^{\circ}$  E.; S.  $18^{\circ}$  W.

CURVE C.—N.  $37^{\circ}$  W.; N.  $33\frac{1}{2}^{\circ}$  E.; S.  $75^{\circ}$  E.; N.  $62^{\circ}$  W.; N.  $58^{\circ}$  W.; N.  $20^{\circ}$  E.; N.  $80^{\circ}$  E.; N.  $58\frac{1}{2}^{\circ}$  W.; N.  $27\frac{1}{2}^{\circ}$  W.; S.  $76^{\circ}$  W.



## Compass Courses, page 151.

CURVE A.—N.  $79^{\circ}$  W.; N.  $27^{\circ}$  E.; S.  $21\frac{1}{2}^{\circ}$  W.; N.  $9^{\circ}$  E.; N.  $41\frac{1}{2}^{\circ}$  E.; N.  $78^{\circ}$  E.; S.  $66^{\circ}$  W.; N.  $21\frac{1}{2}^{\circ}$  E.; N.  $86^{\circ}$  W.

CURVE B.—N.  $83^{\circ}$  W.; N.  $31\frac{1}{2}^{\circ}$  E.; S.  $20\frac{1}{2}^{\circ}$  W.; N.  $10\frac{1}{2}^{\circ}$  E.; N.  $47^{\circ}$  E.; N.  $83\frac{1}{2}^{\circ}$  E.; S.  $61\frac{1}{2}^{\circ}$  W.; N.  $25^{\circ}$  E.; N.  $89^{\circ}$  W.

CURVE C.—S.  $21^{\circ}$  W.; N.  $78^{\circ}$  E.; South; N.  $35\frac{1}{2}^{\circ}$  E.; S.  $73^{\circ}$  E.; S.  $31^{\circ}$  E.; S.  $8^{\circ}$  W.; N.  $65\frac{1}{2}^{\circ}$  E.; S.  $18^{\circ}$  W.

## DIFFERENCE OF LATITUDE AND DEPARTURE, page 169.

| NO. | DIFF. LAT.         | DEF.               | NO. | DIFF. LAT.        | DEF.              |
|-----|--------------------|--------------------|-----|-------------------|-------------------|
| 1.  | $27^{\circ}7'$ S.  | $11^{\circ}5'$ E.  | 8.  | $10^{\circ}8'$ S. | $33^{\circ}3'$ W. |
| 2.  | $9^{\circ}4'$ S.   | $47^{\circ}1'$ E.  | 9.  | $22^{\circ}9'$ N. | $8^{\circ}8'$ W.  |
| 3.  | $100^{\circ}8'$ S. | $91^{\circ}3'$ W.  | 10. | $10^{\circ}9'$ S. | $23^{\circ}3'$ W. |
| 4.  | $12^{\circ}3'$ N.  | $83^{\circ}1'$ W.  | 11. | $2^{\circ}5'$ S.  | $14^{\circ}5'$ W. |
| 5.  | $28^{\circ}8'$ S.  | $48^{\circ}0'$ E.  | 12. | $27^{\circ}3'$ N. | $13^{\circ}9'$ W. |
| 6.  | $142^{\circ}7'$ S. | $173^{\circ}9'$ W. | 13. | $7^{\circ}4'$ S.  | $42^{\circ}2'$ W. |
| 7.  | $44^{\circ}5'$ N.  | $177^{\circ}5'$ E. | 14. | $33^{\circ}2'$ N. | $10^{\circ}8'$ W. |

## COURSES AND DISTANCES, page 171.

| NO. | COURSES.                      | DIST.            | NO. | COURSES.                     | DIST.            |
|-----|-------------------------------|------------------|-----|------------------------------|------------------|
| 1.  | S. $19^{\circ}$ E.            | $77'$            | 6.  | N. $44^{\circ}$ E.           | $52\frac{1}{2}'$ |
| 2.  | N. $67^{\circ}$ E.            | $186\frac{1}{2}$ | 7.  | S. $55^{\circ}$ W.           | 93               |
| 3.  | N. $66\frac{1}{2}^{\circ}$ W. | 161              | 8.  | S. $6^{\circ}$ W.            | $161\frac{1}{2}$ |
| 4.  | S. $21^{\circ}$ E.            | $105\frac{1}{2}$ | 9.  | S. $2\frac{1}{2}^{\circ}$ W. | 173              |
| 5.  | N. $30^{\circ}$ W.            | 480              | 10. | N. $58^{\circ}$ E.           | 310              |

## TRAVERSE SAILING, page 176.

| NO. | D. LAT.            | DEF.               | LAT. IN            | COURSE.                       | DIST.            |
|-----|--------------------|--------------------|--------------------|-------------------------------|------------------|
| 1.  | $95^{\circ}2'$ S.  | $92^{\circ}1'$ W.  | $51^{\circ}23'$ N. | S. $44^{\circ}$ W.            | $132'$           |
| 2.  | $20^{\circ}0'$ S.  | $128^{\circ}8'$ W. | $53^{\circ}52'$ N. | S. $81^{\circ}$ W.            | 130              |
| 3.  | $375^{\circ}6'$ S. | $0^{\circ}0'$      | $2^{\circ}26'$ S.  | S.                            | 376              |
| 4.  | $0^{\circ}0'$      | $76^{\circ}8'$ E.  | $19^{\circ}0'$ S.  | E.                            | 77               |
| 5.  | $75^{\circ}1'$ S.  | $77^{\circ}8'$ E.  | $0^{\circ}15'$ S.  | S. $46^{\circ}$ E.            | 108              |
| 6.  | $120^{\circ}0'$ N. | $149^{\circ}0'$ E. | $0^{\circ}50'$ N.  | N. $51^{\circ}$ E.            | 192              |
| 7.  | $31^{\circ}0'$ S.  | $8^{\circ}4'$ W.   | $46^{\circ}41'$ N. | S. $15^{\circ}$ W.            | 32               |
| 8.  | $24^{\circ}7'$ S.  | $145^{\circ}1'$ W. | $34^{\circ}36'$ N. | N. $80^{\circ}$ W.            | 147              |
| 9.  | $55^{\circ}7'$ N.  | $129^{\circ}9'$ W. | $35^{\circ}39'$ S. | N. $23\frac{1}{2}^{\circ}$ W. | $139\frac{1}{2}$ |
| 10. | $150^{\circ}3'$ S. | $56^{\circ}8'$ W.  | $0^{\circ}44'$ S.  | S. $21^{\circ}$ W.            | 161              |

## PARALLEL SAILING, page 178.

|                       |                        |                        |                        |
|-----------------------|------------------------|------------------------|------------------------|
| 1. $250^{\circ}3'$ W. | 2. $344^{\circ}4'$ E.  | 3. $519^{\circ}2'$ W.  | 4. $471^{\circ}3'$ W.  |
| 5. $148^{\circ}0'$ W. | 6. $512^{\circ}5'$ E.  | 7. $612^{\circ}0'$ W.  | 8. $113^{\circ}8'$ E.  |
| 9. $117^{\circ}7'$ W. | 10. $408^{\circ}0'$ E. | 11. $372^{\circ}2'$ E. | 12. $594^{\circ}5'$ E. |

page 179.

- |  |                                       |
|--|---------------------------------------|
| 1. N. $64^{\circ}17'$ $30^{\circ}$ W., distance 396.7 miles. | 2. 893.4 miles.                       |
| 4. S. $79^{\circ}8'45''$ E., distance 96.5 miles.            | 5. $60^{\circ}$ and $70^{\circ}32'$ . |
| 6. 61.6 miles, or $1^{\circ}1'6''$                           | 7. West, distance 864.1 miles.        |

## MIDDLE LATITUDE SAILING, page 182.

|    |               |            |                    |               |                     |
|----|---------------|------------|--------------------|---------------|---------------------|
| 1. | D. lat. 113'3 | Dep. 273'5 | Lat. in 27° 28' N. | D. long. 305' | Long. in 54° 55' W. |
| 2. | " 99'9        | " 187'0    | " 34 10 N.         | " 224         | " 29 8 W.           |
| 3. | " 89'8        | " 189'8    | " 41 0 S.          | " 248         | " 70 12 E.          |
| 4. | " 165'6       | " 223'3    | " 49 10 S.         | " 334         | " 175 58 W.         |
| 5. | " 96'7        | " 318'7    | " 18 52 N.         | " 338         | " 175 12 E.         |
| 6. | " 114'6       | " 122'9    | " 0 59 S.          | " 123         | " 27 47 W.          |

## MERCATOR'S SAILING, page 186.

| NO. | D. LAT. | M. D. LAT. | D. LONG. | COURSE.       | DIST. |
|-----|---------|------------|----------|---------------|-------|
| 1.  | 97 N.   | 125        | 131 E.   | N. 46° 21' E. | 141   |
| 2.  | 85 S.   | 130        | 76 E.    | S. 30 19 E.   | 98    |
| 3.  | 280 N.  | 497        | 368 E.   | N. 36 31 E.   | 348   |
| 4.  | 81 N.   | 128        | 227 W.   | N. 60 35 W.   | 165   |
| 5.  | 230 S.  | 500        | 270 E.   | S. 28 22 E.   | 261   |
| 6.  | 687 S.  | 785        | 3698 W.  | S. 78 1 W.    | 3309  |
| 7.  | 1232 N. | 1760       | 4732 E.  | N. 69 36 E.   | 3534  |
| 8.  | 115 N.  | 166        | 191 E.   | N. 49 0 E.    | 175   |
| 9.  | 1107 N. | 1230       | 1452 W.  | N. 49 44 W.   | 1713  |
| 10. | 779 S.  | 1080       | 1200 W.  | S. 48 1 W.    | 1165  |
| 11. | 1011 N. | 1139       | 3808 W.  | N. 73 21 W.   | 3528  |
| 12. | 792 S.  | 794        | 1254 E.  | S. 57 39½ E.  | 1480  |
| 13. | 128 N.  | 233        | 725 W.   | N. 72 11 W.   | 418   |
| 14. | 315 S.  | 524        | 365 E.   | S. 34 52 E.   | 384   |
| 15. | 731 S.  | 733        | 2459 E.  | S. 73 24 E.   | 2559  |
| 16. | 150 N.  | 274        | 354 E.   | N. 52 16 E.   | 245   |
| 17. | 4483 N. | 4842       | 3313 E.  | N. 34 23 E.   | 5432  |
| 18. | 1860 S. | 1884       | 412 E.   | S. 12 20 E.   | 1904  |
| 19. | 3355 N. | 3516       | 7587 W.  | N. 65 8 W.    | 7978  |
| 20. | 180 N.  | 190        | 1140 W.  | N. 80 32 W.   | 1094  |

DAY'S WORKS CORRECTED FOR LEEWAY, VARIATION, AND  
DEVIATION, page 208.

NOTE.—In the following key, the first line for each day's work is explained by the titles at the top of the page. The second line contains the True Courses. The third line contains the Diff. Lat. and Dep. corresponding to each course: their names are not given because these are easily seen from the courses in the second line.

| 1 | Courses.                   | Distance.                   | Diff. Lat.                 | Departure.                 | Lat. in.                   | Mid. lat.                 | Diff. long.                | Long. in.                 |
|---|----------------------------|-----------------------------|----------------------------|----------------------------|----------------------------|---------------------------|----------------------------|---------------------------|
|   | N. 63½° E.                 | 227'                        | 101'7 N.                   | 202'7 E.                   | 36° 57' N.                 | 36° 6'                    | 250½' E.                   | 71° 19½' W.               |
|   | N. 89° E. 19'<br>0'3. 19'0 | S. 43° E. 50'2<br>36'7 34'2 | S 71' E 38'3<br>12'5 36'2  | N 55° E 41'8<br>24'0 34'2  | N 3° W 41'6<br>41'5 2'2    | N 15° E 42'2<br>40'8 10'0 | N 82° E 36'7<br>5'1 36'3   | N 41° E 52'<br>39'2 34'1  |
| 2 | S. 77½° E.                 | 99'                         | 21'5 S.                    | 96'6 E.                    | 53° 45½' N.                | 53° 56'                   | 164' E.                    | 2° 39' E.                 |
|   | S. 68° E. 17'<br>6'4 15'8  | N. 73° E. 28<br>8'2 26'8    | S. 75° E. 31'<br>8'0 29'9  | N. 72° E. 20'<br>6'2 19'0  | S. 0° W. 10'<br>18'8 3'0   | S. 5° W. 13'<br>13'0 1'1  | S. 25° E. 10'<br>9'4 3'4   | N. 24° E. 15'<br>13'7 6'1 |
|   | N. 3° W. 6'<br>6'0 0'3     |                             |                            |                            |                            |                           |                            |                           |
| 3 | S. 71° W.                  | 167'                        | 53'7 S.                    | 158'4 W.                   | 36° 9' N.                  | 36° 36'                   | 197½' W.                   | 12° 17½' W.               |
|   | S. 40° W. 14'<br>10'7 9'0  | S. 26° W. 42'<br>37'7 18'4  | S. 48° W. 30'<br>20'1 22'3 | N. 62° W. 40'<br>23'0 43'3 | N 16° W. 41'1<br>39'4 11'3 | S. 3° E. 25'<br>25'0 1'3  | S. 57° W. 31'<br>16'9 26'0 | S. 79° W. 30'<br>5'7 29'4 |

| 4  | Courses.  | Distance.   | Diff. Lat.                        | Departure.                        | Lat. in.                          | Mid. lat.                         | Diff. long.                       | Long. in.                         |
|----|---|---|-----------------------------------|-----------------------------------|-----------------------------------|-----------------------------------|-----------------------------------|-----------------------------------|
|    | N. 71° W.   | 55½'  | 17' 7" N.                         | 52' 5" W.                         | 45° 54' S.                        | 46° 3'                            | 75½' W.                           | 3° 25½' W.                        |
|    | N. 50° W. 20'<br>12' 9" 15' 3"                                | S. 81° W. 26'<br>4' 1" 25' 7"                                     | N. 20° E. 33' 8"<br>30' 4" 14' 8" | S. 31° E. 21' 4"<br>17' 7" 12' 0" | N. 7° W. 24' 3"<br>8' 3" 22' 8"   | N. 64° E. 26' 3"<br>11' 5" 23' 6" | S. 56° W. 23' 2"<br>13' 0" 19' 2" | S. 62° W. 22' 5"<br>10' 6" 19' 9" |
| 5  | S. 45° W.   | 81'   | 57' 5" S.                         | 57' 5" W.                         | 34' 12½' N.                       | 34° 41'                           | 70' W.                            | 6° 46' W.                         |
|    | S. 87° W. 9'<br>0' 5" 9' 0"                                   | S. 20° W. 37' 7"<br>33' 0" 18' 3"                                 | N. 23° W. 45'<br>41' 4" 17' 6"    | N. 77° W. 31' 5"<br>7' 5" 32' 6"  | South 45' 3"                      | S. 29° W. 37' 5"<br>32' 8" 18' 2" | N. 71° E. 24' 8"<br>8' 1" 23' 5"  | S. 79° E. 15'<br>2' 9" 14' 7"     |
| 6  | N. 3° W.  | 28' 5"  | 28' 5" N.                         | 1' 6" W.                          | 30° 27' 5" N.                     | 30° 13'                           | 2' W.                             | 32° 52' E.                        |
|    | S. 3° E. 15'<br>15' 0" 0' 8"                                  | N. 75° W. 12'<br>3' 1" 11' 6"                                     | S. 63° E. 13'<br>5' 9" 11' 6"     | S. 10° E. 25'<br>24' 6" 4' 3"     | N. 8° E. 20'<br>19' 8" 2' 8"      | S. 76° W. 15'<br>3' 6" 14' 6"     | N. 11° W. 27'<br>26' 5" 5' 2"     | N. 20° E. 30'<br>28' 2" 10' 3"    |
| 7  | S. 56° W.   | 119'  | 66' 3" S.                         | 98' 5" W.                         | 45° 26' S.                        | 44° 53'                           | 139' W.                           | 179° 8' W.                        |
|    | N. 88° W. 18'<br>0' 6" 18' 0"                                 | N. 2° E. 37' 8"<br>37' 8" 1' 3"                                   | S. 86° W. 33' 6"<br>2' 3" 33' 5"  | S. 70° W. 47' 6"<br>0' 1" 46' 7"  | S. 16° W. 24' 7"<br>23' 7" 6' 8"  | S. 15° W. 37' 6"<br>36' 3" 0' 7"  | S. 8° E. 50'<br>49' 5" 7' 0"      | N. 26° E. 18'<br>16' 2" 7' 0"     |
| 8  | N. 70° W.   | 162'  | 56' 0" N.                         | 151' 6" E.                        | 63° 14' N.                        | 62° 46'                           | 331' 4" E.                        | 57° 46' W.                        |
|    | N. 66° E. 21'<br>8' 5" 19' 2"                                 | N. 71° E. 49' 7"<br>16' 2" 47' 0"                                 | N. 75° E. 17' 3"<br>4' 5" 16' 7"  | N. 35° E. 31'<br>27' 9" 19' 5"    | S. 28° W. 13' 5"<br>11' 9" 6' 3"  | S. 74° E. 21' 1"<br>5' 8" 20' 3"  | S. 2° W. 16' 8"<br>16' 8" 0' 6"   | N. 47° E. 49'<br>33' 4" 35' 8"    |
| 9  | S. 77½° E.  | 105'  | 22' 7" S.                         | 102' 5" E.                        | 59° 26' N.                        | 59° 37'                           | 202' 5" E.                        | 40° 31' 5" W.                     |
|    | S. 12° E. 14'<br>13' 7" 2' 9"                                 | S. 37° E. 18' 7"<br>14' 9" 11' 3"                                 | N. 11° W. 25' 2"<br>24' 7" 4' 8"  | S. 13° E. 21' 7"<br>21' 1" 4' 9"  | S. 51° E. 33' 3"<br>21' 0" 25' 0" | S. 3° W. 18' 4"<br>18' 4" 1' 3"   | S. 71° E. 24' 9"<br>8' 1" 23' 5"  | N. 79° E. 40' 8"<br>7' 8" 40' 1"  |
| 10 | N. 64° W.   | 115'  | 45' 8" N.                         | 103' 5" W.                        | 35° 20' S.                        | 35° 45'                           | 127½' W.                          | 112° 17½' W.                      |
|    | N. 87° W. 14'<br>0' 7" 14' 0"                                 | West 20' 5"   | N. 69° W. 17' 2"<br>6' 2" 16' 1"  | N. 36° W. 24'<br>19' 4" 14' 1"    | N. 8° W. 22' 3"<br>22' 1" 3' 1"   | N. 73° W. 31' 2"<br>9' 1" 29' 8"  | S. 88° W. 20' 3"<br>0' 7" 20' 3"  | S. 64° E. 16'<br>7' 0" 14' 4"     |
| 11 | N. 73° W.   | 136'  | 39' 9" N.                         | 130' 1" W.                        | 55° 19' S.                        | 55° 39'                           | 231' W.                           | 71° 7' W.                         |
|    | S. 82° W. 17'<br>2' 4" 16' 8"                                 | S. 88° W. 33' 6"<br>1' 2" 33' 6"                                  | N. 31° W. 23' 2"<br>19' 9" 12' 0" | N. 61° W. 44' 6"<br>21' 6" 30' 0" | S. 61° W. 47' 8"<br>23' 2" 41' 8" | N. 3° E. 29' 5"<br>26' 5" 1' 5"   | S. 45° E. 37' 8"<br>26' 7" 26' 7" | N. 34° W. 27'<br>22' 4" 15' 1"    |
| 12 | S. 53½° W.  | 84½'  | 50' 2" S.                         | 67' 8" W.                         | 57° 39' N.                        | 58° 4'                            | 128' W.                           | 8° 20' W.                         |
|    | N. 81° W. 15'<br>2' 3" 14' 8"<br>N. 82° E. 9'<br>1' 3" 8' 9"  | S. 75° W. 25'<br>6' 5" 24' 1"                                     | S. 2° W. 23'<br>23' 0" 0' 8"      | S. 36° W. 10'<br>15' 4" 11' 2"    | N. 21° W. 9'<br>8' 4" 3' 2"       | S. 14° W. 19'<br>18' 4" 4' 6"     | S. 49° W. 16'<br>10' 5" 12' 1"    | N. 27° W. 13'<br>11' 6" 5' 9"     |
| 13 | S. 3½° E.   | 8'  | 7' 8" S.                          | 0' 5" E.                          | 62° 17' S.                        | 62° 13'                           | 1' E.                             | 140° 18' E.                       |
|    | N. 66° E. 25'<br>10' 2" 22' 8"<br>N. 67° W. 3'<br>1' 2" 2' 8" | S. 45° E. 10'<br>7' 1" 7' 1"<br>S. 39° W. 22' 5"<br>17' 5" 14' 2" | N. 62° W. 14'<br>6' 6" 12' 4"     | S. 28° W. 13'<br>11' 5" 6' 1"     | N. 34° E. 13'<br>10' 8" 7' 3"     | N. 25° E. 8'<br>7' 3" 3' 4"       | S. 47° W. 7'<br>4' 8" 5' 1"       | S. 9° E. 3'<br>3' 0" 0' 5"        |
| 14 | S. 45° E.   | 110'  | 77' 3" S.                         | 78' 3" E.                         | 51° 37' S.                        | 50° 58'                           | 124½' E.                          | 22° 14½' E.                       |
|    | S. 39° W. 15'<br>11' 7" 9' 4"                                 | S. 12° E. 15' 3"<br>11' 4" 10' 2"                                 | S. 33° E. 25' 6"<br>21' 5" 13' 9" | N. 44° W. 24'<br>17' 3" 16' 7"    | N. 80° E. 22'<br>3' 8" 21' 7"     | S. 41° W. 21' 7"<br>16' 4" 14' 2" | S. 32' E. 47'<br>39' 9" 24' 9"    | N. 87° E. 48'<br>2' 5" 47' 9"     |
| 15 | West.   | 183'  | 0' 0"                             | 183' 0"                           | 46° 20' S.                        | 46° 20'                           | 265' W.                           | 178° 51' E.                       |
|    | N. 84° W. 23'<br>2' 4" 22' 9"                                 | S. 6° W. 48' 1"<br>47' 8" 5' 0"                                   | S. 61° W. 37' 2"<br>18' 0" 32' 5" | S. 24° W. 30'<br>27' 4" 12' 2"    | N. 75° W. 43' 5"<br>11' 3" 42' 0" | N. 60° W. 38' 4"<br>13' 8" 35' 9" | N. 20° W. 37' 8"<br>35' 5" 12' 9" | N. 33° W. 36'<br>30' 2" 19' 6"    |
| 16 | N. 5½° E.   | 135'  | 85' 8" N.                         | 104' 3" E.                        | 48° 3' N.                         | 47° 20'                           | 154' E.                           | 50° 56' W.                        |
|    | N. 34° E. 19'<br>15' 8" 10' 6"                                | N. 51° E. 20'<br>12' 6" 15' 5"                                    | N. 3° E. 33'<br>1' 7" 1' 7"       | S. 79° E. 30'<br>28' 3" 38' 3"    | S. 73° W. 35'<br>10' 2" 33' 5"    | N. 45° E. 40'<br>28' 3" 28' 3"    | N. 88° E. 32'<br>1' 1" 32' 0"     | N. 42° E. 17'<br>12' 6" 11' 4"    |
| 17 | N. 86° W.   | 171'  | 11' 8" N.                         | 170' 8" W.                        | 51° 20' 18" N.                    | 51° 14' 24"                       | 272' 9" W.                        | 3° 10' W.                         |
|    | N. 12° W. 25'<br>24' 5" 5' 2"                                 | S. 64° W. 40'<br>17' 5" 36' 0"                                    | S. 42° W. 48'<br>35' 7" 32' 1"    | S. 33° W. 33' 8"<br>28' 4" 18' 4" | N. 6° W. 37' 9"<br>37' 7" 4' 0"   | N. 21° W. 42' 5"<br>39' 7" 15' 2" | S. 73° W. 29' 2"<br>8' 5" 27' 9"  | West 32'                          |
| 18 | S. 74° E.   | 269'  | 74' 1" S.                         | 258' 1" E.                        | 36° 31' N.                        | 37° 8'                            | 323' 8" E.                        | 20° 24' E.                        |
|    | S. 78° E. 42'<br>8' 7" 41' 1"                                 | S. 81° E. 53'<br>8' 3" 52' 3"                                     | S. 79° E. 47'<br>9' 0" 46' 1"     | S. 9° E. 22'<br>21' 7" 3' 4"      | N. 17° W. 8'<br>7' 7" 2' 3"       | S. 76° E. 37'<br>9' 0" 35' 9"     | S. 59° E. 34' 5"<br>17' 8" 29' 6" | S. 82° E. 52' 5"<br>7' 3" 52' 0"  |

| 19 | Courses.          | Distance.     | Diff. lat.    | Departure.    | Lat. in.      | Mid. lat.     | Diff. long.   | Long. in.     |
|----|-------------------|---------------|---------------|---------------|---------------|---------------|---------------|---------------|
|    | S. 24° E.         | 92'           | 83° 8' S.     | 37° 9' E.     | 36° 14' S.    | 35° 32'       | 45' E.        | 29° 47' E     |
|    | S. 20° E. 15'     | S. 4° E. 6'   | N. 32° E. 11' | S. 42° E. 19' | S. 66° E. 13' | S. 55° E. 26' | N. 83° E. 7'  | N. 89° W. 13' |
|    | 13° 1' 7" 3       | 9° 0' 6" 0    | 9° 3' 5" 8    | 14° 1' 12" 7  | 5° 3' 11" 9   | 14° 9' 21" 3  | 0° 9' 6" 0    | 0° 2' 10" 0   |
|    | S. 63° E. 12. 22' | N. 10° E. 13' | S. 51° W. 69' |               |               |               |               |               |
|    | 10° 0' 17" 6      | 1° 0' 8" 4    | 37° 8' 45" 0  |               |               |               |               |               |
| 20 | S 11½° W          | 116'          | 113° 6' S     | 23° 3' W      | 27° 33' S.    | 26° 30'       | 26' W         | 44° 41' E     |
|    | S 31° W 17'       | S 6° W 17'    | N 83° W 87'   | S 51° W 27' 9 | S 59° E 28'   | S 43° W 87'   | N 75° E 12' 2 | S 27° W 11' 1 |
|    | 14° 1' 0" 5       | 10° 6' 1" 1   | 0° 8' 8" 7    | 17° 6' 21" 7  | 14° 4' 24" 0  | 6° 4' 5" 9    | 3° 2' 11" 8   | 10° 2' 5" 2   |
|    | S 51° E 11' 2     | S 11° E 6' 7  | S 20° W 35'   |               |               |               |               |               |
|    | 7° 1' 8" 7        | 0° 6' 1" 3    | 30° 6' 17" 0  |               |               |               |               |               |
| 21 | S 7½° E           | 219'          | 75° 0' S.     | 235° 4' E.    | 38° 57' S     | 38° 16'       | 252' E.       | 176° 58' W    |
|    | S 73° E 23'       | S 68° E 52' 9 | S 23° W 10' 5 | N 20° E 23' 4 | S 7° E 12'    | S 34° E 25' 1 | S 57° E 13'   | S 51° E 22' 2 |
|    | 6° 7' 22" 0       | 10° 8' 47" 0  | 9° 7' 4" 1    | 21° 0' 10" 3  | 11° 9' 1" 5   | 20° 8' 14" 0  | 7° 1' 13" 9   | 14° 0' 17" 3  |
|    | S 77° E 37' 6     | N 87° E 47' 8 |               |               |               |               |               |               |
|    | 8° 5' 30" 6       | 2° 5' 47" 9   |               |               |               |               |               |               |
| 22 | N 65° W           | 110'          | 49° 7' N      | 99° 3' W      | 55° 42' S     | 50° 3'        | 178' W        | 71° 35' W     |
|    | N 60° W 15'       | N 58° W 33'   | S 62° W 14' 8 | N 56° E 10' 2 | N 36° W 10' 6 | N 43° E 8' 3  | S 32° W 11'   | N 30° W 12' 4 |
|    | 5° 4' 14" 0       | 15° 9' 25" 4  | 7° 0' 13" 1   | 0° 1' 13" 4   | 13° 4' 0" 8   | 6° 1' 5" 7    | 9° 5' 5" 5    | 10° 7' 6" 2   |
|    | S 68° W 33'       | N 43° W 25' 9 | S 51° W 19'   |               |               |               |               |               |
|    | 11° 2' 27" 8      | 25° 8' 1" 8   | 12° 0' 14" 8  |               |               |               |               |               |
| 23 | S 12° W           | 204'          | 199° 7' S     | 43° 0' W      | 19° 25' S     | 17° 15'       | 45' W         | 179° 39' E    |
|    | South 15          | S 33° W 38'   | S 23° W 26'   | N. 79° W 34'  | S 11° W 50'   | S 15° E 45'   | S 60° E 26'   | S 5° W 24'    |
|    |                   | 31° 9' 20" 7  | 23° 6' 10" 2  | 0° 5' 33" 1   | 55° 0' 10" 7  | 43° 5' 11" 6  | 13° 0' 22" 5  | 23° 9' 2" 1   |

## ASTRONOMICAL DATES, page 219.

- |   |   |  |
|---|---|--|
| 1. Jan. 1 <sup>d</sup> 16 <sup>h</sup> 38 <sup>m</sup> 9 <sup>s</sup> | 2. Feb. 27 <sup>d</sup> 8 <sup>h</sup> 12 <sup>m</sup> 0 <sup>s</sup> | 3. Aug. 14 <sup>d</sup> 6 <sup>h</sup> 28 <sup>m</sup> 40 <sup>s</sup> |
| 4. Mar. 31 19 54 19   | 5. June 3 16 18 3   | 6. Aug. 31 20 10 52  |
| 7. Dec. 31 6 18 34  | 8. July 1 8 3 24  | 9. June 30 23 30 10  |
| 10. Oct. 1 0 10 12  | 11. 1871, Dec. 31 20 9 50   | 12. 1872, Dec. 31 12 44 12   |

## CIVIL DATE, page 219.

- |  |  |
|--|--|
| 1. Jan. 11th, 4 <sup>h</sup> 31 <sup>m</sup> 15 <sup>s</sup> A.M., | Feb. 3rd, 11 <sup>h</sup> 28 <sup>m</sup> 56 <sup>s</sup> P.M. |
| 2. Oct. 15th, 3 17 13 A.M.,  | Dec. 3rd, 5 16 12 P.M.   |
| 3. May 17th, 7 15 11 P.M.,   | Mar. 14th, 11 15 7 A.M.  |
| 4. April 1st, 11 10 16 A.M.,                                       | Mar. 21st, 7 24 12 P.M.  |
| 5. Sept. 1st, 8 10 54 P.M.,  | Sept. 1st, 8 10 54 A.M.  |
| 6. 1872, Jan. 1st, 9 50 41 P.M.,                                   | 1873, Jan. 1st, 10 48 56 A.M.                                  |

## DEGREES INTO TIME, page 220.

- |   |  |   |  |   |
|---|--|---|--|---|
| 1. 1 <sup>h</sup> 15 <sup>m</sup> 36 <sup>s</sup> | 0 <sup>h</sup> 50 <sup>m</sup> 43 <sup>s</sup> | 9 <sup>h</sup> 9 <sup>m</sup> 48 <sup>s</sup> | 6 <sup>h</sup> 24 <sup>m</sup> 43 <sup>s</sup> | 5 <sup>h</sup> 57 <sup>m</sup> 4 <sup>s</sup> |
| 2. 4 30 48  | 5 5 22   | 0 5 40  | 9 22 87  | 4 37 56                                       |
| 3. 0 3 54.4                                       | 3 16 17.33                                     | 0 1 47.2                                      | 0 56 10  | 8 41 16                                       |
| 4. 0 36 56  | 10 52 11.2                                     | 0 2 29.6                                      | 0 9 12.8                                       | 11 21 0                                       |
| 5. 7 14 28  | 0 41 48.9                                      | 0 9 56  | 5 38 50  | 0 2 18  |
| 6. 0 0 54   | 3 24 40.8                                      | 10 27 28                                      | 11 55 19                                       | 0 2 46.8                                      |

## TIME INTO DEGREES, page 221.

- |               |               |               |                 |
|---------------|---------------|---------------|-----------------|
| 1. 18° 28' 0" | 2. 58° 1' 0"  | 3. 10° 33' 0" | 4. 168° 50' 15" |
| 5. 67 16 15   | 6. 147 24 30  | 7. 8 44 33    | 8. 25 15 24     |
| 9. 89 46 0    | 10. 124 16 30 | 11. 5 22 43.5 | 12. 175 16 40   |
| 13. 0 58 0    | 14. 2 29 0    | 15. 0 13 0    | 16. 5 10 15     |
| 17. 9 14 0    | 18. 75 12 45  | 19. 179 59 15 | 20. 0 28 0      |

## GREENWICH DATES, page 224.

|   |   |  |
|---|---|--|
| 1. Jan. 6 <sup>d</sup> 8 <sup>h</sup> 8 <sup>m</sup> 0 <sup>s</sup> | 6. Oct. 31 <sup>d</sup> 21 <sup>h</sup> 22 <sup>m</sup> 10 <sup>s</sup> | 11. Dec. 27 <sup>d</sup> 23 <sup>h</sup> 19 <sup>m</sup> 30 <sup>s</sup> |
| 2. Feb. 12 22 4 19  | 7. Dec. 1 6 32 45   | 12. July 8 at noon.  |
| 3. Jan. 31 7 29 28  | 8. June 30 16 36 52   | 13. Jan. 31 13 45 20   |
| 4. Mar. 15 8 8 6  | 9. Aug. 3 23 50 22  | 14. May 31 18 24 40  |
| 5. May 15 6 6 0   | 10. Sept. 1 6 24 11   | 15. Mar. 2 0 5 40  |
|   | 16. 1872. Dec. 31 14 3 20   |  |

## SUN'S DECLINATION, page 231.

|                   |                   |                 |                 |
|-------------------|-------------------|-----------------|-----------------|
| 1. 22° 39' 14" S. | 2. 16° 49' 45" S. | 3. 4° 20' 9" N. | 4. 2° 18' 1" N. |
| 5. 19 15 5 N.     | 6. 14 47 22 N.    | 7. 23 4 17 N.   | 8. 14 36 54 S.  |
| 9. 8 18 12 N.     | 10. 3 24 25 S.    | 11. 23 20 56 S. | 12. 18 24 43 S. |
| 13. 20 21 38 S.   | 14. 12 31 0 S.    | 15. 0 18 31 N.  | 16. 17 16 6 N.  |
| 17. 23 27 26 N.   | 18. 0 14 22 N.    | 19. 18 51 51 N. | 20. 0 5 11 S.   |
| 21. 3 14 24 S.    | 22. 23 27 20 S.   | 23. 23 1 2 S.   | 24. 0 7 7 S.    |

## EQUATION OF TIME, page 235.

|  |   |  |  |
|--|---|--|--|
| 1. + 5 <sup>m</sup> 34 <sup>s</sup> .8 | 2. + 14 <sup>m</sup> 10 <sup>s</sup> .3 | 3. + 6 <sup>m</sup> 11 <sup>s</sup> .8 | 4. — 0 <sup>m</sup> 18 <sup>s</sup> .5 |
| 5. — 3 43 <sup>s</sup> .5              | 6. + 0 1 <sup>s</sup> .4                | 7. + 5 47 <sup>s</sup> .8              | 8. + 0 15 <sup>s</sup> .3              |
| 9. — 6 7 <sup>s</sup> .1               | 10. — 11 58 <sup>s</sup> .2             | 11. + 0 1 <sup>s</sup> .4              | 12. + 0 11 <sup>s</sup> .0             |
| 13. + 3 52 <sup>s</sup> .4             | 14. + 0 10 <sup>s</sup> .0              | 15. + 15 11 <sup>s</sup> .3            | 16. + 6 7 <sup>s</sup> .9              |
| 17. — 0 0 <sup>s</sup> .7              | 18. — 16 1 <sup>s</sup> .4              | 19. — 0 8 <sup>s</sup> .6              | 20. 0 0 <sup>s</sup> .0                |

## TRUE ALTITUDES, page 237.

|                |                |              |                |
|----------------|----------------|--------------|----------------|
| 1. 17° 52' 42" | 2. 48° 17' 14" | 3. 30° 2' 9" | 4. 76° 14' 16" |
| 5. 58 48 28    | 6. 24 56 49    | 7. 65 13 4   | 8. 85 22 51    |
| 9. 27 51 38    | 10. 67 22 16   | 11. 13 44 33 | 12. 11 45 28   |

## MERIDIAN ALTITUDES, page 243.

| NO. | GREEN. DATE.  | RED. DECL.     | TRUE ALT.   | LATITUDE.     | RAPER'S TRUE ALT. | LATITUDE.     |
|-----|---|----------------|-------------|---------------|-------------------|---------------|
| 1.  | Jan. 10 <sup>d</sup> 3 <sup>h</sup> 19 <sup>m</sup> 24 <sup>s</sup> | 21° 59' 44" S. | 68° 57' 22" | 43° 2' 22" S. | 68° 57' 19"       | 43° 2' 25" S. |
| 2.  | Jan. 31 21 20 36  | 17 13 36 S.    | 72 58 6     | 0 11 42 S.    | 72 58 3           | 0 11 39 S.    |
| 3.  | Mar. 7 18 0 48  | 4 43 32 S.     | 51 58 1     | 33 18 27 N.   | 51 57 51          | 33 18 37 N.   |
| 4.  | April 28 11 1 32  | 14 29 41 N.    | 82 35 15    | 7 4 56 N.     | 82 35 10          | 7 4 51 N.     |
| 5.  | May 1 21 51 48  | 15 32 27 N.    | 45 57 1     | 59 35 26 N.   | 45 56 55          | 59 35 32 N.   |
| 6.  | June 10 19 48 12  | 23 7 44 N.     | 42 37 28    | 24 14 48 S.   | 42 37 24          | 24 14 52 S.   |
| 7.  | July 20 10 26 32  | 20 29 16 N.    | 52 7 9      | 17 23 35 S.   | 52 6 57           | 17 23 47 S.   |
| 8.  | Aug. 19 5 30 0  | 12 31 13 N.    | 57 50 46    | 44 40 27 N.   | 57 50 45          | 44 40 28 N.   |
| 9.  | Aug. 25 17 51 48  | 10 18 26 N.    | 35 48 58    | 43 52 36 N.   | 35 48 54          | 43 52 40 N.   |
| 10. | Sept. 22 12 54 0  | 0 7 37 S.      | 41 42 33    | 48 9 50 N.    | 41 42 23          | 48 10 0 N.    |
| 11. | Oct. 23 6 0 48  | 11 43 10 S.    | 54 51 19    | 23 25 31 N.   | 54 51 13          | 23 25 37 N.   |
| 12. | Nov. 14 18 39 16  | 18 36 26 S.    | 67 56 49    | 3 26 45 N.    | 67 56 40          | 3 26 54 N.    |
| 13. | Dec. 9 20 18 40   | 22 58 31 S.    | 26 4 46     | 40 56 43 N.   | 26 4 36           | 40 56 53 N.   |
| 14. | Sept. 20 19 59 56   | 0 32 15 N.     | 56 37 9     | 32 50 36 S.   | 56 37 5           | 32 50 40 S.   |
| 15. | Mar. 19 18 2 0  | 0 0 0          | 61 58 10    | 28 1 50 N.    | 61 58 1           | 28 1 59 N.    |
| 16. | April 7 9 19 0  | 7 12 57 N.     | 90 13 41    | 6 59 16 N.    | 90 13 40          | 6 59 17 N.    |
| 17. | May 16 3 1 44   | 19 16 34 N.    | 86 50 41    | 16 7 15 N.    | 86 50 34          | 16 7 8 N.     |
| 18. | Sept. 22 17 57 0  | 0 12 33 S.     | 83 52 20    | 5 55 7 N.     | 83 52 14          | 5 55 13 N.    |
| 19. | Nov. 2 16 56 0  | 15 10 50 S.    | 70 42 48    | 34 28 2 S.    | 70 42 44          | 34 28 6 S.    |
| 20. | Sept. 22 11 35 52   | 0 6 21 S.      | 71 34 38    | 18 19 1 N.    | 71 34 32          | 18 19 9 N.    |
| 21. | Feb. 12 0 32 48   | 13 47 39 S.    | 30 4 42     | 46 7 39 N.    | 30 4 36           | 46 7 45 N.    |
| 22. | Mar. 19 18 49 0   | 0 46 N.        | 77 7 26     | 12 51 48 S.   | 77 7 23           | 12 51 51 S.   |
| 23. | Dec. 31 15 37 52  | 23 0 35 S.     | 54 38 7     | 12 21 18 N.   | 54 38 6           | 12 21 19 N.   |
| 24. | Sept. 30 19 14 40   | 3 20 51 S.     | 81 37 15    | 11 43 36 S.   | 81 37 11          | 11 43 40 S.   |

## AMPLITUDES, page 252.

|     | GREEN. DATE.  | RED. DECL.     | TRUE AMP.    | ERROR OF COMPASS | DEVIATION  |
|-----|---|----------------|--------------|------------------|------------|
| 1.  | Jan. 26 <sup>d</sup> 19 <sup>h</sup> 47 <sup>m</sup> 8 <sup>s</sup> | 18° 35' 27" S. | E. 23° 7' S. | 33° 8' W.        | 11° 18' W. |
| 2.  | Feb. 17 4 7 28  | 12 2 21 S.     | W. 14 45 S.  | 19 0 E.          | 11 20 E.   |
| 3.  | March 29 2 20 20  | 3 40 8 N.      | E. 4 4½ N.   | 26 34½ W.        | 2 54½ W.   |
| 4.  | April 4 19 53 0   | 6 15 10 N.     | W. 6 40 N.   | 0 0              | 6 40 W.    |
| 5.  | Nov. 6 22 5 8   | 16 27 19 S.    | E. 18 39½ S. | 21 28 E.         | 7 38 E.    |
| 6.  | May 25 16 44 0  | 21 11 21 N.    | E. 35 23 N.  | 43 49 W.         | 8 29 W.    |
| 7.  | June 2 9 56 26  | 22 19 42 N.    | W. 38 37½ N. | 26 4 W.          | 11 16 E.   |
| 8.  | July 14 2 15 42   | 21 35 42 N.    | E. 24 53 N.  | 22 56 E.         | 11 16 E.   |
| 9.  | Aug. 27 3 18 44   | 9 49 6 N.      | W. 10 31½ N. | 26 2 W.          | 2 52 W.    |
| 10. | Sept. 7 21 37 0   | 5 30 50 N.     | E. 6 3½ N.   | 6 3½ W.          | 6 3½ W.    |
| 11. | Oct. 1 5 29 50  | 3 30 47 S.     | E. 4 47 S.   | 13 13 E.         | 5 37 W.    |
| 12. | Sept. 22 6 1 12   | 0 0 54 S.      | E. 0 2 S.    | 2 47 W.          | 12 47 W.   |
| 13. | Nov. 2 21 27 40   | 15 14 22 S.    | W. 17 33 S.  | 4 57 E.          | 7 47 E.    |
| 14. | Dec. 3 21 13 48   | 22 19 39 S.    | W. 36 13 S.  | 2 28 W.          | 18 28 W.   |
| 15. | March 19 18 2 24  | 0 0 0          | 0 0          | 5 37½ W.         | 20 37½ W.  |
| 16. | Sept. 22 5 4 24   | 0 0 0          | 0 0          | 0 0              | 21 50 E.   |
| 17. | June 8 18 41 24   | 22 58 39 N.    | E. 22 58½ N. | 17 21 W.         | 2 54 E.    |
| 18. | Feb. 25 20 40 28  | 8 53 33 S.     | E. 19 16½ S. | 48 13½ W.        | 12 28½ W.  |
| 19. | April 30 15 43 40   | 5 19 58 N.     | W. 16 46½ N. | 0 6 W.           | 10 6 W.    |
| 20. | May 27 17 32 12   | 21 31 32 N.    | W. 33 1 N.   | 21 46 E.         | 1 31 E.    |
| 21. | June 18 1 24 20   | 23 26 8 N.     | E. 64 41 N.  | 39 23 E.         | 14 23 E.   |
| 22. | March 6 6 5 20  | 5 18 29 S.     | W. 6 13½ S.  | 23 5½ W.         | 5 15½ W.   |
| 23. | April 9 18 50 48  | 8 6 18 N.      | W. 13 52½ N. | 22 19 E.         | 6 9 E.     |
| 24. | Dec. 13 11 35 16  | 23 14 23 S.    | E. 32 4 S.   | 57 56 W.         | 38 36 W.   |

## TIDES, page 256.

|     | 8 <sup>h</sup> 27 <sup>m</sup> A.M. | 8 <sup>h</sup> 52 <sup>m</sup> P.M. |     | 11 <sup>h</sup> 58 <sup>m</sup> A.M. | No                             | P.M. |
|-----|-------------------------------------|-------------------------------------|-----|--------------------------------------|--------------------------------|------|
| 1.  | 8 <sup>h</sup> 27 <sup>m</sup> A.M. | 8 <sup>h</sup> 52 <sup>m</sup> P.M. | 12. | 11 <sup>h</sup> 58 <sup>m</sup> A.M. | No                             | P.M. |
| 2.  | 10 7 "                              | 10 33 "                             | 13. | No "                                 | 0 <sup>h</sup> 20 <sup>m</sup> | "    |
| 3.  | 4 30 "                              | 5 6 "                               | 14. | 2 56 "                               | 3 44 "                         | "    |
| 4.  | 11 33 "                             | No "                                | 15. | No "                                 |                                |      |
| 5.  | 2 12 "                              | 2 28 "                              | 16. | No "                                 | 0 1 "                          | "    |
| 6.  | No "                                | 0 23 "                              | 17. | 0 24 "                               | 0 43 "                         | "    |
| 7.  | 11 46 "                             | No "                                | 18. | 1 37 "                               | 2 26 "                         | "    |
| 8.  | No "                                | 0 2 "                               | 19. | No "                                 | 0 1 "                          | "    |
| 9.  | No "                                | 0 12 "                              | 20. | No "                                 | 0 7 "                          | "    |
| 10. | 11 5 "                              | 11 54 "                             | 21. | No "                                 | 0 21 "                         | "    |
| 11. | No "                                | 0 10 "                              | 22. | 0 56 "                               | 1 15 "                         | "    |

## TIDES.—FOREIGN PORTS, page 259.

- Constant — 0<sup>h</sup> 17<sup>m</sup> corr., for long. + 9<sup>m</sup>; No A.M., 0<sup>h</sup> 4<sup>m</sup> P.M.
- Constant + 3 18 corr., for long. — 29<sup>m</sup>; 11<sup>h</sup> 4<sup>m</sup> ,, 11 42 ,,
- Constant — 1 47 corr., for long. — 8<sup>m</sup>; 10 44 ,, 11 10 ,,
- Constant — 3 41 corr., for long. + 14<sup>m</sup>; 1 37 ,, 1 53 ,,
- Constant + 4 13 corr., for long. — 17<sup>m</sup>; 0 49 ,, 1 37 ,,
- Constant + 4 28 corr., for long. — 19<sup>m</sup>; 10 13 ,, 10 33 ,,
- Constant + 6 58 corr., for long. + 11<sup>m</sup>; 4 41 ,, 5 14 ,,
- Constant — 0 17 corr., for long. — 20<sup>m</sup>; 8 26 ,, 8 55 ,,
- Constant + 7 43 corr., for long. + 10<sup>m</sup>; 11 27 ,, 11 47 ,,
- Constant — 1 47 corr., for long. — 12<sup>m</sup>; 0 41 ,, 1 6 ,,

## FINDING DAILY RATE, page 261.

- |            |               |            |              |
|------------|---------------|------------|--------------|
| 1. 22 days | 3° 8 gaining  | 5. 31 days | 4° 2 losing  |
| 2. 18 "    | 3° 0 losing   | 6. 22 "    | 1° 1 losing  |
| 3. 17 "    | 4° 5 gaining  | 7. 15 "    | 6° 4 losing  |
| 4. 15 "    | 11° 2 gaining | 8. 14 "    | 7° 0 gaining |

## GREENWICH DATE, page 264.

| DAILY RATE.      | ACC. RATE.                       | GR. EN. DATE.   | DAILY RATE.       | ACC. RATE.                      | GREEN. DATE.  |
|------------------|----------------------------------|---|-------------------|---------------------------------|---|
| 1. 6° 8' losing  | 2 <sup>m</sup> 45 <sup>s</sup> 5 | Feb. 16 <sup>d</sup> 7 <sup>h</sup> 47 <sup>m</sup> 47 <sup>s</sup> | 7. 4° 8' gaining  | 7 <sup>m</sup> 5 <sup>s</sup> 7 | Nov. 8 <sup>d</sup> 16 <sup>h</sup> 26 <sup>m</sup> 59 <sup>s</sup> 7 |
| 2. 7° 1' gaining | 4 2 <sup>m</sup> 7               | April 28 4 21 37  | 8. 8° 7' losing   | 6 57 <sup>s</sup> 6             | Aug. 1 0 5 55 <sup>s</sup> 4  |
| 3. 3° 22' losing | 3 49 <sup>s</sup> 2              | May 7 6 25 16   | 9. 1° 5' losing   | 1 2 <sup>s</sup> 5              | May 1 13 28 15  |
| 4. 2° 2' gaining | 2 38 <sup>s</sup> 1              | June 25 20 56 30  | 10. 0° 8' losing  | 0 32 <sup>s</sup> 8             | Jan. 20 0 4 50  |
| 5. 5° 3' gaining | 6 28 <sup>s</sup> 9              | Oct 25 8 34 43  | 11. 1° 9' losing  | 4 29 <sup>s</sup> 2             | Sept. 27 16 39 18   |
| 6. 4° 0' losing  | 5 22                             | Jan. 19 12 33 28  | 12. 2° 6' gaining | 2 2 <sup>s</sup> 8              | April 16 5 33 40  |

## HOUR-ANGLE, page 268.

|   |   |   |  |  |
|---|---|---|--|--|
| 1. 4 <sup>h</sup> 26 <sup>m</sup> 34 <sup>s</sup> | 2. 2 <sup>h</sup> 50 <sup>m</sup> 42 <sup>s</sup> | 3. 4 <sup>h</sup> 50 <sup>m</sup> 20 <sup>s</sup> | 4. 4 <sup>h</sup> 6 <sup>m</sup> 56 <sup>s</sup> | 5. 4 <sup>h</sup> 8 <sup>m</sup> 45 <sup>s</sup> |
| 6. 2 33 42  | 7. 4 3 50 <sup>s</sup> 1                          | 8. 4 29 56  | 9. 3 29 20                                       |  |

## CHRONOMETERS, pages 278—279.

| NO. | RATE.    | GREEN. DATE.  | RED. DECL.     | TRUE ALT.  | IQ. TIME.                       | HOUR-ANGLE.                                    | LONG.                   |
|-----|----------|---|----------------|------------|---------------------------------|--|-------------------------|
| 1.  | — 9° 8'  | Jan. 1 <sup>d</sup> 19 <sup>h</sup> 32 <sup>m</sup> 13 <sup>s</sup> 6 | 22° 58' 33" S. | 4° 19' 18" | + 4 <sup>m</sup> 2 <sup>s</sup> | 2 <sup>h</sup> 58 <sup>m</sup> 27 <sup>s</sup> | 23° 20' 15" E.          |
| 2.  | + 7° 6'  | Feb. 18 19 45 57  | 11 27 38 S.    | 21 34 15   | + 14 8                          | 4 45 51  | 4 25 0 W.               |
| 3.  | — 4° 0'  | Mar. 27 23 25 52  | 3 15 52 N.     | 30 21 7    | + 5 1                           | 3 43 37  | 65 41 30 E.             |
| 4.  | + 5° 6'  | April 5 16 13 47  | 6 37 11 N.     | 16 17 12   | + 2 22                          | 4 46 25  | 0 32 30 E.              |
| 5.  | — 2° 5'  | May 19 0 29 12 5  | 19 54 38 N.    | 30 41 2    | — 3 44                          | 3 43 9   | 47 33 7 <sup>s</sup> E. |
| 6.  | + 9° 4'  | June 14 17 56 42  | 23 20 21 N.    | 39 50 48   | + 0 11                          | 3 26 31  | 39 14 30 E.             |
| 7.  | + 4° 7'  | July 5 0 33 8   | 22 44 50 N.    | 48 47 5    | + 4 21                          | 3 0 10   | 52 14 30 W.             |
| 8.  | + 2° 6'  | Aug. 13 2 20 42   | 14 28 33 N.    | 27 23 29   | + 4 32                          | 3 0 9  | 79 4 45 W.              |
| 9.  | + 0° 7'  | Aug. 31 19 12 18  | 8 8 49 N.      | 44 44 41   | — 0 14                          | 2 37 15  | 111 11 0 E.             |
| 10. | + 4° 7'  | Oct 25 8 35 42  | 12 27 6 S.     | 40 31 1    | — 15 56                         | 2 30 49  | 95 12 15 W.             |
| 11. | — 6° 7'  | Nov. 27 7 13 53   | 21 19 1 S.     | 34 50 6    | — 11 55                         | 4 7 5  | 173 13 15 W.            |
| 12. | — 9° 3'  | Dec. 23 18 37 35  | 23 25 35 S.    | 10 42 56   | 0 0                             | 5 30 16  | 1 57 30 W.              |
| 13. | — 6° 9'  | Jan. 1 14 0 35  | 22 59 46 S.    | 39 9 31    | + 3 55                          | 3 49 33  | 151 47 30 W.            |
| 14. | + 8° 3'  | Feb. 10 21 33 26  | 14 10 5 S.     | 12 17 54   | + 14 29 <sup>s</sup> 5          | 3 0 58 <sup>s</sup> 5                          | 4 58 45 W.              |
| 15. | — 2° 5'  | Oct. 26 0 26 10   | 12 40 36 S.    | 25 10 24   | — 16 0                          | 3 28 12  | 62 35 30 W.             |
| 16. | — 5° 4'  | Feb. 5 23 59 40   | 15 43 18 S.    | 21 21 7    | + 14 19                         | 4 21 49  | 69 7 0 E.               |
| 17. | + 3° 3'  | April 30 18 53 59   | 15 12 21 N.    | 28 18 45   | — 3 3                           | 4 20 12  | 140 47 15 E.            |
| 18. | + 1° 6'  | April 20 15 48 54   | 11 57 34 N.    | 31 59 22   | — 1 23                          | 3 48 51  | 179 52 30 W.            |
| 19. | — 1° 25' | Aug. 21 8 22 2  | 11 48 55 N.    | 34 2 1     | + 2 45                          | 3 40 30  | 179 33 21 E.            |
| 20. | + 0° 3'  | Mar. 20 1 32 46   | 0 7 17 N.      | 29 1 4     | + 7 25                          | 4 3 56   | 82 19 0 W.              |
| 21. | — 8° 0'  | June 13 22 6 12   | 23 18 14 N.    | 30 49 32   | + 0 1                           | 1 53 44  | 165 1 15 E.             |

## TRUE AZIMUTHS, page 282.

|                      |                      |                    |
|----------------------|----------------------|--------------------|
| 1. S. 98° 43' 30" E. | 4. S. 90° 32' 54" E. | 7. S. 56° 4' 0" W. |
| 2. S. 41° 58' 18" E. | 5. S. 50° 9' 36" W.  | 8. East.           |
| 3. N. 75° 58' 4" W.  | 6. N. 49° 7' 14" W.  | 9. N. 84° 5' 2" W. |

## AZIMUTHS, page 288.

| NO. | GREEN. DATE.   | RED. DECL.     | TRUE ALT.   | LOGS.      | TRUE AZIMUTH.      | CORRECTION.    | DEVIATION.     |
|-----|--|----------------|-------------|------------|--------------------|----------------|----------------|
| 1.  | 23 <sup>d</sup> 23 <sup>h</sup> 46 <sup>m</sup> 7 <sup>s</sup> | 19° 17' 40" S. | 38° 34' 32" | 19° 732443 | N. 94° 35' 44" E.  | 15° 50' 14" E. | 11° 14' 44" E. |
| 2.  | 28 9 43 4  | 7 56 26 S.     | 27 7 44     | 19° 289433 | S. 52° 22' 16" W.  | 9 46 16 E.     | 1 43 44 W.     |
| 3.  | 27 0 34 12   | 2 51 33 N.     | 29 41 3     | 19° 705031 | S. 90° 48' 18" W.  | 10 26 42 W.    | 6 56 42 W.     |
| 4.  | 2 19 0 8   | 5 28 40 N.     | 11 50 42    | 19° 654122 | S. 84° 22' 10" W.  | 5 37 50 W.     | 14 47 50 W.    |
| 5.  | 26 21 9 32   | 21 23 18 N.    | 43 19 41    | 19° 420714 | S. 61° 45' 56" E.  | 0 0 56 W.      | 15 44 4 E.     |
| 6.  | 20 6 55 44   | 23 27 28 N.    | 16 49 1     | 19° 808333 | S. 106° 38' 25" W. | 30 1 34 W.     | 7 1 34 W.      |
| 7.  | 31 1 6 46  | 18 7 41 N.     | 43 35 48    | 19° 590598 | S. 78° 11' 54" E.  | 2 51 54 W.     | 5 58 6 E.      |
| 8.  | 23 2 57 58   | 11 12 47 N.    | 7 43 28     | 19° 757568 | S. 98° 18' 20" E.  | 15 21 42 E.    | 10 8 20 W.     |
| 9.  | 31 18 33 2   | 8 9 25 N.      | 30 14 51    | 19° 558129 | N. 73° 55' 14" W.  | 7 38 31 E.     | 11 8 31 E.     |
| 10. | 25 7 30 28   | 20 57 11 S.    | 34 2 21     | 19° 697632 | N. 89° 49' 26" W.  | 2 38 11 W.     | 12 0 11 W.     |
| 11. | 16 22 58 2   | 23 23 42 E.    | 50 13 0     | 19° 712392 | N. 91° 47' 56" E.  | 3 52 4 W.      | 5 52 56 E.     |
| 12. | 2 16 18 50   | 22 57 31 N.    | 14 19 37    | 19° 250818 | N. 50° 29' 24" E.  | 11 30 35 W.    | 5 29 24 E.     |
| 13. | 6 2 49 30  | 22 32 0 S.     | 26 46 54    | 19° 731459 | N. 94° 44' 28" W.  | 10 4 28 W.     | 23 10 32 E.    |
| 14. | 25 1 43 33   | 13 25 16 N.    | 18 52 56    | 19° 437017 | N. 63° 4 6 E.      | 1 14 6 E.      | 15 44 6 E.     |
| 15. | 29 6 53 47   | 17 56 49 S.    | 13 47 28    | 19° 237697 | S. 49° 8' 6 W.     | 31 41 54 W.    | 11 11 54 W.    |
| 16. | 1 2 22 23  | 17 10 11 S.    | 40 7 21     | 19° 053024 | N. 84° 14' 18 W.   | 13 24 18 W.    | 16 15 42 E.    |
| 17. | 26 0 29 58   | 2 28 0 N.      | 32 50 38    | 19° 367425 | S. 57° 43' 44 E.   | 12 53 44 W.    | 13 6 16 E.     |
| 18. | 25 15 40 0   | 8 58 26 S.     | 60 48 32    | 19° 416939 | S. 61° 28' 6 W.    | 0 2 6 E.       | 9 12 54 W.     |
| 19. | 21 7 3 20  | 23 27 23 N.    | 15 46 28    | 19° 841808 | S. 112° 55' 10 W.  | 75 31 5 W.     | 7 41 5 W.      |
| 20. | 10 20 16 0   | 4 23 47 N.     | 42 38 43    | 19° 943200 | N. 34° 27' 36 E.   | 10 22 24 W.    | 1 57 35 E.     |
| 21. | 24 14 32 0   | 13 16 12 N.    | 43 6 34     | 19° 868966 | S. 102° 58' 6 E.   | 1 15 54 E.     | 1 14 6 W.      |
| 22. | 29 20 15 0   | 7 12 39 S.     | 66 26 29    | 19° 173709 | S. 14° 1 52 W.     | 16 50 37 E.    | 16 50 37 E.    |
| 23. | 31 21 25 30  | 22 59 21 S.    | 45 22 20    | 19° 890968 | S. 56° 13' 24 E.   | 11 13 24 W.    | 9 46 36 E.     |

## REDUCTION TO MERIDIAN, pages 298—299.

| NO. | GREEN. DATE.   | TIME NOON.                     | RED. DECL.     | TRUE ALT.   | NAT. NO. | LATITUDE.              |
|-----|--|--------------------------------|----------------|-------------|----------|------------------------|
| 1.  | Jan. 4 <sup>d</sup> 1 <sup>h</sup> 34 <sup>m</sup> 40 <sup>s</sup> | 14 <sup>m</sup> 8 <sup>s</sup> | 22° 45' 41" S. | 32° 26' 19" | 1441     | 34° 42' 7" N. + 31.42  |
| 2.  | Feb. 28 1 4 49   | 14 45                          | 8 4 23 S.      | 38 6 34     | 1480     | +3 42 35 N. 2.3.42.35  |
| 3.  | Mar. 19 16 34 18   | 25 42                          | 0 1 4 S.       | 47 57 15    | 4711     | 41 39 32 S. 2.1.39.32  |
| 4.  | April 20 23 17 6   | 18 30                          | 12 3 52 N.     | 61 39 0     | 2443     | 40 7 6 N. 2.10.06.5    |
| 5.  | May 29 7 38 27   | 30 27                          | 21 46 14 N.    | 30 33 8     | 6514     | 37 14 36 S. 3.7.12.48  |
| 6.  | June 19 0 41 12  | 15 8                           | 23 26 58 N.    | 68 48 28    | 1427     | 44 24 51 N. 4.2.24.51  |
| 7.  | July 16 0 2 19   | 10 19                          | 21 17 14 N.    | 67 52 44    | 944      | 0 41 24 S. 2.1.41.24   |
| 8.  | Aug. 29 15 2 44  | 20 24                          | 8 55 57 N.     | 57 34 6     | 2948     | 41 2 52 N. 2.1.2.52    |
| 9.  | Sept. 8 12 15 43   | 9 43                           | 5 17 1 N.      | 85 30 34    | 883      | 9 4 28 N. 9.5.2.28     |
| 10. | Oct. 10 18 47 58   | 28 10                          | 7 10 31 S.     | 36 44 4     | 5213     | 45 42 50 N. 2.15.42.50 |
| 11. | Nov. 2 17 1 29   | 20 5                           | 15 10 55 S.    | 72 2 22     | 3140     | 32 32 59 S. 2.2.32.59  |
| 12. | Dec. 22 1 38 58  | 9 14                           | 23 26 34 S.    | 65 23 36    | 504      | 47 58 38 S. 2.7.58.38  |
| 13. | Jan. 5 8 58 28   | 17 32                          | 22 37 12 S.    | 58 17 34    | 2668     | 8 47 43 N. 8.4.47.43   |
| 14. | April 28 2 3 11  | 13 37                          | 14 22 40 N.    | 56 40 4     | 1619     | 18 47 6 S. 1.8.47.6    |
| 15. | July 13 9 46 59  | 22 21                          | 21 42 6 N.     | 13 26 24    | 2558     | 54 42 27 S. 5.4.42.27  |
| 16. | Mar. 19 21 28 52   | 16 56                          | 0 3 24 N.      | 70 30 47    | 2580     | 18 58 56 S. 5.4.18.58  |
| 17. | April 12 10 46 29  | 10 19                          | 9 4 41 N.      | 80 36 17    | 1001     | 0 2 28 N. 1.0.2.28     |
| 18. | Sept. 15 14 29 20  | 22 0                           | 2 34 8 N.      | 44 19 4     | 3386     | 42 50 29 S. 1.12.50.29 |
| 19. | Mar. 15 19 49 1  | 4 19                           | 1 33 5 S.      | 50 12 46    | 140      | 38 13 25 N. 3.8.13.25  |
| 20. | Dec. 31 0 40 46  | 10 46                          | 23 3 35 S.     | 14 54 41    | 624      | 51 59 31 N. 5.1.59.31  |
| 21. | Mar. 4 19 8 4  | 20 4                           | 5 52 22 S.     | 50 0 56     | 3175     | 33 49 40 N. 3.3.49.40  |
| 22. | Sept. 22 7 4 42  | 22 6                           | 0 1 56 S.      | 43 55 22    | 3242     | 45 51 4 S. 4.5.51.4    |
| 23. | Dec. 23 0 48 31  | 29 55                          | 23 26 26 S.    | 23 52 44    | 5775     | 42 19 5 N. 2.12.19.5   |

## BY TOWSON:

| NO. | AUG. 1.  | INDEX. | AUG. 11. | LATITUDE.      |
|-----|--|--------|----------|----------------|
| 1.  | + 2' 19"   | 21     | + 3' 22" | 34° 42' 19" N. |
| 2.  | + 0 57   | 26     | + 5 23   | 43 42 43 N.    |
| 3.  | + 0 11   | 68     | + 24 11  | 41 39 49 S.    |
| 4.  | + 2 19   | 41     | + 20 6   | 40 7 5 N.      |
| 5.  | + 10 31  | 77     | + 15 38  | 37 14 29 S.    |
| 6.  | + 2 44   | 24     | + 16 37  | 44 24 37 N.    |
| 7.  | + 1 9  | 11     | + 7 12   | 0 41 41 S.     |
| 8.  | + 2 6  | 50     | + 20 52  | 41 3 5 N.      |
| 9.  | This hour-angle exceeds the limits of the Table. |        |          |                |
| 10. | + 3 10   | 76     | + 19 37  | 45 42 38 N.    |
| 11. | + 3 19   | 47     | + 38 56  | 32 32 55 S.    |
| 12. | + 1 1  | 9      | + 5 15   | 47 58 34 S.    |
| 13. | + 3 34   | 32     | + 13 33  | 8 48 7 N.      |
| 14. | + 1 27   | 22     | + 8 48   | 18 47 1 S.     |
| 15. | + 5 39   | 53     | + 3 18   | 54 42 33 S.    |
| 16. | + 0 0  | 36     | + 27 26  | 18 58 23 S.    |
| 17. | This hour-angle exceeds the limits of the Table. |        |          |                |
| 18. | + 0 42   | 57     | + 15 29  | 42 50 37 S.    |
| 19. | + 0 1  | 2      | + 0 38   | 38 13 30 N.    |
| 20. | + 1 21   | 12     | + 0 50   | 51 59 33 N.    |
| 21. | + 1 23   | 49     | + 15 47  | 33 49 32 N.    |
| 22. | + 0 1  | 57     | + 15 21  | 45 51 14 S.    |
| 23. | + 10 31  | 73     | + 10 51  | 42 19 28 N.    |

## MERIDIAN ALTITUDE OF STAR, page 301.

| NO. | DECLINATION.   | LATITUDE.      | NO. | DECLINATION. | LATITUDE.     |
|-----|----------------|----------------|-----|--------------|---------------|
| 1.  | 28° 24' 51" N. | 43° 18' 56" N. | 11. | 8° 7' 27" S. | 51° 36' 5" N. |
| 2.  | 45 52 22 N.    | 9 46 6 N.      | 12. | 44 50 21 N.  | 25 2 27 S.    |
| 3.  | 38 40 16 N.    | 1 24 42 S.     | 13. | 8 32 42 N.   | 20 41 42 S.   |
| 4.  | 49 25 35 N.    | 11 12 22 N.    | 14. | 16 32 54 S.  | 47 37 45 S.   |
| 5.  | 10 31 5 S.     | 16 15 37 N.    | 15. | 19 49 26 N.  | 30 6 48 N.    |
| 6.  | 57 51 35 S.    | 7 57 5 S.      | 16. | 26 9 34 S.   | 4 52 25 S.    |
| 7.  | 14 30 4 N.     | 26 18 38 N.    | 17. | 60 19 25 S.  | 19 48 3 N.    |
| 8.  | 22 52 59 N.    | 1 8 53 N.      | 18. | 30 16 34 S.  | 50 13 19 S.   |
| 9.  | 16 15 38 N.    | 43 52 13 S.    | 19. | 14 32 11 N.  | 42 11 22 S.   |
| 10. | 62 25 5 S.     | 47 30 4 S.     | 20. | 55 51 41 N.  | 28 4 20 N.    |



EXAMINATION PAPER—No. I, pages 304—305.

1. Log. 5<sup>861612</sup> = nat. no. 727130. (The product by numbers = 727130.)
2. Log. 2<sup>698971</sup> = nat. no. 500. (The quotient.) By Raper: log. 2<sup>698970</sup> = 500.
3. True Courses.—S. 14° W., 15' dep. course; S. 28° W., 45'; N. 76° W., 49'; N. 48° W., 38'; N. 85° W., 31'; S. 22° W., 35'9; S. 54° W., 41'; S. 42° W., 8' current course. Diff. lat. 77'6 S., dep. 183'4 W.; course S. 67° W.; dist. 199'. Lat. in 35° 45' N.; diff. long. 228'; long. in 12° 48' W.
4. Green. date, Jan. 1<sup>d</sup> 6<sup>h</sup> 50<sup>m</sup> 44<sup>s</sup>; red. decl. 23° 1' 13" S.; true alt. 60° 12' 47"; latitude 6° 46' 0" N.  
By Raper: True alt. 60° 12' 38". Latitude 6° 46' 9" N.
5. Log. of diff. long. 2<sup>048016</sup> = diff. long. 111'7.
6. Diff. lat. 219' S.; mer. diff. lat. 292'; diff. long. 380' W.; log. tang. of course 10<sup>114401</sup>; course S. 52° 27' 38" W.; log. of distance 2<sup>555608</sup>; distance 359'4.
7. Standard, Brest constant + 4<sup>h</sup> 2<sup>m</sup>; 6<sup>h</sup> 47<sup>m</sup> A.M., and 7<sup>h</sup> 7<sup>m</sup> P.M.  
,, Portsmouth ,, - 4<sup>h</sup> 40<sup>m</sup>; 6<sup>h</sup> 0<sup>m</sup> A.M., and 6<sup>h</sup> 21<sup>m</sup> P.M.
8. Green. date, January 1<sup>d</sup> 5<sup>h</sup> 23<sup>m</sup> 24<sup>s</sup>; red. decl. 23° 1' 31" S.; log. sine true amp. 9<sup>789125</sup>. True amp. E. 37° 58' 40" S. Error of compass 21° 6' 10" E. Deviation 2° 45' 50" W.
9. Interval 31<sup>d</sup>; rate 6<sup>s</sup> 3 gains. Interval 28<sup>d</sup> 7<sup>h</sup>; acc. rate 2<sup>m</sup> 58<sup>s</sup>2; Green. date Jan. 29<sup>d</sup> 6<sup>h</sup> 53<sup>m</sup> 49<sup>s</sup>; red. decl. 17° 56' 49" S.; true alt. 13° 47' 28"; hour-angle 3<sup>h</sup> 22<sup>m</sup> 9<sup>s</sup>; red. eq. time add 13<sup>m</sup> 23<sup>s</sup>2, mean time at ship 29<sup>d</sup> 3<sup>h</sup> 35<sup>m</sup> 32<sup>s</sup>. Longitude 49° 34' 15" W.  
Raper: True alt. 13° 47' 12"; hour-angle 3<sup>h</sup> 22<sup>m</sup> 9<sup>s</sup>. Longitude 49° 34' 15" W.
10. Green. date, Jan. 15<sup>d</sup> 6<sup>h</sup> 11<sup>m</sup> 12<sup>s</sup>; red. decl. 21° 8' 48" S.; true alt. 55° 18' 24"; sum of logs. 19<sup>723998</sup>; true azimuth N. 93° 24' 4" E. Error of compass 16° 24' 4" E. Deviation 8° 34' 4" E.  
By Raper: True alt. 55° 18' 22"; sine sq. of azimuth 9<sup>723998</sup>; true azimuth N. 93° 24' 4" E. Error of compass 16° 24' 4" E.; Deviation 8° 34' 4" E.
11. Time from noon 16<sup>m</sup> 47<sup>s</sup>; Green. date, January 16<sup>d</sup> 14<sup>h</sup> 18<sup>m</sup> 55<sup>s</sup>; red. decl. 20° 53' 37" S.; true alt. 33° 7' 1"; nat. number 2025, nat. cos. mer. zen. dist. 548375; mer. zen. dist. 56° 44' 40" N. Latitude 35° 51' 3" N.  
METHOD II.—Reduction + 8' 18". Latitude 35° 51' 7" N.  
Towson: Aug. I, 3' 5"; index 30; Aug. II, 5' 10". Latitude 35° 51' 7" N.
12. Star's decl. 16° 15' 38" N.; true alt. 52° 30' 36". Latitude 53° 45' 2" N.  
Raper: True alt. 52° 30' 32". Latitude 53° 45' 6" N.  
The Curve.—Correct magnetic bearing S. 79° W.  
Deviations.—15° W.; 0°; 10° E.; 14° E.; 15° E.; 7° E.; 10° W.; 21° W.  
Compass courses.—N. 47° W.; N. 27½° E.; S. 79° E.; S. 8½° W.  
Magnetic courses.—N. 41½° W.; N. 73° E.; S. 7° E.; S. 67° W.  
Bearings, magnetic.—N. 84° E.; N. 14° W.

EXAMINATION PAPER—No. II, pages 307—309.

1. 7<sup>602321</sup> = 40024074. (The product.)
2. 2<sup>168747</sup> = 147'485. (The quotient.)
3. True Courses.—N. 51° E., 18' dep. course; S. 73° E., 52'; S. 58° E., 43'; N. 57° E., 35'6; N. 38° E., 27'; S. 21° E., 24'; S. 40° E., 29'; S. 39° E., 12'; current course. Diff. lat. 39'9 S.; dep. 181'5 E.; course S. 77½° E., 186'. Lat. in 46° 51' N.; diff. long. (mid. lat.) 267', or 4° 27' E. Longitude in 48° 6' W.
4. Green. date, January 31<sup>d</sup> 18<sup>h</sup> 47<sup>m</sup> 4<sup>s</sup>, or long. in time 5<sup>h</sup> 12<sup>m</sup> 56<sup>s</sup>; red. decl. 17° 15' 23" S.; true alt. 78° 17' 52". Latitude 5° 33' 15" S.  
By Raper: True alt. 78° 17' 51". Latitude 5° 33' 14" S.
5. Log. of diff. long. 2<sup>232899</sup> = Diff. long. 171'0.
6. Diff. lat. 2404' S.; mer. diff. lat. 3104'; diff. long. 3692' W.; tang. course 10<sup>075340</sup>; course S. 49° 56' 42" W.; log. of distance 3<sup>572370</sup>, distance 3736'.

7. Standard, Sunderland, constant  $+ 0^h 58^m$ ;  $3^h 46^m$  A.M., and  $4^h 8^m$  P.M.  
 „ Pembroke „  $- 0^h 20^m$ ;  $5^h 15^m$  A.M., and  $5^h 38^m$  P.M.  
 „ Leith „  $- 2^h 21^m$ ;  $11^h 47^m$  A.M., and no P.M.
8. Green. date, February  $19^d 18^h 10^m 12^s$ ; red. decl.  $11^\circ 7' 29''$  S.; true amp. W.  $11^\circ 22' 30''$  S. *Error of compass*  $19^\circ 33' 45''$  E. *Deviation*  $9^\circ 13' 45''$  E.
9. Interval  $21^d$ ; rate  $10^s 8$  *losing*; Interval  $30^d 9^h 1^m$ ; acc. rate  $5^m 28^s$ ; Green. date, Feb.  $9^d 9^h 30^m 41^s$ ; red. decl.  $14^\circ 39' 18''$  S.; true alt.  $9^\circ 14' 3''$ ; red. eq. time *add*  $14^m 28^s$ ; hour-angle  $3^h 37^m 20^s$ . *Longitude*  $166^\circ 36' 45''$  E.
- Raper: True alt.  $9^\circ 13' 52''$ ; hour-angle  $3^h 37^m 21^s 5$ . *Longitude*  $166^\circ 36' 30''$  E.
10. Green. date, Feb.  $16^d 5^h 29^m 51^s$ ; red. decl.  $12^\circ 22' 15''$  S.; true alt.  $7^\circ 15' 55''$ ; sum of logs.  $19.397026$ ; true azimuth S.  $59^\circ 55' 50''$  E. *Error*  $23^\circ 35' 50''$  W. *Deviation*  $1^\circ 24' 10''$  E.
11. Time from noon  $28^m 48^s$ ; Green. date, Feb.  $14^d 19^h 54^m$ ; red. decl.  $12^\circ 50' 57''$  S.; true alt.  $46^\circ 31' 34''$  N.; nat. no. 4302; nat. cos. 729971; zen. dist.  $43^\circ 6' 52''$  S. *Latitude*  $55^\circ 57' 49''$  S.
- METHOD II.—Reduction  $+ 21' 38''$ . *Latitude*  $55^\circ 57' 51''$  S.  
 Towson: Aug. I,  $6^\circ 0''$ ; index 76; Aug. II,  $27' 28''$ . *Latitude*  $55^\circ 57' 55''$  S.
12. Star's decl.  $5^\circ 32' 29''$  N.; true alt.  $77^\circ 14' 26''$ . *Latitude*  $18^\circ 18' 3''$  N.  
 Raper: True alt.  $77^\circ 14' 16''$ . *Latitude*  $18^\circ 18' 13''$  N.
- The Curve.—Correct magnetic bearing S.  $39^\circ$  E.  
 Deviations.— $5^\circ$  W.;  $19^\circ$  E.;  $23^\circ$  E.;  $13^\circ$  E.;  $4^\circ$  E.;  $8^\circ$  W.;  $22^\circ$  W.;  $24^\circ$  W.  
 Compass courses.—N.  $43^\circ$  E.; N.  $68^\circ$  W.; N.W. by W; N.  $83^\circ$  E.  
 Magnetic courses.—S.  $82^\circ$  W; N.  $52^\circ$  E.; S.  $35^\circ$  W.; S.S.E.  
 Bearings, magnetic.—S.  $80\frac{1}{2}^\circ$  W.; S.  $1\frac{1}{2}^\circ$  E.

### EXAMINATION PAPER—No. III, pages 309—310.

- $3.726356 = 5325.44$  (The product.)
- $1.875495 = 75.075$ . (The quotient.)
- True Courses.**—S.  $70^\circ$  E.,  $17'$  dep. course; S.  $37^\circ$  W.,  $21'$ ; S.  $24^\circ$  W.,  $20'$ ; N.  $62^\circ$  W.,  $24'$ ; N.  $64^\circ$  W.,  $26'$ ; S.  $77^\circ$  E.,  $19'$ ; S.  $28^\circ$  E.,  $18'$ ; N.  $54^\circ$  E.,  $21'$  current course. *Diff. lat.*  $26.1$  S.; *dep.*  $5.3$  W.; *course* S.  $11^\circ$  W.; *dist.*  $27'$ . *Lat. in*  $61^\circ 34'$  N.; *diff. long.*  $11'$  W. *Long. in*  $149^\circ 49'$  E.
- Green. date, March  $19^d 12^h 26^m 48^s$ , or long. in time  $11^h 33^m 12^s$ ; red. decl.  $0^\circ 5' 31''$  S.; true alt.  $89^\circ 54' 38''$ . *Latitude*  $0^\circ 10' 53''$  S.  
 Raper: True alt.  $89^\circ 54' 32''$ . *Latitude*  $0^\circ 10' 59''$  S.
- Log. of diff. long.  $2.679550 = \text{Diff. long. } 478.1$ .
- Diff. lat.  $688'$  N.; mer. diff. lat.  $786'$ ; diff. long.  $3625'$  W.; *course* N.  $77^\circ 45' 58''$  W.; *distance*  $3247'$ .
- Standard, Brest constant  $+ 6^h 19^m$ ; Midnight and  $0^h 19^m$  P.M.  
 „ Brest „  $+ 6^h 4^m$ ; no A.M. and  $0^h 4^m$  P.M.  
 „ Portsmouth „  $- 2^h 31^m$ ;  $11^h 30^m$  A.M., and  $11^h 50^m$  P.M.  
 „ Harwich „  $- 2^h 51^m$ ;  $11^h 37^m$  A.M., and  $11^h 57^m$  P.M.  
 „ Thurso „  $+ 2^h 2^m$ ;  $0^h 26^m$  A.M., and  $0^h 46^m$  P.M.  
 „ Liverpool „  $- 0^h 51^m$ ;  $0^h 27^m$  A.M., and  $0^h 46^m$  P.M.
- Green. date, March  $6^d 14^h 47^m 28^s$ ; red. decl.  $5^\circ 10' 2''$  S.; true amp. W.  $8^\circ 27'$  S. *Correction*  $8^\circ 25' 30''$  E.; *deviation*  $15^\circ 34' 30''$  W.
- Interval  $41^d$ ; rate  $5^s 8$  *gaining*; interval  $90^d 23^h$ ; acc. rate  $8^m 47^s 5$ ; Green. date, March  $30^d 22^h 53^m 7^s$ ; red. decl.  $4^\circ 23' 14''$  N.; true alt.  $29^\circ 19' 56''$ ; hour-angle  $3^h 57^m 26^s$ ; red. eq. time *add*  $4^m 7^s$  mean time ship March  $30^d 20^h 6^m 41^s$ . *Longitude*  $41^\circ 36' 30''$  W.
- Raper: True alt.  $29^\circ 19' 45''$ ; hour-angle  $3^h 57^m 27^s$ . *Longitude*  $41^\circ 36' 45''$  W.

10. Green. date, March 9<sup>d</sup> 9<sup>h</sup> 43<sup>m</sup> 5<sup>s</sup>; red. decl. 4° 4' 54" S.; true alt. 18° 6' 51"; sum of logs. 19° 602167; true azimuth N. 78° 28' 28" E. *Correction* 7° 5' 58" E.; *deviation* 3° 44' 2" W.

11. Time from noon 10<sup>m</sup> 14<sup>s</sup>; Green. date, March 24<sup>d</sup> 18<sup>h</sup> 13<sup>m</sup> 34<sup>s</sup>; red. decl. 1° 58' 24" N.; true alt. 71° 20' 43"; nat. no. 936; nat. cos. mer. zen. dist. 948399 = 18° 29' 11" N. *Latitude* 20° 27' 35" N.

METHOD II.—+ 10° 23". *Latitude* 20° 27' 24" N.

Towson: Aug. I, + 0° 7"; index no. 13. Aug. II, + 10° 14". *Lat.* 20° 27' 34" N.

12. Arcturus' decl. 19° 49' 24" N.; true alt. 36° 7' 27". *Latitude* 34° 3' 9" S.

Raper: True alt. 36° 7' 22". *Latitude* 34° 3' 14" S.

**The Curve.**—Correct magnetic bearing S. 70° E.

Deviations.—3° W.; 20° E.; 25° E.; 23° E.; 2° E.; 24° W.; 25° W.; 18° W.

Compass courses.—N. 35° E.; S. 82° W.; N. 85½° W.; S. 49° E.

Magnetic courses.—S E. by S.; N. 84½° E.; N. 86° W.; N.W. by N.

Bearings, magnetic.—N. 87½° W.; N. 78½° E.

### EXAMINATION PAPER—No. IV, pages 310—312.

1. 4'119863 = 13178.4. (The product.)

2. 3'510784 = 3241.78 nearly. (The quotient.)

3. **True Courses.**—S., 19° dep. course; S. 59° W., 58'; N. 11° W., 15'; S. 28° E., 9'; S. 82° W., 50'; N. 72° E., 12'; S. 58° W., 22'; S. 62° W., 42', current course. *Diff. lat.* 76' 8 S.; *dep.* 142' 3 W.; *course* S. 62° W.; *dist.* 162'. *Lat. in* 51° 29' S.; *diff. long.* 225' W. *Longitude in* 183° 25' W., or 176° 35' E.

4. Green. date, April 1<sup>d</sup> 5<sup>h</sup> 50<sup>m</sup> 48<sup>s</sup>; red. decl. 4° 53' 7" N.; true alt. 48° 55' 26". *Latitude* 45° 57' 41" N.

Raper: True alt. 48° 55' 18". *Latitude* 45° 57' 49" N.

5. Log. of diff. long. 2'364667 = *Diff. long.* 231.6.

6. Diff. lat. 325' N.; mer. diff. lat. 552'; diff. long 325' W.; tang. course 9° 769944; *course* N. 30° 29' 17" W.; *distance* 377.2.

|                     |                                    |                                       |   |
|---------------------|------------------------------------|---------------------------------------|---|
| 7. Standard, Brest, | + 2 <sup>h</sup> 45 <sup>m</sup> ; | no A.M.,                              | and 0 <sup>h</sup> 8 <sup>m</sup> P.M.  |
| „ Hull,             | + 0 <sup>h</sup> 1 <sup>m</sup> ;  | no A.M.,                              | and 0 <sup>h</sup> 4 <sup>m</sup> P.M.  |
| „ Thurso            | — 1 <sup>h</sup> 56 <sup>m</sup> ; | no A.M.,                              | and 0 <sup>h</sup> 34 <sup>m</sup> P.M. |
| „ Pembroke          | + 0 <sup>h</sup> 4 <sup>m</sup> ;  | 11 <sup>h</sup> 33 <sup>m</sup> A.M., | and no P.M.                             |
| „ Weston-super-mare | + 0 <sup>h</sup> 2 <sup>m</sup> ;  | no A.M.,                              | and 0 <sup>h</sup> 5 <sup>m</sup> P.M.  |
| „ Waterford         | + 0 <sup>h</sup> 44 <sup>m</sup> ; | 11 <sup>h</sup> 33 <sup>m</sup> A.M.  | no P.M.                                 |

8. Green. date, April 27<sup>d</sup> 23<sup>h</sup> 18<sup>m</sup> 50<sup>s</sup>; red. decl. 14° 20' 32" N.; true amplitude W. 18° 24' 15" N. *Error* 15° 20' 45" W.; *deviation* 3° 49' 15" E.

9. Interval 12 days; rate 11<sup>m</sup> 3<sup>s</sup> *losing*; interval 71<sup>d</sup> 22<sup>h</sup>; acc rate 13<sup>m</sup> 32<sup>s</sup> 6; Green. date, April 14<sup>d</sup> 21<sup>h</sup> 59<sup>m</sup> 14<sup>s</sup>; red. decl. 9° 57' 50" N.; red. eq. time *sub.* 0<sup>m</sup> 5<sup>s</sup>; true alt. 26° 37' 25"; hour-angle 2<sup>h</sup> 58<sup>m</sup> 19<sup>s</sup>. *Longitude* 74° 45' E.

10. Green. date, April 17<sup>d</sup> 2<sup>h</sup> 43<sup>m</sup> 25<sup>s</sup>; red. decl. 10° 44' 20" N.; true alt. 42° 20' 39"; sum of logs. 19° 453401 true azimuth S. 64° 24' 44" W. *Error* 25° 35' 16" W.; *deviation* 5° 45' 16" W.

11. Time from noon 28<sup>m</sup> 38<sup>s</sup>; Green. date, April 18<sup>d</sup> 11<sup>h</sup> 38<sup>m</sup> 34<sup>s</sup>; red. decl. 11° 12' 57" N.; true alt. 54° 20' 16"; nat. no. 5288; nat. cos. mer. zen. dist. 817756 = 35° 8' 17" N. *Latitude* 46° 21' 13" N.

METHOD II.—+ 31' 40". *Latitude* 46° 21' 4" N.

Towson: Aug. I, + 5' 10"; index no. 76. Aug. II, + 36' 28". *Latitude* 46° 21' 23" N.

12. Spica's decl. 10° 31' 5" S. *Latitude* 58° 38' 15" N.

Raper: True alt. 20° 50' 30". *Latitude* 58° 38' 25" N.

**The Curve.**—Correct magnetic bearing S.  $2^{\circ}$  E.

Deviations.— $4^{\circ}$  W.;  $7^{\circ}$  W.;  $12^{\circ}$  W.;  $18^{\circ}$  W.;  $3^{\circ}$  E.;  $22^{\circ}$  E.;  $15^{\circ}$  E.;  $1^{\circ}$  E.

Compass courses.—N.  $88^{\circ}$  E.; N.  $59^{\circ}$  W.; S.  $14^{\circ}$  W.; S.  $19^{\circ}$  E.

Magnetic courses.—N.  $56^{\circ}$  W.; N.  $87\frac{1}{2}^{\circ}$  W.; East; N.E.

Bearings, magnetic.—N.  $67^{\circ}$  W.; S.  $84\frac{1}{2}^{\circ}$  W.

### EXAMINATION PAPER.—No. V, pages 312—314.

1.  $4^{\circ}83'07'' = \text{nat. no. } 68876.5.$
  2.  $2^{\circ}82'66'' = \text{nat. no. } 670^{\circ}905.$
  3. **True Courses.**—S.  $65^{\circ}$  E.,  $23'$  dep. course; S.  $6^{\circ}$  E.,  $56'$ ; S.  $14^{\circ}$  W.,  $17'$ ; N.  $80^{\circ}$  W.,  $13'$ ; E.,  $37'$ ; S.  $49^{\circ}$  W.,  $10'$ ; N.  $26^{\circ}$  E.,  $17'$ ; S.  $40^{\circ}$  W.,  $21'$ ; N.  $85^{\circ}$  E.,  $48'$  current course. Diff. lat.  $82^{\circ}8'$  S., dep.  $81^{\circ}1'$  E.; course S.  $44^{\circ}$  E., dist.  $116'$ . Lat. in  $65^{\circ}25'$  S., diff. long.  $190'$  E. Long. in  $143^{\circ}31'$  E.
  4. Green. date, May  $8^{\text{d}} 7^{\text{h}} 1^{\text{m}} 8^{\text{s}}$ ; red. decl.  $17^{\circ} 20' 20''$  N.; true alt.  $76^{\circ} 14' 11''$ . Latitude  $3^{\circ} 34' 31''$  N.
  5. Log. of diff. long.  $2.992876 = \text{Diff. long. } 983.7.$
  6. Diff. lat.  $732'$  S.; mer. diff. lat.  $881'$ ; diff. long.  $1098'$  W.; log. tang.  $10.095626$ ; course S.  $51^{\circ} 15' 27''$  W.; distance  $1169.6.$
  7. Standard, Greenock, constant —  $0^{\text{h}} 56^{\text{m}}$ ;  $11^{\text{h}} 35^{\text{m}}$  A.M., and  $11^{\text{h}} 52^{\text{m}}$  P.M.  
 „ Liverpool, „ —  $0^{\text{h}} 1^{\text{m}}$ ;  $11^{\text{h}} 42^{\text{m}}$  A.M., and  $11^{\text{h}} 59^{\text{m}}$  P.M.  
 „ Sunderland, „ —  $1^{\text{h}} 4^{\text{m}}$ ;  $2^{\text{h}} 42^{\text{m}}$  A.M., and  $2^{\text{h}} 58^{\text{m}}$  P.M.  
 „ Brest, „ +  $2^{\text{h}} 18^{\text{m}}$ ;  $6^{\text{h}} 26^{\text{m}}$  A.M., and  $6^{\text{h}} 42^{\text{m}}$  P.M.  
 „ Dover, „ —  $0^{\text{h}} 27^{\text{m}}$ ;  $11^{\text{h}} 9^{\text{m}}$  A.M., and  $11^{\text{h}} 27^{\text{m}}$  P.M.
  8. Green. date, May  $20^{\text{d}} 16^{\text{h}} 6^{\text{m}} 24^{\text{s}}$ ; red. decl.  $20^{\circ} 15' 3''$  N.; true amp. E.  $29^{\circ} 49'$  N. Error of compass  $12^{\circ} 22'$  E. deviation  $19^{\circ} 28'$  W.
  9. Interval  $37^{\text{d}}$ ; rate  $4^{\circ}8'$  gaining; interval  $50^{\text{d}} 21^{\text{h}}$ ; acc. rate —  $4^{\text{m}} 4^{\text{s}}.2$ ; Green. date, May  $21^{\text{d}} 20^{\text{h}} 59^{\text{m}} 21^{\text{s}}$ ; red. decl.  $20^{\circ} 29' 22''$  N.; red. eq. time *sub.*  $3^{\text{m}} 33^{\text{s}}.5$ ; true alt.  $32^{\circ} 19' 31''$ ; hour-angle  $4^{\text{h}} 17^{\text{m}} 32^{\text{s}}.5$ ; mean time at ship May  $21^{\text{d}} 19^{\text{h}} 38^{\text{m}} 54^{\text{s}}$ . Longitude  $20^{\circ} 6' 45''$  W.
  10. Green. date, May  $25^{\text{d}} 9^{\text{h}} 53^{\text{m}} 51^{\text{s}}$ ; red. decl.  $21^{\circ} 8' 27''$  N.; true alt.  $40^{\circ} 54' 26''$ ; logs.  $19.634762$ ; true azimuth S.  $82^{\circ} 6' 4''$  W. or N.  $97^{\circ} 53' 56''$  W. Error  $20^{\circ} 36' 4''$  E.; deviation  $10^{\circ} 6' 4''$  E.
  11. Time from noon  $25^{\text{m}} 25^{\text{s}}$ ; Green. date  $10^{\text{d}} 7^{\text{h}} 54^{\text{m}} 25^{\text{s}}$ ; red. decl.  $17^{\circ} 52' 21''$  N.; true alt.  $43^{\circ} 39' 55''$ ; nat. no.  $5152$ ; mer. zen. dist.  $45^{\circ} 55' 31''$  S. Latitude  $28^{\circ} 3' 10''$  S.  
 METHOD II.—+  $24' 35''$ . Latitude  $28^{\circ} 3' 15''$  S.  
 Towson: Aug. I, +  $6' 16''$ ; index 63. Aug. II, +  $18' 17''$ . Latitude  $28^{\circ} 3' 11''$  S.
  12. Star's decl.  $10^{\circ} 31' 5''$  S.; zen. dist.  $19^{\circ} 53' 44''$  S. Latitude  $30^{\circ} 24' 49''$  S.
- The Curve.**—Correct magnetic bearing N.  $87^{\circ}$  E.  
 Deviations.— $3^{\circ}$  W.;  $15^{\circ}$  W.;  $23^{\circ}$  W.;  $22^{\circ}$  W.;  $2^{\circ}$  E.;  $24^{\circ}$  E.;  $23^{\circ}$  E.;  $13^{\circ}$  E.  
 Compass courses.—N.  $45\frac{1}{2}^{\circ}$  E.; S.  $71\frac{1}{2}^{\circ}$  W.; S.  $49^{\circ}$  E.; S.  $39\frac{1}{2}^{\circ}$  W.  
 Magnetic courses.—N.  $20\frac{1}{2}^{\circ}$  W.; N.  $46^{\circ}$  E.; S.  $76\frac{1}{2}^{\circ}$  E.; S.  $61^{\circ}$  W.  
 Bearings magnetic.—S.  $8^{\circ}$  E.; S.  $85^{\circ}$  W.

### EXAMINATION PAPER.—No. VI, pages 314—315.

1.  $0.622110 = \text{nat. no. } 4.189.$  (The product).
2.  $4.021468 = \text{nat. no. } 10506.77.$  (The quotient).
3. **True Courses.**—S.  $73^{\circ}$  E.,  $22'5$  dep. course; S.  $75^{\circ}$  E.,  $17'$ ; S.  $33^{\circ}$  E.,  $22'$ ; S.  $1^{\circ}$  W.,  $24'$ ; S.  $61^{\circ}$  E.,  $25'$ ; N.  $66^{\circ}$  W.,  $18'$ ; S.  $43^{\circ}$  W.,  $17'$ ; N.  $11^{\circ}$  E.,  $16'$  current course. Diff. lat.  $55^{\circ}8'$  S., dep.  $46^{\circ}1'$  E.; course S.  $39\frac{1}{2}^{\circ}$  E., dist.  $72\frac{1}{2}'$ . Lat. in  $55^{\circ} 16'$  N.; diff. long. (Mercator)  $82^{\circ}9'$  E., long. in  $134^{\circ} 17'$  W. Diff. long. (by mid. lat.)  $82^{\circ}$  E., long. in  $134^{\circ} 18'$  W.
4. Green. date, May  $31^{\text{d}} 17^{\text{h}} 34^{\text{m}} 52^{\text{s}}$ ; red. decl.  $22^{\circ} 6' 44''$  N.; true alt.  $75^{\circ} 49' 26''$ ; Latitude  $7^{\circ} 56' 9''$  N.
5. Log. of diff. long.  $2.487692 = \text{Diff. long. } 307.4.$

6. Diff. lat.  $21^{\circ} 81' S.$ ; mer. diff. lat.  $2301'$ ; diff. long.  $3038' W.$ ; tangent course  $10^{\circ} 120671$ ; course  $S. 52^{\circ} 51' 34'' W.$ ; distance  $3612' 3$ .
7. Standard, Dover,  $+ 4^h 33^m$ ;  $3^h 49^m$  A.M.,  $3^h 49^m$  P.M.  
 „ Harwich —  $0^h 33^m$ ;  $11^h 43^m$  A.M., no P.M.  
 „ Brest, —  $0^h 47^m$ ; corr. for long.  $+ 7^m$ ;  $3^h 9^m$  A.M.,  $3^h 28^m$  P.M.
8. Green. date, June  $21^d 13^h 34^m 48^s$ ; red. decl.  $23^{\circ} 27' 19'' N.$ ; sine of true amp.  $9^{\circ} 898987$ ; true amp.  $52^{\circ} 25' N.$  Error  $46^{\circ} 1' W.$ ; deviation  $6^{\circ} 29' E.$
9. Interval  $29^d$ ; daily rate  $8^s 3$ ; interval  $44^d 22^h$ ; acc. rate  $6^m 13^s$ ; Green. date June  $13^d 21^h 45^m 12^s$ ; red. decl.  $23^{\circ} 18' 12'' N.$ ; true alt.  $28^{\circ} 49' 40''$ ; red. eq. time  $0^m 1^s$  additive; hour-angle  $3^h 49^m 6^s$ ; mean time ship June  $13^d 27^h 49^m 7^s$ . Longitude  $90^{\circ} 58' 45'' E.$
10. Green. date, June  $7^d 22^h 0^m 12^s$ ; red. decl.  $22^{\circ} 54' 18'' N.$ ; true alt.  $31^{\circ} 18' 54''$ ; logs.  $19.813501$ ; true azimuth  $S. 107^{\circ} 33' 48'' E.$  Error  $2^{\circ} 26' 12'' E.$ ; deviation  $17^{\circ} 6' 12'' E.$
11. Time from noon  $37^m 26^s$ ; Green. date, June  $4^d 14^h 16^m 2^s$ ; red. decl.  $22^{\circ} 34' 51'' N.$ ; true alt.  $50^{\circ} 3' 22''$ ; nat. no.  $5776$ ; mer. zen. dist.  $39^{\circ} 25' 32'' N.$  Lat.  $62^{\circ} 0' 23'' N.$   
 METHOD II.  $+ 31' 18''$ . Latitude  $62^{\circ} 0' 25'' N.$   
 Towson: Beyond the limits of the Table.
12. Star's decl.  $28^{\circ} 19' 34'' N.$ ; true alt.  $48^{\circ} 33' 45''$ . Latitude  $13^{\circ} 6' 41'' S.$   
 The Curve.—Correct magnetic bearing  $S. 79^{\circ} W.$   
 Deviations  $12^{\circ} W.$ ;  $0$ ;  $17^{\circ} E.$ ;  $21^{\circ} E.$ ;  $12^{\circ} E.$ ;  $4^{\circ} E.$ ;  $18^{\circ} W.$ ;  $24^{\circ} W.$   
 Compass courses.—N.W. by N.; S.  $70^{\circ} W.$ ; N.  $27^{\frac{1}{2}}^{\circ} E.$ ; S.  $1^{\frac{1}{2}}^{\circ} E.$   
 Magnetic courses.—N.W. by W.; S.  $61^{\circ} W.$ ; S.  $17^{\circ} W.$ ; S.  $40^{\frac{1}{2}}^{\circ} E.$   
 Correct magnetic bearing.—N.  $11^{\circ} E.$ ; N.  $87^{\frac{1}{2}}^{\circ} W.$

# EXAMINATION PAPER.—No. VII, pages 315—317.

1.  $4^{\circ} 141829 = 138621$ .
2.  $2^{\circ} 537818 = 345^{\circ} 0$ .
3. True Courses.—S.  $14^{\circ} W.$ ,  $17'$ ; S.  $68^{\circ} E.$ ,  $22'$ ; S.  $57^{\circ} E.$ ,  $7'$ ; N.  $53^{\circ} W.$ ,  $6'$ ; S.  $54^{\circ} W.$ ,  $26'$ ; S.  $61^{\circ} E.$ ,  $17'$ ; S.  $25^{\circ} W.$ ,  $27'$ ; S.  $42^{\circ} E.$ ,  $15'$ ; S.  $26^{\circ} E.$ ,  $18'$ ; N.  $62^{\circ} W.$ ,  $9'$  current course. Diff. lat.  $96' 0'' S.$ , dep.  $9' 9'' E.$ ; course S.  $6^{\circ} E.$ , dist.  $96^{\frac{1}{2}}$ . Lat. in  $49^{\circ} 49' N.$ , diff. long.  $16' E.$  Long. in  $9^{\circ} 13' W.$
4. Green. date, July  $26^d 0^h 49^m 16^s$ ; red. decl.  $19^{\circ} 19' 0'' N.$ ; true alt.  $15^{\circ} 46' 12''$ . Latitude  $54^{\circ} 54' 48'' S.$
5. Log. of diff. long.  $2.633861 = \text{Diff. long. } 43^{\circ} 4$  nearly.
6. Diff. lat.  $745' S.$ ; mer. diff. lat.  $1042'$ ; diff. long.  $1292' W.$ ; log. tang.  $10^{\circ} 093395$ ; course  $S. 51^{\circ} 6' 50'' W.$ ; distance  $1186' 7$ .
7. Standard, Brest, constant —  $0^h 2^m$ ;  $8^h 9^m$  A.M.,  $8^h 34^m$  P.M.  
 „ Brest, „ —  $0^h 45^m$ ;  $7^h 26^m$  A.M.,  $7^h 51^m$  P.M.  
 „ Brest, „ —  $0^h 5^m$ ;  $8^h 6^m$  A.M.,  $8^h 31^m$  P.M.  
 „ Brest, „ —  $0^h 29^m$ ;  $7^h 42^m$  A.M.,  $8^h 7^m$  P.M.  
 „ Brest, „  $+ 3^h 3^m$ ;  $11^h 14^m$  A.M.,  $11^h 39^m$  P.M.
8. Green. date, July  $12^d 6^h 36^m 32^s$ ; red. decl.  $21^{\circ} 52' 5'' N.$ ; true amp.  $W. 25^{\circ} 13' N.$  Correction  $5^{\circ} 32' E.$ ; deviation  $16^{\circ} 52' E.$
9. Interval  $8^d$ ; rate  $5^s 55$  losing; interval  $32^d 22^h$ ; acc. rate  $+ 3^m 28^s 7$ ; Green. date July  $16^d 21^h 58^m 19^s$ ; red. decl.  $21^{\circ} 7' 57'' N.$ ; true alt.  $13^{\circ} 31' 23''$ ; red. eq. time  $5^m 52^s$  additive; hour-angle  $3^h 51^m 38^s$ ; mean time ship  $16^d 27^h 5^m 30^s$ . Longitude  $89^{\circ} 47' 45'' E.$
10. Green. date, July  $4^d 1^h 53^m 22^s$ ; red. decl.  $22^{\circ} 50' 12'' N.$ ; true alt.  $12^{\circ} 21' 31''$ ; sum of logs.  $19.207424$ ; true azimuth  $N. 47^{\circ} 20' 50'' E.$  Error  $28^{\circ} 4' 50'' E.$ ; deviation  $10^{\circ} 44' 50'' E.$
11. Time from noon  $25^m 20^s$ ; Green. date July  $30^d 18^h 52^m 32^s$ ; red. decl.  $18^{\circ} 11' 31'' N.$ ; true alt.  $26^{\circ} 24' 19''$ ; nat. no.  $4094$ ; mer. zen. dist.  $63^{\circ} 19' 57'' S.$  Latitude  $45^{\circ} 8' 26'' S.$   
 METHOD II.  $+ 15' 45''$ . Latitude  $45^{\circ} 8' 32'' S.$   
 Towson: Aug. I,  $+ 6' 17''$ ; index  $63$ . Aug. II,  $+ 9' 27''$ . Latitude  $45^{\circ} 8' 26'' S.$
12. Star's decl.  $26^{\circ} 9' 34'' S.$ ; true alt.  $70^{\circ} 5' 46''$ . Latitude  $46^{\circ} 3' 48'' S.$

**The Curve.**—Correct magnetic bearing N.  $89^{\circ}$  W.

Deviations.— $1^{\circ}$  E.;  $19^{\circ}$  E.;  $21^{\circ}$  E.;  $9^{\circ}$  E.;  $4^{\circ}$  W.;  $11^{\circ}$  W.;  $19^{\circ}$  W.;  $16^{\circ}$  W.

Compass courses.—N.  $51^{\circ}$  E.; S.  $81\frac{1}{2}^{\circ}$  E.; S.  $23\frac{1}{2}^{\circ}$  W.; North.

Magnetic courses.—S.  $70^{\circ}$  W.; N.  $6^{\circ}$  E.; N.  $80\frac{1}{2}^{\circ}$  E.; S.  $33^{\circ}$  E.

Bearings magnetic.—N.  $75^{\circ}$  E.; N.  $66\frac{1}{2}^{\circ}$  E.

### EXAMINATION PAPER—No. VIII, pages 317—318—319.

1.  $5^{\circ}889986 = 776221^{\circ}4$ .
  2.  $2^{\circ}676541 = 474^{\circ}833$ .
  3. **True Courses.**—N.  $59^{\circ}$  E.,  $15'$  dep. course; S.  $20^{\circ}$  E.,  $26'$ ; N.  $61^{\circ}$  W.,  $27'$ ; N.  $70^{\circ}$  W.,  $22'$ ; S.  $24^{\circ}$  E.,  $25'$ ; S.  $29^{\circ}$  E.,  $22'$ ; N.  $88^{\circ}$  W.,  $43'$ ; S.  $19^{\circ}$  W.,  $18'$  current course. *Diff. lat.*  $53^{\circ}6'S$ ; *dep.*  $50^{\circ}5'W$ ; *course* S.  $43\frac{1}{2}^{\circ}W$ ; *dist.*  $73\frac{1}{2}'$ . *Latitude in*  $0^{\circ}44'S$ ; *diff. long.*  $50\frac{1}{2}'W$ . *Longitude in*  $172^{\circ}59\frac{1}{2}'E$ .
  4. Green. date, Aug.  $11^d 17^h 51^m 12^s$ ; red. decl.  $14^{\circ}53'15''N$ ; true alt.  $42^{\circ}50'18''$ . *Latitude*  $32^{\circ}16'27''S$ .
  5. Log. of diff. long.  $2^{\circ}805956 = \text{Diff. long. } 639^{\circ}7$ .
  6. Diff. lat.  $421'N$ ; mer. diff. lat.  $590'$ ; diff. long.  $249'E$ ; *course* N.  $22^{\circ}52'53''E$ , *distance*  $457'$  nearly.
  7. Standard, Brest —  $1^h 17^m$ ; no A.M. and  $0^h 5^m$  P.M.  
 „ Brest — 2 2;  $11^h 20^m$  A.M. and  $11^h 50^m$  P.M.  
 „ Leith + 0 5;  $11^h 56^m$  A.M. and no P.M.
  8. Green. date, Aug.  $20^d 11^h 10^m 24^s$ ; red. decl.  $12^{\circ}6'38''N$ ; true amp. W.  $16^{\circ}25'N$ . *Correction*  $27^{\circ}40'E$ ; *deviation*  $8^{\circ}25'E$ .
  9. Interval  $7^d$ ; daily rate  $6^{\circ}6'$  losing; interval  $16^d 20\frac{1}{2}^h$ ; acc. rate  $+1^m 51^s$ ; Green. date, Aug.  $6^d 20^h 32^m 37^s$ ; red. decl.  $16^{\circ}18'58''N$ ; true alt.  $24^{\circ}17'1''$ ; red. eq. time  $5^m 29^s$  additive; hour-angle  $4^h 25^m 44^s$ ; mean time ship  $6^d 28^h 31^m 13^s$ . *Longitude*  $119^{\circ}39'E$ .
  10. Green. date, Aug.  $19^d 20^h 37^m 41^s$ ; red. decl.  $12^{\circ}18'45''N$ ; true alt.  $17^{\circ}36'21''$ ; sum of logs.  $19^{\circ}060115$ ; true azimuth N.  $39^{\circ}37'6''W$ . *Error*  $3^{\circ}3'21''W$ ; *deviation*  $36^{\circ}53'21''W$ .  
*Raper:* True alt.  $17^{\circ}36'15''$ ; sine sq. logs.  $9^{\circ}060205 = N. 39^{\circ}37'22''W$ . *Error*  $3^{\circ}3'37''W$ ; *deviation*  $36^{\circ}53'37''W$ .
  11. Time from noon  $35^m 15^s$ ; Green. date, Aug.  $1^d 10^h 12^h 55^m 5^s$ ; red. decl.  $15^{\circ}14'58''N$ ; true alt.  $34^{\circ}48'15''$ ; nat. no.  $8845$ ; mer. zen. dist.  $54^{\circ}34'36''S$ . *Latitude*  $39^{\circ}19'38''S$ .  
**METHOD II.**—*Reduction*  $+37'26''$ . *Latitude*  $39^{\circ}19'26''S$ .  
*Towson:* Aug. I,  $+10'26''$ ; index  $90$ ; Aug. II,  $+26'35''$ . *Latitude*  $39^{\circ}19'46''S$ .
  12. Star's decl.  $8^{\circ}32'38''N$ ; true alt.  $66^{\circ}48'17''$ . *Latitude*  $14^{\circ}39'5''S$  (*Norie*).  
 „ „ „  $66^{\circ}48'13''$  „  $14^{\circ}39'9''S$  (*Raper*).
- The Curve.**—Correct magnetic bearing S.  $8^{\circ}$  E.  
 Deviations.— $4^{\circ}$  E.;  $2^{\circ}$  E.;  $14^{\circ}$  W.;  $17^{\circ}$  W.;  $4^{\circ}$  W.;  $9^{\circ}$  E.;  $12^{\circ}$  E.;  $8^{\circ}$  E.  
 Compass courses.—N.  $85\frac{1}{2}^{\circ}$  E.; S.  $51\frac{1}{2}^{\circ}$  W.; N.  $38^{\circ}$  W.; S.  $50^{\circ}$  E.  
 Magnetic courses.—N.  $32^{\circ}$  W.; S.  $85^{\circ}$  W.; N.  $1^{\circ}$  W.; N.  $86\frac{1}{2}^{\circ}$  W.  
 Bearings, magnetic.—S.  $12^{\circ}$  E.; S.  $23\frac{1}{2}^{\circ}$  E.

### EXAMINATION PAPER—No. IX, pages 319—320.

1.  $7^{\circ}888411 = 0007734$  (The product.)
2.  $6854294 = 00071498$ . (The quotient.)
3. **True Courses.**—S.  $89^{\circ}$  E.,  $20'$  dep. course; S.  $66^{\circ}$  E.,  $41'2$ ; S.  $56^{\circ}$  E.,  $49'8$ ; S.  $83^{\circ}$  E.,  $42'6$ ; S.  $66^{\circ}$  E.,  $32'7$ ; S.  $49^{\circ}$  E.,  $26'7$ ; S.  $50^{\circ}$  E.,  $36'1$ ; N.  $85^{\circ}$  E.,  $32'$  current course. *Diff. lat.*  $101'4S$ ; *dep.*  $125'4E$ ; *course* S.  $68^{\circ}1'$ ; *dist.*  $271'$ . *Latitude in*  $52^{\circ}26'N$ ; *diff. long.*  $420'E$ . *Longitude in*  $6^{\circ}55'E$ .
4. Green. date, Sept.  $22^d 8^h 15^m$ ; red. decl.  $5^{\circ}3'5''S$ ; true alt.  $90^{\circ}1'49''$ . *Latitude*  $0^{\circ}1'16''S$ .

5. Log. of diff. long.  $2.574252 = \text{diff. long. } 375'.2$ .
6. Diff. lat.  $3607''$  S.; mer. diff. lat.  $3798''$ ; diff. long.  $4007'$  E.; tang.  $10.023264$ ; course S.  $46^\circ 32'$  E.; distance  $5243'$ .
7. Standard, Brest  $+ 2^h 59^m$ ;  $3^h 17^m$  A.M. and  $3^h 36^m$  P.M.  
 „ Brest  $+ 4 13$ ; corr. for long.  $- 14^m$ ;  $4 17$  A.M. and  $4 56$  P.M.  
 „ Brest  $+ 3 47$ ; „  $- 11$ ;  $3 54$  A.M. and  $4 33$  P.M.
8. Green. date, September  $30^d 6^h 33^m 40^s$ ; red. decl.  $3^\circ 8' 32''$  S.; true amp. W.  $5^\circ 10''$  S. Error  $41' 44''$  W. Deviation  $11^\circ 16'$  W.
9. Interval  $15^d$ ; rate  $2^s 6$  gains; interval  $19^d 15^h 15^m$ ; acc. rate  $- 0^m 51^s$ ; Green. date, August  $31^d 15^h 35^m 8^s$ ; red. decl.  $8^\circ 12' 7''$  N.; red. eq. time  $0^m 11^s$  subtractive; true alt.  $62^\circ 25' 7''$ ; hour-angle  $1^h 51^m 34^s$ ; mean time at ship, August  $31^d 25^h 51^m 23^s$ . Longitude  $154^\circ 3' 45''$  E.
10. Green. date, September  $16^d 1^h 29^m 54^s$ ; red. decl.  $2^\circ 23' 23''$  N.; true alt.  $29^\circ 41' 59''$ ; sum of logs.  $19.700958$ ; true azimuth N.  $90^\circ 15' 48''$  E. Error  $3^\circ 35' 48''$  W. Deviation  $11^\circ 55' 48''$  W.
11. Time from noon  $16^h 41^s$ ; Green. date, September  $22^d 12^h 27^m 55^s$ ; red. decl.  $0^\circ 7' 11''$  S.; true alt.  $62^\circ 9' 19''$ ; nat. no.  $2348$ ; mer. zen. dist.  $27^\circ 33' 19''$  S. Latitude  $27^\circ 40' 30''$  S.

METHOD II.  $+ 17' 32''$ . Latitude  $27^\circ 40' 27''$  S.

Towson: Aug. I,  $+ 1''$ , in lex 35; Aug. II,  $+ 17' 29''$ . Latitude  $27^\circ 40' 23''$  S.

12. Star's decl.  $19^\circ 49' 38''$  N.; true alt.  $86^\circ 31' 18''$ . Latitude  $16^\circ 20' 56''$  N.

The Curve.—Correct magnetic bearing S.  $88^\circ$  W.

Deviations.— $2^\circ$  E.;  $20^\circ$  E.;  $22^\circ$  E.;  $9^\circ$  E.;  $4^\circ$  W.;  $12^\circ$  W.;  $20^\circ$  W.;  $17^\circ$  W.

Compass courses.—West; N.  $2^\circ$  E.; N.  $59\frac{1}{2}^\circ$  E.; S.  $61\frac{1}{2}^\circ$  E.

Magnetic courses.—N.  $2^\circ$  E.; S.  $17^\circ$  W.; S.  $57\frac{1}{2}^\circ$  E.; N.  $72^\circ$  E.

Bearings, magnetic.—S.  $84\frac{1}{2}^\circ$  E.; N.  $76\frac{1}{2}^\circ$  W.

## EXAMINATION PAPER—No. X, pages 320—321—322.

1.  $7.447213 = 28003548$ . (The product.)
2.  $1.936010 = 86.30$ . (The quotient.)
3. True Courses.—S.  $75^\circ$  E.,  $36'$  dep. course; S.  $8^\circ$  E.,  $43'$ ; S.  $15^\circ$  W.,  $19'$ ; N.  $69^\circ$  E.,  $50'$ ; N.  $77^\circ$  E.,  $21'$ ; S.  $5^\circ$  E.,  $3'$ ; S.  $38^\circ$  W.,  $3'$ ; S.  $51^\circ$  E.,  $22'$ ; N.  $88^\circ$  E.,  $48'$  current course. Diff. lat.  $65'.2$  S.; dep.  $166'.7$  E.; course S.  $69\frac{1}{2}^\circ$  E.; dist.  $179'$ . Lat. in  $58^\circ 44'$  N.; diff. long.  $326\frac{1}{2}'$  E. Long. in  $38^\circ 27\frac{1}{2}'$  W.
4. Green. date, Oct.  $20^d 10^h 1^m 40^s$ ; red. decl.  $10^\circ 43' 13''$  S.; true alt.  $50^\circ 11' 14''$ . Lat.  $50^\circ 31' 58''$  S.
5. Raper: True alt.  $50^\circ 11' 9''$ . Latitude  $50^\circ 32' 3''$  S.
6. Log. of diff. long.  $2.019277 = \text{Diff. long. } 104.5$ .
7. Diff. lat.  $140'$  N.; mer. diff. lat.  $142'$ ; diff. long.  $214'$  E.; tang. course  $10.178126$ ; course N.  $56^\circ 26'$  E.; distance  $253'.2$ .
7. Standard, Brest  $- 1^h 17^m$ ; corr. for long.  $- 11^m$ ;  $10^h 51^m$  A.M. and  $11^h 23^m$  P.M.  
 „ Devenport  $- 0 46$ ; no A.M. and  $0 38$  P.M.  
 „ Sunderland  $+ 0 49$ ; no A.M. and  $0 31$  P.M.
8. Green. date, Oct.  $8^d 11^h 13^m 48^s$ ; red. decl.  $6^\circ 17' 52''$  S.; true amp. E.  $6^\circ 39' 8''$  S. Error  $9^\circ 28'$  E. Deviation  $11^\circ 18'$  E.
9. Interval  $7^d$ ; rate  $2^s 4$  losing; interval  $22^d 12^h$ ; acc. rate  $0^m 54^s$ ; Green. date, Oct.  $30^d 12^h 0^m 22^s$ ; red. decl.  $14^\circ 9' 57''$  S.; true alt.  $28^\circ 42' 59''$ ; hour-angle  $2^h 45^m 6^s$ ; red. eq. time  $16^m 17^s$  sublt.; mean time at ship, Oct.  $30^d 2^h 28^m 49^s$ . Longitude  $142^\circ 53' 15''$  W.
10. Green. date, Sept.  $30^d 18^h 43^m 48^s$ ; red. decl.  $3^\circ 20' 31''$  S.; true alt.  $14^\circ 7' 3''$ ; sum of log.  $19.692568$ ; true azimuth N.  $89^\circ 9' 42''$  W. Correction  $4^\circ 47' 12''$  W. Deviation  $12^\circ 27' 12''$  W.
11. Time from noon  $17^m 8^s$ ; Green. date Oct.  $2^d 1^h 17^m 8^s$ ; red. decl.  $3^\circ 49' 58''$  S.; true alt.  $47^\circ 39' 40''$ ; nat. no.  $2190$ ; mer. zen. dist.  $42^\circ 9' 9''$  N. Latitude  $38^\circ 19' 11''$  N.

METHOD II.—*Red.*  $+ 11^{\circ} 15'$ ; *lat.*  $38^{\circ} 19' 7''$  N (*Norie*).;  $38^{\circ} 19' 16''$  N. (*Raper*).

Towson: Aug. I,  $+ 38'$ , index 36; Aug. II,  $+ 10^{\circ} 28'$ . *Latitude*  $38^{\circ} 19' 16''$  N.

12. Star's decl.  $14^{\circ} 32' 42''$  N.; true alt.  $54^{\circ} 6' 7''$ . *Latitude*  $50^{\circ} 26' 35''$  N.

The Curve.—Correct magnetic bearing S.  $38^{\circ}$  W.

Deviations.— $1^{\circ}$  E.;  $17^{\circ}$  W.;  $22^{\circ}$  W.;  $19^{\circ}$  W.;  $3^{\circ}$  W.;  $18^{\circ}$  E.;  $24^{\circ}$  E.;  $19^{\circ}$  E.

Compass courses.—S.S.E.  $\frac{3}{4}$  E.; E. by N.  $\frac{3}{4}$  N.; S.  $9^{\circ}$  W.; S.  $72^{\circ}$  E.

Magnetic courses.—S.  $45\frac{1}{2}^{\circ}$  E.; S.  $10^{\circ}$  W.; N.  $49^{\circ}$  E.; North.

Bearings, magnetic.—N.  $85\frac{1}{2}^{\circ}$  W.; N.  $89^{\circ}$  W.

### EXAMINATION PAPER—No. XI, pages 322—323—324.

1.  $2.645548 = 442.128$ . (The product.)

2.  $1.999489 = 99.88$ . (The quotient.)

3. True Courses.—S.  $42^{\circ}$  W.,  $16'$  dep. course; N.  $14^{\circ}$  E.,  $17'$ ; S.  $45^{\circ}$  E.,  $19'$ ; S.  $87^{\circ}$  W.,  $31'$ ; S.  $63^{\circ}$  E.,  $17'$ ; S.  $5^{\circ}$  E.,  $19'$ ; S.  $56^{\circ}$  W.,  $25'$ ; S.  $88^{\circ}$  E.,  $22'$ ; current course. *Diff. lat.*  $51^{\circ} 8'$  S.; *dep.*  $6^{\circ} 1'$  W.; *course* S.  $7^{\circ}$  W.; *dist.*  $52'$ . *Lat. in*  $51^{\circ} 8'$  N.; *diff. long.*  $10'$ . *Longitude in*  $119^{\circ} 50'$  E.

4. Green. date, Nov.  $14^d 18^h 39^m 16^s$ ; red. decl.  $18^{\circ} 36' 25''$  S.; true alt.  $67^{\circ} 57' 49''$ . *Latitude*  $40^{\circ} 38' 36''$  S.

5. Log. of diff. long.  $2.294311 = \text{Diff. long. } 196.9$ .

6. Diff. lat.  $1928'$  N.; mer. diff. lat.  $2383'$ ; diff. long.  $4290'$  E.; tangent course  $10^{\circ} 25' 33.33$ ; *course* N.  $60^{\circ} 57'$  E.; *distance*  $3971'$ .

7. Standard, Brest  $+ 7^h 53^m$ ; corr. for long.  $- 10^m$ ;  $10^h 0^m$  A.M.,  $10^h 21^m$  P.M.

„ Dover  $+ 0 39$ ;  $10 16$  A.M.,  $10 40$  P.M.

„ Devonport  $+ 0 17$ ;  $4 29$  A.M.,  $4 52$  P.M.

8. Green. date, November  $9^d 12^h 20^m 44^s$ ; red. decl.  $17^{\circ} 12' 1''$  S.; true amp. E.  $34^{\circ} 9'$  S. *Correction*  $41^{\circ} 47'$  W. *Deviation*  $58^{\circ} 17'$  W.

9. Interval  $12^d$ ; rate  $1^s 2'$  losing; Interval  $36^d 3^h$ ; acc. rate  $43^s 2'$ ; Green. date, Nov.  $30^d 2^h 48^m 52^s$ ; red. decl.  $21^{\circ} 47' 11''$  S.; red. eq. time  $10^m 54^s$  subtractive; true alt.  $39^{\circ} 47' 8''$ ; hour-angle  $3^h 42^m 21^s$ ; mean time ship Nov.  $29^d 20^h 6^m 45^s$ . *Longitude*  $100^{\circ} 31' 45''$  W.

10. Green. date, Nov.  $15^d 10^h 46^m 27^s$ ; red. decl.  $18^{\circ} 46' 44''$  true alt.  $43^{\circ} 55' 7''$ ; sum of logs.  $19.516742$  true azimuth N.  $69^{\circ} 57' 34''$  W., or S.  $110^{\circ} 2' 26''$  S. *Correction*  $11^{\circ} 32' 26''$  E. *Deviation*  $19^{\circ} 22' 26''$  E.

11. Time from noon  $39^m 26^s$ ; Green. date, November  $13^d 2^h 36^m 2^s$ ; red. decl.  $18^{\circ} 10' 35''$  S.; true alt.  $56^{\circ} 11' 50''$ ; nat. no. 8855; mer. zen. dist.  $32^{\circ} 52' 45''$  S. *Latitude*  $51^{\circ} 3' 20''$  S.

Towson: Hour-angle exceeds limits of Table.

12. Star's decl.  $30^{\circ} 16' 35''$  S.; true alt.  $59^{\circ} 36' 2''$ . *Latitude*  $60^{\circ} 40' 33''$  S.

The Curve.—Correct magnetic bearing S.  $89^{\circ}$  W.

Deviations.— $1^{\circ}$  E.;  $19^{\circ}$  E.;  $21^{\circ}$  E.;  $9^{\circ}$  E.;  $3^{\circ}$  W.;  $11^{\circ}$  W.;  $19^{\circ}$  W.;  $16^{\circ}$  W.

Compass courses.—N.  $85^{\circ}$  W.; N.  $45\frac{1}{2}^{\circ}$  W.; N.  $86^{\circ}$  E.; South.

Magnetic courses.—S.  $77^{\circ}$  W.; N.  $58^{\circ}$  W.; S.  $49^{\circ}$  E.; N.  $56^{\circ}$  E.

Bearings, magnetic.—S.  $76^{\circ}$  W.; S.  $56^{\circ}$  E.

### EXAMINATION PAPER—No. XII, pages 324—325.

1.  $3.364038 = .00231227$ .

2.  $1.168317 = 14.7339$ .

3. True Courses.—S.  $45^{\circ}$  W.,  $16'$  dep. course; N.  $73^{\circ}$  E.,  $15'$ ; S.  $49^{\circ}$  W.,  $23'$ ; S.  $43^{\circ}$  E.,  $15'$ ; N.  $47^{\circ}$  W.,  $24'$ ; N.  $80^{\circ}$  E.,  $22'$ ; S.  $53^{\circ}$  W.,  $12'$ ; S.  $14^{\circ}$  E.,  $6'$  current course. *Diff. lat.*  $25^{\circ} 8'$  S.; *dep.*  $8^{\circ} 2'$  W.; *course* S.  $18^{\circ}$  W.; *dist.*  $27'$ . *Lat. in*  $49^{\circ} 34'$  N.; *diff. long.*  $13'$  W. *Long. in*  $40^{\circ} 13'$  W.



4. Green. date, Dec.  $31^d 8^h 15^m$ ; red. decl.  $23^\circ 2' 6''$  S.; true alt.  $67^\circ 20' 49''$ . *Latitude*  $0^\circ 22' 55''$  S.  
 Raper: True alt.  $67^\circ 20' 46''$  *Latitude*  $0^\circ 22' 51''$  S.
5. Log. of diff. long.  $2.346353 = \text{Diff. long. } 222'$ .
6. Diff. lat.  $4766'$  S.; mer. diff. lat.  $5205'$ ; diff. long.  $3735'$  W.; tangent course  $9^\circ 8' 55.870$ ; course S.  $35^\circ 39' 45''$  W.; distance  $5866'$ .
7. Standard, Brest, constant  $+ 6^h 13^m$ ; corr. for long.  $14^m$ ;  $9^h 58^m$  A.M.,  $10^h 17^m$  P.M.  
 „ Queenstown, constant  $- 1^h 19^m$ ;  $3^h 56^m$  A.M.,  $4^h 15^m$  P.M.  
 „ Galway,  $+ 0^h 7^m$ ;  $4^h 56^m$  A.M.,  $5^h 15^m$  P.M.
8. Green. date, Dec.  $28^d 4^h 10^m 49^s$ ; red. decl.  $23^\circ 15' 10''$  S.; true amp. E.  $35^\circ 12\frac{1}{2}'$  S. *Correction*  $9^\circ 53\frac{1}{2}'$  E.; *deviation*  $5^\circ 36\frac{1}{2}'$  W.
9. Interval  $12^d$ ; rate  $5^s.7$  losing; interval  $42^d 8^h$ ; acc. rate  $4^m 0^s.5$ . Green. date, Dec.  $24^d 8^h 18^m 54^s$ ; red. decl.  $23^\circ 24' 46''$  S.; red. eq. time *additive*  $0^m 17^s$ ; true alt.  $40^\circ 54' 8''$ ; hour-angle  $3^h 41^m 17^s$ . *Longitude*  $178^\circ 58' 30''$  W.
10. Green. date, Dec.  $27^d 4^h 40^m 10^s$ ; red. decl.  $23^\circ 18' 17''$  S.; true alt.  $20^\circ 27' 7''$ ; sum of logs  $19.362795$ ; true azimuth S.  $57^\circ 23' 36''$  E. *Correction*  $12^\circ 55' 9''$  E.; *deviation*  $5^\circ 35' 9''$  E.  
 Raper: True alt.  $20^\circ 26' 54''$ ; log. sin. sq.  $9.362825 =$  S.  $57^\circ 23' 44''$  E.; error  $12^\circ 55' 1''$  E.; *deviation*  $5^\circ 35' 1''$  E.
11. Time from noon  $30^m 40^s$ ; Green. date, Dec.  $4^d 1^h 30^m$ ; red. decl.  $22^\circ 21' 2''$  S.; true alt.  $60^\circ 7' 18''$ ; nat. no.  $5101$ ; zen. dist.  $29^\circ 17' 11''$  S. *Latitude*  $51^\circ 38' 13''$  S.  
 METHOD II.— $+ 35' 33''$ ; *latitude*  $51^\circ 38' 14''$  S.  
 Towson: Exceeds limits of Table.
12. Star's decl.  $5^\circ 32' 24''$  N.; true alt.  $52^\circ 45' 55''$ . *Latitude*  $31^\circ 41' 41''$  S.  
 The Curve.—Correct magnetic bearing S.  $2^\circ$  E.  
 Deviations.— $4^\circ$  W.;  $6^\circ$  W.;  $12^\circ$  W.;  $18^\circ$  W.;  $3^\circ$  E.;  $22^\circ$  E.;  $14^\circ$  E.;  $1^\circ$  E.  
 Compass courses.—East; S.  $50^\circ$  E.; S.  $40^\circ$  W.; N.  $4^\circ$  W.  
 Magnetic courses.—S.  $33^\circ$  E.; N.  $88\frac{1}{2}^\circ$  W.; S.  $30^\circ$  W.; S.E. by E.  
 Bearings, magnetic.—N.  $86\frac{1}{2}^\circ$  W.; N.  $2^\circ$  W.

### EXAMINATION PAPER—No. XIII, pages 325—326—327.

1.  $1.302556 = 20.0704$ . (The product).
2.  $0.060635 = 1.14983$ . (The quotient).
3. True Courses.—S.  $14^\circ$  W.  $23'$  dep. course; S.  $23^\circ$  W.,  $50' 6''$ ; N.  $87^\circ$  W.,  $45' 4''$ ; S.  $44^\circ$  E.,  $21' 7''$ ; N.  $78^\circ$  W.,  $17' 8''$ ; N.  $14^\circ$  W.,  $44' 1''$ ; S.  $3^\circ$  E.,  $12' 4''$ ; West  $52'$  current course. *Diff. lat.*  $48' 0''$  S., *dep.*  $135' 0''$  W.; *course* S.  $70^\circ$  W., *dist.*  $143'$ . *Lat. in*  $61^\circ 30'$  S., *diff. long.*  $287'$  W. *Long. in*  $78^\circ 30'$  E.
4. Green. date, Aug.  $10^d 17^h 51^m 12^s$ ; red. decl.  $15^\circ 11' 16''$  N.; true altitude  $42^\circ 50' 17''$ . *Latitude*  $31^\circ 58' 27''$  S.
5. Log. of diff. long.  $2.663420 = \text{Diff. long. } 460.7$ .
6. Diff. lat.  $1890'$  S.; mer. diff. lat.  $2392'$ ; diff. long.  $1774' 43''$  W.; course S.  $36^\circ 34'$  W.; distance  $2353'$ .
7. Standard, Brest —  $1^h 47^m$ ; corr. for long.  $-9^m$ ;  $5^h 30^m$  A.M., and  $5^h 52^m$  P.M.  
 „ Brest —  $0 7$ ;  $7 19$  A.M., and  $7 41$  P.M.  
 „ Brest  $+ 2 38$ ;  $10 4$  A.M., and  $10 26$  P.M.
8. Green. date, Oct.  $28^d 4^h 14^m 48^s$ ; red. decl.  $13^\circ 23' 56''$  S.; true amp. E.  $20^\circ 59'$  S. *Correction*  $31^\circ 39'$  E.; *deviation*  $7^\circ 49'$  E.
9. Interval  $15^d$ ; rate  $11^s.2$  gaining; interval  $16^d 21\frac{1}{2}^h$ ; acc. rate  $3^m 9^s$ . Green. date, April  $17^d 21^h 21^m 54^s$ ; red. decl.  $11^\circ 0' 35''$  N.; true alt.  $38^\circ 22' 36''$ ; red. eq. time  $0^m 47^s$  *subtractive*; hour-angle  $2^h 41^m 23^s$ . *Longitude*  $1^\circ 1' 0''$  W.
10. Green. date, March  $8^d 16^h 22^m 6^s$ ; red. decl.  $4^\circ 21' 52''$  S.; true alt.  $28^\circ 33' 55''$ ; sum of logs  $19.594457$ ; true azimuth N.  $77^\circ 39'$  E. *Correction*  $22^\circ 1'$  W.; *deviation*  $4^\circ 51'$  W.

11. Time from noon  $25^m 52^s$ : Green. date, July  $28^d 2^h 10^m 8^s$ : red. decl.  $18^\circ 50' 39''$  N.: true alt.  $69^\circ 22' 19''$ : mer. zen. dist.  $19^\circ 51' 7''$  N. *Latitude*  $38^\circ 41' 46''$  N.

METHOD II.— $+46^\circ 59''$ ; *latitude*  $38^\circ 41' 25''$  N.

Towson: Exceeds limits of Table.

12. Star's decl.  $47^\circ 33' 32''$  S.: true alt.  $49^\circ 54' 3''$ . *Latitude*  $7^\circ 27' 35''$  S.

The Curve.—Correct magnetic bearing S.  $13^\circ$  W.

Deviations.— $12^\circ$  W.:  $8^\circ$  W.:  $8^\circ$  W.:  $3^\circ$  W.:  $12^\circ$  E.:  $20^\circ$  E.:  $7^\circ$  E.:  $8^\circ$  W.

Compass courses.—S.  $36^\circ$  W.: N.  $75^\circ$  E.: S.  $4^\circ$  W.: N.  $31^\circ$  E.

Magnetic courses.—N.  $49^\circ$  E.: N.  $47^\circ$  W.: N.  $5^\circ$  W.: S.  $2\frac{1}{2}^\circ$  E.

Bearings, magnetic.—N.  $75^\circ$  E.: S.  $75^\circ$  W.

### EXAMINATION PAPER—No. XIV, pages 327—328.

1.  $5903094 = 8000074$ .

2.  $8850814 = 0709274$ .

3. True Courses.—S.  $40^\circ$  E.,  $21'$  dep. course: S.  $65^\circ$  E.,  $14'$ : N.  $54^\circ$  W.,  $9'$ : N.  $23^\circ$  E.,  $18'$ : S.  $10^\circ$  W.,  $22'$ : S.  $60^\circ$  W.,  $29'$ : N.  $16^\circ$  E.,  $20'6$ : N.  $79^\circ$  E.,  $14'$  current course. *Diff. lat.*  $13'8$  S., *dep.*  $16'4$  E.: *course* S.  $49\frac{1}{2}^\circ$  E., *dist.*  $21\frac{1}{2}'$ . *Lat. in*  $34^\circ 42'$  S., *diff. long.*  $20'$  E. *Long. in*  $18^\circ 48'$  E.

4. Green. date, Feb.  $10^d 21^h 50^m 40^s$ : red. decl.  $14^\circ 9' 38''$  S.: true alt.  $30^\circ 33' 20''$ . *Latitude*  $45^\circ 17' 2''$  N.

5. Log. of diff. long.  $2010904 = \text{Diff. Long. } 102'5$ .

6. Diff. lat.  $4202'$  N: mer. diff. lat.  $4555'$ : diff. long.  $4847'$  E.: tang. course  $10^\circ 26' 85$ : *course* N.  $46^\circ 47'$  E.: *distance*  $6136'$ .

7. Standard, Brest, constant  $+4^h 43^m$ ; corr. for long.  $+9^m$ ;  $5^h 26^m$  A.M.,  $6^h 0^m$  P.M.

„ Waterford,

$1^h 42^m$  A.M.,  $2^h 20^m$  P.M.

„ Leith,  $-1^h 49^m$ ;

$9^h 48^m$  A.M.,  $10^h 21^m$  P.M.

8. Green. date, March  $30^d 7^h 41^m 8^s$ : red. decl.  $4^\circ 8' 37''$  N.; true amp. E.  $4^\circ 10'$  N. *Correction*  $8^\circ 1'$  W.; *deviation*  $14^\circ 1'$  W.

9. Interval  $15^d$ ; rate  $4^s 9$  gaining; interval  $32^d 21^h$ ; acc. rate  $2^m 41^s$ ; Green. date, May  $26^d 21^h 10^m 6^s$ : red. decl.  $21^\circ 23' 19''$  N.; red. eq. time  $3^m 4^s$  sub.; true alt.  $43^\circ 20' 9''$ ; hour-angle  $2^h 53^m 55^s$ , *Longitude*  $1^\circ 46' 15''$  W.

10. Green. date, July  $10^d 0^h 25^m 20^s$ : red. decl.  $22^\circ 10' 41''$  N.; true alt.  $44^\circ 59' 38''$ ; sum of logs.  $19^\circ 22' 8412$ ; true azimuth S.  $48^\circ 34' 44''$  E. *Correction*  $54^\circ 12' 14''$  W.; *deviation*  $3^\circ 12' 14''$  W.

11. Time from noon  $30^m 41^s$ ; Green. date, November  $7^d 18^h 31^m 53^s$ : red. decl.  $16^\circ 42' 12''$  S.; true alt.  $40^\circ 4' 47''$ ; mer. zen. dist.  $49^\circ 22' 51''$  N. *Latitude*  $32^\circ 40' 39''$  N.

METHOD II.— $+32' 17''$ . *Latitude*  $32^\circ 40' 49''$  N.

Towson: Aug. I,  $+8' 30''$ ; index  $81$ ; Aug. II,  $+24' 10''$ . *Latitude*  $32^\circ 40' 21''$  N.

12. Star's decl.  $57^\circ 7' 43''$  S.; true alt.  $32^\circ 48' 59''$ . *Latitude*  $0^\circ 3' 18''$  N.

The Curve.—Correct magnetic bearing S.  $17^\circ$  E.

Deviations.— $27^\circ$  E.;  $39^\circ$  E.;  $22^\circ$  E.;  $5^\circ$  W.;  $29^\circ$  W.;  $27^\circ$  W.;  $23^\circ$  W.;  $5^\circ$  W.

Compass courses.—N.  $28^\circ$  W.; N.  $58^\circ$  W.; S.  $79\frac{1}{2}^\circ$  W.; S.  $89^\circ$  W.

Magnetic courses.—S.  $80^\circ$  E.; S.  $42^\circ$  E.; N.  $66^\circ$  W.; S.  $87^\circ$  E.

Bearings magnetic.—N.  $28^\circ$  E.; S.  $62^\circ$  E.

### EXAMINATION PAPER—No. XV, pages 329—330.

1.  $1351334 = 224561$ .

2.  $9030734 = 107333$ .

3. True Courses.—S.  $72^\circ$  E.,  $25'$  dep. course; N.  $41^\circ$  E.,  $35'4$ ; N.  $62^\circ$  E.,  $48'$ ; N.  $53^\circ$  W.,  $43'$ ; S.  $60^\circ$  E.,  $26'$ ; N.  $18^\circ$  W.,  $18'$ ; S.  $46^\circ$  E.,  $32'$ ; N.  $82^\circ$  E.,  $36'$ . *Diff. lat.*  $54'3$  N., *dep.*  $130'6$  E.; *course* N.  $67\frac{1}{2}^\circ$  E., *dist.*  $141\frac{1}{2}'$ . *Lat. in*  $38^\circ 31'$  N., *diff. long.*  $166'$  E. *Long. in*  $2^\circ 5'$  E.

4. Green. date, Nov. 20<sup>d</sup> 19<sup>h</sup> 18<sup>m</sup> 40<sup>s</sup>; red. decl. 20° 1' 50" S.; true alt. 80° 28' 59"; latitude 29° 32' 51" S.
5. Log. of diff. long. 1.909671 = *diff. long.* 81.22.
6. Diff. lat. 731' S.; mer. diff. lat. 733'; diff. long. 1259' W.; tang. course 10° 234922; course S. 59° 47½' W.; distance 1453'.
7. Standard, Brest, + 5<sup>h</sup> 13<sup>m</sup>; corr. for long. — 15<sup>m</sup>; 9<sup>h</sup> 26<sup>m</sup> A.M. and 9<sup>h</sup> 42<sup>m</sup> P.M.  
 „ Dover, + 0<sup>h</sup> 8<sup>m</sup>; no A.M. and 0<sup>h</sup> 7<sup>m</sup> P.M.  
 „ Dover, + 5<sup>h</sup> 13<sup>m</sup>; 4<sup>h</sup> 53<sup>m</sup> A.M. and 5<sup>h</sup> 12<sup>m</sup> P.M.
8. Green. date, Jan. 16<sup>d</sup> 8<sup>h</sup> 2<sup>m</sup> 24<sup>s</sup>; red. decl. 20° 56' 37" S.; true amp. W. 29° 17½' S. Correction 13° 21½' W.; deviation 9° 58½' E.
9. Interval 18<sup>d</sup>; rate 4<sup>s</sup> 0 *losing*; interval 72<sup>d</sup> 12<sup>h</sup>; Greenwich date, June 4<sup>d</sup> 12<sup>h</sup> 33<sup>m</sup> 40<sup>s</sup>; red. decl. 22° 34' 25" N.; true alt. 28° 18' 52"; red. eq. time *subt.* 1<sup>m</sup> 48<sup>s</sup>; hour-angle 3<sup>h</sup> 52<sup>m</sup> 13<sup>s</sup>. Longitude 113° 4' 45" E.
10. Green. date, Nov. 9<sup>d</sup> 14<sup>h</sup> 58<sup>m</sup> 46<sup>s</sup>; red. decl. 17° 14' 2" S.; true alt. 6° 11' 26"; sum of logs. 19.300927; true azimuth S. 53° 7' 24" E. Correction 3° 17' 24" W.; deviation 10° 37' 24" W.
11. Time from noon 9<sup>m</sup> 5<sup>s</sup>; Green. date, Jan. 8<sup>d</sup> 3<sup>h</sup> 31<sup>m</sup> 43<sup>s</sup>; red. decl. 22° 16' 35" S.; true alt. 76° 57' 49"; nat. no. 594; mer. zen. dist. 12° 53' 5" S. Latitude 35° 9' 40" S.  
 METHOD II. — + 9' 9". Latitude 35° 9' 42" S.  
 Towson: True alt. exceeds the limits of the Table.
12. Star's decl. 16° 32' 50" S.; true alt. 37° 45' 59". Latitude 35° 41' 11" N.  
 The Curve.—Correct magnetic bearing N. 12° E.  
 Deviations.—12° E.; 0°; 17° W.; 24° W.; 12° W.; 7° E.; 17° E.; 17° E.  
 Compass courses.—N. 85° W.; S. 57° W.; S. 34° E.; S. 8° E.  
 Magnetic courses.—N. 86° E.; S.E. by S.; N. 38½° W.; N. 79° W.  
 Bearings magnetic.—(Deviation for ship's head E. by S. ½ S. = 20½° W.); N. 82½° W.; S. 37½° E.

# EXAMINATION PAPER—No. XVI, pages 330—331—332.

1. Log. of product 6.498062 = product 3148195.6 Log 6.233506, product .000001712.
2. Log. of quotient 4.986680 = quotient 96979.6. Log. 2.439691, product .027523.
3. True Courses.—N. 69° W., 15' dep. course; N. 58° W., 51'; S. 63° W., 42'; N. 51° E., 30'; N. 36° W., 46'; S. 27° W., 11'; S. 68° E., 16'; S. 51° W., 32' current course. *Diff. lat.* 37° 0' N., *dep.* 122.8 W.; *course* N. 73° W., *dist.* 128; *Lat. in* 36° 50' S., *diff. long.* 152' W. *Long. in* 71° 9' W.
4. Green. date 1876, December 31<sup>d</sup> 12<sup>h</sup> 48<sup>m</sup> 24<sup>s</sup>; red. decl. 23° 1' 13" S.; true alt. 83° 52' 24". Latitude 16° 53' 33" S.
5. Diff. long. 192.5 W. *Long. in* 182° 29.5 W., or 177° 30½' E.
6. Diff. lat. 2747' S.; mer. diff. lat. 2919'; diff. long. 6340' W.; tang. course 10° 336855; course S. 65° 17' W.; distance 6570.
7. Standard, Brest, — 1<sup>h</sup> 27<sup>m</sup>; 5<sup>h</sup> 37<sup>m</sup> A.M., and 5<sup>h</sup> 57<sup>m</sup> P.M.  
 „ Brest, — 3<sup>h</sup> 17<sup>m</sup>; corr. for long. — 7<sup>m</sup>, 3<sup>h</sup> 40<sup>m</sup> A.M., and 4<sup>h</sup> 0<sup>m</sup> P.M.  
 „ Brest, + 4<sup>h</sup> 2<sup>m</sup>; corr. for long. + 10<sup>m</sup>, 11<sup>h</sup> 16<sup>m</sup> A.M., and 11<sup>h</sup> 36<sup>m</sup> P.M.
8. Green. date, Nov. 3<sup>d</sup> 17<sup>h</sup> 28<sup>m</sup> 30<sup>s</sup>; red. decl. 15° 29' 49" S.; true amp. E. 22° 55' S. Correction 27° 42½' W.; deviation 11° 12½' W.
9. Interval 14<sup>d</sup>; rate 8.5 *gaining*; interval 124<sup>d</sup> 20<sup>h</sup>; acc. rate 17<sup>m</sup> 41<sup>s</sup>; Green. date, August 31<sup>d</sup> 19<sup>h</sup> 54<sup>m</sup> 30<sup>s</sup>; red. decl. 8° 8' 11" N.; eq. time — 0<sup>m</sup> 14<sup>s</sup>; true alt. 15° 25' 44"; hour-angle 4<sup>h</sup> 45<sup>m</sup> 41<sup>s</sup>. Longitude 10° 6' 15" W.
10. Green. date, May 31<sup>d</sup> 16<sup>h</sup> 13<sup>m</sup>; red. decl. 22° 6' 17" N.; true alt. 39° 20' 26"; sum of logs. 19.779730; true azimuth S. 101° 47' 34" E. Correction 3° 21' 19" W.; deviation 4° 11' 19" W.
11. Green. date, April 12<sup>d</sup> 14<sup>h</sup> 1<sup>m</sup> 5<sup>s</sup>; time from noon 10<sup>m</sup> 15<sup>s</sup>; red. decl. 9° 7' 38" N. true alt. 80° 43' 11"; nat. no. 987; mer. zen. dist. 8° 55' 22" S. Latitude 0° 12' 15" N.  
 METHOD II.— + 21' 24". Latitude 0° 12' 2" N.

Towson: The altitude exceeds the limits of the Table.

12. Star's decl.  $60^{\circ} 19' 27''$  S.; true alt.  $9^{\circ} 52' 32''$ . *Latitude*  $19^{\circ} 48' 1''$  N.

**The Curve.**—Correct magnetic bearing S.  $14^{\circ}$  W.

Deviation.— $20^{\circ}$  W.;  $16^{\circ}$  W.;  $4^{\circ}$  W.;  $16^{\circ}$  E.;  $20^{\circ}$  E.;  $14^{\circ}$  E.;  $1^{\circ}$  E.;  $11^{\circ}$  W.

Compass courses.—S.  $4^{\circ}$  E.; S.  $89^{\circ}$  E.; N.  $34^{\circ}$  E.; N.  $13\frac{1}{2}^{\circ}$  E.

Magnetic courses.—S.  $7^{\circ}$  W.; East; S.  $50^{\circ}$  W.; N.  $15^{\circ}$  W.

Bearing magnetic.—N.  $79\frac{1}{2}^{\circ}$  W.; S.  $85^{\circ}$  E.

### EXAMINATION PAPER—No. XVII, pages 333—334.

1. Log. of product  $2'577492 =$  product  $378$ ;  $2'138598 =$  '013759 and  $1'301030 = 20$ .

2. Log. of quotient  $3'954292 =$  quotient  $9001'0$ ;  $5'301030 =$  '000002;  $6'301030 =$  '000002.

3. True Courses.—S.  $4^{\circ}$  W.,  $16'$  dep. course; N.  $71^{\circ}$  E.,  $30'$ ; S.  $47^{\circ}$  W.,  $15'4$ ; S.  $71^{\circ}$  E.,  $50'$ ; N.  $41^{\circ}$  W.,  $9'$ ; S.  $18^{\circ}$  W.,  $28'$ ; S.  $76^{\circ}$  E.,  $47'$ ; N.  $82^{\circ}$  E.,  $42'$  current course. *Diff. lat.*  $50'9$ ; S., *dep.*  $157'6$  E.; *course* S.  $72^{\circ}$  E., *dist.*  $165\frac{1}{2}'$ . *Lat. in*  $51^{\circ} 16'$  S. *Diff. long.*  $249\frac{1}{2}'$  E., *long. in*  $183^{\circ} 49\frac{1}{2}'$  E., or  $176^{\circ} 10\frac{1}{2}'$  W.

4. Green. date, Sept.  $22^d 20^h 9^m$ ; red. decl.  $0^{\circ} 14' 41''$  S.; true alt.  $84^{\circ} 21' 18''$ . *Latitude*  $5^{\circ} 53' 23''$  S. Raper: True alt.  $84^{\circ} 21' 8''$ . *Latitude*  $5^{\circ} 53' 33''$  S.

5. *Diff. long.*  $220'9$  E., or  $5^{\circ} 41'$  E. *Long. in*  $3^{\circ} 1'$  E.

6. *Diff. lat.*  $2531'$  S.; mer. *diff. lat.*  $2701$ ; *diff. long.*  $7433'$  E.; log. tang.  $10'439639$ ; *course* S.  $70^{\circ} 2'$  E.; *distance*  $7412'$ .

7. Standard, Leith, constant —  $1^h 17^m$ ; no A.M., and  $0^h 17^m$  P.M.

„ Devonport, „ —  $1^h 13^m$ ;  $3^h 18^m$  A.M., and  $3^h 45^m$  P.M.

„ Weston-super-mare, „ +  $0^h 19^m$ ;  $6^h 2^m$  A.M., and  $6^h 31^m$  P.M.

„ Portsmouth, „ —  $1^h 11^m$ ;  $9^h 24^m$  A.M., and  $9^h 50^m$  P.M.

8. Green. date, Nov.  $4^d 21^h 23^m$ ; red. decl.  $15^{\circ} 51' 4''$  S.; true amp. W.  $16^{\circ} 59'$  S. *Correction*  $19^{\circ} 35'$  E.; *deviation*  $18^{\circ} 35'$  E.

9. Green. date, Aug.  $5^d 8^h 8^m 44^s$ ; red. decl.  $16^{\circ} 44' 18''$  N.; red. eq. time +  $5^m 40^s$ ; true alt.  $35^{\circ} 16' 45''$ ; hour-angle  $3^h 53^m 55^s$ . *Longitude at sight*  $179^{\circ} 14' 45''$  W.; *diff. long. since sight*  $55' 42''$ . *Longitude at noon*  $180^{\circ} 10' 27''$  W., or  $179^{\circ} 49' 33''$  E.

10. Green. date, Aug.  $13^d 2^h 20^m 40^s$ ; red. decl.  $14^{\circ} 28' 33''$  N.; true alt.  $27^{\circ} 23' 29''$ ; sum of logs.  $19'259920$ ; true azimuth N.  $50^{\circ} 29' 48''$  E. *Error*  $25^{\circ} 29' 48''$  E. *Deviation*  $9^{\circ} 9' 48''$  E.

11. Green. date, June  $11^d 19^h 43^m 30^s$ ; time from noon  $32^m 18^s$ ; red. decl.  $23^{\circ} 11' 32''$  N.; true alt.  $50^{\circ} 14' 43''$ ; nat. no. 8768. *Latitude*  $15^{\circ} 46' 14''$  S.

**METHOD II.** +  $47' 52''$ . *Latitude*  $15^{\circ} 46' 3''$  S.

Towson: Aug. I, +  $12' 16''$ ; index 81; Aug. II, +  $34' 38''$ . *Latitude*  $15^{\circ} 46' 41''$  S.

12. Star's decl.  $22^{\circ} 52' 59''$  N.; true alt.  $60^{\circ} 23' 4''$ . *Latitude*  $52^{\circ} 29' 55''$  N.

**The Curve.**—Correct magnetic bearing S.  $20^{\circ}$  E.

Deviations.— $22^{\circ}$  W.;  $10^{\circ}$  W.;  $3^{\circ}$  E.;  $14^{\circ}$  E.;  $15^{\circ}$  E.;  $10^{\circ}$  E.;  $0^{\circ}$ ;  $10^{\circ}$  W.

Compass courses.—N.  $24^{\circ}$  W.; S.  $14^{\circ}$  W.; N.  $35\frac{1}{2}^{\circ}$  E.; N.  $13^{\circ}$  E.

Magnetic courses.—S.S.W.; S.  $41^{\circ}$  E.; S.  $72\frac{1}{2}^{\circ}$  W.; S.  $1^{\circ}$  E.

Bearings, magnetic.—S.  $80\frac{1}{2}^{\circ}$  W.; N.  $68\frac{1}{2}^{\circ}$  W.

### EXAMINATION PAPER—No. XVIII, pages 334—335—336.

1.  $7'754166 = 56776104$ .  $3'806197 =$  '00640025.

2.  $8'201561 =$  '015906.  $13'000000 =$  10000000000000.

3. True Courses.—S.  $6^{\circ}$  W.,  $19'$  dep. course; N.  $50^{\circ}$  W.,  $23'7$ ; S.  $47^{\circ}$  E.,  $16'3$ ; N.  $18^{\circ}$  E.,  $17'6$ ; S.  $8^{\circ}$  W.,  $14'1$ ; N.  $87^{\circ}$  E.,  $42'3$ ; S.  $75^{\circ}$  E.,  $12'$ ; S.  $65^{\circ}$  W.,  $15'$  current course. *Diff. lat.*  $19'3$  S.; *dep.*  $35'3$  E.; *course* S.  $61\frac{1}{2}^{\circ}$  E.; *dist.*  $40\frac{1}{2}'$  E. *Lat. in*  $56^{\circ} 41'$  N.; *Diff. long.*  $65'$  E. *Long. in*  $38^{\circ} 55'$  W.

4. Green. date, June  $24^d 20^h 3^m$ ; red. decl.  $23^{\circ} 23' 46''$  N.; true alt.  $60^{\circ} 4' 7''$ . *Latitude*  $6^{\circ} 32' 7''$  S.

- Raper: True alt.  $60^{\circ} 4' 1''$  N. Latitude  $6^{\circ} 32' 13''$  S.
5. Diff. long.  $153^{\circ} 9' W.$ , or  $2^{\circ} 34' W.$  Longitude in  $12^{\circ} 4' W.$
6. Diff. lat.  $4728' 5''$  N.: mer. diff. lat.  $4896' 5''$ : diff. long.  $3540' E.$ : log. tang.  $9^{\circ} 859117$ : true course N.  $35^{\circ} 52' E.$  Compass course N.  $15^{\circ} 52' E.$ : distance  $5588'$ .
7. Standard, Brest  $+ 6^h 28^m$ : corr. for long.  $- 12^m$ :  $1^h 15^m$  A.M. and  $1^h 33^m$  P.M.  
 „ Brest  $+ 3 42$ : corr. for long.  $+ 9$ :  $11 8$  A.M. and  $11 26$  P.M.  
 „ Queenstown  $- 0 59$ : :  $7 33$  A.M. and  $7 49$  P.M.
8. Green. date, June  $23^d 18^h 48^m 12^s$ : red. decl.  $23^{\circ} 25' 23''$  N.: true amp.  $23^{\circ} 25\frac{1}{2}'$  N.: Error of compass  $54^{\circ} 21\frac{1}{2}' W.$  Deviation  $32^{\circ} 41\frac{1}{2}' W.$
9. Interval  $32^d$ : rate  $0^s 8$ : interval  $113^d 5^h$ : ace. rate  $1^m 30^s 5$ . Green. date, Sept.  $22^d 4^h 57^m 35^s$ : red. decl.  $0^{\circ} 0' 0''$ : red. eq. time  $- 7^m 34^s 5$ : true alt.  $16^{\circ} 56' 12''$ : hour-angle  $4^h 52^m 15^s 2$ . Longitude  $149^{\circ} 21' 9'' W.$
10. Green. date, March  $21^d 13^h 51^m 16^s$ : red. decl.  $0^{\circ} 43' 8''$  N.: true alt.  $42^{\circ} 57' 18''$ : sum of logs.  $19.619736$ : true azimuth N.  $80^{\circ} 24' W.$  Error of compass  $15^{\circ} 13\frac{1}{2}' E.$  Deviation  $7^{\circ} 23\frac{1}{2}' E.$
11. Green. date, Oct.  $3^d 14^h 27^m 9^s$ : time from noon  $10^m 51^s$ : red. decl.  $4^{\circ} 25' 54''$  S. true alt.  $63^{\circ} 47' 10''$ : nat. no. 963. Latitude  $30^{\circ} 31' 12''$  S.
- METHOD II.  $+ 7' 34''$ . Latitude  $30^{\circ} 31' 12''$  S.
- Towson: Aug. I,  $+ 0' 16''$ : index  $15''$ . Aug. II,  $+ 8' 6''$ . Latitude  $30^{\circ} 30' 54''$  S.
12. Star's decl.  $55^{\circ} 51' 19''$  N.: true alt.  $84^{\circ} 56' 45''$ . Latitude  $60^{\circ} 54' 34''$  N.
- The Curve.—Correct magnetic bearing N.  $8^{\circ} W.$
- Deviations.— $10^{\circ} E.$ :  $9^{\circ} E.$ :  $5^{\circ} E.$ :  $0^{\circ}$ :  $6^{\circ} W.$ :  $9^{\circ} W.$ :  $7^{\circ} W.$ :  $2^{\circ} W.$
- Compass courses.—S.  $76^{\circ} W.$ : N.  $48^{\circ} E.$ : S.  $6^{\circ} E.$ : N.  $88\frac{1}{2}^{\circ} W.$
- Magnetic courses.—S.  $40\frac{1}{2}^{\circ} W.$ : S.  $2^{\circ} E.$ : S.  $88^{\circ} E.$ : S.  $65^{\circ} E.$
- Bearings, magnetic.—N.  $84\frac{1}{2}^{\circ} W.$ : N.  $64\frac{1}{2}^{\circ} E.$

# EXAMINATION PAPER—No. XIX, pages 336—337—338.

1.  $6742037 = 55212405$ .  $5109096 = 128557$ .
2.  $1903505 = 800767$ .  $7922575 = 836709615$ .
- True Courses.—N.  $53^{\circ} E.$ ,  $21'$  dep. course: S.  $74^{\circ} E.$ ,  $16' 6''$ : S.  $25^{\circ} W.$ ,  $13' 4''$ : N.  $35^{\circ} E.$ ,  $19' 3''$ : S.  $1^{\circ} W.$ ,  $19' 1''$ : S.  $65^{\circ} W.$ ,  $47' 6''$ : N.  $77^{\circ} E.$ ,  $21' 3''$ : N.  $48^{\circ} E.$ ,  $49'$  current course. Diff. lat.  $10' 1''$  N.: dep.  $52' 0''$  E.: course N.  $79^{\circ} E.$ : dist.  $53'$ . Lat. in  $62^{\circ} 30' N.$ : diff. long.  $112 E.$  Long. in  $62^{\circ} 48' W.$
4. Green. date, May  $31^d 21^h 1^m 20^s$ : red. decl.  $22^{\circ} 7' 52''$  N.: true alt.  $72^{\circ} 28' 57''$ . Lat.  $39^{\circ} 38' 55''$  N.
5. Log. of diff. long.  $1.747719 = \text{diff. long. } 55' 94''$ .
6. Diff. lat.  $3757' S.$ : mer. diff. lat.  $4255'$ : diff. long.  $7560' E.$ : log. tangent.  $10.249622$ : course S.  $60^{\circ} 38' E.$ : distance  $7661$ .
7. Standard, Leith  $- 1^h 17^m$ :  $11^h 59^m$  A.M. and no P.M.  
 „ Leith  $- 2 55$ :  $10 21$  A.M. and  $10^h 42^m$  P.M.  
 „ Brest  $+ 6 57$ :  $9 18$  A.M. and  $9 39$  P.M.
8. Green. date, Dec.  $27^d 11^h 35^m$ : red. decl.  $23^{\circ} 17' 27''$  S.: true amp. E.  $31^{\circ} 9\frac{1}{2}' S.$  Error of compass  $58^{\circ} 50\frac{1}{2}' W.$  Deviation  $39^{\circ} 40\frac{1}{2}' W.$
9. Green. date, Jan.  $28^d 16^h 36^m 50^s$ : red. decl.  $18^{\circ} 6' 23''$  S.: red. eq. time  $+ 13^m 17^s$ : true alt.  $17^{\circ} 52' 42''$ : hour-angle  $3^h 46^m 35^s$ : long. at sight  $170^{\circ} 45' 30'' E.$ : diff. long. since sight  $19' W.$  Long. at noon  $171^{\circ} 4' 30'' E.$
10. Green. date, July  $9^d 17^h 50^m 10^s$ : red. decl.  $22^{\circ} 12' 50''$  N.: true alt.  $14^{\circ} 36' 40''$ : sum of logs.  $19.176158$ : true azimuth N.  $45^{\circ} 34' 36'' W.$  Error of compass  $47^{\circ} 49' 36'' W.$  Deviation  $54^{\circ} 34' 36'' W.$

11. Green. date, Nov., 28<sup>d</sup> 15<sup>h</sup> 58<sup>m</sup> 31<sup>s</sup>: time from noon 12<sup>m</sup> 11<sup>s</sup>: red. decl. 21° 33' 0" S.: true alt. 74° 15' 51": nat. no. 1306': mer. zen. dist. 15° 27' 27" N.: latitude 6° 5' 33" S.

METHOD II. + 17' 6". Latitude 6° 5' 53" S.

12. Star's decl. 8° 20' 44" S.: true alt. 52° 11' 54": latitude 29° 27' 22" N.

Towson: Hour-angle exceeds the limits of Table.

**The Curve.**—Correct magnetic bearing S. 8° E.

Deviations.—15° E.: 3° E.: 13° W.: 28° W.: 14° W.: 10° E.: 13° E.: 14° E.

Compass courses.—S. by W.: S. 87° E.: S. 13° E.: S. 85½° W.

Magnetic courses.—N. 20° W.: N. 54° W.: S. 32° E.: N. 32° E.

Bearings, magnetic.—S. 68° W.: West.

### EXAMINATION PAPER—No. XX, pages 338—339—340.

1. 7891486 = 77890714. 8763323 = 00000057986.

2. 2900314 = 794904. 7950265 = 89179388.

3. True Courses.—East. 30° dep. course: S. 38° E., 54' 2": N. 48° E., 41' 6": S. 76° W., 14' 4": S. 22° E., 46' 5": N. 9° W., 29' 1": S. 51° E., 49' 2": N. 79° E., 40' 8" current course. Diff. lat. 15' 2" S.: dep. 192' 2" E.: course S. 85½° W.: dist. 193'. Latitude in 59° 34' N.: diff. long. 380½° E.: longitude in 37° 49½° W.

4. Green. date, Sept. 30<sup>d</sup> 18<sup>h</sup> 21<sup>m</sup> 20<sup>s</sup>: red. decl. 3° 19' 58" S.: true alt. 56° 56' 24": lat. 29° 43' 38" N.

4.\* Green. date, July 2<sup>d</sup> 8<sup>h</sup> 59<sup>m</sup>, red. decl. 2° 59' 0" N., true alt. 10° 25' 59", latitude 77° 26' 59" N.

5. Diff. long. 369' 7" E., or 6° 10' E.: longitude in 21° 18' W. Compass course N. 61° 29' E., or N.E. by E. ½ E. nearly.

6. Diff. lat. 2000' N.: mer. diff. lat. 2043': diff. long. 2043' W.: log. tang. 10.000000: true course N. 45° W. Compass course N. 32° 7½° W. Dist. 2828' 4.

7. Standard, Brest — 2<sup>h</sup> 2<sup>m</sup> 11<sup>h</sup> 52<sup>m</sup> A.M. and no P.M.

„ Portsmouth — 1 11 8 4 A.M. and 8<sup>h</sup> 35<sup>m</sup> P.M.

„ Brest — 1 17 corr. for long. — 1<sup>m</sup> 0 6 A.M. and 0 36 P.M.

8. Green. date, April, 25<sup>d</sup> 0<sup>h</sup> 34<sup>m</sup> 48<sup>s</sup>: red. decl. 13° 24' 19" N.: true amp. W. 25° 25' N. Error of compass 67° 24' W. Deviation 31° 34' W.

9. Green. date, Aug. 23<sup>d</sup> 18<sup>h</sup> 16<sup>m</sup> 50<sup>s</sup>: red. decl. 10° 59' 40" N.: red. eq. time + 2<sup>m</sup> 7<sup>s</sup>: true alt. 37° 26' 49", hour-angle 3<sup>h</sup> 23<sup>m</sup> 6<sup>s</sup>. Long at sight 35° 31' 45" E.: diff. long. 10' 45" W. Longitude at noon 35° 22' 0" E.

10. Green. date, Oct. 31<sup>d</sup> 22<sup>h</sup> 15<sup>m</sup> 44<sup>s</sup>: red. decl. 14° 37' 27" S.: true alt. 12° 23' 17": sum of logs. 19.217276: true azimuth S. 47° 55' 14" E. Error 50° 43' 59" W. Deviation 17° 23' 59" W.

11. Green. date, May 29<sup>d</sup> 9<sup>h</sup> 58<sup>m</sup> 28<sup>s</sup>: time from noon 4<sup>m</sup> 12<sup>s</sup>: red. decl. 21° 47' 7" N.: true alt. 67° 53' 11": nat. no. 160: mer. zen. dis. 22° 5' 21" S. Latitude 0° 18' 14" S.

METHOD II. + 1' 29". Latitude 0° 18' 17" S.

Towson: Aug. I, + 0' 12": index 2. Aug. II, + 1' 18": latitude 0° 18' 12" S.

12. Star's decl. 6° 48' 49" N.: true alt. 28° 58' 36": latitude 54° 12' 35" S.

**The Curve.**—Correct magnetic bearing S. 49° W.

Deviations.—20° W.: 16° W.: 2° W.: 14° E.: 20° E.: 15° E.: 1° W.: 11° W.

Compass courses.—S. 33° W.: S. 43° E.: N. 63° W.: N. 24° E.

Magnetic courses.—N. 9° E.: S. 74° W.: S. 10° W.: S. 60° W.

Bearings, magnetic.—S. 2° E.: S. 88° W.

### INDEX ERROR, page 347.

|             |                |             |                |
|-------------|----------------|-------------|----------------|
| 1. + 2' 15" | Semid. 15' 57" | 2. — 1' 40" | Semid. 15' 45" |
| 3. + 27 45  | „ 16 12        | 4. + 0 52   | „ 16 49        |
| 5. + 38 20  | „ 15 50        | 6. + 35 5   | „ 16 17.5      |

## EXERCISES ON THE CHART.

FOR ONLY MATE, FIRST MATE, AND MASTER.

*North Sea, pages 351—352.*

|  |           |  |            |
|--|-----------|--|------------|
| 1. Course W. $\frac{1}{4}$ S.  | Dist. 49' | 2. Course S.W. $\frac{1}{4}$ W.  | Dist. 163' |
| 3. " S. by W. $\frac{3}{4}$ W.   | " 19      | 4. " S.W. $\frac{1}{4}$ S.   | " 67       |
| 5. " S.E. $\frac{1}{4}$ S.   | " 149     | 6. " N. $\frac{1}{2}$ E.   | " 35       |
| 7. " W. by S. $\frac{1}{4}$ S.   | " 41      | 8. " S.E. by S.  | " 50       |
| 9. " N.W. by W.  | " 66      | 10. " N.W. $\frac{1}{2}$ N.  | " 30       |
| 11. { True course N.E. $\frac{1}{2}$ E.<br>Mag. do., E. by N. $\frac{1}{4}$ N. } | 329       | 12. { True course S.E. $\frac{1}{2}$ S.<br>Mag. do., S. by E. $\frac{1}{2}$ E. } | 351        |

13. The ship is in latitude  $55^{\circ} 59' N.$ , longitude  $2^{\circ} 40' E.$ , and must sail S.E.  $\frac{1}{2}$  S. (mag.) 209 miles.

14. The place of meeting was lat.  $56^{\circ} 5' N.$ , long.  $3^{\circ} 11' E.$ : the course steered by the ship from Heligoland was N.W.  $\frac{3}{4}$  W. (true), and by the ship from Hartlepool was N.E. by E.  $\frac{1}{2}$  E.

|   |                          |                                |  |
|---|--------------------------|--------------------------------|--|
| 15. Lat. $55^{\circ} 15\frac{1}{2}' N.$   | Long. $1^{\circ} 11' W.$ | Course S.S.W.                  | Distance 34'                             |
| 16. " 57 16 N.  | " 1 28 W.                | " S.S.W. $\frac{1}{4}$ W.      | " 96                                     |
| 17. " 60 4 N.   | " 0 24 W.                | " S.W. $\frac{1}{2}$ S. (nrly) | " 159                                    |
| 18. " 54 27 N.  | " 0 3 E.                 | " S. $\frac{3}{4}$ E.          | " 69                                     |
| 19. " 55 49 N.  | " 1 34 W.                | { Farn Lights<br>Berwick Light | " 12 $\frac{1}{2}$<br>" 14 $\frac{1}{2}$ |
| 20. " 53 20 N.  | " 1 36 E.                | Course N.N.W. $\frac{3}{4}$ W. | " 75 $\frac{1}{2}$                       |
| 21. 1st Station—Lat. $54^{\circ} 24' N.$ , long. $0^{\circ} 20' W.$ , distance 6 miles. |                          |                                |  |
| 2nd " " 54 24 N., " 0 1 W., " 14 "  |                          |                                |  |
| 22 1st " " 55 8 N., " 1 8 W., " 12 "  |                          |                                |  |
| 2nd " " 54 53 N., " 1 1 W., " 16 "  |                          |                                |  |

*English and Bristol Channels, and South Coast of Ireland, pp.—352—354.*

|  |                                    |   |                    |
|--|------------------------------------|---|--------------------|
| 1. Course S.W. by W.   | Dist. 21'                          | 2. Course S.S.E. $\frac{1}{2}$ E.                                     | Dist. 37'          |
| 3. " N. by E. $\frac{1}{2}$ E.   | " 44 $\frac{1}{2}$                 | 4. " N. by E. (nrly.)   | " 25               |
| 5. " N.N.E. $\frac{1}{4}$ E.   | " 25 $\frac{1}{2}$                 | 6. " N.E. $\frac{3}{4}$ E.  | " 72 $\frac{1}{2}$ |
| 7. Portland E. by N. $\frac{1}{4}$ N.                                      | " 36                               | 8. " N. by W. $\frac{1}{4}$ W.  | " 21               |
| 9. Course E. by N. $\frac{1}{4}$ N.  | " 50                               | 10. " S.E. $\frac{1}{4}$ E.   | " 77               |
| 11. " N.N.E. $\frac{1}{4}$ E.  | " 26                               | 12. " E. by S. $\frac{1}{4}$ S.                                       | " 40               |
| 13. " E. by N. $\frac{1}{2}$ N.  | " 53                               | 14. " N. by E. $\frac{1}{4}$ E.                                       | " 21               |
| 15. " N. by W. $\frac{3}{4}$ W.  | " 65                               | 16. " N. $\frac{3}{4}$ W.   | " 67               |
| 17. " E. $\frac{1}{4}$ S.  | " 76                               | 18. " E. $\frac{1}{8}$ S.   | " 35 $\frac{1}{2}$ |
| 19. Lat. $49^{\circ} 48' N.$   | Long. $6^{\circ} 7\frac{1}{2}' W.$ | Course E. by S.   | Distance 37'       |
| 20. " 49 40 N.   | " 1 3 W.                           | " S.E. $\frac{3}{4}$ E.   | " 45               |
| 21. " ....   | " ....                             | " E. $\frac{1}{4}$ N.   | " 40               |
| 22. " 50 28 N.   | " 2 9 W.                           | " .....   | " ..               |
| 23. " ....   | " ....                             | " N. by W. $\frac{1}{2}$ W.   | " 134              |
| 24. " 52 2 N.  | " 6 19 W.                          | " S.S.E. $\frac{1}{2}$ E.   | " 30               |
| 25. " 52 4 N.  | " 1 58 E.                          | " N. $\frac{3}{4}$ E.   | " 27               |
| 26. " 50 35 N.   | " 0 55 W.                          | " N.W. by W. $\frac{3}{4}$ W.   | " 15               |
| 27. " 50 32 N.   | " 1 30 $\frac{1}{2}$ W.            | " N.W. by W.  | " 21               |
| 28. " 51 25 N.   | " 4 59 W.                          | " N.N.W. $\frac{1}{2}$ W.   | " 32               |
| 29. " 49 51 $\frac{1}{2}$ N.   | " 5 35 W.                          | " N.W. by W. $\frac{1}{2}$ W.   | " 30               |
| 30. " 51 47 N.   | " 7 42 $\frac{1}{2}$ W.            | " W. by N.  | " 32 $\frac{1}{2}$ |
| 31. " 51 41 N.   | " 5 39 W.                          | " S.E. by S. $\frac{1}{2}$ S.   | " 46 $\frac{1}{2}$ |
| 32. " 50 39 $\frac{1}{2}$ N.   | " 0 35 E.                          | { Dist. off Dungeness Light, 21 miles.<br>" off Beachy Head Lt., 15 " |                    |
| 33. First Course—S.E. by S. (true), or S. by E. (mag.), distance 24 miles. |                                    |   |                    |
| 34. Second " N. by E. (true), or N.E. by N. (mag.), distance 24 miles.     |                                    |   |                    |

## SOUNDINGS.

DEPTHS, &amp;c., page 361.

1. Time from high water  $1^h 31^m$ ; half-range for day 18 feet 4 inches; table B + 13 feet. Depth of water required 55 feet 7 inches, or  $9\frac{1}{4}$  fathoms.
2. Time *before* high water  $1^h 47^m$ ; half-range for day 7 feet 2 inches; table B + 4 feet 2 inches. Depth 60 feet 4 inches, or 10 fathoms.
3. Time *before* high water  $1^h 46^m$ ; half-range for day 11 feet 3 inches; table B + 6 feet 9 inches. Depth by chart 8 feet 3 inches.
4. Time from high water  $0^h 15^m$ ; half-range for day 20 feet 9 inches; table B + 20 feet 5 inches. Corr. to low water 43 feet 5 inches. Water below sounding 7 feet 5 inches.
5. Time from high water  $5^h 41^m$ ; half-range for day 14 feet 5 inches; corr., table B, *sub.* 14 feet 3 inches; height of water 1 foot 3 inches below zero.
6. Time from high water  $3^h 59^m$ ; half-range for day 5 feet 5 inches; table B *sub.* 0 feet 10 inches. Sounding by chart 71 feet 2 inches, or 12 fathoms nearly.





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